# STATISTICS FUNDAMENTALS, PART 2

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## STATISTICS FUNDAMENTALS, PART 2

## LEARNING OBJECTIVES

- Explain the difference between causation and correlation
- Test a hypothesis within a sample case study
- Validate your findings using statistical analysis (p-values, confidence intervals)

### **COURSE**

# PRE-WORK

#### **PRE-WORK REVIEW**

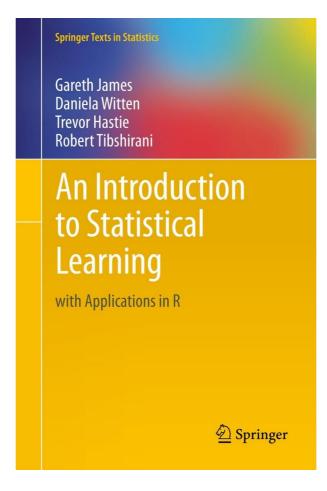
- Use descriptive statistics to understand your data
  - What are some goto methods to understand your data?

#### **OPENING**

# STATISTICS FUNDAMENTALS, PART 2

#### **DATA SOURCE**

Today, we'll use advertising data from an example in *An Introduction to Statistical Learning*.



#### INTRODUCTION

# CAUSATION AND CORRELATION

- If an association is observed, the first question to ask should always be... is it real?
- Think of various examples you've seen in the media related to food.

#### A few cups of coffee may lower colon cancer risk

Posted: 01 August 2007 1708 hrs

TOKYO: Drinking a few cups of coffee a day may lower the risk of advanced colon cancer, at least for women, Japanese researchers said Wednesday.

The study, supported by Japan's health ministry, showed women who drink more than three cups of coffee a day were 56 percent less likely to develop advanced colon cancer than those who drink no coffee at all.

"Drinking coffee sustains the secretion of bile acid and keeps down cholesterol levels, the mechanisms thought to prevent colon cancer." the report said.

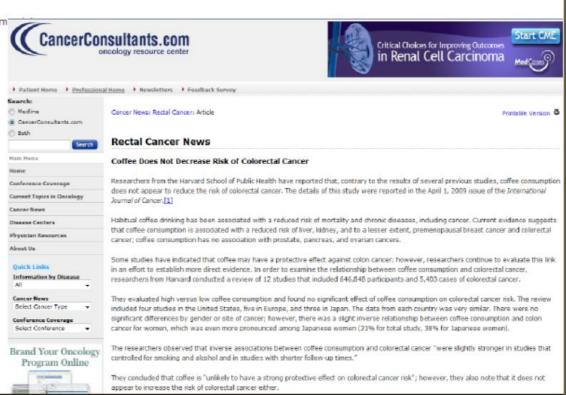
But unfortunately the effect was not seen in men, the medical research team said.

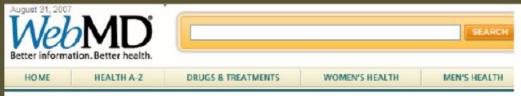
Many men smoke and drink alcohol more than women, and those habits probably offset the effect of coffee, the study said.

The research team tracked down about 96,000 people in Japan aged from 40 to 69 between the early 1990s and 2002, of whom 726 men and 437 wom suffered colon cancer.



#### Causal claims are often inconsistent and contradictory!





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#### Drinking and Dementia: Is There a Link?

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Study Shows Drinkers With Genetic Predisposition to Alzheimer's Disease at Higher Risk

By Salvnn Boyles WebMD Medical News

Sept. 2, 2004 -- Drinking alcohol in middle age may increase the risk of late-life dementia in people who are genetically predisposed to develop Alzheimer's disease, according to findings from a Scandinavian study.

Researchers from Stockholm's Karolinska Institute reported that infrequent drinkers have a twofold increase in the risk of dementia in old age among carriers of a gene that has been linked to Alzheimer's. Gene carriers who frequently drink had a threefold increase in risk.

But the findings also show a protective effect for infrequent drinkers who did not have the genetic risk factor. Low-risk teetotalers and frequent drinkers in the study were twice as likely to experience mild cognitive declines later in life as infrequent drinkers.

The findings are reported in the Sept. 4 issue of the BMJ (formerly the British Medical Journal).

