

# Connecting Program Synthesis and Reachability:

## Automatic Program Repair using Test-Input Generation

ThanhVu (Vu) Nguyen\*,  
Westley Weimer<sup>†</sup>, Deepak Kapur<sup>‡</sup>, Stephanie Forrest<sup>‡</sup>

\*University of Nebraska, <sup>†</sup>University of Michigan, <sup>‡</sup>University of New Mexico

TACAS 2017

# Connecting Verification to Synthesis

## Program Verification

Checks if program satisfies a given spec



Significant research development, e.g.,  
formal methods, software testing

# Connecting Verification to Synthesis

## Program Verification

Checks if program satisfies a given spec



Significant research development, e.g.,  
formal methods, software testing

## Program Synthesis

Creates program that meets a given spec



Less work compared to verification,  
*"among the last tasks that computers will  
do well"*

# Connecting Verification to Synthesis

## Program Verification

Checks if program satisfies a given spec



Significant research development, e.g.,  
formal methods, software testing

## Program Synthesis

Creates program that meets a given spec



Less work compared to verification,  
*"among the last tasks that computers will  
do well"*

- **Implicit assumption:** verification and synthesis are related
  - Many verification techniques adopted to synthesize programs
  - Synthesis using constraint solving, program repairs using symexe, etc
- **Goal:** finding and formalizing this relation
  - Allow for comparisons between complexity and underlying structures
  - Leverage existing verification/synthesis techniques and tools to synthesize/check programs

# Contributions

## Relation between certain formulations of synthesis and verification

- Focus on *template-based synthesis* and view verification as *reachability* task
- Constructively prove that they are *equivalent*
  - ① Reduce template-based synthesis into a program consisting of a special loc, reachable only when code could be synthesized
  - ② Transform a reachability problem into a specific template-based synthesis instance, solvable only when the loc in the original problem is reachable
- Thus, reachability solvers can be used to generate code, and conversely, synthesis tools can be applied to check reachability

# Contributions

## Relation between certain formulations of synthesis and verification

- Focus on *template-based synthesis* and view verification as *reachability* task
- Constructively prove that they are *equivalent*
  - ① Reduce template-based synthesis into a program consisting of a special loc, reachable only when code could be synthesized
  - ② Transform a reachability problem into a specific template-based synthesis instance, solvable only when the loc in the original problem is reachable
- Thus, reachability solvers can be used to generate code, and conversely, synthesis tools can be applied to check reachability

## New *automatic program repair* technique

- Treat program repair as a form of template-based synthesis
- **CETI**: repair C programs violating *test-suite specification*
  - Use fault localization to rank suspicious stmts
  - Transform program, suspicious stmts, and test suite into reachability prob
  - Apply off-the-shelf test-input generation tool to find inputs
  - Map input values to changes allowing program to pass test suite

# Example: Synthesize Program Repairs

```
int isUp(int in,int up,int down){
    int bias, r;
    if (in)
        //fix: bias = up + 100
        bias = down;
    else
        bias = up;
    if (bias > down)
        r = 1;
    else
        r = 0;
    return r;
}
```

Test	Inputs			Output		Passed?
	in	up	down	expected	observed	
1	1	0	100	0	0	✓
2	1	11	110	1	0	✗
3	0	100	50	1	1	✓
4	1	-20	60	1	0	✗
5	0	0	10	0	0	✓
6	0	0	-10	1	1	✓

# Example: Synthesize Program Repairs

```
int isUp(int in,int up,int down){  
    int bias, r;  
    if (in)  
        //fix: bias = up + 100  
        bias = down;  
    else  
        bias = up;  
    if (bias > down)  
        r = 1;  
    else  
        r = 0;  
    return r;  
}
```

Test	Inputs			Output		Passed?
	in	up	down	expected	observed	
1	1	0	100	0	0	✓
2	1	11	110	1	0	✗
3	0	100	50	1	1	✓
4	1	-20	60	1	0	✗
5	0	0	10	0	0	✓
6	0	0	-10	1	1	✓

- Synthesize programs using *templates*,  
e.g., linear comb of variables:  $\boxed{c_0} + \boxed{c_1}v_1 + \boxed{c_2}v_2$



# Example: Synthesize Program Repairs

```
int isUp(int in,int up,int down){  
  int bias, r;  
  if (in)  
    //fix: bias = up + 100  
    bias = down;  
  else  
    bias = up;  
  if (bias > down)  
    r = 1;  
  else  
    r = 0;  
  return r;  
}
```

