## Part1. Decision Tree

```
<ahng-01 ~/my scratch/web/Codes/CS534/HW4 1000$ python3 part1.py</p>
training accuracy with depth: 2 is : 75.5223880597015
validation accuracy with depth: 2 is : 75.919191919192
training accuracy with depth: 5 is: 78.43781094527364
validation accuracy with depth: 5 is : 78.64646464646464
training accuracy with depth: 10 is: 79.50248756218905
validation accuracy with depth: 10 is : 78.30303030303031
training accuracy with depth: 20 is: 83.66169154228855
validation accuracy with depth: 20 is : 77.5555555555556
training accuracy with depth: 25 is: 86.49751243781094
validation accuracy with depth: 25 is : 76.86868686868686
training accuracy with depth: 30 is: 89.32338308457712
validation accuracy with depth: 30 is: 75.31313131313131
training accuracy with depth: 35 is: 91.39303482587064
validation accuracy with depth: 35 is: 75.15151515151514
training accuracy with depth: 40 is: 92.98507462686567
validation accuracy with depth: 40 is: 74.34343434343434
training accuracy with depth: 45 is : 94.0497512437811
validation accuracy with depth: 45 is: 73.8989898989899
training accuracy with depth: 50 is: 95.2139303482587
validation accuracy with depth: 50 is : 73.45454545454545
```

Figure 1. Decision Tree implementation

(a) What are the first three splits selected by your algorithm? This is for the root, and the two splits immediately beneath the root. What are their respective information gains?

```
'information gain': 0.3075677298204409,
    'leaf': False,
    'left': {
                 'depth': 1,
                 'information_gain': 0.03490775046162631,
                 'leaf': False,
                 'left': None,
                 'node': 'Vehicle_Damage',
                 'right': None},
    'node': 'Previously Insured',
    'node': '--.
'node_index': 2,
'tepth': 1,
    'right': {
                  'information_gain': 0.004327417692095228,
                  'leaf': False,
                  'left': None,
'node': 'Vehicle_Damage',
                  'right': None}}
training accuracy with depth: 2 is: 75.5223880597015
validation accuracy with depth: 2 is : 75.919191919192
```

Figure 2. Depth 2 tree node

The figure 1 is the result of decision tree with depth 2. To print out the tree structure, I used the dictionary file format. In the root, appeared with 'depth: 0', the split node is 'Previously\_Insured' and its information gain is 0.3076. The split criteria that I used is if the value of feature is zero then go to the left node, and if the value of feature is one then go to the right node. Both nodes after the

first splits, immediately beneath the root, are 'Vehicle\_Damage'. The information gain of left 'Vehicle\_Damage' node is 0.0349, and the information gain of right 'Vehicle\_Damage' node is 0.0043.

(b) Evaluate and plot the training and validation accuracies of your trees as a function for *dmax*. When do you see your tree start overfitting?

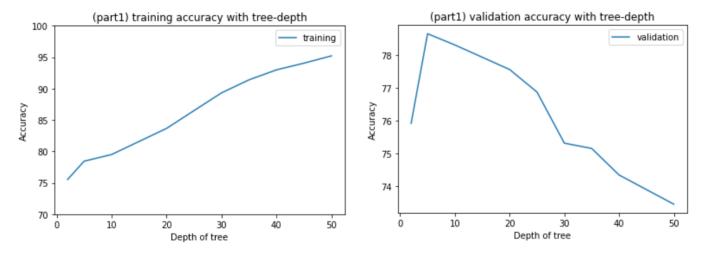


Figure 3. Each Training and Validation accuracy according to the depth of the tree

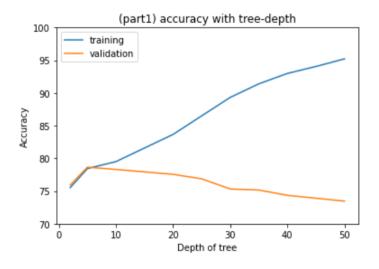


Figure 4. Both Training and Validation accuracy according to the depth of the tree

