

The RTM package

a Learning Environment for Reaction Transport Modelling in R

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July 2021

Abstract

Since many years we have been teaching courses on environmental and reaction-transport modelling to master students at Ghent and Utrecht University. Our aim is to teach students how to create models “from scratch” and apply them to advance their understanding of natural systems, including those perturbed by anthropogenic activities. Typically, students attending our classes have different backgrounds and highly variable levels of skills in quantitative and computational methods, which makes it difficult to find a teaching style that suits everyone. To overcome this issue, we revised our didactic approach and now teach in the form of a “flipped class”, where students prepare themselves ahead of the class using material available on-line, and then, during the class, put the learned concepts into practice by solving problems and exercises with a direct feedback from us. To facilitate this teaching approach, we created short educational videos, quizzes, exercises, and extra readers to guide the students in learning and exploring the topics covered in the courses. Here, we present the R-package RTM, which merges this teaching material into a common platform and thus simplifies their delivery to students.

Introduction

The courses Environmental Modelling and Reactive Transport Modelling in the Hydrosphere have been taught at Ghent University (Belgium) and Utrecht University (The Netherlands), respectively, since many years. Students attending these courses learn how to make mechanistic models that start from first principles of physics, chemistry, biology, and ecology, are mathematically formulated as differential equations, and are solved numerically by a computer. The models aim to advance their understanding of natural systems by allowing prediction of the systems’ behaviour under various scenarios (e.g., response of the global carbon cycle to burning of fossil fuels).

The aim of the courses is to teach students how to make models “from scratch”. This differs from many modelling courses where students merely learn how to apply existing models. More specifically, students in our courses learn to

- create conceptual models that describe environmental scenarios or problems,
- translate conceptual models into mechanistic models and, ultimately, mathematical equations that describe the variation of the state variables characterising the system in time and space,
- implement these mathematical equations in a computer program and solve them,
- interpret the results in terms of the original environmental scenario or problem, and
- apply the models to realistic scenarios.

We use R (R core team 2020) as the programming language for implementing and solving these models. This is mainly because there is an “ecosystem” of R-packages that provide methods for solving the type of differential equations that we deal with in the courses, including *rootSolve*, *deSolve*, *ReacTran* (Soetaert, 2009; Soetaert et al., 2010; Soetaert and Meysman, 2012). These packages have been implemented so that they hide much of the mathematical details behind the methods, allowing students to focus on the original problem rather than being concerned with finding a numerical approach to solve it. Additionally, they provide auxiliary functions that facilitate tabulation and visualisation of model results, fitting of models to data, etc.

Our students typically follow a master program in Earth or Life Sciences, and are interested in disciplines such as oceanography, biology, biogeochemistry, hydrology, or physics. Some have a good understanding of the processes occurring in the natural environment, but have never written a computer program before; others have ample experience in programming, mathematics or computer science, but little knowledge about the processes in nature. Due to this variation in background, knowledge and skills, a big challenge is to find a teaching style that can stimulate efficient and effective learning for all students.

Previously, we have employed the more “traditional” teaching approach, where the instructor explains the context, theory and examples during lectures, and encourages students to practice the taught material by themselves (or in small groups) outside the class (e.g., by solving problems and exercises given as homework assignments). In this approach, however, the brighter students often get bored as they feel that the material is being taught too slowly, while the less bright students become demotivated or frustrated as they cannot follow. Additionally, the percentage of students that works on the outside-the-class assignments is typically less than desired.

Based on this experience, we decided to experiment with our didactic approach and employ the so-called “flipped class” teaching approach. In this approach, students obtain the theoretical lectures in advance and prepare themselves before the class. Then, during the class, they practice the learned concepts by solving problems and exercises with a direct feedback from the instructor. One of the advantages of the flipped class is that students can work more focused and thus obtain a more thorough understanding of the material. Before the class, students can take the time they need to prepare themselves individually. Subsequently, while in the classroom, they can directly interact with tutors and therefore explore the topics to the depth determined by their own ability, motivation and ambition. This provides more room for tutoring “a la tete du client”.

The modelling course taught by Karline Soetaert and Dries Bonte at Ghent University has been in the form of a flipped class since the academic year 2019–2020, while the course taught by Lubos Polerecky and Karline Soetaert at Utrecht University first implemented this approach in the academic year 2020–2021. This way of teaching proved to be a positive experience: while in previous years students would complain that they did not get enough practice in class, there is now ample time for practical exercises. Also the class is much more dynamic, with dramatically improved students participation and involvement.

