



EECS 490 – Lecture 21

Logic, Constraints, and Dependencies

1

12/2/17

Announcements

- ▶ Project 4 due tonight at 8pm
- ▶ HW5 due Tue 12/5 at 8pm
- ▶ Project 5 due Tue 12/12 at 8pm

Prolog Example: Quicksort

► Partition:

```
partition(_, [], [], []).  
partition(Pivot, [Item|Rest], [Item|Less], NotLess) :-  
    Item < Pivot,  
    partition(Pivot, Rest, Less, NotLess).  
partition(Pivot, [Item|Rest], Less, [Item|NotLess]) :-  
    Item >= Pivot,  
    partition(Pivot, Rest, Less, NotLess).
```

► Sort:

```
quicksort([], []).  
quicksort([Item|Rest], Sorted) :-  
    partition(Item, Rest, Less, NotLess),  
    quicksort(Less, SortedLess),  
    quicksort(NotLess, SortedNotLess),  
    append(SortedLess, [Item|SortedNotLess], Sorted).
```

Prolog Example: Primes

- Sieve of Eratosthenes:

```
numbers(2, [2]).
numbers(Limit, Numbers) :-
    M is Limit - 1, numbers(M, NumbersToM),
    append(NumbersToM, [Limit], Numbers).

is_not_multiple(N, D) :- R is mod(N, D), R =\= 0.

filter_not_multiple(_, [], []).
filter_not_multiple(Factor, [First|Rest],
    [First|FilteredRest]) :-
    is_not_multiple(First, Factor),
    filter_not_multiple(Factor, Rest, FilteredRest).
filter_not_multiple(Factor, [_|Rest], FilteredRest) :-
    filter_not_multiple(Factor, Rest, FilteredRest).

sieve([]).
sieve([First|Rest], [First|SievedRest]) :-
    filter_not_multiple(First, Rest, FilteredRest),
    sieve(FilteredRest, SievedRest).

primes(Limit, Primes) :-
    numbers(Limit, Numbers), sieve(Numbers, Primes).
```

$$N = Z^2 = X^2 + Y^2$$

Constraint Logic Programming

- Extension of logic programming to include constraints on variables
- Basic Prolog includes limited arithmetic constraints that require variables to be instantiated

\rightarrow `square_sum([N, X, Y, Z]) :-`
`N ::= Z * Z, N ::= X * X + Y * Y,`
`X > 0, Y > 0, Z > 0, X < Y, N < 1000.`

`?- square_sum(S).`

\rightarrow `ERROR: ==/2: Arguments are not sufficiently instantiated`

CLP(FD)

$$X < Y$$

$$<(X, Y)$$

- The CLP family of libraries provide constraint logic programming as extensions to Prolog
- CLP(FD) is included in SWI-Prolog and works on finite domains (integer subsets)

Import
CLP(FD)
module

```
:- use_module(library(clpfd)).
```

CLP(FD)
constraint
operator

```
square_sum_c([N, X, Y, Z]) :-  
  N #= Z * Z, N #= X * X + Y * Y,  
  X #> 0, Y #> 0, Z #> 0, X #< Y, N #< 1000,  
  label([N, X, Y, Z]).
```

Require given
variables to
be grounded

```
?- square_sum_c(S).  
S = [25, 3, 4, 5] ;  
S = [100, 6, 8, 10] ;  
S = [169, 5, 12, 13] ;  
...
```

Search in CLP

- Search follows the same general strategy as Prolog, except that a *constraint store* keeps track of the set of constraints
 - Start with a set of goal terms
 - For first goal term, find a clause whose head can be unified with the term
 - Unification can instantiate or bind variables
 - Insert body terms that are not constraints into the front of the set of goal terms
 - Insert body terms that are constraints into the constraint store
 - Check whether the constraint store is unsatisfiable
 - If so, backtrack
- Search succeeds when no more goal terms remain, and the constraint store is not unsatisfiable

Example: Verbal Arithmetic

- Find a solution to the following such that each digit is distinct, and leading digits are non-zero:

$$\begin{array}{r}
 \text{S E N D} \\
 + \text{M O R E} \\
 \hline
 = \text{M O N E Y}
 \end{array}$$

