MULTI-VARIATE EARNING DYNAMICS

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ABSTRACT

The current stochastic process used to model earnings and decompose them into temporary and permanent shocks is extremely important for studying the structure of earnings processes. This actual modeling of the dynamics of the earning process can be enhanced with a multi-variable effect. The large amounts of data that can now be obtained to model earning processes are very vast and correlated with each other, this means that each time we will want to correlate more variables that we see that affect our stochastic process and somehow incorporate them into our study. For the decomposition of transitory and permanent shock, we therefore need a good scheme and a good one to correlate these objects.

Keywords: Earnings processes, Incomplete markets, Partial insurance, Estimation

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1 INTRODUCTION

We can use vector autoregression strategies and a multi-variable approach to encompass more complex processes. [1].

A current study carried out by Hryshko and Manovskii (2020), indicates a modern earning process modeling based on the decomposition in transitory and permanent shocks, in fact it is an improved version of the one indicated in the study previously done by Friedman (1957) . In this work by Hryshko and Manovskii, they present what can be interpreted as ways to optimize the equation, seen from the point of view of a pure statistician or a mathematician, in addition, we want it to be understood and in this way be used in production by practicing statesman's, graduates and engineers. Hideously complicated as the masterpieces explained by their creators are defined. We have another document that makes an implementation of this model

2 DEFINITIONS

We have in our first approaches to the literature that, in the first place, indicate rigorous mathematical definitions, the first definition of the decomposition in shocks of the earning process is given by:

$$y_{it} = \alpha_i + p_{it} + t_{it}$$
$$p_{it} = \varphi_p p_{it} - 1 + \xi_{it}(1)$$
$$t_{it} = \theta(L)\epsilon_{it},$$

"...where log-earnings y_{it} of individual i at time t consist of the permanent component, p_{it}, and the transitory component, t_{it}. If φ_p is close to 1, the shocks ξ_{it} are highly persistent (and are truly permanent if φ_p is 1), and if $\theta(L) = 1$ (where $\theta(L)$ is a moving average polynomial in the lag operator L), the shocks ϵ_{it} are completely transitory."

— Daly, Hryshko 2020

2.1 Intuitive Definition

DESCRIPTIVE We have seen a change in the way we interpret the model in the following definition:

$$W_{it} = W_{it}^P + W_{it}^T,$$
$$E(W_{it}^P) = E(W_{it}^T) = E(W_{it}^P + W_{it}^T) = 0$$

"...The Friedman's formulation is far too simplistic."

— Cappellari 2010

2.2 Less Abstract Definition

WAY MORE INTUITIVE In a second approach to the literature of this modeling, we have seen a definition for a clearer public or in this case, something more intuitive, at first it could be seen that it is the same as the first quote but really here we give a more intuitive sketch to proceed with our solution.

A TYPICAL EARNING PROCESS

1. y_{it} is individuals i log-earnings residuals at a given t
2. p_{it} is the permanent component (Random Walk)
3. t_{it} is the transitory component (MA(1), ARMA(1,1), AR(1), or iid;)

2.3 Some Equivalences

Now according to the definitions of the different authors we have a description of what the profit process model is good enough to implement a paradigm shift to the current model, we can proceed to see certain similarities through the mathematical language.

PERMANENT COMPONENT We can assume that the permanent component is a basic Random Walk model given by:

$$x_t = x_{t-1} + w_t, \tag{4.18}$$

"...Alternatively (Dickens 2000, Cappellari and Leonardi 2010): Random walk (RW) model."

$$W_{it}^{P} = r_{iexp(t)} = r_{iexp(t-1)} + \xi_{iexp(t)}$$
$$r_{i0\ i}(0, \sigma_r^2); \xi_{iexp(t)\ ie}(0, \sigma_\xi^2)$$

TRANSITORY COMPONENT t_{it} is the transitory component: MA(1), ARMA(1,1), AR(1), or iid; (Hryshko Manovskii, 2020)

THEREFORE Assume low order ARMA, e.g. ARMA(1,1). (Capellari 2010)

3 IMPROVEMENTS AND DISCUSSIONS

"...When you think about someone's income, it is a function of a persistent component (usually thought of as their productivity and ability) and a transitory component (something contemporaneous that hits them). But, data has problems and so there are better ways to do the decomposition than others."

— Makridis 2021

In fact it is totally true, most of the authors have an accurate opinion, there is a lot of literature on how to measure the processes of earning dynamics.

"There is an extensive literature estimating stochastic processes for individual earnings."

— Manovskii 2020

3.1 What Improvements?

UNBALANCED DATA Allowing for an unbalanced sample.

ERROR Allowing for measurement error in income.

MORE VARIABLES Allowing for the incorporation of consumption and/or labor supply (hours worked) data.

Due to the nature of the data, the number of processes in place, and the number of correlations that exist, academics try to balance this and generalize it to values of degrees of difference. Another improvement given is the lack of existence of a public version of a package to calculate the dynamics of the profit directly by some end user.

LACK OF AUDIENCE This is also really one of the inspirations for this work, to facilitate the study of these models for users and researchers in the area.

4 PROPOSED SOLUTION

After analyzing the model we have very well and the proposed improvements, a solution that is consistent enough to be applied can be designed, this design could allow an unbalanced data panel and at the same time multiple variables.

4.1 Multi-variate Approach

4.2 ARMA model automation

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Table 1: Table of Grades

Name		
First name	Last Name	Grade
John	Doe	7.5
Richard	Miles	2

Reference to Table 1.

4.3 Figure Composed of Subfigures

Reference the figure composed of multiple subfigures as Figure 1 on the next page. Reference one of the subfigures as Figure 1b on the following page.

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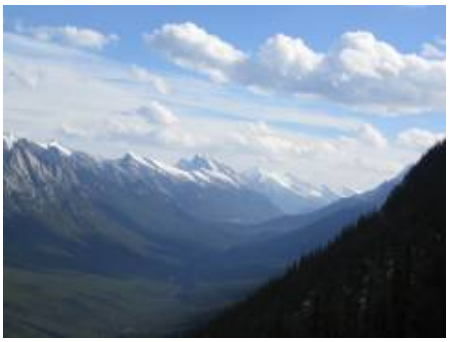
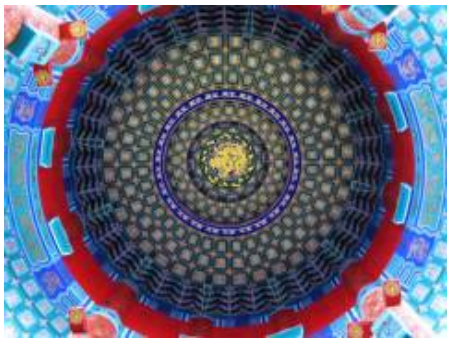
(a) A city market.

(b) Forest landscape.



(c) Mountain landscape.



(d) A tile decoration.

Figure 1: A number of pictures with no common theme.

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