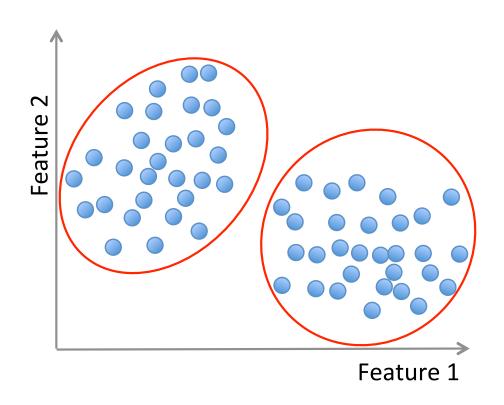
Artificial Intelligence Machine Learning Unsupervised learning



Unsupervised Learning

Training data: "examples" x.

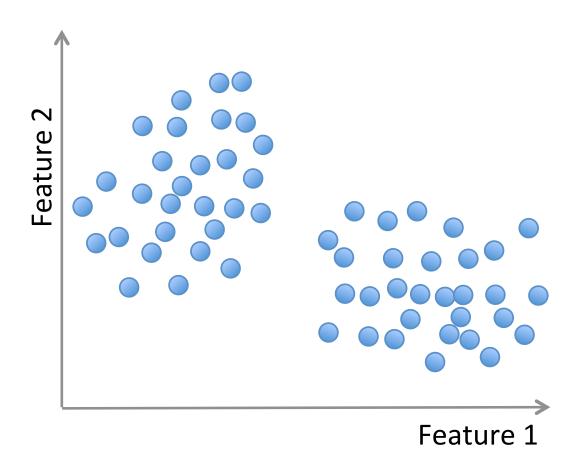
$$x_1, \dots, x_n, \ x_i \in X \subset \mathbb{R}^n$$

• Clustering/segmentation:

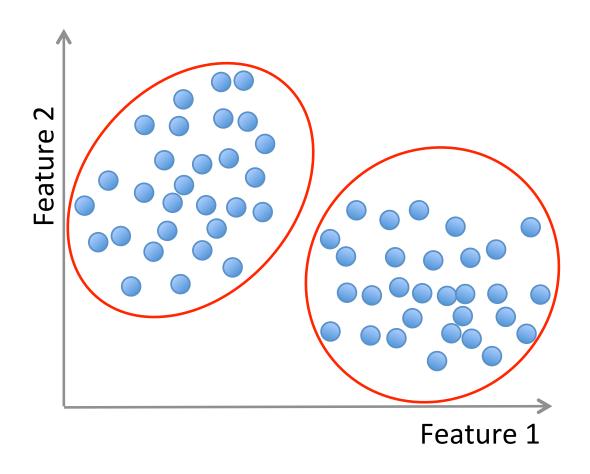
$$f: \mathbb{R}^d \longrightarrow \{C_1, \dots C_k\}$$
 (set of clusters).

Example: Find clusters in the population, fruits, species.