In the figure 3, left figure is training dataset accuracy and right side is validation dataset accuracy. When see the left figure, the accuracy of training dataset is tending to get higher as the depth of the tree gets higher. However, in the right figure, the accuracy of validation dataset is decreasing after about depth 5 of decision tree. If we compare both accuracies on figure 4, both training and validation accuracy gets higher until the depth of tree is about 5, and after that validation accuracy is decreasing. Therefore, we can say that this tree start overfitting after depth 5.

```
train accuracy: d_max : 2, m : 5 with tree num :
                                                   20 = 67.55223880597015
valid accuracy: d_max : 2, m : 5 with tree num :
train accuracy: d_max : 2, m : 5 with tree num :
                                                  40 = 65.85858585858585
                                                   50 = 64.6766169154229
valid accuracy: d_max : 2, m : 5 with tree num :
                                                   50 = 64.88888888888889
train accuracy: d_max : 2, m : 5 with tree num : 60 = 66.57711442786069
valid accuracy: d_max : 2, m : 5 with tree num :
                                                   70 = 65.67676767676768
train accuracy: d_max : 2, m : 5 with tree num : valid accuracy: d_max : 2, m : 5 with tree num : train accuracy: d_max : 2, m : 5 with tree num :
                                                   90 = 65.23383084577115
valid accuracy: d_max : 2, m : 5 with tree num :
train accuracy: d_max : 2, m : 25 with tree num : 10 = 63.03482587064677
30 = 72.5074626865671530 = 72.74747474747475
train accuracy: d_max : 2, m : 25 with tree num :
valid accuracy: d_max : 2, m : 25 with tree num : 30 = 72.74747474747475 train accuracy: d_max : 2, m : 25 with tree num : 40 = 72.26865671641791
                                                    40 = 72.1010101010101
50 = 74.85572139303483
valid accuracy: d_max : 2, m : 25 with tree num :
train accuracy: d_max : 2, m : 25 with tree num :
train accuracy: d_max : 2, m : 25 with tree num : valid accuracy: d_max : 2, m : 25 with tree num :
                                                    60 = 75.01010101010101
valid accuracy: d_max : 2, m : 25 with tree num :
                                                    80 = 73.43434343434343

90 = 70.44776119402985
30 = 75.4726368159204
30 = 75.43434343434343
train accuracy: d_max : 2, m : 50 with tree num :
valid accuracy: d_max : 2, m : 50 with tree num :
train accuracy: d_max : 2, m : 50 with tree num :
                                                    40 = 75.61616161616162
50 = 75.68159203980099
valid accuracy: d_max : 2, m : 50 with tree num :
train accuracy: d_max : 2, m : 50 with tree num :
valid accuracy: d_max : 2, m : 50 with tree num :
                                                    60 = 75.67164179104478
60 = 75.65656565656566
train accuracy: d_max : 2, m : 50 with tree num :
valid accuracy: d_max : 2, m : 50 with tree num :
                                                    70 = 75.68159203980099
train accuracy: d_max : 2, m : 50 with tree num :
                                                    70 = 75.6767676767678
80 = 75.67164179104478
valid accuracy: d_max : 2, m : 50 with tree num :
train accuracy: d_max : 2, m : 50 with tree num :
                                                    80 = 75.67164179104478
80 = 75.6565656565656
90 = 75.67164179104478
90 = 75.65656565656566
valid accuracy: d_max : 2, m : 50 with tree num :
train accuracy: d_max : 2, m : 50 with tree num :
valid accuracy: d_max : 2, m : 50 with tree num : 90 = 75.67164179104476 train accuracy: d_max : 2, m : 50 with tree num : 90 = 75.6565656565666 train accuracy: d_max : 2, m : 50 with tree num : 100 = 75.83084577114428 valid accuracy: d_max : 2, m : 50 with tree num : 100 = 75.91919191919192
```

```
train accuracy: d_max : 2, m : 100 with tree num : 10 = 75.5223880597015 valid accuracy: d_max : 2, m : 100 with tree num : 10 = 75.91919191919192 train accuracy: d_max : 2, m : 100 with tree num : 20 = 75.5223880597015
valid accuracy: d_max : 2, m :
                                        100 with tree num : 20 = 75.91919191919192
train accuracy: d_max : 2, m : 100 with tree num : 30 = 75.5223880597015
                                        100 with tree num : 30 = 75.91919191919192
100 with tree num : 40 = 75.5223880597015
valid accuracy: d_max : 2, m : 100 with tree num :
train accuracy: d_max : 2, m
valid accuracy: d_max : 2, m :
                                        100 with tree num : 50 = 75.5223880597015
train accuracy: d_max : 2, m :
valid accuracy: d max : 2, m :
                                        100 with tree num : 50 = 75.91919191919192
                                        100 with tree num : 60 = 75.5223880597015
100 with tree num : 60 = 75.91919191919192
train accuracy: d_max : 2, m :
valid accuracy: d_max : 2, m
train accuracy: d max : 2, m :
                                        100 with tree num : 70 = 75.5223880597015
valid accuracy: d max : 2, m :
                                                                  70 = 75.91919191919192
                                        100 with tree num :
train accuracy: d max : 2, m :
                                        100 with tree num : 80 = 75.5223880597015
valid accuracy: d_max : 2, m :
train accuracy: d_max : 2, m
valid accuracy: d_max : 2, m :
                                        100 with tree num :
train accuracy: d_max : 2, m : 100 with tree num : 100 = 75.5223880597015 valid accuracy: d_max : 2, m : 100 with tree num : 100 = 75.91919191919192
```