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Friday, 25 January, 2002, 12:13 GMT

#### World Alcohol 'could reduce UK Politics dementia risk'



B B C SPORT

B B C Weather

Mobiles/PDAs

Moderate alcohol consumption could be beneficial

Small amounts of alcohol could reduce the risk of dementia in older people Daily E-mail regardless of the type of alcoholic drink News Ticker consumed, research suggests.

Feedback It is known that light-to-moderate Help consumption lessens the risk of coronary heart disease and stroke, but Dutch Low Graphics scientists think it could be good for mental . Alzheimer's Society health.

#### See also:

- 17 Apr 01 | Health Alcohol 'protects old | against heart failure'
- 01 Feb 01 | Health £6bn bill for alcohol abuse
- ▶ 06 Dec 00 | Health Alcohol 'improves IO'
- 15 Apr 01 | Health Why alcohol affects women more
- . 06 Jan 01 | Health Alcohol 'cuts strokes in women'
- ▶ 18 Dec 00 | Health Beer 'keeps cataracts' away'
- 30 Oct 00 | Health Alcoholic liver disease linked to genes

#### Internet links:

- British Heart Foundation
- The Lancet

Why is this?

Sensational headlines?

There is neglect of a robust data analysis.

- There is also often a lack of understanding of the difference between causation and correlation.
- Understanding this difference is critical in the data science workflow, especially when **Identifying** and **Acquiring** data.
- We need to fully articulate our question and use the right data to answer it, including any *confounders*.

- Additionally, this comes up when we **Present** our results to stakeholders.
- We don't want to overstate what our model measures.
- Be careful not to say "caused" when you really mean "measured" or "associated".

#### **LECTURE**

# CAUSATION VS CORRELATION

#### **CAUSAL CRITERIA**

- Causal criteria is one approach to assessing causal relationships.
- However, it's **very hard to define** universal causal criteria.
- One attempt that is commonly used in the medical field is based on work by Bradford Hill.

#### **CAUSAL CRITERIA**

- He developed a list of "tests" that an analysis must pass in order to indicate a causal relationship. Note the terminology here is more relevant for diseases but the concept still holds nonetheless:
  - a. Strength of association correlation
  - b. Consistency reproducibility
  - c. Temporality causality

#### **CAUSAL CRITERIA**

- Most commonly, we find an *association* between two variables. This means there is an observed **correlation** between the variables.
- We may not fully understand the causal direction (e.g. does smoking cause cancer or does cancer cause smoking?).
- We also might not understand *other* factors influencing the association.

#### INTRODUCTION

# CONFOUNDING AND DAGS

## **CONFOUNDING**

• Often times, associations may be influenced by another *confounding* factor.

Let's say we did an analysis to understand what causes lung cancer.

• We find that people who carry cigarette lights are 2.4 times more likely to

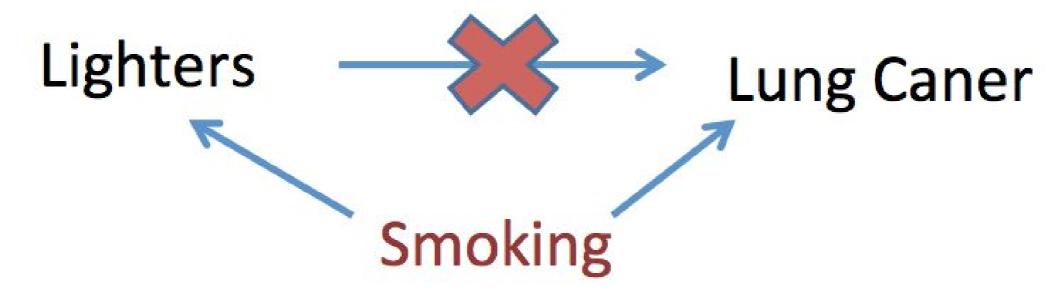
contract lung cancer as people who don't carry lighters.

Does this mean that the lighters are causing cancer?



