



## COS 210 Worksheet 6

- This worksheet consists of **3 questions** for a total of **12 marks**
- Show your working for all calculations and reasoning.

### Question 1 ..... (5 marks)

Prove by contradiction that the following language is not regular.

$$L_1 = \{a^n b^m a^n : n \geq 0, m \geq 0\}$$

Make use of the Pumping Lemma in your proof and write down all steps.

### Question 2 ..... (5 marks)

Prove by contradiction that the following language is not regular.

$$L_2 = \{0^n 1^m : n \neq m, n \geq 0, m \geq 0\}$$

Do NOT use the Pumping Lemma.

Instead, make use of closure properties of operations on regular languages, and make use of the fact that the language  $A = \{0^n 1^n : n \geq 0\}$  is not regular (proven in Lecture 12).

### Question 3 ..... (2 marks)

Is the following language over  $\Sigma = \{0, 1\}$  regular or not? Prove your answer.

$$L_3 = \{w : \text{the substring } 01 \text{ occurs exactly as often in } w \text{ as the substring } 10\}$$

(An example of a string in the language is 010 because there is one occurrence of the substring 01 and one occurrence of the substring 10. An example of a string NOT in the language is 0101 because there are two occurrences of the substring 01 but only one occurrence of the substring 10.)