Here, we discuss how the flipped modelling class is implemented. Specifically, we describe a newly developed R-package RTM, which merges the main components of the teaching material — tutorials, exercises, template files, and extra readers — into a common platform and thus simplifies its delivery to students.

Implementation of the flipped class

To prepare for each lesson, students are offered the choice to either read one or more chapters from the course textbook (Soetaert and Herman, 2009), or watch one or more short knowledge clips that explain the theory. Then they are encouraged to test their understanding of the theory by answering a number of short (often multiple-choice) questions delivered in a quiz-like format. This initial “priming” phase is done individually by each student. Subsequently, students go to the classroom and submerge themselves, under the guidance of tutors, in solving more substantial exercises. The work in this second phase is done in small groups (2–4 students per group), which facilitates exchange of ideas among the students and thus boosts their overall participation and involvement.

Knowledge clips

The theory behind the material taught in the modelling courses is explained in a series of knowledge clips. The videos, which typically take between 5 to 15 minutes, were developed by (1) creating a series of didactically sound slide presentations, (2) writing down the narrative for each slide, and (3) recording and combining the narrative and slides into a video. Steps 1 and 2 were developed by the tutors, while step 3 was partially outsourced and partially executed by the tutors.

Creation of the knowledge clips offers several longer-term advantages. For example, they are available to the public via a YouTube playlist,¹ and so can serve as an online course. Also, if students wish to refresh their knowledge of the subject, they can re-watch the clips at any time and in any order. Importantly, they dictate the pace at which they watch and learn from the clips.

Quiz-like questions

Each knowledge clip is accompanied by a set of quiz-like questions and short exercises (Figure 2). These were implemented in the form of *tutorials* provided by the R-package *learnr* (Schloerke et al., 2020). They mostly consist of multiple-choice questions, sprinkled here and there with a more substantial exercise that needs to be solved by completing an R-code embedded within the text.

The quizzes were designed to allow the students to test their basic understanding of the subject explained in the knowledge clip. Before we introduced these quizzes, we often noted that some students overestimate their grasp of the theory and are overly confident, while others are baffled by the complexity of the material and may lose confidence that they will eventually manage to understand it. The quizzes allow students to make this assessment by, and for, themselves. They are *not* graded, but students are encouraged to use them for their own benefit, as they facilitate better preparation for the more substantial exercises in the classroom and, ultimately, for the exam.

Classroom exercises

While in the classroom, students work on practical modelling *exercises* that address current environmental problems. The overall philosophy of this activity is that students design, develop and implement their models “from scratch”. That is, after being given a text that defines a problem, they start from a conceptual diagram and progress until they develop an R-code that generates quantitative predictions about the behaviour of the studied system. Based on these predictions they can discuss how to tackle the original problem.

At the time of writing this text, the exercises address, among others, the following environmental problems:

- *The CO₂ problem.* Atmospheric CO₂ concentrations are described by an Earth-system box model that comprises carbon fluxes among the major Earth’s carbon reservoirs. The model is used to estimate the impact of anthropogenic activities (e.g., burning of fossil fuels, deforestation) on the atmospheric CO₂ concentrations and to explore the effects of certain mitigation strategies (e.g., ocean fertilisation). This exercise is an example of a linear model.
- *The ozone problem.* Ozone is a green-house gas and, at high concentrations, harmful to humans and animals. It also plays an important protective role by absorbing harmful UV radiation. The ozone model is used to test how anthropogenic emissions of NO (nitric oxide) due to combustion or burning of fuels alter the natural ozone dynamics in the lower atmosphere. It is an example of a “typical” chemistry model.
- *Ocean acidification.* This is a very complex problem as it deals with equilibrium chemistry. The topic is introduced by three exercises of increasing complexity. A more extensive model dealing with ocean acidification is not part of the mandatory course material, but is provided as auxiliary material that students may consult if they are interested in the topic (see below).
- *The COVID pandemic.* An epidemiological model (so-called SIR model) is developed to describe the spread of the SARS-CoV2 (corona) virus within a population. In addition to infection and recovery, the model includes hospitalisations, mortality, vaccination, and virus mutations. The students practice how to use information from epidemiologists (who are not modelers) to develop and apply such models.
- *Agricultural eutrophication.* This model describes how fertilization with nutrients affects the competition between crops and weeds, and explores the impact of different fertilization strategies on agricultural run-off. In addition to ecological interactions, the model also contains a (simplistic) economic component that lets students explore the monetary aspects of farming.

