

Question 1:

Consider a disk with the following characteristics:

block size $B=512$ bytes

interblock gap size $G=128$ bytes,

number of blocks per track=20,

number of tracks per surface=400.

A disk pack consists of 15 double-sided disks.

(a) What is the total capacity of a track and what is its useful capacity (excluding interblock gaps)?

$$\begin{aligned}\text{Total Track Capacity} &= (\text{Block Size} + \text{interblock gap size}) * \# \text{ of Blocks per track} \\ &= (B + G) * R \\ &= (512 + 128) * 20 \\ &= 640 * 20 \\ &= 12,800 \text{ bytes}\end{aligned}$$

$$\begin{aligned}\text{Total Useful Capacity per track} &= B * R \\ &= 512 * 20 \\ &= 10,240 \text{ bytes}\end{aligned}$$

(b) How many cylinders are there?

$$\begin{aligned}\# \text{ of tracks per surface} &= \# \text{ of cylinders} \\ 400 \text{ tracks per surface} \therefore \text{there are } &400 \text{ cylinders}\end{aligned}$$

(c) What is the total capacity and the useful capacity of a cylinder?

Because each disk is double sided, and we have 15 total for our disk pack we have 30 track for each cylinder.

$$\begin{aligned}\text{Total Capacity of Cylinder} &= \# \text{ of tracks} * \text{total track capacity} \\ &= 30 * 12,800 \\ &= 384,000 \text{ bytes}\end{aligned}$$

$$\begin{aligned}\text{Total Useful Capacity of Cylinder} &= \# \text{ of tracks} * \text{total useful capacity per track} \\ &= 30 * 10,240 \\ &= 307,200 \text{ bytes}\end{aligned}$$

(d) What is the total capacity and the useful capacity of a disk pack?

$$\begin{aligned}\text{Disk Pack} &= 400 \\ \text{Total Capacity of Disk Pack} &= \text{Tracks Per surface} * \text{Total Capacity of Cylinder} \\ &= 400 * 384,000 \\ &= 153,600,000 \text{ bytes}\end{aligned}$$

$$\begin{aligned}\text{Total Useful Capacity of Disk Pack} &= \text{Tracks Per surface} * \text{Total useful Capacity of Cylinder} \\ &= 400 * 307,200 \\ &= 122,880,000 \text{ bytes}\end{aligned}$$

(e) Suppose the disk drive rotates the disk pack at a speed of 2400 rpm (revolutions per minute);

1. What is the transfer rate (tr) in bytes/msec and the block transfer time (btt) in msec?

$$P = 2400 \text{ rpm}$$

$$tr = \frac{\text{Total Capacity}}{\left(\frac{60 \times 1000}{P}\right)}$$

$$= 12800 / \left(\frac{60 \times 1000}{2400}\right)$$

$$= 12800 / 25$$

$$= 512 \text{ bytes}$$

$$B = 512 \text{ bytes}$$
$$btt = \frac{B}{tr} \quad tr = 512 \text{ bytes}$$

$$= 512 / 512$$

$$= 1 \text{ msec}$$

2. What is the average rotational delay (rd) in msec?

$$rd = \left(\frac{1}{2}\right) \left(\frac{1}{P}\right) (60 \times 1000) = \left(\frac{1}{2}\right) (60,000) \left(\frac{1}{2400}\right)$$
$$= \frac{30,000}{2400}$$

$$= 12.5 \text{ msec}$$

3. What is the bulk transfer rate (btr)?

$$B = 512 \quad G = 128 \quad tr = 512$$

$$btr = \left(\frac{B}{B+G}\right) tr = \left(\frac{512}{512+128}\right) 512 = 0.8 \times 512$$

$$= 409.6 \text{ bytes/msec}$$

(f) Suppose the average seek time is 30 msec. How much time does it take (on the average) in msec to locate and transfer a single block given its block address?

$$(S + rd + btt) \quad S = 30 \quad rd = 12.5 \quad btt = 1$$

$$30 + 12.5 + 1$$

$$= 43.5 \text{ msec}$$

(g) Calculate the average time it would take to transfer 20 random blocks (may not be on the same cylinder) and compare it with the time it would take to transfer 20 consecutive blocks (all in on cylinder).

$$\text{noncontiguous} = K \times (S + rd + btt) \quad K = 20 \quad (S + rd + btt) = 43.5$$
$$= 20 \times 43.5$$

$$= 870 \text{ msec}$$

$$\text{contiguous} = S + rd + (K \times btt) \quad K = 20 \quad S = 30 \quad rd = 12.5 \quad btt = 1$$
$$= 30 + 12.5 + (20 \times 1)$$

$$= 62.5 \text{ msec}$$

Question 2:

A file has $r=200000$ STUDENT records of fixed-length.

Each record has the following fields:

NAME (30 bytes)
SSN (9 bytes)
ADDRESS (40 bytes)
PHONE (10 bytes)
BIRTHDATE (8 bytes)
SEX (1 byte)
MAJORDEPTCODE (4 bytes)
MINORDEPTCODE (4 bytes)
CLASSCODE (4 bytes, integer)
DEGREEPROGRAM (3 bytes).
An additional byte is used as a deletion marker

The file is stored on the disk whose parameters are given in Question 1.

- (a) Calculate the record size R in bytes.

$$\begin{aligned} R &= \text{Sum up all fields} \\ &= 30 + 9 + 40 + 10 + 8 + 1 + 4 + 4 + 4 + 3 + 1 \\ &= 114 \text{ bytes} \end{aligned}$$

- (b) Calculate the blocking factor (bfr) and the number of file blocks b assuming an unspanned organization.

$$\begin{aligned} B &= 512 \text{ bytes} \quad R = 114 \text{ bytes} \\ bfr &= \lfloor B/R \rfloor \\ &= \lfloor 512/114 \rfloor = \lfloor 4.49 \rfloor = 4 \text{ bytes} \end{aligned}$$

$$\begin{aligned} b &= r/bfr \quad r = 200,000 \quad bfr = 4 \\ &= 200000/4 \\ &= 50,000 \text{ blocks} \end{aligned}$$

- (c) Calculate the average time it takes to find a record by doing a linear search of the file if
1. The file blocks are stored contiguously

$$\begin{aligned} \text{contiguously} &= s + rd + (k * btt) \quad k = \frac{50,000}{2} \quad s = 30 \quad rd = 12.5 \quad btt = 1 \\ &= 30 + 12.5 + \left(\frac{50,000}{2} * 1\right) \\ &= 25,042.5 \text{ msec} \end{aligned}$$

2. If the file blocks are not stored contiguously

$$\begin{aligned} \text{noncontiguous} &= k * (s + rd + btt) \quad k = \frac{50,000}{2} \quad s = 30 \quad rd = 12.5 \quad btt = 1 \\ &= \frac{50,000}{2} * (30 + 12.5 + 1) \\ &= 1,087,500 \text{ msec} \end{aligned}$$

- (d) Assume the file is ordered by SSN; calculate the time it takes to search for a record given its SSN value by doing a binary search

$$\text{Binary Search} = O(\log(b)) = \log(50,000)$$

$$\begin{aligned} \text{noncontiguous} &= k * (s + rd + btt) \quad k = \log(50,000) \quad s = 30 \quad rd = 12.5 \quad btt = 1 \\ &= \log(50,000) * (30 + 12.5 + 1) \\ &= 15.61 * 43.5 \\ &= 679.035 \text{ msec} \end{aligned}$$