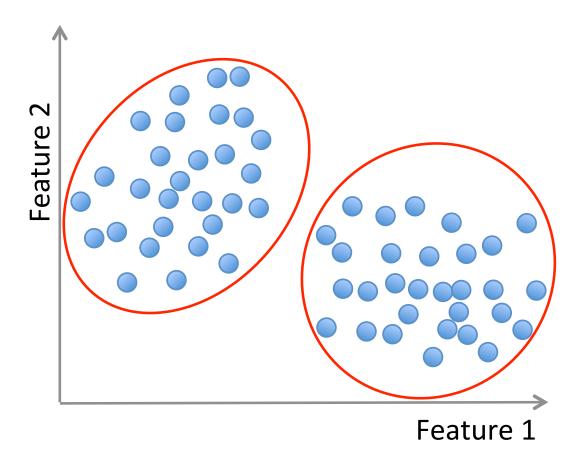
Unsupervised learning



Unsupervised learning



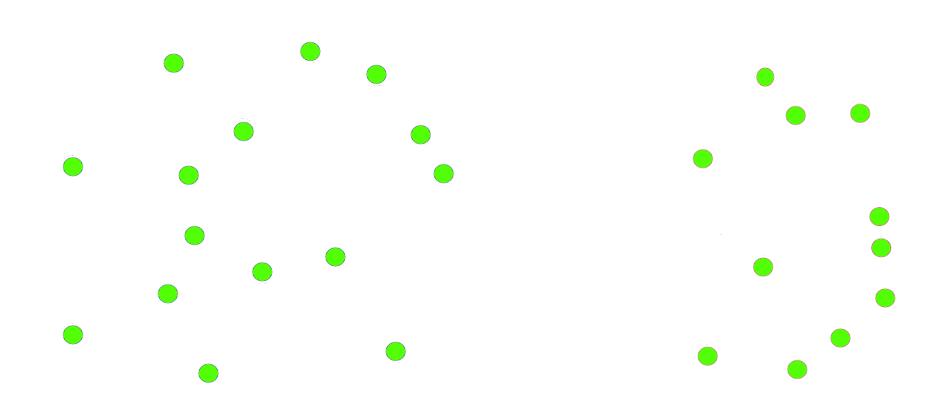
Unsupervised learning

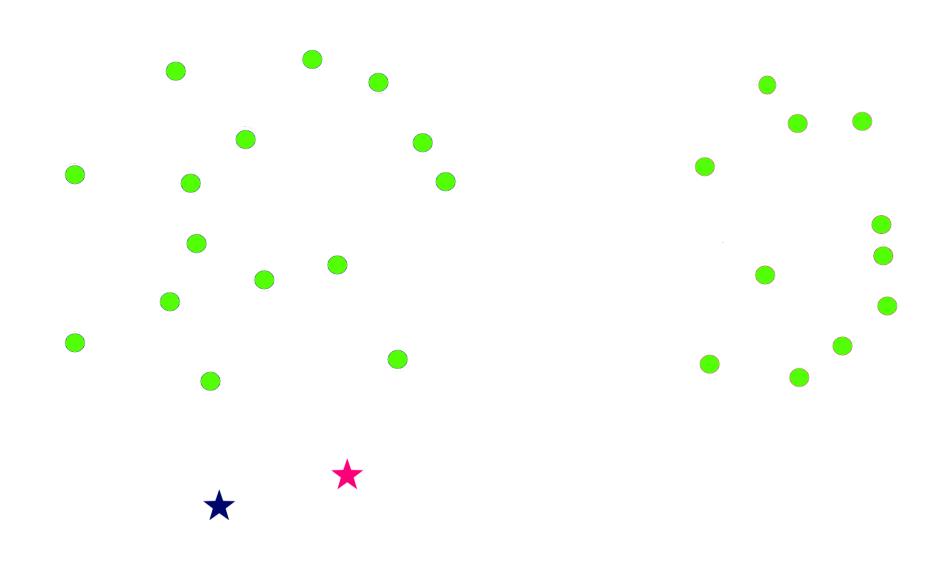


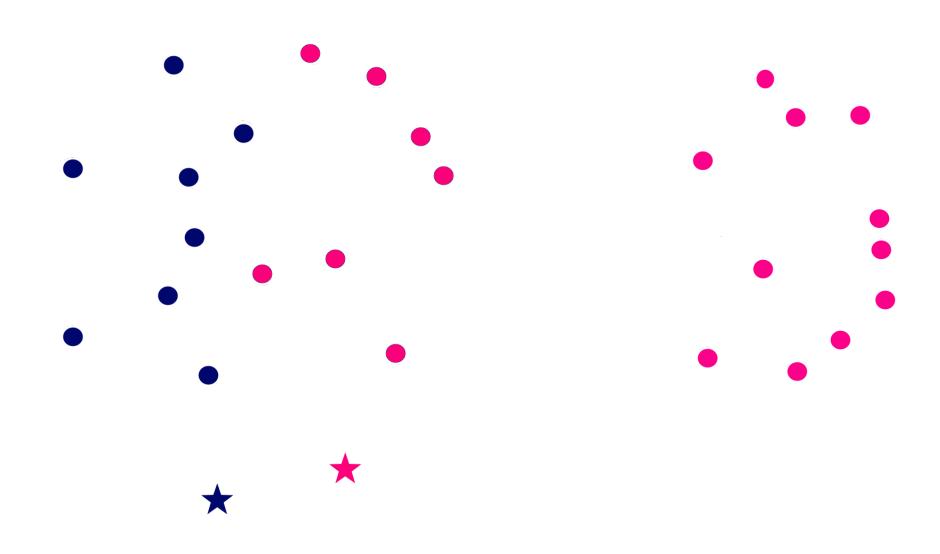
Methods: K-means, gaussian mixtures, hierarchical agglomerative clustering, spectral clustering, DBScan, etc.