¹<https://www.youtube.com/playlist?list=PLx8PHcDdmF-uD1Pr07TU9SzhlGpfrxqn>

- *Dead zones in a river.* This one-dimensional reaction-transport model describes the distribution of dissolved oxygen concentrations in a river subjected to excessive input of nutrients (ammonia). The model is used to estimate the maximal nutrient input that can be allowed to keep the minimal oxygen concentration above a certain critical level.

Additional exercise topics include

- introduction to R for modellers,
- making of conceptual diagrams and formulating of mass balance equations,
- dissolution of silica particles (e.g., diatom frustules),
- bacteria-mediated mineralisation of detritus,
- early diagenesis in marine sediments (a simplified P cycle, and the coupled cycles of C, N, O, and S),
- food web modelling of a lake or river ecosystem,
- competition between plants in grasslands,
- competition between floating plants and algae in shallow lakes,
- virus dynamics in the ocean,
- bio-economic modelling of a Scallop aquaculture.

New material can be added in the future, thus creating a repository from which modules can be selected based on students' interests that vary from year to year.

Auxiliary material

In addition to tutorials and exercises, the RTM package provides a number of smaller readers that explain various topics in somewhat greater detail. Their aim is to satisfy the curiosity of students with the greatest motivation to learn modelling in R. The topics covered in these readers are not compulsory for the course, so the students get to see them after the mid-term exam, but before they start to work on their final projects. They include

- implementation of *events* in dynamic models developed in R,
- use of *forcing functions* based on data in models developed in R,
- display of *observed data* alongside model results in R,
- *fitting* of a 1D reaction-transport model to data in R,
- *visualisation* of multi-dimensional outputs from a 1D reaction-transport model in R,
- modelling of *pH dynamics* in a 1D reaction-transport model in R,
- mathematical analysis of the response of a system to a *perturbation from an equilibrium*,
- development of *interactive applications* in R,
- the basics about the *numerical methods* used for reaction-transport modelling in R,
- the basics about collaborative model development via *git*.

Model templates

Although students develop their models from scratch, they do not necessarily start from an empty sheet when implementing them in R. Instead, they start from a number of R Markdown templates that are provided by the RTM package. Thus, rather than becoming easily confused or frustrated by the need to generate a syntactically correct R-code, students can focus on the implementation of the modelled processes and generation and visualisation of outputs using R-code chunks provided by the templates. The templates included in the package facilitate the development of

- dynamic models without the spatial component (*RTM_0D*),
- dynamic one-dimensional reaction-transport models (*RTM_1D*),
- dynamic one-dimensional reaction-transport models in porous media (*RTM_porous1D*).

Additionally, they include templates used in some of the exercises, including models that deal with

- local equilibrium chemistry (*RTM_equilibrium*),

- a basic food-web and element cycling model in an aquatic ecosystem (*RTM_npzd*).

Final projects

After completing the tutorials, exercises, and the written mid-term exam, students proceed with a work on a larger project of their choice. This involves the development of a model about a specific environmental topic and is done in small groups of 2–4 people. In contrast to the exercises made in the classroom, they do this with less guidance from the tutors. They also need to document their work in a written report, where they outline the scientific rationale, describe their model (including assumptions and implementation), and present and interpret the results, much like they would do when writing a scientific paper. Note that the topics of these final projects are *not* part of the RTM package.

Workflow example

We recommend that students use *RStudio* to learn and develop their models in R. At the beginning of the course, students install the RTM package. At present, this is done using the R-command

```
devtools::install_github("dynamic-R/RTM", depend=TRUE)
```

Loading the package into R implements the following public functions: `RTMtutorial()`, `RTMexercise()`, `RTMtemplate()`, and `RTMreader()`. Additionally, it implements the private function `RTManswer()`.

Tutorials

The list of available tutorials (Table 1) is displayed by using the R-command

```
RTMtutorial()
```

Table 1: List of available tutorials provided by the RTM package.

	x	description
1	introduction	About the modelling course at Utrecht University
2	why	Why is modelling useful?
3	conceptual	Making conceptual models
4	massbalance	Creating mass balance equations
5	Rmodels	Dynamic modelling in the R language
6	largescale	Large-scale models (e.g. System-Earth’s carbon cycle)
7	chemical	Elementary chemical reactions
8	equilibrium	Equilibrium (reversible) chemical reactions
9	enzymatic	Enzymatic reactions
10	partitioning	Partitioning between phases
11	ecology	Ecological interactions
12	transportProcesses	The general reaction-transport equation
13	transportFluxes	Transport fluxes due to advection and diffusion/dispersion
14	transportPorous	Reaction-transport in porous media
15	transportBoundaries	Boundary conditions in reaction-transport models
16	transportR	Implementation of reaction-transport models in R