Figure 5. Random Forest result with d max = 2

```
valid accuracy: d_max : 10, m : 5 with tree num : 20 = 74.96969696969697
train accuracy: d_max : 10, m : 5 with tree num : 30 = 75.31343283582089 valid accuracy: d_max : 10, m : 5 with tree num : 30 = 74.68686868686869
train accuracy: d_max : 10, m : 5 with tree num : 40 = 74.98507462686567
valid accuracy: d_max : 10, m : 5 with tree num : 40 = 74.5656565656565657
train accuracy: d_max : 10, m : 5 with tree num : 50 = 76.02985074626865
valid accuracy: d_max : 10, m : 5 with tree num : 50 = 75.71717171717171
train accuracy: d_max : 10, m : 5 with tree num : 60 = 76.32835820895522 valid accuracy: d_max : 10, m : 5 with tree num : 60 = 76.20202020202021 train accuracy: d_max : 10, m : 5 with tree num : 70 = 75.98009950248756
valid accuracy: d_max : 10, m : 5 with tree num : 70 = 75.79797979797979
train accuracy: d_max : 10, m : 5 with tree num : 80 = 75.13432835820896 valid accuracy: d_max : 10, m : 5 with tree num : 80 = 74.828282828282828284
train accuracy: d_{max}: 10, m : 5 with tree num : 90 = 74.09950248756219
train accuracy: d_max : 10, m : 25 with tree num : 10 = 79.0547263681592
valid accuracy: d_max : 10, m : 25 with tree num : 10 = 79.0909090909091
train accuracy: d_max : 10, m : 25 with tree num : 20 = 78.92537313432835
valid accuracy: d_max : 10, m : 25 with tree num : 20 = 79.01010101010101
train accuracy: d_max : 10, m : 25 with tree num : 30 = 78.8955223880597 valid accuracy: d_max : 10, m : 25 with tree num : 30 = 78.989898989898999
train accuracy: d_max : 10, m : 25 with tree num : 40 = 78.98507462686567
valid accuracy: d_max : 10, m : 25 with tree num : 50 = 79.090909090909
train accuracy: d_max : 10, m : 25 with tree num : 70 = 79.07462686567163
valid accuracy: d_max : 10, m : 25 with tree num : 70 = 79.11111111111111
train accuracy: d_max : 10, m : 25 with tree num : 80 = 79.14427860696517
valid accuracy: d_max : 10, m : 25 with tree num : 80 = 79.1111111111111111
train accuracy: d_max : 10, m : 25 with tree num : 90 = 79.12437810945273 valid accuracy: d_max : 10, m : 25 with tree num : 90 = 79.15151515151516 train accuracy: d_max : 10, m : 25 with tree num : 100 = 79.11442786069651
valid accuracy: d max : 10, m : 25 with tree num : 100 = 79.11111111111111
```

```
train accuracy: d_{max}: 10, m : 50 with tree num : 10 = 78.87562189054727 valid accuracy: d_{max}: 10, m : 50 with tree num : 10 = 79.01010101010101
valid accuracy: d_max : 10, m : 50 with tree num :
train accuracy: d_max : 10, m : 50 with tree num :
                                                               20 = 78.92537313432835
valid accuracy: d_max : 10, m : 50 with tree num :
train accuracy: d_max : 10, m : 50 with tree num :
                                                               20 = 79.03030303030303
valid accuracy: d_max : 10, m : 50 with tree num :
train accuracy: d_max : 10, m :
                                       50 with tree num
                                                               40 = 79.11442786069651
40 = 78.98989898989899
valid accuracy: d_max : 10, m :
train accuracy: d_max : 10, m : 50 with tree num :
valid accuracy: d max : 10, m :
                                       50 with tree num
                                                                  = 78.98989898989899
train accuracy: d max : 10, m :
                                                               60 = 79.1542288557214
valid accuracy: d_max : 10, m :
                                       50 with tree num
                                                               70 = 79.14427860696517
70 = 79.07070707070707
train accuracy: d max : 10, m :
                                       50 with tree num
valid accuracy: d_max : 10, m :
                                       50 with tree num
train accuracy: d_max : 10, m :
valid accuracy: d max : 10, m :
                                                                  = 79.07070707070707
train accuracy: d max : 10, m :
                                                                90 = 79.22388059701493
                                       50 with tree num
valid accuracy: d_max : 10, m : 50 with tree num
train accuracy: d max :
                                       50 with tree num
                                                                100 = 79.22388059701493
valid accuracy: d max : 10, m : 50 with tree num
                                                               100 = 79.17171717171718
train accuracy: d_{max}: 10, m : 100 with tree num : 10 = 79.28358208955224
valid accuracy: d_max : 10, m : 100 with tree num
train accuracy: d_max : 10, m : 100 with tree num
                            10, m : 100 with tree num : 10, m : 100 with tree num :
valid accuracy: d max
                                                                 = 78.92929292929293
train accuracy: d max :
                                                                 = 79.46268656716417
                                                              30 = 79.17171717171718
40 = 79.67164179104478
40 = 79.25252525252525
valid accuracy: d_max : 10, m : 100 with tree num :
train accuracy: d_max : 10, m : 100 with tree num
valid accuracy: d_max : 10, m : 100 with tree num
                            10, m : 100 with tree num
10, m : 100 with tree num
                                                                 = 79.73134328358209
= 79.1919191919192
train accuracy: d max :
valid accuracy: d max :
train accuracy: d_max : 10, m : 100 with tree num : valid accuracy: d_max : 10, m : 100 with tree num :
                                                              60 = 79.69154228855722
valid accuracy: d_max :
                                                              70 = 79.67164179104478
train accuracy: d_max : 10, m : 100 with tree num
                             10, m: 100 with tree num
valid accuracy: d_max :
                                                                 = 79.66169154228857
train accuracy: d_max : 10, m : 100 with tree num
valid accuracy: d max : 10, m : 100 with tree num :
train accuracy: d max : 10, m : 100 with tree num :
                                                                 = 79.62189054726369
train accuracy: d_max :
valid accuracy: d_max : 10, m : 100 with tree num
                                                               90 = 79.41414141414141
                                                              100 = 79.61194029850746
100 = 79.373737373737
train accuracy: d_max : 10, m : 100 with tree num :
valid accuracy: d_max : 10, m : 100 with tree num :
```