Test	Inputs			Output		Passed?
	in	up	down	expected	observed	
1	1	0	100	0	0	✓
2	1	11	110	1	0	✗
3	0	100	50	1	1	✓
4	1	-20	60	1	0	✗
5	0	0	10	0	0	✓
6	0	0	-10	1	1	✓

- Synthesize programs using *templates*,  
e.g., linear comb of variables:  $\boxed{c_0} + \boxed{c_1}v_1 + \boxed{c_2}v_2$
- Replace suspicious stmt `bias = down;` with  
`bias =  $\boxed{c_0} + \boxed{c_1}$ bias +  $\boxed{c_2}$ in +  $\boxed{c_3}$ up +  $\boxed{c_4}$ down;`

# Example: Synthesize Program Repairs

```
int isUp(int in,int up,int down){
  int bias, r;
  if (in)
    //fix: bias = up + 100
    bias = down;
  else
    bias = up;
  if (bias > down)
    r = 1;
  else
    r = 0;
  return r;
}
```

Test	Inputs			Output		Passed?
	in	up	down	expected	observed	
1	1	0	100	0	0	✓
2	1	11	110	1	0	✗
3	0	100	50	1	1	✓
4	1	-20	60	1	0	✗
5	0	0	10	0	0	✓
6	0	0	-10	1	1	✓

- Synthesize programs using *templates*,  
e.g., linear comb of variables:  $\boxed{c_0} + \boxed{c_1}v_1 + \boxed{c_2}v_2$
- Replace suspicious stmt `bias = down;` with  
`bias =  $\boxed{c_0}$  +  $\boxed{c_1}$ bias +  $\boxed{c_2}$ in +  $\boxed{c_3}$ up +  $\boxed{c_4}$ down;`
- Find unknowns  $\boxed{c_i}$  by creating and solving a special *reachability* instance

## Example: Constructing Reachability Instance

```
int isUp(int in,int up,int down){
    int bias, r;
    if (in)
        //template stmt
        bias = c0+c1bias+c2in+c3up+c4down;
    else
        bias = up;
    if (bias > down)
        r = 1;
    else
        r = 0;
    return r;
}
```

Test	Inputs			Output		Passed?
	in	up	down	expected	observed	
1	1	0	100	0	0	✓
2	1	11	110	1	0	✗
3	0	100	50	1	1	✓
4	1	-20	60	1	0	✗
5	0	0	10	0	0	✓
6	0	0	-10	1	1	✓

Transform the program, test suite, and template stmts into a program  $Q$  having:

- 1 the template code with the params  $c_i$  represented as *global vars*
- 2 a location  $L$  guarded by conditional expressions representing test cases

## Example: Constructing Reachability Instance

```
int isUp(int in,int up,int down){
    int bias, r;
    if (in)
        //template stmt
        bias = c0+c1bias+c2in+c3up+c4down;
    else
        bias = up;
    if (bias > down)
        r = 1;
    else
        r = 0;
    return r;
}
```

Test	Inputs			Output		Passed?
	in	up	down	expected	observed	
1	1	0	100	0	0	✓
2	1	11	110	1	0	✗
3	0	100	50	1	1	✓
4	1	-20	60	1	0	✗
5	0	0	10	0	0	✓
6	0	0	-10	1	1	✓

Transform the program, test suite, and template stmts into a program  $Q$  having:

- 1 the template code with the params  $\boxed{c_i}$  represented as *global vars*
- 2 a location  $L$  guarded by conditional expressions representing test cases

**Objective:** finding values for  $\boxed{c_i}$  allowing  $Q$  to reach  $L$

## Example: Solving Reachability Instance

```
int c0,c1,c2,c3,c4; //global inputs
```

```
int isUpP(int in,int up,int down){  
    int bias, r;  
    if (in)  
        //template stmt  
        bias = c0+c1bias+c2in+c3up+c4down;  
    else  
        bias = up;  
    if (bias > down)  
        r = 1;  
    else  
        r = 0;  
    return r;  
}
```

```
int main() {  
    if(isUpP(1, 0,100) == 0 &&  
        isUpP(1, 11,110) == 1 &&  
        isUpP(0,100, 50) == 1 &&  
        isUpP(1,-20, 60) == 1 &&  
        isUpP(0, 0, 10) == 0 &&  
        isUpP(0, 0,-10) == 1){  
  
        [L] //target location  
    }  
    return 0;  
}
```