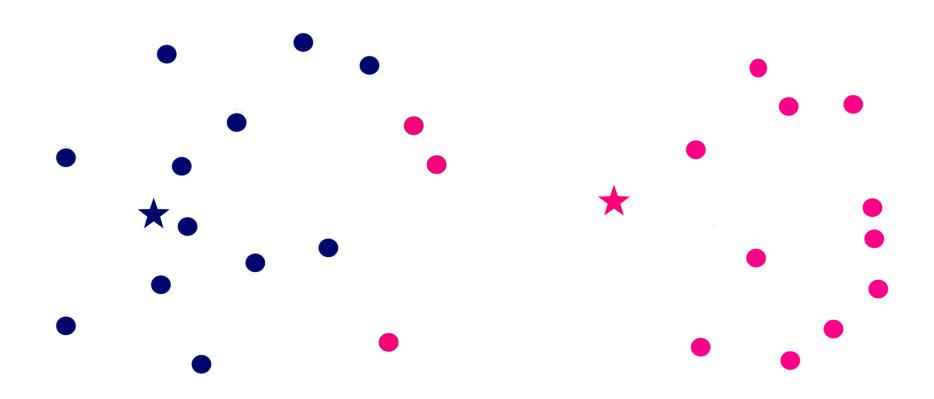
Clustering examples

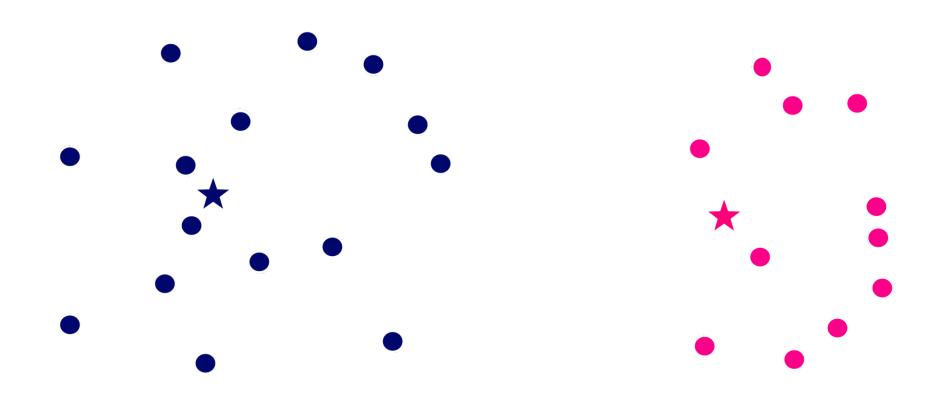
- Clustering of the population by their demographics.
- Clustering of geographic objects (mineral deposits, houses, etc.)
- Clustering of stars
- Audio signal separation. Example?
- Image segmentation. Example?

