

Universal Quantification as Iterated Conjunction

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Universal Quantification

Classic view: generalized Boolean conjunction

$\llbracket \text{Every student left} \rrbracket =$

$\text{left } x_1 \wedge \text{left } x_2 \wedge \dots \wedge \text{left } x_k, \quad \text{for } x_1, \dots, x_k \in \text{student}$

The Proposal: generalized dynamic conjunction

$\llbracket \text{Every student left} \rrbracket =$

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The Empirical Payoff:

- ▶ Pair-list readings
- ▶ Internal adjectives

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- ▶ Pair-list readings
- ▶ Internal adjectives

Outline

1. Data on pair-lists and adjectives in English
2. Dynamic conjunction and relation composition
3. Applications of iterated conjunction to data

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Universal quantification and pair-list questions

Matrix pair-list questions only possible with distributive universal quantifiers

(Szabolcsi 1993, 1997; Krifka 2001; a.o.)

(1) Which dish did every boy make?

- a. Pasta
- b. His favorite
- c. ✓ Al (made) pasta, Bill salad, Carl pudding

(2) Which dish did most/several/no boys make?

- a. Pasta
- b. Their favorite
- c. # Al (made) pasta, Bill salad, Carl pudding

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Universal quantification and “functional readings”

Pair-list varieties of functional readings only possible with distributive universal quantifiers

(Chierchia 2001; Schwarz 2001; Schlenker 2006; a.o.)

- (3) If each guest brought a certain dish, the party was a sure success

$\checkmark \exists f: \text{guest} \rightarrow \text{dish}. (\forall x \in \text{guest}. \text{brought}(fx) x) \Rightarrow \dots$

- (4) If no/three/all the guests brought a certain dish, the party was probably a success

$\# \exists f: \text{guest} \rightarrow \text{dish}. (\neg \exists / \exists_3 / \forall x \in \text{guest}. \text{brought}(fx) x) \Rightarrow \dots$

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Universal quantification and internal adjectives

Internal readings of singular adjectives only possible with distributive universal quantifiers

(Carlson 1987; Beck 2000; Brasoveanu 2011; a.o.)

(5) Each guest brought a different/more elaborate dish

$\checkmark \exists f: \text{guest} \xrightarrow{1:1/+} \text{dish}. \forall x \in \text{guest}. \text{brought}(fx) x$

(6) No/At least three/Few guests brought a different/more elaborate dish

$\# \exists f: \text{guest} \xrightarrow{1:1/+} \text{dish}. \neg \exists / \exists_3 / \text{Few } x \in \text{guest}. \text{brought}(fx) x$

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A little dynamics

- Propositions in dynamic semantics: relations over “contexts” (here, stacks á la Dekker 1994)

$$\llbracket \text{John left} \rrbracket \rightsquigarrow \lambda s. \{s \cdot j \mid \text{left } j\}$$

- Existentials in dynamic semantics: potential multiplicity of output contexts for any given input

$$\llbracket \text{A man left} \rrbracket \rightsquigarrow \lambda s. \{s \cdot x \mid \text{left } x \wedge \text{man } x\}$$

- Conjunction in dynamic semantics: relation composition

$$\llbracket \phi ; \psi \rrbracket \equiv \lambda s. \bigcup \{ \llbracket \psi \rrbracket s' \mid s' \in \llbracket \phi \rrbracket s \}$$

Iterated conjunction and alternatives

(7) John read a book and Tom read a book

$$\begin{array}{c}
 \text{John read a book} \\
 \hline
 \lambda s. \left\{ s \cdot j \cdot x \mid \begin{array}{l} \text{book } x \\ \text{read } x j \end{array} \right\}
 \end{array}
 ;
 \begin{array}{c}
 \text{Tom read a book} \\
 \hline
 \lambda s. \left\{ s \cdot t \cdot y \mid \begin{array}{l} \text{book } y \\ \text{read } y t \end{array} \right\}
 \end{array}$$

$$\rightsquigarrow
 \begin{array}{c}
 \lambda s. \left\{ \begin{array}{l} s \cdot j \cdot x \\ \cdot t \cdot y \end{array} \mid \begin{array}{l} x, y, z, \in \text{book}, \\ \langle j, x \rangle, \langle t, y \rangle \in \text{read} \end{array} \right\} \\
 \hline
 \left\{ \begin{array}{ll} \text{John read } W\&P & \text{and Tom read } W\&P \\ \text{John read } W\&P & \text{and Tom read } AK \\ \vdots & \\ \text{John read } AK & \text{and Tom read } AK \end{array} \right\}
 \end{array}$$

A set of alternatives pairing John and Tom with books they read

Iterated conjunction and alternatives

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 \text{John read a book} \\
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 ;
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 \end{array}$$

