
GEOS 397/597

Lecture #18: Curve fitting

use `practical_18.m`

1) Update from github

2) polyfit, polyval, corrcoef, roots

MATLAB provides several built-in functions to fit curves

- Many require the “Curve Fitting Toolbox”, or other toolboxes.
- We will only use the basic curve fitting functions that are part of standard MATLAB
- We will focus on:

1) polyfit

2) polyval

3) corrcoef

4) roots

3) Review polynomials

Polynomials come in different **orders** or **degrees**.

- 0^{th} order: a single constant value

Examples:

$$y = 4$$

$$y = 2.75$$

$$y = -12.1$$

- 1^{st} order: a linear equation (i.e. independent variable is to 1^{st} power)

Examples:

$$y = 4x$$
$$y = 2.75x + 7$$
$$y = -12.1x - 21.3$$

- 2^{nd} order: a quadratic equation

Examples:

$$y = 4x^2$$
$$y = 2.75x^2 + 7$$
$$y = -12.1x^2 - 21.3x + 1.4$$

- 3^{rd} order: a cubic equation

Examples:

$$y = 4x^3$$
$$y = 2.75x^3 + 7$$
$$y = -12.1x^3 - 21.3x + 1.4$$
$$y = 12x^3 + 3x^2 - 11x + 2$$

- n^{th} order: a polynomial where n is the largest exponent on the independent variable
- Can be represented in MATLAB as a row vector of the coefficients in front of the independent variable of decreasing order

$$[3, 2.7, 1, -5.7] \rightarrow 3x^3 + 2.7x^2 + x - 5.7$$

The polynomial **order** is always

$$1 \mid n = \text{numel}(\text{vector}) - 1$$

Remember the 0^{th} order term! Also remember that the equation order doesn't matter, but the vector order does! (It is a good habit to organize the terms based on reducing order though.)

$$x - 5.7 + 3x^3 + 2.7x^2 \rightarrow [3, 2.7, 1, -5.7]$$

polyval() -- evaluate polynomial

These vectors can be interpreted by **polyval()** as coefficients of a polynomial and used to make a curve.

Try first practical exercise.

polyfit() -- fit polynomial to data

This function can be used to estimate the coefficients from an existing curve.

Try second practical exercise.

Linear least-squares fitting

Goodness of fit

4) Student exercises in class