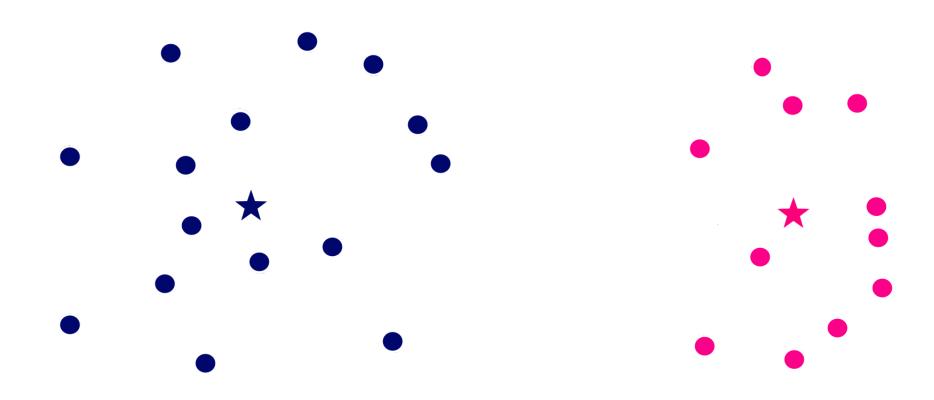












• Goal: Assign each example (x_1, \ldots, x_n) to one of the k clusters $\{C_1, \ldots, C_k\}$.

- **Goal**: Assign each example (x_1, \ldots, x_n) to one of the k clusters $\{C_1, \ldots, C_k\}$.
- \bullet μ_{j} is the mean of all examples in the j^{th} cluster.

- **Goal**: Assign each example (x_1, \ldots, x_n) to one of the k clusters $\{C_1, \ldots, C_k\}$.
- ullet μ_j is the mean of all examples in the j^{th} cluster.
- Minimize:

$$J = \sum_{j=1}^{k} \sum_{x_i \in C_j} ||x_i - \mu_j||^2$$

Algorithm K-Means:

Initialize randomly $\mu_1, \cdots \mu_k$.

Algorithm K-Means:

```
Initialize randomly \mu_1, \cdots \mu_k. Repeat
```

Assign each point x_i to the cluster with the closest μ_j .

Algorithm K-Means:

Initialize randomly $\mu_1, \cdots \mu_k$.

Repeat

Assign each point x_i to the cluster with the closest μ_j . Calculate the new mean for each cluster as follows:

$$\mu_j = \frac{1}{|\mathcal{C}_j|} \sum_{x_i \in \mathcal{C}_j} x_i$$

Until convergence*.

Algorithm K-Means:

Initialize randomly $\mu_1, \cdots \mu_k$.

Repeat

Assign each point x_i to the cluster with the closest μ_j . Calculate the new mean for each cluster as follows:

$$\mu_j = \frac{1}{|\mathcal{C}_j|} \sum_{x_i \in \mathcal{C}_j} x_i$$

Until convergence*.

*Convergence: Means no change in the clusters OR maximum number of iterations reached.

K-Means: pros and cons

+ Easy to implement

BUT...

- Need to know K
- Suffer from the curse of dimensionality
- No theoretical foundation

K-Means: questions

- 1. How to set k to optimally cluster the data?
- 2. How to evaluate your model?
- 3. How to cluster non circular shapes?

K-Means: question 1

How to set k to optimally cluster the data?

G-means algorithm (Hamerly and Elkan, NIPS 2003)

- 1. Initialize k to be a small number
- Run k-means with those cluster centers, and store the resulting centers as C
- 3. Assign each point to its nearest cluster
- 4. Determine if the points in each cluster fit a Gaussian distribution (Anderson-Darling test).
- 5. For each cluster, if the points seem to be normally distributed, keep the cluster center. Otherwise, replace it with two cluster centers.
- 6. Repeat this algorithm from step 2. until no more cluster centers are created.

K-Means: question 2

How to evaluate your model?

- Not trivial (as compared to counting the number of errors in classification).
- Internal evaluation: using same data. high intra-cluster similarity (documents within a cluster are similar) and low intercluster similarity. E.g., Davies-Bouldin index that takes into account both the distance inside the clusters and the distance between clusters. The lower the value of the index, the wider is the separation between different clusters, and the more tightly the points within each cluster are located together.
- External evaluation: use of ground truth of external data. E.g., mutual information, entropy, adjusted random index, etc.

K-Means: question 3

How to cluster non circular shapes?

There are other methods: spectral clustering, DBSCAN, BIRCH, etc. that handle other shapes.