$$F :: (a \to b) \to SGa \to SGb$$

$$F = \lambda f m . \{\lambda r . f(\alpha r) \mid \alpha \in m\}$$

$$H :: (a \to b) \to GSa \to GSb$$

$$H = \lambda f m r . \{f x \mid x \in m\}$$

$$\varepsilon :: SGa \to GSa$$

 $\varepsilon = \lambda mr . \{ \alpha r \mid \alpha \in m \}$

$$\begin{array}{ccc}
\mathsf{SG}a & \xrightarrow{Ff} & \mathsf{SG}b \\
\downarrow^{\varepsilon} & & \downarrow^{\varepsilon} \\
\mathsf{GS}a & \xrightarrow{Hf} & \mathsf{GS}b
\end{array}$$

$$\begin{split} \varepsilon \circ F &f = \lambda m \,.\, \varepsilon \,(F \,f \,m) \\ &= \lambda m \,.\, \varepsilon \,\{\lambda r \,.\, f \,(\alpha \,r) \mid \alpha \in m\} \\ &= \lambda m r \,.\, \{\beta \,r \mid \beta \in \{\lambda r \,.\, f \,(\alpha \,r) \mid \alpha \in m\}\} \\ &= \lambda m r \,.\, \{f \,(\alpha \,r) \mid \alpha \in m\} \end{split} \qquad \qquad = \lambda m r \,.\, \{f \,(\alpha \,r) \mid \alpha \in m\} \} \\ &= \lambda m r \,.\, \{f \,(\alpha \,r) \mid \alpha \in m\} \end{split}$$