## Example: Solving Reachability Instance

```
int c0,c1,c2,c3,c4; //global inputs
```

```
int isUpP(int in,int up,int down){  
    int bias, r;  
    if (in)  
        //template stmt  
        bias = c0+c1bias+c2in+c3up+c4down;  
    else  
        bias = up;  
    if (bias > down)  
        r = 1;  
    else  
        r = 0;  
    return r;  
}
```

```
int main() {  
    if(isUpP(1, 0,100) == 0 &&  
        isUpP(1, 11,110) == 1 &&  
        isUpP(0,100, 50) == 1 &&  
        isUpP(1,-20, 60) == 1 &&  
        isUpP(0, 0, 10) == 0 &&  
        isUpP(0, 0,-10) == 1){  
        [L] //target location  
    }  
    return 0;  
}
```

Reaching  $L$  means fixing the original program

- $L$  is reachable iff program passes all (6) tests
- Use values found for  $\boxed{c_i}$  to represent new (repaired) stmts

## Example: Solving Reachability Instance

```
int c0,c1,c2,c3,c4; //global inputs
```

```
int isUpP(int in,int up,int down){  
    int bias, r;  
    if (in)  
        //template stmt  
        bias = c0+c1bias+c2in+c3up+c4down;  
    else  
        bias = up;  
    if (bias > down)  
        r = 1;  
    else  
        r = 0;  
    return r;  
}
```

```
int main() {  
    if(isUpP(1, 0,100) == 0 &&  
        isUpP(1, 11,110) == 1 &&  
        isUpP(0,100, 50) == 1 &&  
        isUpP(1,-20, 60) == 1 &&  
        isUpP(0, 0, 10) == 0 &&  
        isUpP(0, 0,-10) == 1){  
        [L] //target location  
    }  
    return 0;  
}
```

Reaching  $L$  means fixing the original program

- $L$  is reachable iff program passes all (6) tests
- Use values found for  $\boxed{C_i}$  to represent new (repaired) stmts

Apply an off-the-self test-input generation tool

- E.g., KLEE determines  $c_0 = 100, c_1 = 0, c_2 = 0, c_3 = 1, c_4 = 0$
- Map to new stmt `bias = 100 + up;` that fixes the orig program

# Preliminaries

- Consider imperative language like C
- Include usual constructs (e.g., assignments, conditionals, loops, functions)
- Input a (potentially empty) tuple of values and output a value
- Consist of a finite set of functions, including a starting function  $\text{main}_p$
- Semantics are specified by a test suite of finite input/output pairs
- For simplicity, assume support for exceptions (e.g., C++ and Java)



## Reachability Problem

- Determines if a program can reach a given location
- Used in many verification tasks:
  - Model checking: check reachability of states representing bad behaviors
  - Test-input generation: produce inputs giving high program coverage
- Undecidable in general

## Reachability Problem

- Determines if a program can reach a given location
- Used in many verification tasks:
  - Model checking: check reachability of states representing bad behaviors
  - Test-input generation: produce inputs giving high program coverage
- Undecidable in general

### Definition:

Given a program  $P$ , set of program variables  $\{x_1, \dots, x_n\}$  and target location  $L$ , do there exist input values  $c_i$  such that the execution of  $P$  with  $x_i$  initialized to  $c_i$  reaches  $L$  in a finite number of steps?

## Reachability Problem

- Determines if a program can reach a given location
- Used in many verification tasks:
  - Model checking: check reachability of states representing bad behaviors
  - Test-input generation: produce inputs giving high program coverage
- Undecidable in general

### Definition:

Given a program  $P$ , set of program variables  $\{x_1, \dots, x_n\}$  and target location  $L$ , do there exist input values  $c_i$  such that the execution of  $P$  with  $x_i$  initialized to  $c_i$  reaches  $L$  in a finite number of steps?

```
int x, y; //global inputs

int P(){
  if (2 * x == y)
    if (x > y + 10)
      [L] //target location

  return 0;
}

//reaches L using x=-20,y=-40
```

## Template-based Synthesis

- Practical synthesis techniques work on partially-complete programs and generate code from specific forms or templates
- *Template*: express shape of program constructs and contain holes (template params), e.g.,  $\boxed{c_0} + \boxed{c_1} v_1 + \boxed{c_2} v_2$
- *Template program* contains stmts with templates (e.g.,  $s := \boxed{c_0} + \dots$ )
- To synthesize template programs, existing techniques
  - Encode the program *and the specs* as a logical formula  $f$
  - Use constraint solvers to find param values for  $c_i$  satisfying  $f$
  - Instantiate templates with the param values to produce complete program

