

EECS 490 – Lecture 9

Lambdas

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Announcements

- Project 2 due Fri 10/6

Agenda

- Lambda Expressions
- Common Functional Patterns

$$\text{lambda } x, y : x > y$$

$$\lambda f$$

$$\lambda f$$

Anonymous Functions

- Names provide an abstraction for an entity that can be used multiple times, but they can be cumbersome if the entity is used in only one place

```
def add_one(x):
    y = 1
    return x + y
```

Handwritten notes: A red arrow points from the function definition to the variable `y`. A red curly brace groups the last two lines, with the text `return x + 1` written next to it.

- This is the case for functions as well

```
def add_one_to_all(values):
    def add_one(x):
        return x + 1
    return map(add_one, values)
```

Handwritten notes: A red curly brace groups the inner `add_one` function definition. Another red curly brace groups the `map` function call. Red arrows point from the `add_one` function call in `map` to its definition.

- Anonymous functions are also called *lambda functions*

Handwritten note: `return map(lambda x: x + 1, values)`

$(\text{lambda } (x) (+ x 1))$

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Lambda in Scheme

- The `lambda` special form is used to define a function

`(define (<name> <parameters>) <body>)`

→

`(define <name> (lambda (<parameters>) <body>))`

- Nested functions can also be defined with `lambda`

→ `(define (make-adder n) (lambda (x) (+ x n)))`

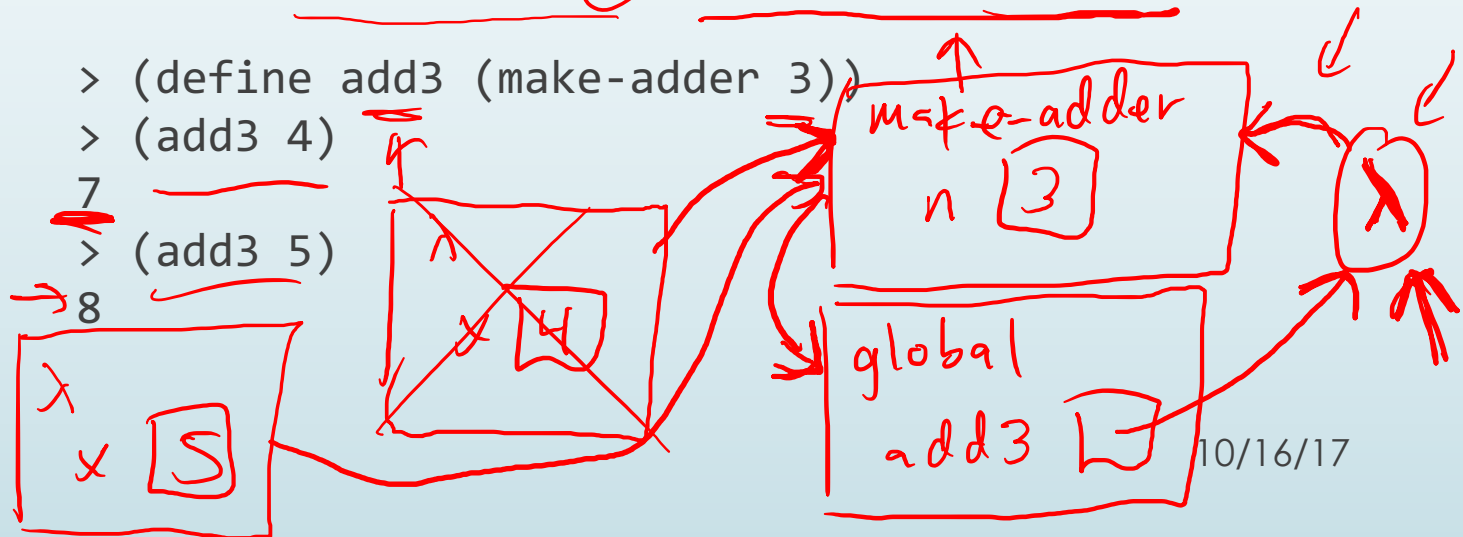
> `(define add3 (make-adder 3))`

> `(add3 4)`

7

> `(add3 5)`

8



$(\text{let } (\text{count } 0)) \text{ } ^{(+ \text{count } 1)} \text{ } \text{count}$