A specific tutorial is started by including the name, or the corresponding index, of the tutorial as the input argument to `RTMtutorial()`. For example, the “ecology” tutorial is started using one of the following commands:

```
RTMtutorial("ecology")
RTMtutorial(11)
RTMtutorial("ecology", output = "RMD")
```

The first two commands open the tutorial in a web browser. In case this fails, the third command can be used to open the tutorial's R Markdown file in the *RStudio* editor. Subsequently, the tutorial is started by clicking the “Run Document” button at the top of the editor window.

The first item in the tutorial provides a link to a short knowledge clip and a reference to chapters in the course textbook (Figure 1). These two resources are used to explain the theory behind the topics covered in the class.

RTM course - Ecological Rate Laws

Karlina Soetaert and Lubos Polerecky
June 2021

Tutorial
Ecological interactions: virus infection
Ecological interactions: predation
Ecological interactions: algal N-uptake
Simple differential equations - I
Simple differential equations - II
Simple differential equations - III
Interactive differential equations
Logistic model
Logistic curve
Recognizing rate expressions
Biochemistry: Bacterial uptake of DOC
Implementation in R
More exercises
References

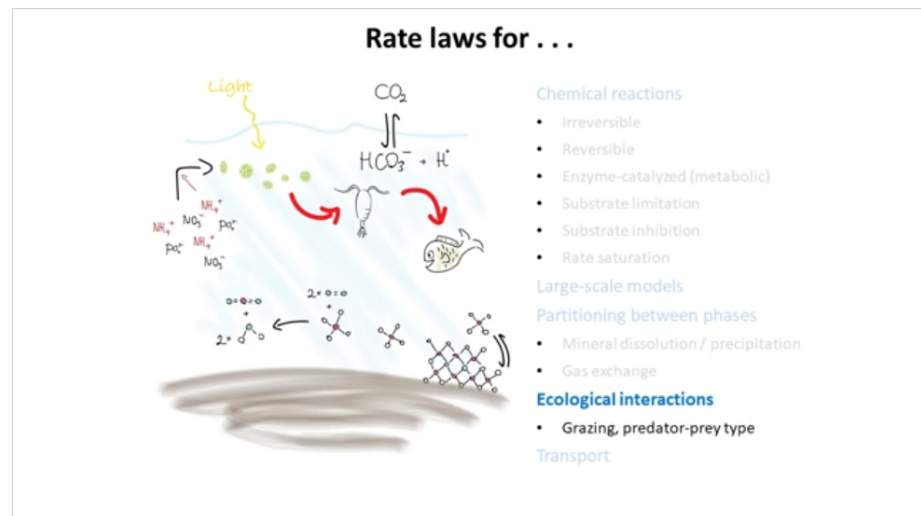
Start Over

Tutorial

You are advised to watch the following video first.

Video timeline

- 0:00 Worker vs. Resource (limitation, inhibition)
- 2:21 Logistic growth model
- 4:49 Lotka-Volterra model



You can also read the following section(s) of the textbook:

- Chapter 2.5. Basic Formulation of Ecological Interactions
- Chapter 2.6. Coupled Model Equations
- Chapter 2.7. Model Simplifications

(You can download each chapter of the textbook via the e-book University library for free!)

Continue

Figure 1: An example of a tutorial provided by the RTM package. Each tutorial starts with a short knowledge clip and a reference to chapters in the course textbook.

Subsequently, students proceed by clicking on any of the quiz-like questions listed in the left panel. After selecting and submitting an answer (Figure 2, top), students receive feedback that explains the rationale behind the correct answer (Figure 2, middle). Each tutorial ends with a list of exercises that students should be able to solve after they have understood the material covered in the tutorial (Figure 2, bottom). These exercises are solved by the students in the classroom under the supervision of the tutors.

RTM course - Ecological Rate Laws

Karline Soetaert and Lubos Polerecky
June 2021

Tutorial
Ecological interactions: virus infection
Ecological interactions: predation
Ecological interactions: algal
N-uptake
Simple differential equations - I
Simple differential equations - II

Ecological interactions: virus infection

In a population comprising individuals that are *susceptible* to a virus and *infected* by a virus, infection can be modelled as a process similar to an elementary chemical reaction: a susceptible person can become infected if he/she "collides" with an infected person. Suppose that the *probability* that a susceptible person meets an infected person, whereby this encounter leads to the susceptible person becoming infected, is described by a parameter b (in units of $\text{ind}^{-1} \text{d}^{-1}$). The amounts of susceptible and infected individuals in the population are denoted by S and I , respectively.