## Template-based Synthesis

- Practical synthesis techniques work on partially-complete programs and generate code from specific forms or templates
- *Template*: express shape of program constructs and contain holes (template params), e.g.,  $\boxed{c_0} + \boxed{c_1} v_1 + \boxed{c_2} v_2$
- *Template program* contains stmts with templates (e.g.,  $s := \boxed{c_0} + \dots$ )
- To synthesize template programs, existing techniques
  - Encode the program *and the specs* as a logical formula  $f$
  - Use constraint solvers to find param values for  $c_i$  satisfying  $f$
  - Instantiate templates with the param values to produce complete program

### Definition:

Given a template program  $Q$  with a finite set of template params  $S = \{\boxed{c_1}, \dots, \boxed{c_n}\}$  and a finite test suite of input/output pairs  $T = \{(i_1, o_1), \dots, (i_m, o_m)\}$ , do there exist param values  $c_i$  such that

$$\forall (i, o) \in T . (Q[\boxed{c_1}, \dots, \boxed{c_n}])(i) = o?$$

# Template-based Synthesis

- Practical synthesis techniques work on partially-complete programs and generate code from specific forms or templates
- *Template*: express shape of program constructs and contain holes (template params), e.g.,  $\boxed{c_0} + \boxed{c_1}v_1 + \boxed{c_2}v_2$
- *Template program* contains stmts with templates (e.g.,  $s := \boxed{c_0} + \dots$ )
- To synthesize template programs, existing techniques
  - Encode the program *and the specs* as a logical formula  $f$
  - Use constraint solvers to find param values for  $c_i$  satisfying  $f$
  - Instantiate templates with the param values to produce complete program

## Definition:

Given a template program  $Q$  with a finite set of template params  $S = \{\boxed{c_1}, \dots, \boxed{c_n}\}$  and a finite test suite of input/output pairs  $T = \{(i_1, o_1), \dots, (i_m, o_m)\}$ , do there exist param values  $c_i$  such that

$$\forall (i, o) \in T. (Q[c_1, \dots, c_n])(i) = o?$$

```
int isUp(int in,int up,int down){
    int bias, r;
    if (in)
        //template stmt
        bias = c_0+c_1bias+c_2in+c_3up+c_4down;
    else
        bias = up;
    if (bias > down) r = 1;
    else r = 0;
    return r;
}

//Test suite
Q(1,0,100)=0
Q(1,11,110)=1
Q(0,100,50)=1
Q(1,-20,60)=1
Q(0,0,10)=0
Q(0,0,-10)=1

/*Passes test suite using
c_0=100,c_1=1,c_2=0,c_3=1,c_4=0*/
```

## Theorem 1: Template-based synthesis is Reducible to Reachability

**Reduction Sketch:** *GadgetS2R* reduces a template-based synthesis instance

$(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$  to a specific reachability problem  $(P, L)$ ,  
satisfiable iff the synthesis instance can be solved

## Theorem 1: Template-based synthesis is Reducible to Reachability

**Reduction Sketch:** *GadgetS2R* reduces a template-based synthesis instance  $(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$  to a specific reachability problem  $(P, L)$ , satisfiable iff the synthesis instance can be solved

- For every template param  $\boxed{c_i}$ , create a fresh global variables  $v_i$



## Theorem 1: Template-based synthesis is Reducible to Reachability

**Reduction Sketch:** *GadgetS2R* reduces a template-based synthesis instance

$(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$  to a specific reachability problem  $(P, L)$ , satisfiable iff the synthesis instance can be solved

- For every template param  $\boxed{c_i}$ , create a fresh global variables  $v_i$
- For every fun  $q \in Q$ , define a similar fun  $q_P \in P$  that has every reference to a  $c_i$  replaced with the corresponding var  $v_i$

## Theorem 1: Template-based synthesis is Reducible to Reachability

**Reduction Sketch:** *GadgetS2R* reduces a template-based synthesis instance  $(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$  to a specific reachability problem  $(P, L)$ , satisfiable iff the synthesis instance can be solved

- For every template param  $\boxed{c_i}$ , create a fresh global variables  $v_i$
- For every fun  $q \in Q$ , define a similar fun  $q_P \in P$  that has every reference to a  $c_i$  replaced with the corresponding var  $v_i$
- The test suite  $T$  as a conjunctive expression  $e$ :

$$e = \bigwedge_{(i,o) \in T} \text{main}_{Q_P}(i) = o$$

## Theorem 1: Template-based synthesis is Reducible to Reachability

**Reduction Sketch:** *GadgetS2R* reduces a template-based synthesis instance  $(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$  to a specific reachability problem  $(P, L)$ , satisfiable iff the synthesis instance can be solved

