



**GALAHAD** RAND

PACKAGE SPECIFICATION

GALAHAD Optimization Library version 2.1

#### 1 SUMMARY

GALAHAD\_RAND is a suite of Fortran procedures for generating uniformly distributed pseudo-random numbers. Random reals are generated in the range  $0 < \xi < 1$  or the range  $-1 < \eta < 1$  and random integers in the range  $1 \le k \le N$  where N is specified by the user.

A multiplicative congruent method is used where a 31 bit generator word g is maintained. On each call to a procedure of the package,  $g_{n+1}$  is updated to  $7^5g_nmod(2^{31}-1)$ ; the initial value of g is  $2^{16}-1$ . Depending upon the type of random number required the following are computed  $\xi = g_{n+1}/(2^{31}-1)$ ;  $\eta = 2\xi - 1$  or  $k = \text{integer part } \xi N + 1$ .

The package also provides the facility for saving the current value of the generator word and for restarting with any specified value.

ATTRIBUTES — Versions: GALAHAD\_RAND\_single, GALAHAD\_RAND\_double, Uses: None. Date: March 2001. Origin: N. I. M. Gould and J. K. Reid, Rutherford Appleton Laboratory. Language: Fortran 95 + TR 15581 or Fortran 2003.

## 2 HOW TO USE THE PACKAGE

Access to the package requires a USE statement such as

Single precision version

USE GALAHAD\_RAND\_single

Double precision version

USE GALAHAD\_RAND\_double

If it is required to use both modules at the same time, the derived type RAND\_seed (Section 2.1) and the sub-routinesRAND\_random\_real, RAND\_random\_integer, RAND\_get\_seed, and RAND\_set\_seed (Section 2.2) must be renamed on one of the USE statements. Their seeds will be independent.

### 2.1 The derived data types

The user must provide a variable of derived type RAND\_seed to hold the current seed value which must be passed to all calls of RAND. The seed value component is private and can only be set and retrieved through the RAND\_set\_seed and RAND\_get\_seed entries.

## 2.2 Argument lists and calling sequences

There are five procedures for user calls. The initialization entry must be called before any call to the RAND\_random\_real, RAND\_random\_integer and RAND\_get\_seed entries.

## 2.2.1 Subroutine to initialize the generator word

This entry must be called first to initialize the generator word.

CALL RAND\_initialize( seed )

seed is a scalar INTENT (OUT) argument of derived type RAND\_seed that holds the seed value.

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#### 2.2.2 Subroutine to obtain a random real value

A random real value may be obtained as follows:

```
CALL RAND_random_real( seed, positive, random_real )
```

seed is a scalar INTENT (INOUT) argument of derived type RAND\_seed that holds the seed value.

positive is a scalar INTENT(IN) argument of type default LOGICAL. If positive is .TRUE., the generated random number is a real value in the range  $0 < \xi < 1$ , while if positive is .FALSE., the generated random number is a real value in the range  $-1 < \eta < 1$ .

random\_real is a scalar INTENT(OUT) argument of type REAL (double precision in GALAHAD\_RAND\_double). It is set to the required random number.

## 2.2.3 Subroutine to obtain a random integer value

A random integer value may be obtained as follows:

```
CALL RAND_random_integer( seed, n, random_integer )
```

seed is a scalar INTENT (INOUT) argument of derived type RAND\_seed that holds the seed value.

is a scalar INTENT (IN) argument of type default INTEGER. It must be set by the user to specify the upper bound for the range  $1 \le k \le n$  within which the generated random number k is required to lie. **Restriction:** n must be positive.

random\_integer is a scalar INTENT(OUT) argument of type default INTEGER. It is set to the required random integer k.

#### 2.2.4 Subroutine to obtain the current generator word

The current generator word may be obtained as follows:

```
CALL RAND_get_seed( seed, value )
```

seed is a scalar INTENT(IN) argument of derived type RAND\_seed that must be provided to hold the seed value.

value is a scalar INTENT(OUT) argument of type default INTEGER. It is set to the current value of the generator word g.

## 2.2.5 Subroutine to reset the current value of the generator word

The current value of the generator word may be reset as follows:

```
CALL RAND_set_seed( seed, value )
```

seed is a scalar INTENT (OUT) argument of derived type RAND\_seed that holds the seed value.

value is a scalar INTENT(IN) argument of type default INTEGER that must be set by the user to the required value of the generator word. It is recommended that the value should have been obtained by a previous call of RAND\_get\_seed. It should have a value in the range  $0\ LT$  value  $\le$  P, where P =  $2^{31}-1=2147483647$ . If it is outside this range, the value value mod( $2^{31}-1$ ) is used.

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## **GENERAL INFORMATION**

Use of common: None.

Workspace: None.

Other routines called directly: None.

Other modules used directly: None.

Input/output: None. **Restrictions:** n > 0.

**Portability:** ISO Fortran 95 + TR 15581 or Fortran 2003. The package is thread-safe.

## **METHOD**

The code is based on that of L.Schrage, "A More Portable Fortran Random Number Generator", TOMS, 5(2) June 1979. The method employed is a multiplicative congruential method. The generator word g is held as an integer and is updated on each call as follows

$$g_{n+1} = 7^5 g_n mod(2^{31} - 1)$$

The result returned from RAND\_random\_real, for a non-negative argument, is  $\xi$ , where

$$\xi = g_{n+1}/(2^{31}-1)$$

and for a negative argument is

$$2\xi - 1$$
.

The value of k returned by RAND\_random\_integer is

integer part  $\xi N + 1$ .

# **EXAMPLE OF USE**

Suppose we wish to generate two random real numbers lying between plus and minus one, reset the generator word to its original value, and then find two positive random integers with values no larger than one hundred. Then we might use the following piece of code.

```
PROGRAM GALAHAD_RAND_spec
  USE GALAHAD_RAND_double
  IMPLICIT NONE
  TYPE (RAND_seed) seed
  INTEGER :: random_integer, value
  REAL ( kind = KIND( 1.0D+0 ) ) :: random_real
! Initialize the generator word
  CALL RAND_initialize( seed )
! Get the current generator word
  CALL RAND_get_seed( seed, value )
  WRITE( 6, "( ' generator word = ', I10 )" ) value
! Generate a random real in [-1, 1]
  CALL RAND_random_real( seed, .FALSE., random_real )
```

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```
WRITE( 6, "( ' random real = ', F10.2 )" ) random_real
! Generate another random real
  CALL RAND_random_real( seed, .FALSE., random_real )
  WRITE( 6, "( ' second random real = ', F10.2 )" ) random_real
! Restore the generator word
  CALL RAND_set_seed( seed, value )
! Generate a random integer in [1, 100]
  CALL RAND_random_integer( seed, 100, random_integer )
  WRITE( 6, "( ' random integer = ', I3 )" ) random_integer
! Generate another random integer
  CALL RAND_random_integer( seed, 100, random_integer )
  WRITE( 6, "( ' second random integer = ', I3 )" ) random_integer
  END PROGRAM GALAHAD_RAND_spec
```

## This produces the following output:

```
generator word = 65535
random real = 0.03
second random real = -0.34
random integer = 52
second random integer = 33
```

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