- Plain Prolog:

```
money([S, E, N, D, M, O, R, Y]) :-
```

```
is_digit(S), is_digit(E), is_digit(N), is_digit(D),
```

```
is_digit(M), is_digit(O), is_digit(R), is_digit(Y),
```

```
S \= 0, M \= 0,
```

```
S \= E, S \= N, S \= D, S \= M, S \= O, S \= R, S \= Y,
```

```
E \= N, E \= D, E \= M, E \= O, E \= R, E \= Y,
```

```
N \= D, N \= M, N \= O, N \= R, N \= Y,
```

```
D \= M, D \= O, D \= R, D \= Y,
```

```
M \= O, M \= R, M \= Y,
```

```
O \= R, O \= Y,
```

```
R \= Y,
```

```
1000 * S + 100 * E + 10 * N + D
```

```
+ 1000 * M + 100 * O + 10 * R + E
```

```
== 10000 * M + 1000 * O + 100 * N + 10 * E + Y.
```

Takes 90
seconds to
solve on
Macbook

Example: Verbal Arithmetic

- Find a solution to the following such that each digit is distinct, and leading digits are non-zero:

$$\begin{array}{r}
 \text{S E N D} \\
 + \text{M O R E} \\
 \hline
 = \text{M O N E Y}
 \end{array}$$

- Prolog + CLP(FD):

```

money_c([S, E, N, D, M, O, R, Y]) :-
    L = [S, E, N, D, M, O, R, Y],
    L ins 0 .. 9, S #\= 0, M #\= 0, all_distinct(L),

```

Takes 0.2
seconds to
solve on
Macbook

Require variables in L to
be members of set [0, 9]

Constrain variables in L
to have distinct values

$$\begin{array}{r}
 1000 * S + 100 * E + 10 * N + D \\
 + 1000 * M + 100 * O + 10 * R + E \\
 \hline
 \neq 10000 * M + 1000 * O + 100 * N + 10 * E + Y, \\
 \text{label(L)}.
 \end{array}$$

Example: Sudoku

► Sudoku solver:

Higher-order predicate

Partial application

```
sudoku(Rows) :-
```

```
length(Rows, 9), maplist(same_length(Rows), Rows),
append(Rows, Values), Values ins 1..9,
maplist(all_distinct, Rows),
transpose(Rows, Columns),
maplist(all_distinct, Columns),
Rows = [Row1, Row2, Row3, Row4, Row5, Row6, Row7, Row8, Row9],
blocks(Row1, Row2, Row3),
blocks(Row4, Row5, Row6),
blocks(Row7, Row8, Row9),
maplist(label, Rows).
```

```
blocks([], [], []).
```

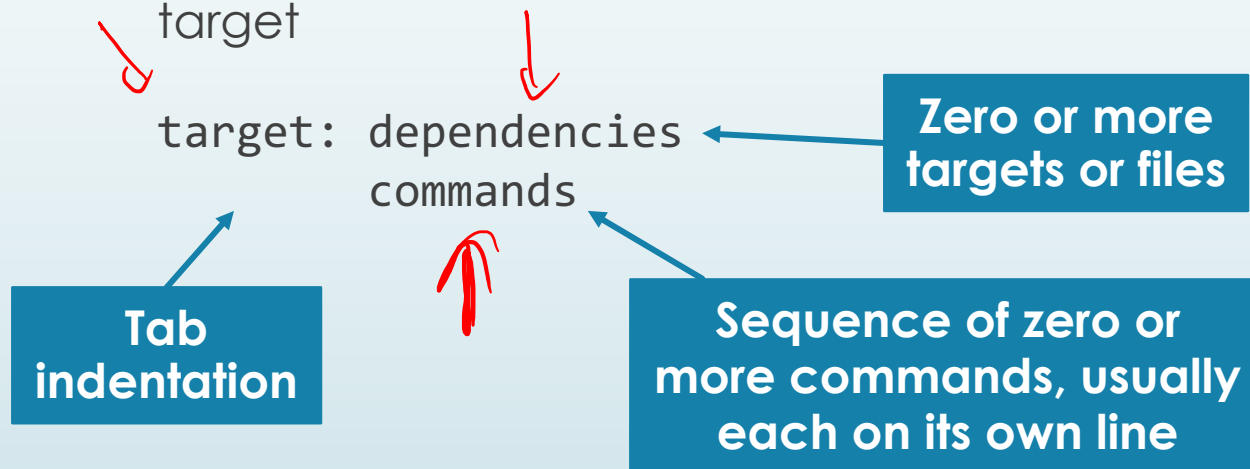
```
blocks([N1, N2, N3 | RestRow1],
       [N4, N5, N6 | RestRow2],
       [N7, N8, N9 | RestRow3]) :-
```

```
all_distinct([N1, N2, N3, N4, N5, N6, N7, N8, N9]),
blocks(RestRow1, RestRow2, RestRow3).
```