- For every template param  $\boxed{c_i}$ , create a fresh global variables  $v_i$
- For every fun  $q \in Q$ , define a similar fun  $q_P \in P$  that has every reference to a  $c_i$  replaced with the corresponding var  $v_i$
- The test suite  $T$  as a conjunctive expression  $e$ :

$$e = \bigwedge_{(i,o) \in T} \text{main}_{QP}(i) = o$$

- Starting function  $\text{main}_P$  consisting of conditional stmt leading to a target location  $L$  iff  $e$  is true

```
int mainP() {  
  if (e) [L]  
}
```

## Theorem 1: Template-based synthesis is Reducible to Reachability

**Reduction Sketch:** *GadgetS2R* reduces a template-based synthesis instance  $(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$  to a specific reachability problem  $(P, L)$ , satisfiable iff the synthesis instance can be solved

- For every template param  $\boxed{c_i}$ , create a fresh global variables  $v_i$
- For every fun  $q \in Q$ , define a similar fun  $q_P \in P$  that has every reference to a  $c_i$  replaced with the corresponding var  $v_i$
- The test suite  $T$  as a conjunctive expression  $e$ :

$$e = \bigwedge_{(i,o) \in T} \text{main}_{QP}(i) = o$$

- Starting function  $\text{main}_P$  consisting of conditional stmt leading to a target location  $L$  iff  $e$  is true

```
int mainP() {  
  if (e) [L]  
}
```

- $P$  consists of the new variables  $v_i$ , funs  $q_P$ , and  $\text{main}_P$

## Example:

```
int isUp(int in,int up,int down){
    int bias, r;
    if (in)
        bias = c0+c1bias+c2in+c3up+c4down;
    else
        bias = up;
    if (bias > down) r = 1;
    else r = 0;
    return r;
}
// Test suite
Q(1,0,100)=0; Q(1,-20,60)=1
Q(1,11,110)=1; Q(0,0,10)=0
Q(0,100,50)=1; Q(0,0,-10)=1
```



```
int c0,c1,c2,c3,c4; //global inputs
int isUpP(int in,int up,int down){
    int bias, r;
    if (in)
        bias = c0+c1bias+c2in+c3up+c4down;
    else
        bias = up;
    if (bias > down) r = 1;
    else r = 0;
    return r;
}

int main() {
    if(isUpP(1, 0,100) == 0 &&
        isUpP(1, 11,110) == 1 &&
        isUpP(0,100, 50) == 1 &&
        isUpP(1,-20, 60) == 1 &&
        isUpP(0, 0, 10) == 0 &&
        isUpP(0, 0,-10) == 1){
        [L] //target location
    }
    return 0;
}
```

Input: Template-based instance

Output: Reachability instance

## Example:

```
int isUp(int in,int up,int down){
  int bias, r;
  if (in)
    bias = c0+c1bias+c2in+c3up+c4down;
  else
    bias = up;
  if (bias > down) r = 1;
  else r = 0;
  return r;
}
// Test suite
Q(1,0,100)=0; Q(1,-20,60)=1
Q(1,11,110)=1; Q(0,0,10)=0
Q(0,100,50)=1; Q(0,0,-10)=1
```



```
int c0,c1,c2,c3,c4; //global inputs
int isUpP(int in,int up,int down){
  int bias, r;
  if (in)
    bias = c0+c1bias+c2in+c3up+c4down;
  else
    bias = up;
  if (bias > down) r = 1;
  else r = 0;
  return r;
}

int main() {
  if(isUpP(1, 0,100) == 0 &&
    isUpP(1, 11,110) == 1 &&
    isUpP(0,100, 50) == 1 &&
    isUpP(1,-20, 60) == 1 &&
    isUpP(0, 0, 10) == 0 &&
    isUpP(0, 0,-10) == 1){
    [L] //target location
  }
  return 0;
}
```

Input: Template-based instance

Output: Reachability instance

$GadgetS2R : (Q, S, T) \mapsto (P, L)$

- **Correctness:** relies on two key invariants
  - ①  $funs \in P$  have the same behavior as  $funs \in Q$
  - ②  $L$  is reachable iff values of  $c_i$  can be assigned to  $v_i$  allowing  $Q$  to pass all tests
- **Complexity:** *linear* in program size and test cases of synthesis instance