What is a suitable expression for the infection rate?

- ☐ $\text{InfectionRate} = b \times (S + I)$
- ☐ $\text{InfectionRate} = b \times S$
- ☐ $\text{InfectionRate} = b \times I$
- ☒ $\text{InfectionRate} = b \times S \times I$
- ☐ $\text{InfectionRate} = S \times \frac{I}{I+b}$
- ☐ $\text{InfectionRate} = b \times I^2 \times S$

Submit Answer

Previous Topic

Next Topic

RTM course - Ecological Rate Laws

Karline Soetaert and Lubos Polerecky
June 2021

Tutorial
Ecological interactions: virus infection
Ecological interactions: predation
Ecological interactions: algal
N-uptake
Simple differential equations - I
Simple differential equations - II
Simple differential equations - III
Interactive differential equations

Ecological interactions: virus infection

In a population comprising individuals that are *susceptible* to a virus and *infected* by a virus, infection can be modelled as a process similar to an elementary chemical reaction: a susceptible person can become infected if he/she "collides" with an infected person. Suppose that the *probability* that a susceptible person meets an infected person, whereby this encounter leads to the susceptible person becoming infected, is described by a parameter b (in units of $\text{ind}^{-1} \text{d}^{-1}$). The amounts of susceptible and infected individuals in the population are denoted by S and I , respectively.

What is a suitable expression for the infection rate?

- ☐ $\text{InfectionRate} = b \times (S + I) \times$
- ☐ $\text{InfectionRate} = b \times S \times$
- ☐ $\text{InfectionRate} = b \times I \times$
- ☒ $\text{InfectionRate} = b \times S \times I \checkmark$
- ☐ $\text{InfectionRate} = S \times \frac{I}{I+b} \times$
- ☐ $\text{InfectionRate} = b \times I^2 \times S \times$

To become infected, a susceptible person needs to 'collide' with *one* infected person. Therefore, the infection rate is *first-order* with respect to the infected and susceptible persons, i.e., $\text{InfectionRate} = b \times S \times I$. The proportionality constant, b , describes the probability (expressed per individual per day) that a susceptible person meets an infected person and their encounter results in the susceptible person becoming infected.

Previous Topic

Next Topic

RTM course - Ecological Rate Laws

Karline Soetaert and Lubos Polerecky
June 2021

Tutorial
Ecological interactions: virus infection

More exercises

To learn more about modelling of ecological interactions, solve additional exercises available in the R-package RTM. To display these exercises, type one of the following commands in the R-console:

```
require(RTM)
RTMexercise("detritus")
RTMexercise("COVID")
RTMexercise("npzd")
RTMexercise("crops_weeds")
```

Previous Topic

Next Topic

Figure 2: An example of a tutorial provided by the RTM package. Top and middle panel shows a question just before and just after submitting the answer, respectively. Bottom panel shows a list of extra exercises recommended after the completion of the tutorial.

Exercises

The list of available exercises (Table 2) is displayed by using the R-command

`RTMexercise()`

Table 2: List of available exercises provided by the RTM package.

	x	description	type
2	conceptual	Translating problems into a conceptual diagram	massbalance
3	massbalance_chemistry	Creating mass balance equations in chemistry	massbalance
4	massbalance_ecology	Creating mass balance equations in ecology	massbalance
5	carbonCycle	An Earth-system box model of the carbon cycle	linearmodels
6	ozone	Ozone dynamics in the troposphere	chemistry
7	dissolutionSi	Dissolution kinetics of Si particles	chemistry
8	equilibriumNH3	Equilibrium chemistry - ammonium/ammonia	chemistry
9	equilibriumHCO3	Equilibrium chemistry - the carbonate system	chemistry
10	equilibriumOMD	Equilibrium chemistry - impact of mineralisation on pH	chemistry
11	detritus	Bacterial decay of detritus	biogeochemistry
12	npzd	nutrients, phytoplankton, zooplankton, detritus	biogeochemistry
13	crops_weed	Crops and weed competition for nutrients	biogeochemistry
14	COVID	The COVID pandemic (population dynamics)	epidemiology
15	virus	Virus dynamics in the ocean	epidemiology
16	bears_salmon	Foodweb model comprising bears, salmon and scavengers	ecology
17	plant_coexistence	Competition and coexistence of plants in grasslands	ecology
18	hyacinth_algae	Competition between floating plants and algae	ecology
19	aquaculture	Model of scallop aquaculture, including economics	individualbased
20	riverAnoxia	Anoxia in an estuary (1-D model)	reaction_transport
21	Pdiagenesis	Simple phosphorus diagenesis in marine sediments (1D)	reaction_transport
22	diagenesis	Complex diagenesis in marine sediments (C,N,O ₂ ,S)	reaction_transport