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 \end{array}$$

A set of alternatives pairing John and Tom with books they read

Universal quantification as iterated conjunction

(8) Every student read a book

$$\begin{array}{c}
 \text{John read a book} \qquad \qquad \qquad \text{Tom read a book} \qquad \qquad \qquad \dots \\
 \hline
 \lambda s. \left\{ s \cdot j \cdot x \mid \begin{array}{l} \text{book } x \\ \text{read } x j \end{array} \right\} ; \lambda s. \left\{ s \cdot t \cdot y \mid \begin{array}{l} \text{book } y \\ \text{read } y t \end{array} \right\} ; \dots
 \end{array}$$

$$\rightsquigarrow \lambda s. \left\{ \begin{array}{l} s \cdot j \cdot x \\ \cdot t \cdot y \cdot \dots \end{array} \mid \begin{array}{l} x, y, z, \in \text{book}, \\ \langle j, x \rangle, \langle t, y \rangle \in \text{read} \end{array} \right\}$$

$$\left\{ \begin{array}{l} \text{John read } W\&P \text{ and Tom read } W\&P \text{ and } \dots \\ \text{John read } W\&P \text{ and Tom read } AK \text{ and } \dots \\ \vdots \end{array} \right\}$$

A set of alternatives pairing each student with a book he read

Universal quantification as iterated conjunction

(8) Every student read a book

$$\begin{array}{c}
 \text{John read a book} \qquad \qquad \text{Tom read a book} \qquad \qquad \dots \\
 \hline
 \lambda s. \left\{ s \cdot j \cdot x \mid \begin{array}{l} \text{book } x \\ \text{read } x j \end{array} \right\} ; \lambda s. \left\{ s \cdot t \cdot y \mid \begin{array}{l} \text{book } y \\ \text{read } y t \end{array} \right\} ; \dots \\
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 \end{array}$$

A set of alternatives pairing each student with a book he read

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Pair-list functional readings

(9) Each guest brought a dish

$$\rightsquigarrow \left\{ \begin{array}{l} \text{Al made pasta and Bill made salad and Carl made pudding} \\ \text{Al made pasta and Bill made salad and Carl made salad} \\ \vdots \end{array} \right\}$$

Like other sources of nondeterminism — indefinites, disjunctions — these alternatives can take exceptional scope

(Kratzer & Shimoyama 2002; Alonso-Ovalle 2006; Charlow 2014)

(10) If each guest brought a certain dish, the party was a sure success

$$\{p \Rightarrow \text{success the.party} \mid p \in \llbracket (9) \rrbracket\}$$

Internal adjectives

Comparative adjectives are essentially anaphoric
(e.g. Brasoveanu 2011)

- (11) John bought a computer.
Mary bought a different/faster computer.

$$\llbracket \text{different} \rrbracket \equiv \lambda P x s. \{ s' \mid s' \in P x s \wedge x \notin s' \}$$

$$\llbracket \text{faster} \rrbracket \equiv \lambda P y s. \left\{ s' \mid \begin{array}{l} s' \in P x s \\ \text{speed } x > \max \{ \text{speed } v \mid v \in s \wedge P v s \neq \emptyset \} \end{array} \right\}$$

Internal adjectives

(12) In 2010, I bought a faster computer

$$\lambda s. \left\{ s \cdot 2010 \cdot x \mid \begin{array}{l} \text{comp } x \\ \text{speed } x > \max\{\text{speed } u \mid \text{comp } u \wedge u \in s\} \end{array} \right\}$$

(13) Every year, I bought a faster computer

[[In 09, I bought a faster computer]] ;

[[In 10, I bought a faster computer]] ;

⋮

$$\lambda s. \left\{ \begin{array}{l} s \cdot 09 \cdot x \\ \cdot 10 \cdot y \\ \cdot 11 \cdot z \\ \dots \end{array} \mid \begin{array}{l} x, y, z, \dots \in \text{comp}, \quad \langle j, x, 09 \rangle, \langle j, y, 10 \rangle, \langle j, z, 11 \rangle, \dots \in \text{bought} \\ \text{speed } x > \max\{\text{speed } u \mid \text{comp } u \wedge u \in s\} \\ \text{speed } y > \max\{\text{speed } u \mid \text{comp } u \wedge u \in s \cdot 09 \cdot x\} \\ \text{speed } z > \max\{\text{speed } u \mid \text{comp } u \wedge u \in s \cdot 09 \cdot x \cdot 10 \cdot y\}, \dots \end{array} \right\}$$

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Conclusion

- ▶ Uniform distribution of pair-lists and internal readings accounted for
- ▶ No need to resort to choice functions or quantification over pairs
(Schwarz 2001; Schlenker 2006; Brasoveanu 2011; a.o.)
- ▶ Consonant with theories like Szabolcsi 2013 that take universals to be morphosemantically composed of conjunction, and conjunction to be dynamic by default

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Thanks!