## Theorem 2: Reachability is reducible to Template-based synthesis

**Reduction Sketch:** *GadgetR2S* reduces a reachability problem  $(P, L)$  to a specific template-based synthesis instance  $(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$ , solvable iff the reachability problem can be satisfied

## Theorem 2: Reachability is reducible to Template-based synthesis

**Reduction Sketch:** *GadgetR2S* reduces a reachability problem  $(P, L)$  to a specific template-based synthesis instance  $(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$ , solvable iff the reachability problem can be satisfied

- For every variable  $v_i$ , define a fresh template variables  $\boxed{c_i}$ . The set  $S$  of template params contain each  $\boxed{c_i}$



## Theorem 2: Reachability is reducible to Template-based synthesis

**Reduction Sketch:** *GadgetR2S* reduces a reachability problem  $(P, L)$  to a specific template-based synthesis instance  $(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$ , solvable iff the reachability problem can be satisfied

- For every variable  $v_i$ , define a fresh template variables  $\boxed{c_i}$ . The set  $S$  of template params contain each  $\boxed{c_i}$
- For every fun  $p \in P$ , define a similar fun  $p_Q \in Q$ 
  - Replace each call to  $p$  with a corresponding call to  $p_Q$
  - Replace each use of  $v_i$  with a read from  $c_i$

## Theorem 2: Reachability is reducible to Template-based synthesis

**Reduction Sketch:** *GadgetR2S* reduces a reachability problem  $(P, L)$  to a specific template-based synthesis instance  $(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$ , solvable iff the reachability problem can be satisfied

- For every variable  $v_i$ , define a fresh template variables  $\boxed{c_i}$ . The set  $S$  of template params contain each  $\boxed{c_i}$
- For every fun  $p \in P$ , define a similar fun  $p_Q \in Q$ 
  - Replace each call to  $p$  with a corresponding call to  $p_Q$
  - Replace each use of  $v_i$  with a read from  $c_i$
- Raise a unique *exception* REACHED at the  $\text{loc} \in Q$  corresponding to  $L \in P$

## Theorem 2: Reachability is reducible to Template-based synthesis

**Reduction Sketch:** *GadgetR2S* reduces a reachability problem  $(P, L)$  to a specific template-based synthesis instance  $(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$ , solvable iff the reachability problem can be satisfied

- For every variable  $v_i$ , define a fresh template variables  $\boxed{c_i}$ . The set  $S$  of template params contain each  $\boxed{c_i}$
- For every fun  $p \in P$ , define a similar fun  $p_Q \in Q$ 
  - Replace each call to  $p$  with a corresponding call to  $p_Q$
  - Replace each use of  $v_i$  with a read from  $c_i$
- Raise a unique *exception* REACHED at the loc  $\in Q$  corresponding to  $L \in P$
- Starting function  $main_Q$  that returns 1 (indicating when REACHED is caught)

```
int mainQ() {  
    try {mainPQ();}  
    catch (REACHED) {return 1;}  
    return 0;  
}
```

## Theorem 2: Reachability is reducible to Template-based synthesis

**Reduction Sketch:** *GadgetR2S* reduces a reachability problem  $(P, L)$  to a specific template-based synthesis instance  $(Q, S = \{\boxed{c_i}, \dots, \boxed{c_n}\}, T = \{(i_1, o_1), \dots\})$ , solvable iff the reachability problem can be satisfied

- For every variable  $v_i$ , define a fresh template variables  $\boxed{c_i}$ . The set  $S$  of template params contain each  $\boxed{c_i}$
- For every fun  $p \in P$ , define a similar fun  $p_Q \in Q$ 
  - Replace each call to  $p$  with a corresponding call to  $p_Q$
  - Replace each use of  $v_i$  with a read from  $c_i$
- Raise a unique *exception* REACHED at the loc  $\in Q$  corresponding to  $L \in P$
- Starting function  $main_Q$  that returns 1 (indicating when REACHED is caught)

```
int main_Q() {  
    try {main_P_Q();}  
    catch (REACHED) {return 1;}  
    return 0;  
}
```

- $Q$  consists of template parameters  $S = \{\boxed{c_1}, \dots, \boxed{c_n}\}$ , funs  $p_Q$ 's, and  $main_Q$ . The test suite  $T$  for  $Q$  consists of exactly one test case  $Q() = 1$ .