- We'll start again in five minutes.

Make

- Tool for automating the building of software packages, tracking dependencies between components
- Programming model is a combination of declarative and imperative
- A *rule* declares a relation between a target and its dependencies, specifies commands to build the target



Simple Example

- Rule contained within Makefile:

hello:

echo "Hello world!"

No dependencies

Build hello
target

Build first
target in
Makefile

```
> make hello  
echo "Hello world!"  
Hello world!  
  
> make  
echo "Hello world!"  
Hello world!
```

Target has no
dependencies, so
it will always build

Building an Executable

- More complex dependency trees can be specified

```
→ main: a.o b.o c.o  
      g++ -o main a.o b.o c.o  
  
a.o: a.cpp  
      g++ --std=c++14 -Wall -pedantic -c a.cpp  
  
b.o: b.cpp  
      g++ --std=c++14 -Wall -pedantic -c b.cpp  
  
c.o: c.cpp  
      g++ --std=c++14 -Wall -pedantic -c c.cpp
```

```
> make
```

```
g++ --std=c++14 -Wall -pedantic -c a.cpp  
g++ --std=c++14 -Wall -pedantic -c b.cpp  
g++ --std=c++14 -Wall -pedantic -c c.cpp  
g++ -o main a.o b.o c.o
```

Rebuilding a Target

- A target is only rebuilt when one of its dependencies has been modified

Modify timestamp
on b.cpp

```
> touch b.cpp
> ls -l
-rw-r--r--  1 kamil  staff   229 Nov 17 01:01 Makefile
-rw-r--r--  1 kamil  staff    90 Nov 17 00:57 a.cpp
-rw-r--r--  1 kamil  staff  6624 Nov 17 01:01 a.o
-rw-r--r--  1 kamil  staff    31 Nov 17 01:12 b.cpp
-rw-r--r--  1 kamil  staff   640 Nov 17 01:01 b.o
-rw-r--r--  1 kamil  staff    33 Nov 17 00:58 c.cpp
-rw-r--r--  1 kamil  staff   640 Nov 17 01:01 c.o
-rwxr-xr-x  1 kamil  staff 15268 Nov 17 01:01 main
> make
g++ --std=c++14 -Wall -Werror -pedantic -c b.cpp
g++ -o main a.o b.o c.o
```

Example: Makefile for Notes

```

all: foundations functional theory data declarative
foundations: foundations.html foundations.tex
functional: functional.html functional.tex
theory: theory.html theory.tex
data: data.html data.tex
declarative: declarative.html declarative.tex
asynchronous: asynchronous.html asynchronous.tex
metaprogramming: metaprogramming.html metaprogramming.tex

%.html: %.rst
    rst2html.py --stylesheet=../style/style.css $< > $@

%.tex: %.rst
    rst2latex.py --stylesheet=../style/style.sty $< > $@
    pdflatex $@
    pdflatex $@
    pdflatex $@

clean:
    rm -vf *.html *.tex *.pdf *.aux *.log *.out
  
```

Not
currently
built

Pattern
rule

Build PDF
file

Dependencies

Target