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Our interest is in **Dynamics**

Late 1600s	Newton	Calculus, planetary motion
Late 1800s	Poincare	Geometric approach, chaos hints
Early 1900s		Nonlinear oscillators (radio, radar, laser)
Early to mid 1900s	Birkhoff, Kolmogorov, Moser	Complex behavior in Hamiltonian mechanics
1963	Lorenz	Chaos in weather
1970s	May, Feigenbaum, Takens, Mandelbrot	Maps, universality, turbulence, fractals

- Dynamics Differential equations and iterated maps
- Simple harmonic oscillator as a system of eqs
- Nonlinearity
- Geometric view (phase space)

		Nı	umber of variables					
	n = 1	n = 2	$n \ge 3$	n >> 1	Continuum			
	Growth, decay, or equilibrium	Oscillations		Collective phenomena	Waves and patterns			
		Linear oscillator	Civil engineering,	Coupled harmonic oscillators	Elasticity			
Lincon	Exponential growth RC circuit	Mass and spring	structures	Solid-state physics	Wave equations			
Linear		RLC circuit	Electrical engineering	Molecular dynamics	Electromagnetism (Maxwell)			
	Radioactive decay	2-body problem (Kepler, Newton)		Equilibrium statistical mechanics	Quantum mechanics (Schrödinger, Heisenberg, Dirac)			
ity					Heat and diffusion			
ear					Acoustics			
ine					Viscous fluids			
Nonlinearity		The frontier						
ž			Chaos		Spatio-temporal complexity			
	Fixed points	Pendulum	Strange attractors	Coupled nonlinear oscillators	Nonlinear waves (shocks, solitons)			
•		Anharmonic oscillators	(Lorenz)	Lasers, nonlinear optics	Plasmas			
	Overdamped systems,	tional dynamics Biological oscillators	3-body problem (Poincaré)	Nonequilibrium statistical mechanics	Earthquakes			
Nonlinear Logistic equation			Chemical kinetics		General relativity (Einstein)			
	(neurons, heart cells)	Iterated maps (Feigenbaum)	Nonlinear solid-state physics	Quantum field theory				
	for single species	Predator-prey cycles Nonlinear electronics	Fractals (Mandelbrot)	(semiconductors) Josephson arrays	Reaction-diffusion, biological and chemical waves			
	(van der Pol, Josephson) Forced nonline	Forced nonlinear oscillators	Heart cell synchronization	Fibrillation				
		(Levinson, Smale)	(Levinson, Smale)	Neural networks	Epilepsy			
				Immune system	Turbulent fluids (Navier-Stokes)			
			Practical uses of chaos	Ecosystems	Life			
			Quantum chaos?	Economics				

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			Practical uses of chaos	Immune system	Turbulent fluids (Navier-Stokes)		
			Quantum chaos ?	Ecosystems	Life		
			Simple climate /	Economics			
I.			eanography models	Flocking			

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- General programming languages
 - → C, C++, Java, Python, Fortran, R, etc...
- Commercial languages
 - → Matlab, Mathematica, etc...