Ulan Rechi CS 498 HW 9.1 f: R -> R by f(=) = aT = a) mean  $(\{f\}) = \frac{1}{N} \sum_{i} f(\vec{x}_{i})$  $= \frac{1}{N} \sum_{i} \vec{a}^{T} \vec{x}_{i} = \vec{a}^{T} \left( \frac{1}{N} \sum_{i} \vec{x}_{i} \right)$ = aT mean(gx) < (Coumat  $(\sqrt{x})$ ) =  $\frac{1}{N}$   $\sum_{i} (\vec{x}_{i} - mean(\vec{x}_{i}))$ var(4F3) = var (4 ((x), -((x))) = \( \sum \sum \( \bar{a} \) = 1 [ (a (x; - meon (x)))2 =  $\overline{N}$   $\overline{a}^{T}(\overline{x}_{i}-mean(\overline{x}^{T}))(\overline{a}^{T}(\overline{x}_{i}-mean(\overline{x}^{T})))$ = \(\) \(\bar{a}\) \(\bar{z}\_i - meen(\bar{z}\_i)\) \(\bar{z}\_i - meen(\bar{z}\_i)\) \(\bar{a}\) = aT Coumat (dzis) a

10.1 c) (ef à Cournet (xx) à = 0

which means var (xx) = 0

So,

i Si (à x; - à mean(xx)) = 0

Which implies à x; - a mean(xx) = 0 Vie R

Hence, each xi lies on a hyperplane
with normal à and intercept - à mean(xx)

10.2 (Drawn of figure 10.31 below)

10.2) Mark the mean of the dataset, the first principal component, and the second principal component.

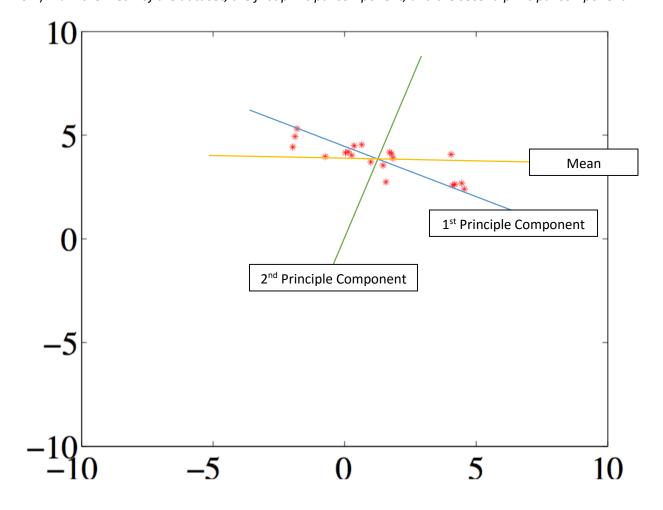


FIGURE 10.31: Figure for the question