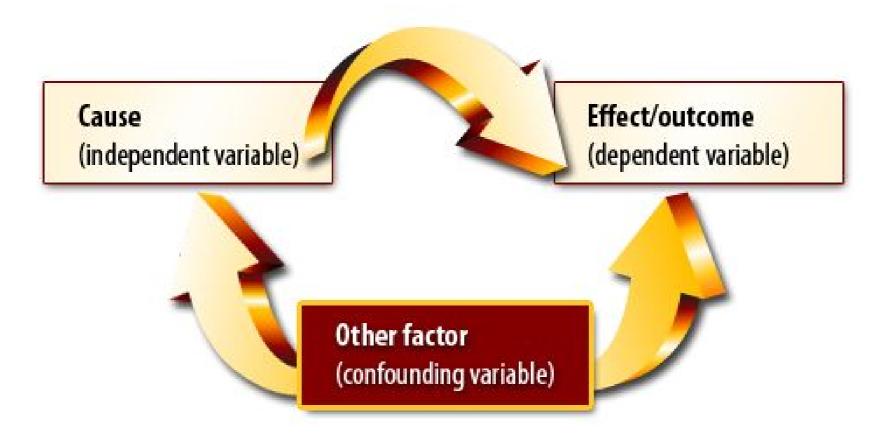
## **CONFOUNDING**

No!



#### **CONFOUNDING**

• Confounding variables often hide the true association between causes and outcomes.



#### DIRECTED ACYCLIC GRAPH

The DAG for how TV ads and Google ads affect sales might look like the following:



### **SEASONALITY**

- Suppose TV ads were run in November/December (peak buying season) while Google ads were run during February/March (low buying season).
- If we compare the two, we're likely to reach the wrong conclusion! Seasonal trends are affecting our associations.
- This is an example of *bias* and *confounding*. It isn't that TV ads are better than Google ads; it's that November/December is a better buying season than February/March, an inherent bias.

#### A FEW KEY TAKEAWAYS

- It is important to have deep subject area knowledge to be aware of biases in your field. This knowledge supplements statistical techniques.
- A DAG can be a useful tool for thinking through the logic of your model.
- There is a difference between causation and correlation. Statistics usually show *correlation*, not *causation* (remember our smoking example).
- Good data is important. Your analysis is only as good as your understanding of the problem and the data you have to work with.

#### INTRODUCTION

# HYPOTHESIS TESTING

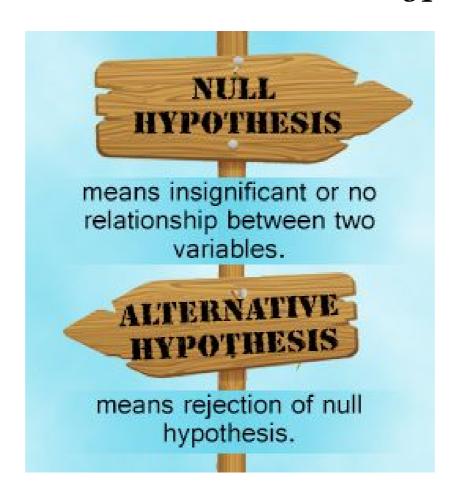
### **HYPOTHESIS TESTING**

- How can we tell the difference between two groups of observations (e.g. smokers vs. non-smokers)?
- Imagine we are testing the health of smokers vs. non-smokers. At a cursory glance, our results may show that smokers are marginally healthier than non-smokers.
- Are they healthier due to random chance or is there a statistically significant difference? Maybe we happened to assemble a strange group of smoking triathletes and a group of non-smoking couch potatoes.
- This is where hypothesis testing can help.

## **VALIDATE YOUR FINDINGS**

- We know how to carry out a hypothesis test, but how do we tell if the association we found is *statistically significant*?
- Statistical significance is the probability that a result or relationship is caused by something other than random chance.
- Statistical hypothesis testing is traditionally employed to determine if a result is statistically significant or not.

• First, you need a hypothesis to test, referred to as the *null hypothesis*. The opposite of this would be the *alternative hypothesis*.



- For example, if we want to test the relationship between gender and sales, we may have the following hypotheses.
- Null hypothesis: There is no relationship between Gender and Sales.
- Alternative hypothesis: There is a relationship between Gender and Sales.