A specific exercise is displayed by including the name, or the corresponding index, of the exercise as the input argument to `RTMexercise()`. For example, the “covid” exercise is started using one of the following commands:

```
RTMexercise("covid")
RTMexercise(14)
RTMexercise("covid", output = "PDF")
```

By default, the exercise is converted into a HTML format and displayed in a web browser. Additional output formats include RMD, PDF, or WORD. Note that the PDF option requires an installation of L^AT_EX, while the WORD option requires an installation of programs such as Microsoft Word or LibreOffice.

Exercise solutions are also provided within the RTM package. They can be used by students to compare their solutions to those worked out by us, which helps them learn how to write models more efficiently. They can also gain ideas how to start or make a certain step in the model development if they are unable to do so on their own. Students are advised to check the solutions only *after* they have tried their best to solve the exercise on their own, and it is their responsibility whether they follow this advice or not. Answer to a specific exercise (e.g., “covid”) is displayed using the R-command

```
RTM::RTManswer("covid", output = <output>)
```

where the <output> format is one of "HTML", "PDF", "WORD", or "RMD".

Templates

In one of the tasks in the “covid” exercise, students are asked to develop a model that describes the spread of a viral infection in a population of susceptible, infected and recovered individuals (the so-called SIR model). To implement the model in R, they are offered the possibility to use a template R Markdown file rather than start from a blank sheet.

The list of available templates (Table 3) is displayed by using the R-command

```
RTMtemplate()    ### note that presently this does not work. one must use (x = "?")
```

Table 3: List of available templates provided by the RTM package.

	x	description
1	rtm0D	Template for models in 0D
2	rtm1D	Template for reaction-transport models in 1D
3	porous1D	Template for reaction-transport models in porous media in 1D
4	porous1D_extensive	Template for reaction-transport models in porous media in 1D (with text)
5	rtmEquilibrium	Template for local equilibrium chemistry model
6	npzd	Template to be used for the NPZD exercise
7	rmarkdown_small	Template to be used for the introductionR exercise

A specific template file is opened by including the name, or the corresponding index, of the template as the input argument to `RTMtemplate()`. Alternatively, one can access it via the *RStudio* menu File → New File → R Markdown → From Template.

For the “covid” exercise, the template `RTM_OD.Rmd` is recommended. This template is opened using one of the R-commands

```
RTMtemplate("rtm0D")
RTMtemplate(1)
```

The core part of the template file is shown in Figure 3 (left panel). Using this template and the differential equations that the students formulated in the first part of the exercise, it should not be too difficult for them to implement the model in R. All they need to do is to modify the R-chunks where the initial values of the state variables, model parameters, rate expressions, mass balance equations (i.e., time-derivatives of the state variables), and extra output of the model function (e.g., process rates) are defined and the model is solved, as indicated in Figure 3 (right panel).

Auxiliary material

The list of extra readers (Table 4), which are used as auxiliary material in the course for students that wish to explore specific topics in greater depth, is displayed by using the R-command

```
RTMreader()
```

Table 4: List of extra readers provided by the RTM package.

	x	description
1	events	Events in dynamic models developed in R
2	forcings	Forcing functions based on data in models developed in R
3	observations	Showing observed data alongside model results in R
4	fitting	Fitting a 1D reaction-transport model to data in R
5	visualisation	Visualising outputs from a 1D reaction-transport model in R

	x	description
6	pHprofiles	Estimating pH in a 1D reaction-transport model in R
7	perturbation_I	Response of systems to a perturbation from equilibrium - Part I
8	perturbation_II	Response of systems to a perturbation from equilibrium - Part II
9	interactive	Developing interactive applications in R
10	numericalR	Numerical methods used for reaction-transport modelling in R
11	git_sharing_code	Sharing code with the world via Git in RStudio

A specific reader is opened by including the name, or the corresponding index, of the template as the input argument to `RTMreader()`.

