16-715: Advanced Robot Dynamics and Simulation

Fall 2021

Course Description

This course explores the fundamental mathematics behind modeling the physics of robots, as well as state-of-the-art algorithms for robot simulation. We will review classical topics like Lagrangian mechanics and Hamilton's Principle of Least Action, as well as modern computational methods like discrete mechanics and fast linear-time algorithms for dynamics simulation. A particular focus of the course will be rigorous treatments of 3D rotations and non-smooth contact interactions (impacts and friction) that are so prevalent in robotics applications. We will use numerous case studies to explore these topics, including quadrotors, fixed-wing aircraft, wheeled vehicles, quadrupeds, humanoids, and manipulators. Homework assignments will focus on practical implementation of algorithms and a course project will encourage students to apply simulation methods to their own research.

Prerequisites: Strong linear algebra skills, experience with a high-level programming language like Python, MATLAB, or Julia, and basic familiarity with ordinary differential equations.

Instructors

Prof. Zac Manchester	**Email:** zacm@cmu.edu
TA: Kevin Tracy	**Email:** ktracy@andrew.cmu.edu

Logistics

- Lectures will be held Tuesdays and Thursdays 10:10–11:30 AM Eastern time in NSH 1305.
- Office hours will be TODO: based on survey.
- Homework assignments will be due by 11:59 PM Eastern time on Wednesdays. Two weeks will be given to complete each assignment.
- GitHub will be used to distribute and collect assignments.
- Slack will be used for general discussion and Q&A outside of class and office hours.
- There will be no exams. Instead, each student will complete a project on a topic of their choice.

Learning Objectives

By the end of this course, students should be able to:

1. Derive differential equations for simple mechanical systems using classical Newton-Euler and Lagrangian techniques
2. Model more complex industrial, wheeled, legged, aerial, underwater, and space robotic systems using modern computational techniques
3. Simulate environmental contact interactions like impacts and Coulomb friction
4. Understand the trade-offs and limitations of different dynamics formulations and simulation techniques
5. Build high-performance simulation tools that can be deployed in machine learning and control design applications

Learning Resources

There is no textbook required for this course. Video recordings of lectures and lecture notes will be posted online. Additional references for further reading will be provided with each lecture.

Homework

Homework will be posted every 2 weeks and students will be given at least one full week to complete assignments. All homework will be distributed and collected using GitHub. Solutions and grades will be returned within one week of homework due dates.

Grading

Grading will be based on:

- 50% Project
- 40% Homeworks
- 10% Participation

Attendance during lectures is not required to earn a full participation grade. Students can also participate through any combination of office hours, Slack discussions, project presentations, and by offering constructive feedback about the course to the instructors.

Course Policies

Late Homework: Students are allowed a budget of 6 late days for turning in homework with no penalty throughout the semester. They may be used together on one assignment, or separately on two assignments. Beyond these six days, no other late homework will be accepted.

Accommodations for Students with Disabilities: If you have a disability and are registered with the Office of Disability Resources, I encourage you to use their online system to notify me of your accommodations and discuss your needs with me as early in the semester as possible. I will work with you to ensure that accommodations are provided as appropriate. If you suspect that

you may have a disability and would benefit from accommodations but are not yet registered with the Office of Disability Resources, I encourage you to contact them at access@andrew.cmu.edu.

Statement of Support for Students' Health & Well-Being: Take care of yourself. Do your best to maintain a healthy lifestyle this semester by eating well, exercising, avoiding drugs and alcohol, getting enough sleep, and taking some time to relax. This will help you achieve your goals and cope with stress.

If you or anyone you know experiences any academic stress, difficult life events, or feelings like anxiety or depression, we strongly encourage you to seek support. Counseling and Psychological Services (CaPS) is here to help: call 412-268-2922 and visit http://www.cmu.edu/counseling. Consider reaching out to a friend, faculty, or family member you trust for help getting connected to the support that can help.

If you or someone you know is feeling suicidal or in danger of self-harm, call someone immediately, day or night:

CaPS: 412-268-2922
Re:solve Crisis Network: 888-796-8226

If the situation is life threatening, call the police:

On campus: CMU Police: 412-268-2323
Off campus: 911

If you have questions about this or your coursework, please let me know. Thank you, and have a great semester.

Tentative Schedule

Week	Dates	Topics	Assignments
1	Aug 31	Course Overview & Review of Newtonian Mechanics Concepts	
	Sep 2	Particles, Pendulums, and Orbits	
2	Sep 7	Energy and Stability	HW 1 Out
	Sep 9	Numerical Solution of ODEs and Runge-Kutta Methods	
3	Sep 14	No Class	
	Sep 16	Rigid Bodies, Euler's Equation, and Lie Groups	
4	Sep 21	Quaternions and Numerical Simulation	HW 1 Due
	Sep 23	Quadrotors, Airplanes, and Spacecraft	HW 2 Out
5	Sep 28	Constrained Optimization Pt. 1	
	Sep 30	The Least-Action Principle	
6	Oct 5	Coordinates, Constraints, and Manifolds	HW2 Due
	Oct 7	D'Alembert, Virtual Work, and Generalized Forces	HW3 Out
7	Oct 12	Lagrangian Mechanics and Manipulators	
	Oct 14	No Class	
8	Oct 19	Momentum, Duality, and the Hamiltonian	
	Oct 21	Lie Algebras and Euler's Equation from a Lagrangian	
9	Oct 26	Discrete Mechanics and Variational Integrators	HW3 Due
	Oct 28	Constrained Optimization Pt. 2	
10	Nov 2	Impacts as Inequality Constraints	HW4 Out
	Nov 4	Coulomb Friction and The Maximum Dissipation Principle	
11	Nov 9	Legged Robots and Hybrid Systems	
	Nov 11	Sparsity and Linear-Time Algorithms	
12	Nov 16	Case Studies	HW4 Due
	Nov 18	Case Studies	
13	Nov 23	Case Studies	
	Nov 25	No Class	
14	Nov 30	Project Presentations	
	Dec 2	Project Presentations	

Project Guidelines

Students should work in groups of 1–4 to complete a substantial final project. The goal is for students to apply the coarse content to their own research. Project proposals will be solicited in late September and topics will be selected in consultation with the instructors.

Project grades will be based on a short presentation given during the last week of class and a final report submitted via Google drive by May 18 Anywhere on Earth. Reports should be written in the form of a 6 page (plus references) ICRA or IROS conference paper using the standard two-column IEEE format. Sections should include an abstract, introduction and/or background to motivate your problem, 2–3 main technical sections on your contributions, conclusions, and references. Grading will be based on the following criteria:

10%	Class presentation
10%	Adherence to IEEE formatting and length requirements
10%	Innovation & Creativity: Is what you did new/cool/interesting? Convince me.
30%	Clarity of presentation: Can I understand what you did from your writing + plots?
40%	Technical correctness: Are your results reasonable? Is your code correct?