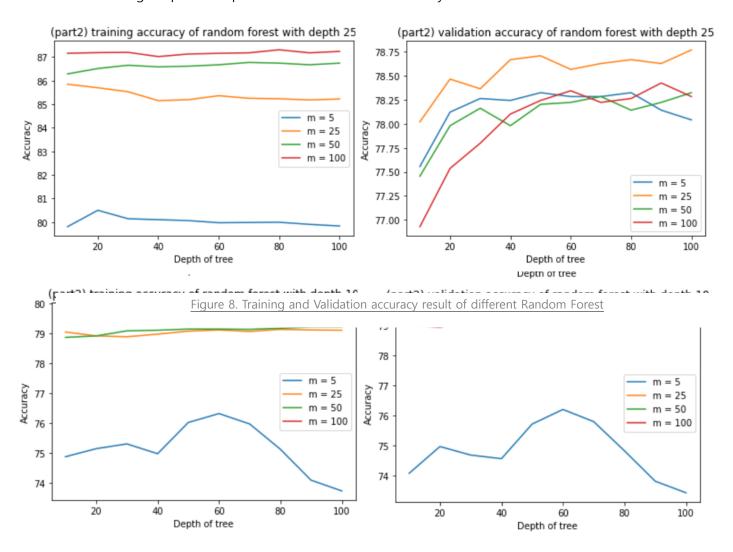
Figure 6. Random Forest result with d\_max = 10

```
train accuracy: d_max : 25, m : 5 with tree num : 10 = 79.80099502487562
valid accuracy: d max : 25, m : 5 with tree num : 10 = 77.55555555555555
train accuracy: d_max : 25, m : 5 with tree num : 20 = 80.49751243781095
                                                        20 = 78.12121212121212
30 = 80.13930348258707
valid accuracy: d_max : 25, m : 5 with tree num :
train accuracy: d_max : 25, m : 5
valid accuracy: d_max : 25, m : 5 with tree num : 30 = 78.262626262627
train accuracy: d_max : 25, m : 5 with tree num : 40 = 80.09950248756219
valid accuracy: d_max : 25, m : 5 with tree num
                                                      \mathbf{1} 40 = 78.242424242425
train accuracy: d_max : 25, m : 5
                                     with tree num : 50 = 80.05970149253731
valid accuracy: d_max : 25, m : 5 with tree num :
                                                        50 = 78.3232323232323
train accuracy: d_max : 25, m
                                                        60 = 79.97014925373135
valid accuracy: d_max : 25, m : 5 with tree num : 60 = 78.28282828282829
                                                     : 70 = 79.98009950248756
: 70 = 78.28282828282829
train accuracy: d_max : 25, m : 5 with tree num :
valid accuracy: d_max : 25, m : 5 with tree num
train accuracy: d_max : 25, m : 5
                                     with tree num : 80 = 79.99004975124379
                                                        80 = 78.32323232323233
90 = 79.90049751243781
valid accuracy: d_max : 25, m : 5 with tree num :
train accuracy: d_max : 25, m
valid accuracy: d_max : 25, m : 5 with tree num : 90 = 78.141414141415
train accuracy: d_{max}: 25, m : 5 with tree num : 100 = 79.83084577114428 valid accuracy: d_{max}: 25, m : 5 with tree num : 100 = 78.04040404040404
```

```
train accuracy: d_max : 25, m : 25 with tree num : 10 = 85.85074626865672
valid accuracy: d_max : 25, m : 25 with tree num : 10 = 78.02020202020202
train accuracy: d_max : 25, m : 25 with tree num : 30 = 85.53233830845771
valid accuracy: d_max : 25, m : 25 with tree num : 30 = 78.3636363636363637
train accuracy: d_max : 25, m : 25 with tree num : 40 = 85.15422885572139
train accuracy: d_max : 25, m : 25 with tree num : 50 = 85.19402985074626 valid accuracy: d_max : 25, m : 25 with tree num : 50 = 78.70707070707
train accuracy: d_max : 25, m : 25 with tree num : 60 = 85.363184079602
valid accuracy: d_max : 25, m : 25 with tree num : 70 = 78.626262626262
train accuracy: d max: 25, m: 25 with tree num: 80 = 85.23383084577114
train accuracy: d_max : 25, m : 25 with tree num : 90 = 85.18407960199005
valid accuracy: d_max
train accuracy: d_max : 25, m : 25 with tree num : 100 = 85.22388059701493
train accuracy: d_max : 25, m : 50 with tree num : 10 = 86.28855721393035
                                                10 = 77.45454545454545
valid accuracy: d max :
train accuracy: d_max
                                                  = 86.51741293532338
                                                    77.97979797979798
valid accuracy: d_max
train accuracy: d_max
                                                30 = 86.65671641791045
valid accuracy: d max
                                                    78.16161616161617
train accuracy: d max
                             50 with tree num:
                                                40 = 86.58706467661692