## Example:

```
//global inputs
int x, y;

int P(){
  if (2 * x == y)
    if (x > y + 10)
      [L] //target location

  return 0;
}
```



```
int PQ() {
  if (2*x == y)
    if(x > y+10)
      //loc L in P
      raise REACHED;

  return 0;
}
```

```
int mainQ() {
  //synthesize cx, cy
  int x = cx;
  int y = cy;
  try
    PQ();
  catch (REACHED)
    return 1;

  return 0;
}
//Test suite: Q() = 1
```

Input: Reachability instance

Output: Template-based instance

## Example:

//global inputs

int x, y;

int P(){

if (2 \* x == y)

if (x > y + 10)

[L] //target location

return 0;

}



int P<sub>Q</sub>() {

if (2\*x == y)

if(x > y+10)

//loc L in P

raise REACHED;

return 0;

}

int main<sub>Q</sub>() {

//synthesize  $c_x, c_y$

int x =  $c_x$ ;

int y =  $c_y$ ;

try

P<sub>Q</sub>();

catch (REACHED)

return 1;

return 0;

}

//Test suite: Q() = 1

Input: Reachability instance

Output: Template-based instance

$GadgetR2S : (P, L) \mapsto (Q, S, T)$

- **Correctness** of *GadgetR2S* relies on two key invariants:
  - 1 For any  $c_i$ , execution in  $Q$  mirrors execution in  $P$  with  $v_i \mapsto c_i$
  - 2  $Q$  raises the exception REACHED iff  $P$  can reach  $L$
- **Complexity** of *GadgetR2S* is *linear* in the input  $P, L$  (and  $v_i \in P$ )

# Program Repair as a Synthesis Problem

## Definition:

Given a program  $Q$  that *fails* at least one test in a finite test suite  $T$  and a finite set of parameterized templates  $S$ , does there exist a set of stmts  $\{s_i\} \subseteq Q$  and parameter values  $c_1, \dots, c_n$  for the templates in  $S$  such that  $s_i$  can be replaced with  $S[c_1, \dots, c_n]$  and the resulting program passes all tests in  $T$ ?

# Program Repair as a Synthesis Problem

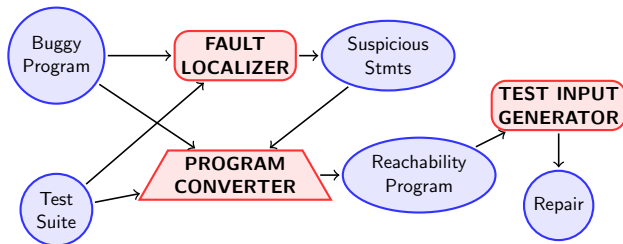
## Definition:

Given a program  $Q$  that *fails* at least one test in a finite test suite  $T$  and a finite set of parameterized templates  $S$ , does there exist a set of stmts  $\{s_i\} \subseteq Q$  and parameter values  $c_1, \dots, c_n$  for the templates in  $S$  such that  $s_i$  can be replaced with  $S[c_1, \dots, c_n]$  and the resulting program passes all tests in  $T$ ?

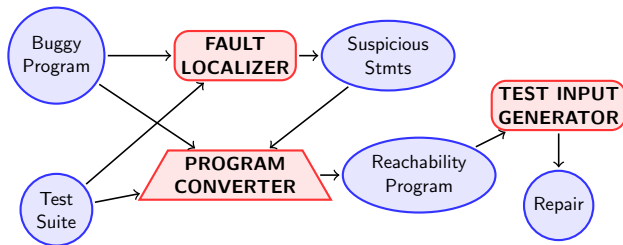
- Allows edits to multiple program stmts (e.g., can replace multilines with parameterized templates).
- *Single-edit* repair problem restricts the edits to one stmt



# CETI: program repair using test-input generation



# CETI: program repair using test-input generation



## CETI: correcting errors using test-inputs

- 1 Use fault localization to obtain suspicious stmts
- 2 Apply synthesis templates to create template-based synthesis instances
- 3 Use reduction theorem to convert to reachability programs
- 4 Employ an off-the-shelf test-input generator to solve reachability, i.e., creating repairs

# Repair Components

# Repair Components

## ① Fault Localization

- Identify suspicious statements to modify (e.g., `bias = down;`)
- Implement the statistical algorithm Tarantula to compute suspicious scores of program stmts (based on exe freq in passing and failing runs)

# Repair Components

## ① Fault Localization

- Identify suspicious statements to modify (e.g., `bias = down;`)
- Implement the statistical algorithm Tarantula to compute suspicious scores of program stmts (based on exe freq in passing and failing runs)