Mutating Non-Local Variables

- In Scheme, there is no distinction between functions defined with `define` and those with `lambda`
- Nested lambda functions have the full power available to nested functions

```
(define (make-counter)
  (let ((count 0))
    (lambda ()
      (set! count (+ count 1))
      (- count 1))))
```

Modify existing binding with `set!`

```
> (define counter (make-counter))
```

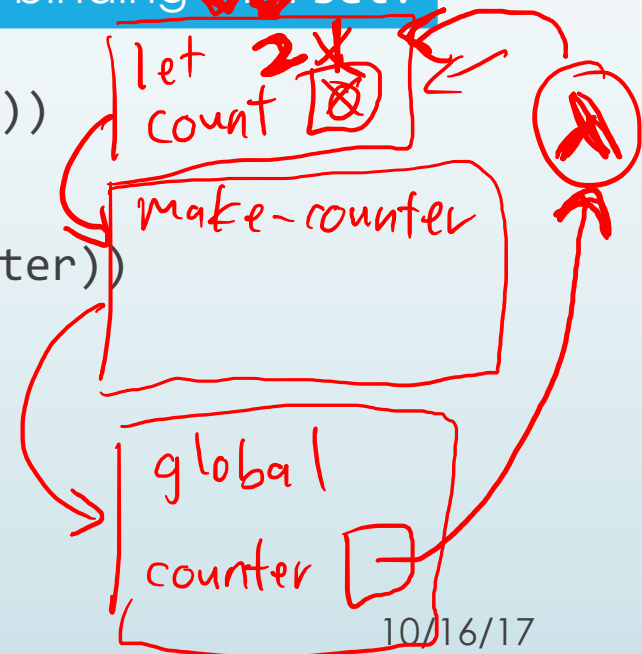
```
> (counter)
```

0

```
> (counter)
```

1

$(\text{lambda } (\text{count}) \text{ } ^{(+ \text{count } 1)} \text{ } \text{count}) 0$




Lambda in Python


- A lambda expression creates an anonymous function

lambda <parameters>: <body expression>



- The body must be a single expression, and its value is automatically the return value

 **def** make_greater_than(threshold):
 return lambda value: value > threshold



```
>>> gt3 = make_greater_than(3)
```

```
>>> gt3(2)
```

 False

```
>>> gt3(20)
```

 True

$y = x = 4$ if x = 4 :

Limitations of Python Lambdas

- ▶ Python lambdas are lexically scoped and have access to their non-local environment
- ▶ However, they are syntactically prohibited from modifying a non-local binding

```
def make_counter():  
    ⚡ count = 0  
    return lambda: ???  
    ↑
```


Lambda Expressions in Java

- Lambda expressions in Java create an instance of an anonymous functor-like class

```
static IntPredicate makeGreaterThan(int threshold) {  
    return value -> value > threshold;  
}
```

Base type of
anonymous class
inferred from use

Parameters;
types are
optional

Body can be
single expression
or a block

```
IntPredicate gt3 = makeGreaterThan(3);  
System.out.println(gt3.test(2)); // prints out false  
System.out.println(gt3.test(20)); // prints out true
```

Must call method

Limitations of Java Lambdas

- Can only access `final` or "effectively final" variables in enclosing environment
- Effective implementation:

```
static IntPredicate makeGreaterThan(int threshold) {  
    return Anonymous(threshold);  
}
```

```
class Anonymous implements IntPredicate {  
    private final int threshold;  
    Anonymous(int threshold) {  
        this.threshold = threshold;  
    }  
    public boolean test(int value) {  
        return value > threshold;  
    }  
}
```

Lambda Expressions in C++

- Capture list specifies which variables are captured, and whether they are captured by value or reference
- Can specify default capture as well as specific capture type for individual variables

```
auto make_greater_than(int threshold) {  
    return [=](int value) {  
        return value > threshold;  
    };  
}
```

Type deduction
used to infer
type of lambda

Capture non-
locals used in
lambda by
value

```
auto gt3 = make_greater_than(3);  
cout << gt3(2) << endl;  
cout << gt3(20) << endl;
```

Capture-Free Lambdas

- Lambdas that don't capture anything are equivalent to top-level functions
- They can even bind to function pointers

```
int max_element(int *array, size_t size,  
               bool (*less)(int, int));
```

```
int main() {  
    int array[4] = { 3, 1, 4, 2, 5 };  
    cout << max_element(array, 5,  
                        [](int a, int b) {  
                            return a > b;  
                        })  
    << endl;  
}
```

