

$$1. \quad m(a+bx) = \frac{1}{N} \sum_{i=1}^N a + bx_i = \frac{1}{N} \left( \sum_{i=1}^N a + b \sum_{i=1}^N x_i \right) = \frac{1}{N} \left( Na + b \sum_{i=1}^N x_i \right)$$

$$= a + b \left( \frac{1}{N} \sum_{i=1}^N x_i \right) = a + b m(x)$$

$$2. \quad \text{cov}(X, a+bx) = \frac{1}{N} \sum_{i=1}^N (x_i - m(x)) ((a+bx_i) - m(a+bx))$$

$$(a+bx_i) - m(a+bx) = b(x_i - m(x))$$

$$\text{cov}(X, Y) = \frac{1}{N} \sum_{i=1}^N (x_i - m(x)) \cdot b(x_i - m(x)) = b \left( \frac{1}{N} \sum_{i=1}^N (x_i - m(x))(x_i - m(x)) \right)$$

$$= b \text{cov}(X, Y)$$

~~$$3. \quad \text{cov}(a+bx, a+bx) = \frac{1}{N} \sum_{i=1}^N (a+bx_i - m(a+bx)) (a+bx_i - m(a+bx))$$~~