valid accuracy: d max
train accuracy: d max
                             50 with tree num
                                                50 = 86.61691542288558
valid accuracy: d max
                             50 with tree num:
                                                60 = 86.67661691542288
train accuracy: d_max
                              50 with tree num :
valid accuracy: d max
                              50 with tree num:
                                                70 = 86.77611940298507
train accuracy: d_max
                                                70 = 78.28282828282829
valid accuracy: d_max
                              50 with tree num
                                                80 = 86.74626865671642
train accuracy: d max
valid accuracy: d max
                              50 with tree num :
                                                80 = 78.14141414141415
train accuracy: d max
                              50 with tree num
valid accuracy: d max
train accuracy: d max
                                                100 = 86.74626865671642
                                                100 = 78.32323232323233
valid accuracy: d max :
                             50 with tree num :
train accuracy: d max: 25, m: 100 with tree num: 10 = 87.16417910447761
valid accuracy: d_max : 25, m : 100 with tree num :
                       25, m : 100 with tree num :
                                                  20 = 87.19402985074626
train accuracy: d_max :
valid accuracy: d_max :
train accuracy: d_max : 25, m : 100 with tree num :
                                                 30 = 87.20398009950249
valid accuracy: d_max : 25, m : 100 with tree num :
                                                  30 = 77.79797979797979
                                                 40 = 87.02487562189056
train accuracy: d_max : 25, m : 100 with tree num
                      25, m:
valid accuracy: d max :
                              100 with tree num :
train accuracy: d_max : 25, m :
                              100 with tree num :
                                                 50 = 87.13432835820896
valid accuracy: d_max : 25, m :
                                                 50 = 78.242424242425
train accuracy: d_max : 25, m : 100 with tree num :
                                                 60 = 87.16417910447761
valid accuracy: d_max : 25, m :
                                                 60 = 78.34343434343435
                              100 with tree num:
train accuracy: d max : 25, m :
                                                  70 = 87.18407960199005
                              100 with tree num :
valid accuracy: d_max : 25, m :
                                                 70 = 78.222222222223
train accuracy: d max :
                                                    = 87.31343283582089
valid accuracy: d max : 25, m :
                              100 with tree num :
                                                 80 = 78.26262626262627
train accuracy: d_max : 25, m : 100 with tree num : valid accuracy: d_max : 25, m : 100 with tree num :
                                                  90 = 78.42424242424244
train accuracy: d_max : 25, m : 100 with tree num :
                                                  100 = 87.24378109452736
valid accuracy: d_max : 25, m : 100 with tree num : 100 = 78.28282828282829
```