Lambdas and Functors

- Capturing lambda equivalent to instance of anonymous class


```
void foo(int x, int y) {
    auto fn = [=x, &y](int z) { y = x + z; };
    auto fn2 = Anon(x, y); // equivalent
}
```


```
class Anon {
    const int x;
    int &y;
public:
    Anon(int xin, int &yin) : x(xin), y(yin) {}
    void operator()(int z) {
        y = x + z;
    }
};
```

Variables captured by value are const by default

Lifetime of Captured Objects

- ▶ Capturing a variable by reference does not extend its lifetime
 - ▶ RAll requires that an automatic variable be destroyed upon exit from its enclosing scope
- ▶ Programmer needs to ensure that a capturing lambda is not used after captured objects die

 `auto make_counter() {
 int count = 0;
 return [&]() {
 return count++;
 };
}`

 `auto make_counter() {
 int count = 0;
 return [=]() mutable {
 return count++;
 };
}`

Allows variable
captured by value
to be modified

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- ▶ We'll start again in five minutes.

Map

- The *map* pattern applies a function to each element in a sequence, producing a new sequence consisting of the results

```
(define (map fn items)
  (if (null? items)
    '()
    (cons (fn (car items))
          (map fn (cdr items)))))
```

```
> (map (lambda (x) (+ x 1)) '(1 2 3 4))
(2 3 4 5)
```


Reduce

- The *reduce* pattern applies a function to a pair of items from a sequence, then to the result of that and the next item, and so on until the sequence is exhausted
- Can be right or left associative

```
(define (reduce-right fn items)
  (if (null? (cdr items))
      (car items)
      (fn (car items)
        (reduce-right fn (cdr items))))))
```

Assumes at least
one item in list

```
> (reduce-right (lambda (x y) (+ x y)) '(1 2 3))
6
> (reduce-right (lambda (x y) (if (> x y) x y))
  '(2 3 4 1))
4
```

Filter

- The *filter* pattern applies a predicate to the items in a sequence, producing a new sequence that only includes the items that test true

```
(define (filter pred items)
  (if (null? items)
      items
      (if (pred (car items))
          (cons (car items)
                (filter pred (cdr items)))
          (filter pred (cdr items)))))
```

```
> (filter (lambda (x) (> x 0)) '(1 -3 4 0))
(1 4)
```

```
> (filter (lambda (x) (even? x)) '(1 -3 4 0))
(4 0)
```

Map, Reduce, Filter in Python

- Python has built-in map, reduce, and filter
- Reduce located in `functools` module
- Result of `map()` and `filter()` are separate iterator types

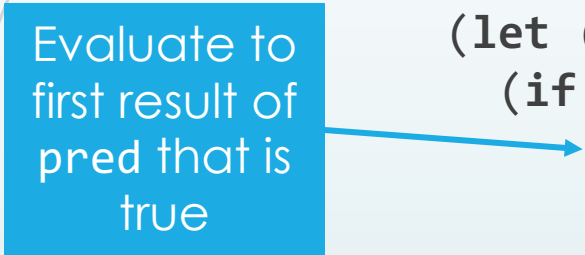
```
>>> from functools import reduce
>>> map(lambda x: x + 1, [1, 2, 3, 4])
<map object at 0x10b438390>
>>> list(map(lambda x: x + 1, [1, 2, 3, 4]))
[2, 3, 4, 5]
>>> list(filter(lambda x: x > 0, [-1, 2, 0, 4]))
[2, 4]
>>> reduce(lambda x, y: x + y, [1, 2, 3, 4])
10
```

Any and Every

- The *any* and *every* patterns are higher-order generalizations of *or* and *and*

```
(define (any pred items)
  (if (null? items)
      #f
      (let ((result (pred (car items))))
        (if result
            result
            (any pred (cdr items))))))
```

Evaluate to
first result of
pred that is
true



```
> (any (lambda (x) (< x 0)) '(1 2 3 4))
#f
> (any (lambda (x) (< x 0)) '(1 -2 -3 4))
#t
```

Compose

- Applying a function to the result of another function is a common operation
- Can define the composition of two functions

```
(define (compose f g)  
  (lambda (x) (f (g x))))
```

```
> (map (compose (lambda (x) (+ x 1))  
                (lambda (x) (* 3 x)))  
      '(3 5 7))  
(10 16 22)
```