## ② Synthesis Templates

- Repair rhs of *assignment* stmts, e.g.,  $s := e \mapsto s := \text{parameterized template}$
- Supports templates to modify constants, linear expressions, and logical, comparisons, and arithmetic ops, e.g.,

$$\begin{array}{ll} s := x \leq y & \mapsto s := x < y \\ s := x + y & \mapsto s := x - y \\ s := 10 & \mapsto s := 3x + 4y - 200 \end{array}$$

# Repair Components

## ① Fault Localization

- Identify suspicious statements to modify (e.g., `bias = down;`)
- Implement the statistical algorithm Tarantula to compute suspicious scores of program stmts (based on exe freq in passing and failing runs)

## ② Synthesis Templates

- Repair rhs of *assignment* stmts, e.g.,  $s := e \mapsto s := \text{parameterized template}$
- Supports templates to modify constants, linear expressions, and logical, comparisons, and arithmetic ops, e.g.,

$$\begin{array}{ll} s := x \leq y & \mapsto s := x < y \\ s := x + y & \mapsto s := x - y \\ s := 10 & \mapsto s := 3x + 4y - 200 \end{array}$$

## ③ Test-input Generation

- Employs the symbolic execution tool KLEE to find test inputs for C programs
- Can easily be extended to use other verification tools such as CPAChecker, JPF, PEX, etc
- Advantage of reduction: admit other reachability/verification tools, regardless of technologies used

# Implementation and Evaluation

## CETI

- Written in OCaml, employ CIL to parse and modify C programs
- Take as input a testsuite  $T$ , and a C program  $P$  that fails  $T$ , return modified statements allowing  $P$  to pass  $T$
- Synthesize correct-by-construction repairs (guarantee to pass test suite)
- Currently support single-edit repairs (can be extended to multiline repairs by considering  $k$  susp stmts)

# Implementation and Evaluation

## CETI

- Written in OCaml, employ CIL to parse and modify C programs
- Take as input a testsuite  $T$ , and a C program  $P$  that fails  $T$ , return modified statements allowing  $P$  to pass  $T$
- Synthesize correct-by-construction repairs (guarantee to pass test suite)
- Currently support single-edit repairs (can be extended to multiline repairs by considering  $k$  susp stmts)

## Evaluation

- Evaluate using the **TCAS** program from SIR benchmark
  - Implement aircraft traffic collision avoidance system, 180 LoC's
  - About 1608 tests and 41 faulty (seeded defects) functions (changed operators, incorrect constant values, missing code, and incorrect control flow)
  - Have the most introduced defects (41) in SIR, and been used to benchmark modern bug repair techniques
- Use all available tests to guarantee that any repair found is correct wrt entire test suite



# Experimental Results

- Fixed 26 of 41 defects, including multiple defects of different types, avg 22s
- Found 100% of repairs with single-edit changes under considered templates
- Found several ways to fix defects and also obtained unexpected repairs

# Experimental Results

- Fixed 26 of 41 defects, including multiple defects of different types, avg 22s
- Found 100% of repairs with single-edit changes under considered templates
- Found several ways to fix defects and also obtained unexpected repairs
- Not able to repair 15 of 41 defects (require multiloc edits or code not under considered templates)

# Experimental Results

- Fixed 26 of 41 defects, including multiple defects of different types, avg 22s
- Found 100% of repairs with single-edit changes under considered templates
- Found several ways to fix defects and also obtained unexpected repairs
- Not able to repair 15 of 41 defects (require multiloc edits or code not under considered templates)
- Performs well compared to other repair tools
  - GenProg, which uses a genetic algorithm, can repair 11 of these defects
  - FoREnSiC, which uses the concolic execution in CREST, repairs 23 defects
  - Other repair techniques, including random mutation, equivalence checking, and counterexample guided refinement, repair 9, 15 and 16 defects, respectively.
  - SemFix outperforms CETI, repairing 34 defects
- Existing approaches *integrates* verification techniques, CETI eschews heavyweight analyses
  - Reduction and offload synthesis to KLEE
  - Unoptimized CETI already performed reasonably well

# Conclusions

Formal **connection** between template-based program synthesis and the reachability problem in verification

- Constructively prove an equivalence between these two problems
- Reduce template-based synthesis reachability, and conversely
- Connect the two problems and enable the application of ideas, optimizations, and tools developed for one problem to the other

CETI: new **automatic program repair** technique

- An algorithm and tool for repairing C programs using test-input generation
  - Transform the task of synthesizing program repairs to a reachability problem
  - Use off-the-shelf test-input generation tool to synthesize repaired stmts
  - Achieve higher success rates than many other standard repair approaches.

<https://bitbucket.org/nguyenthanhvuh/ceti>