Figure 7. Random Forest result with d\_max = 25

(a) Compare your training curves with the validation curves, do you think your model is overfitting or underfitting for particular parameter combinations? And why?



In figure 8, figures on the left side represent training accuracy according to the depth of tree, and right side represent validation accuracy according to the depth of tree. I think random forest with depth 2 with different values of the number of features selected in each step shows some underfitting. If we compare the training accuracy and validation accuracy of random forest with depth 2, we can see that both accuracies show almost same result. Also, random forest with depth 25 with different number of selected features in each step such as 100 or 50 is shows overfitting. If we compare the training accuracy and validation accuracy of this random forest, we can see that validation accuracy is getting lower as the training accuracy gets higher. This result is showing some overfitting.

Random forest with depth 2 is showing underfitting result, validation accuracy shows very high accuracy. It means this model is predicting the new data too well. This is because even though there are lots of features to consider when training, tree with depth 2 only compare 2 features, and it will cause too biased trained model. Therefore, it will predict data with biased model and could cause the underfitting result. On the other hands, random forest with depth 25 with high m values are showing overfitting result. It means that this model is not good for predicting new data. This is because it considers too many features which leads to a high variance trained model. The model overly trains the features that are not even common in one decision boundary. So, the model will be good at predicting trained data but not with new data.

Therefore, based on the two result, we can see that model that is trained with too small number of features will be highly biased and show low variance. However, model that is trained with too many features will show high variance result but with low bias. Both models will have high errors. Then we can train this random forest tree model with medium amount split criteria features because it will show low biased and low variance and will generate acceptable and understandable validation accuracy.

If we create large depth tree, the more the depth gets dipper, there will be smaller number of data to be split. Then it will cause the model to be more specific and highly variance, and this will make the performance increase difficult.