In one of the tasks in the “covid” exercise, students are asked to enhance their SIR model by considering that in order to curb the spread of the viral infection, the society takes measures by temporarily reducing social interactions by 90% between days 30 and 70 after the viral outbreak. One way to model this is by introducing a parameter *sInt* that is dynamically lowered from 1 to 0.1 during this time interval and then used as a factor to lower the infection rate constant *b*. A convenient way to implement such a model in R is through the use of a forcing function. The reader that explains the use of forcing functions in dynamic R-models is generated using the R-command

```
RTMreader("forcings", output="PDF")
```

By studying this reader, students will learn that all they need to do to implement such temporary measures in their model is to implement a forcing function based on data, add a forcing function as one of the input arguments of the model function, and include the forcing function when solving the model (Figure 4).

Conclusion

The RTM package contains tutorials, exercises, model templates, and extra readers that students study and work through during the course *Reactive transport modeling in the Hydrosphere* (taught at Utrecht University, The Netherlands) or *Environmental modelling* (taught at Ghent University, Belgium). Anyone who wants to learn environmental or reaction-transport modelling can consult the tutorials and make the exercises. The answers are also provided, and can be viewed using the R-command `RTM:::RTManswer()`.

New material can be added in the future, thus creating a repository from which modules can be selected based on students’ interests that vary from year to year.

References

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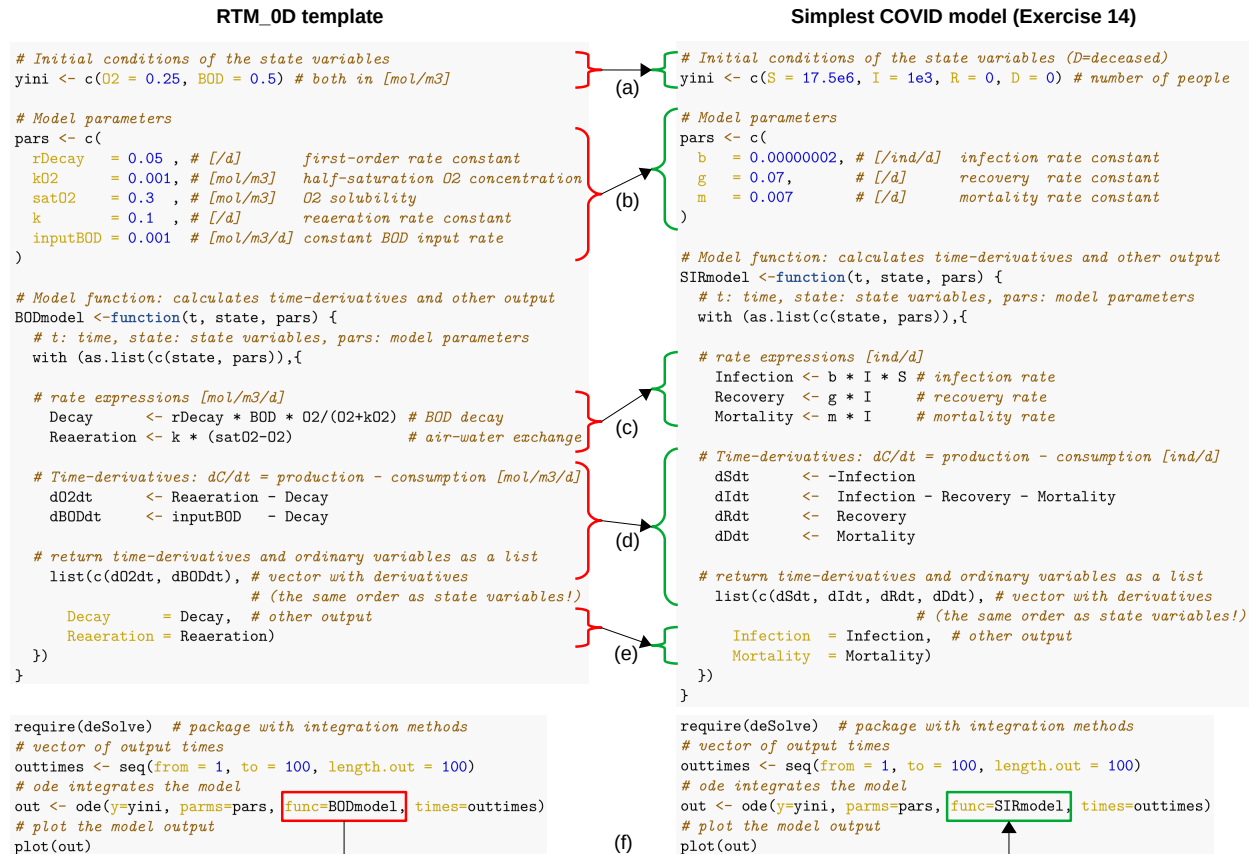


Figure 3: Core part of R Markdown files for solving dynamic models in 0D. Left panel shows the template, right panel shows the modified code implementing a simple SIR model. The different R-chunks are used to define the initial values of the state variables (a), model parameters (b), rate expressions (c), mass balance equations (d), and extra output of the model function (e). The R-chunk on the bottom solves the model depending on the model function (f) and plots the solution.