- One sample test example
  - Test a sample value against a population mean. Null hypothesis is that the sample value is the same as the population mean.
  - Calculate the t-statistic (number of std deviations that your sample mean is away from the population mean) and the corresponding probability associated to that t-statistic
  - Confidence interval of the sample mean would include population mean if the null hypothesis cannot be rejected

Two sided test:
Null Hypothesis:
sample mean = population mean

Alternative Hypothesis: Sample mean != population mean

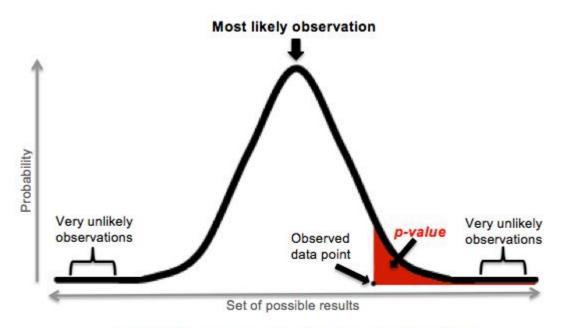
$$t = \frac{\overline{X} - \mu}{\frac{S}{\sqrt{N}}} \qquad \overline{X} \pm t_{\alpha/2} \frac{S}{\sqrt{n}}$$

t-Statistic

Confidence Interval

### **VALIDATE YOUR FINDINGS**

• Typically, a cut point of 5% is used. This means that we say something is statistically significant if there is a less than a 5% chance that our finding was due to random chance alone.



A p-value (shaded red area) is the probability of an observed (or more extreme) result arising by chance

## **VALIDATE YOUR FINDINGS**

#### TABLE 1

#### Relationship between Common Language and Hypothesis Testing

COMMON LANGUAGE	STATISTICAL STATEMENT	CONVENTIONAL TEST THRESHOLD
"Statistically significant" "Unlikely due to chance"	The null hypothesis was rejected.	P < 0.05
"Not significant" "Due to chance"	The null hypothesis could not be rejected.	P > 0.05

- Once you have your hypotheses, you can check whether the data supports rejecting the null hypothesis or failing to reject the hypothesis.
- **Note**: Failing to reject the null is **NOT** the same as accepting that there is no relationship. While the alternative hypothesis **might** be true, we don't have enough data to support that claim specifically.
  - Reject the null hypothesis (p-value <= alpha) and conclude that the alternative hypothesis is true at the 95% confidence level (or whatever level you've selected).
  - Fail to reject the null hypothesis (p-value > alpha) and conclude that not enough evidence is available to suggest the null is false at the 95% confidence level.
- Keep this in mind so you don't overstate your findings.

### **HYPOTHESIS TESTING**

- Many variations of the tests:
  - Two sample test
  - Proportion tests
  - Small number of samples
  - Sampling statistic is non normally distributed
  - Categorical variables
  - Many more...

#### Further reference:

http://sphweb.bumc.bu.edu/otlt/mph-modules/bs/bs704\_confidence\_intervals/bs704\_confidence\_intervals\_print.html

# HYPOTHESIS TESTING CASE STUDY

#### **HYPOTHESIS TESTING CASE STUDY**

- We're going to walk through Part 1 of the guided-demo-starter-code notebook in the class repo for lesson 4.
- There are several questions to answer. We'll answer those questions in small groups and then discuss with the class.

# P-VALUES AND CONFIDENCE INTERVALS CASE STUDY

## P-VALUES AND CONFIDENCE INTERVALS CASE STUDY

- We're now going to walk through Part 2 of the guided-demo-starter-code notebook in the class repo for lesson 4.
- There are several questions to answer. We'll answer those questions in small groups and then discuss with the class.

#### INDEPENDENT PRACTICE

# INTERPRETING RESULTS

#### **ACTIVITY: INTERPRETING RESULTS**



#### **DIRECTIONS (35 minutes)**

- 1. Using the lab-starter-code-4, you will look through a variety of analyses and interpret the findings.
- 2. You will be presented with a series of outputs and tables from a published analysis.
- 3. Read the outputs and determine if the findings are statistically significant or not.

#### **DELIVERABLE**

Answers to the questions in the notebook

#### **LESSON**

# EXIT TICKET

DON'T FORGET TO FILL OUT YOUR EXIT TICKET