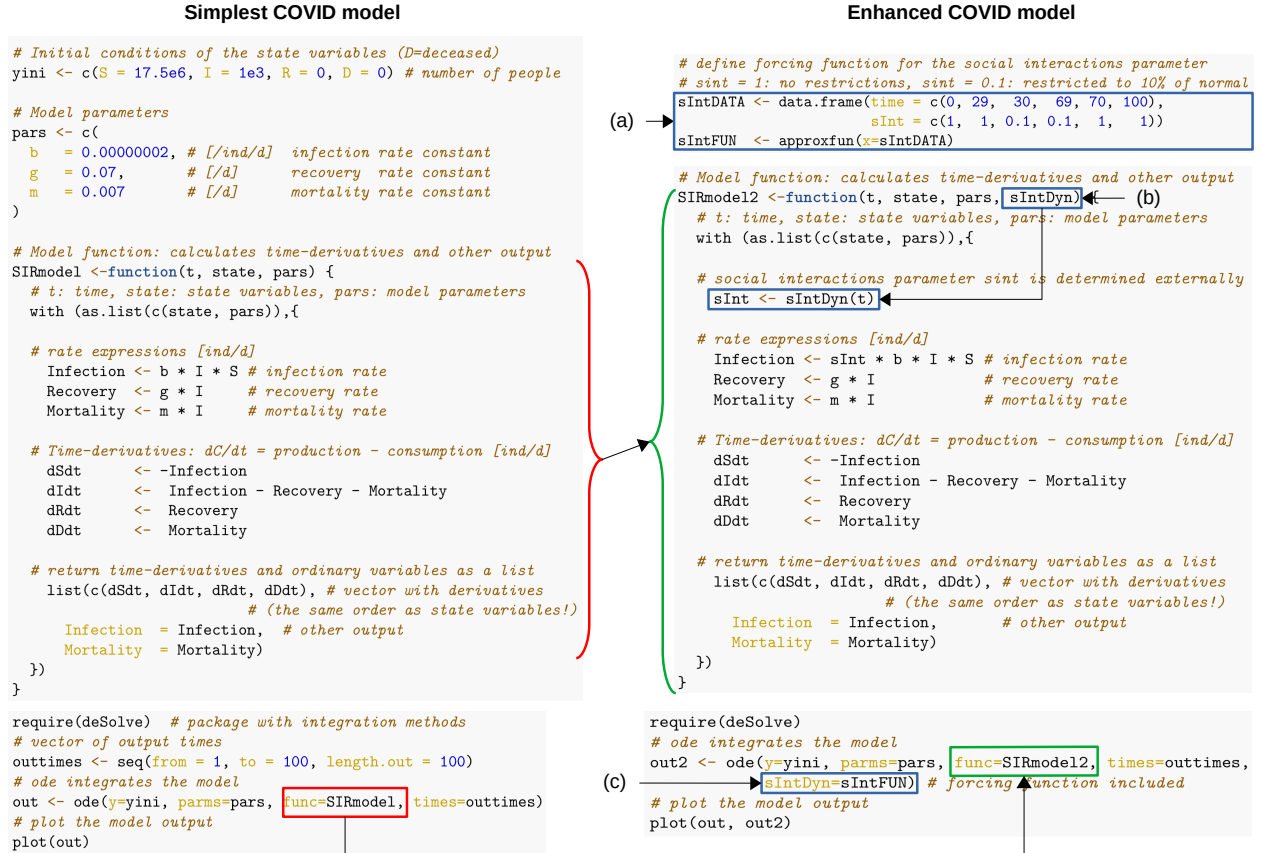


Figure 4: Core parts of the simplest and enhanced COVID model. The simplest model is reproduced from the right panel in Figure 3. The enhanced model is developed by implementing the forcing function based on data (a), adding a forcing function as input of the model function (b), and including the forcing function when solving the model (c).