EECS 490 – Lecture 19

Logic Programming

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Announcements

- HW4 due tonight at 8pm
- Project 4 due Tue 11/21 at 8pm

Internal Linkage

- C does not have namespaces, so it uses linkage specifiers to avoid name conflicts between translation units
 - Also in C++, since it's mostly compatible with C
- A variable or function at global scope can be declared static, which specifies internal linkage
 - Name will not be visible outside of translation unit, avoiding name conflicts at link stage
- Variables and functions defined, not just declared, in a header should generally be static

```
static const double PI = 3.1415926535;
static double area(double r) {
  return PI * r * r;
}
```

External Linkage

- A global variable or function has external linkage if it does not have the static specifier
 - The name will be accessible from other translation units
- An entity with external linkage must have exactly one definition among the translation units of a program
- A function can be declared but not defined by leaving out the function body
- A variable declaration is also a definition, unless it has the extern specifier
 Just a declaration

extern int count;
int count;

A definition that default initializes count

Information Hiding

- Languages often support information hiding at the granularity of a module or package
- In Java, a non-public class is available only to the same package
- Java and C# have module or package-level access modifiers for class members
- In C and C++, entities declared with internal linkage in a .c or .cpp file are not available to other translation units

Opaque Types in C

■ In C, struct members can be hidden by providing only a declaration and not the definition of a struct in the header file

```
typedef struct list *stack;
stack stack_make();
void stack_push(stack s, int i);
int stack_top(stack s);
void stack_pop(stack s);
void stack_free(stack s);
```

 Other translation units can make use of the interface, but cannot access members or even directly create an object of an opaque type

```
stack s = stack_make();
stack_push(s, 3);
stack_pop(s);
```

Initialization

- Languages specify semantics for initialization of the contents of a class, module, or package
- In Java, a class is initialized the first time it is used
 - Generally when an instance is created or a static member is accessed for the first time
- In Python, a module's code is executed when it is imported
 - If a module is imported again from the same module, its code does not execute again

Circular Dependencies

- Circular dependencies between modules should be avoided
- Can require restructuring code
- Example:

```
> python3 foo.py
Traceback (most recent call last):
   File "foo.py", line 1, in <module>
        import bar
   File "bar.py", line 1, in <module>
        import foo
   File "foo.py", line 9, in <module>
        print(func1())
   File "foo.py", line 4, in func1
        return bar.func3()
AttributeError: module 'bar' has no
attribute 'func3'
```

```
import bar
              foo.py
def func1():
    return bar.func3()
def func2():
    return 2
print(func1())
import foo
              bar.py
def func3():
    return foo.func2()
```

Initialization in C++

- C++ has a multi-step initialization process
 - Static initialization: initialize compile-time constants to their values, and all other variables with static storage duration to zero
 - **2. Dynamic initialization**: initialize static-storage variables using their specified initializers
 - Can be delayed until first use of the translation unit
- Within a translation unit, initialization is in program order, with some exceptions
- Order is undefined between translation units
 - Cannot rely on another translation unit being initialized first

Logic Programming

- Imperative programming: express computation as sequences of operations on the program state
- Functional programming: express computation as mappings between function inputs and outputs
- Logic programming: express computation as relations between pieces of data
- First-order predicate calculus is the foundation of logic programming

$$\forall X. \exists Y. P(X) \lor \neg Q(Y) \forall X. \exists Y. Q(Y) \Rightarrow P(X)$$

Horn Clauses

- A logic program is expressed as a set of axioms that are assumed to be true
- An axiom takes the form of a Horn clause, which specifies a reverse implication:

This is equivalent to

(B1
$$\wedge$$
 B2 \wedge ... \wedge BN) \Rightarrow H

with implicit quantifiers.

Queries

A goal is a query that the system attempts to prove from the axioms

Possible reasoning:

Prolog

- Prolog is the foundational language of logic programming and is the most widely used
- A Prolog program consists of a set of Horn clauses, using the syntax on the preceding slides
- A Horn clause has a head term and optional body terms
- A term may be atomic, compound, or a variable
 - Atomic: atoms and numbers
 - Atom: Scheme-like symbol or quoted string
 - If an atom starts with a letter, it must be lowercase

hello =< + 'logic programming'

Variables: symbols that start with an uppercase letter

Hello X

Compound Terms

 A compound term consists of a functor, which is an atom, followed by a list of one or more argument terms

```
pair(1, 2) wizard(harry) writeln(hello(world))
```

- A compound term is interpreted as a predicate, with a truth value, if it is a head term, a body term, or the goal
- Otherwise, the compound term is interpreted as data
 - e.g. hello(world) in writeln(hello(world))

Facts and Rules

■ A Horn clause with no body is a fact, since it is always true

```
mother(molly, bill).
mother(molly, charlie).
end of clause
```

A Horn clause with a body is a rule

```
parent(P, C) :- mother(P, C).
sibling(A, B) :- parent(P, A), parent(P, B).
```

- Meaning:
 - If mother(P, C) is true, then so is parent(P, C)
 - If parent(P, A) and parent(P, B) are true, then so is sibling(A, B)
- A program is a set of Horn clauses

Goals and Queries

- A goal is a predicate that the interpreter attempts to prove
- Loading the program from the previous slide and entering the goal sibling(bill, S) produces:

```
?- sibling(bill, S).
S = bill;
S = charlie.
Ask for more solutions
```

- A semicolon asks for more solutions
- A period ends a query
 - Can be entered by the user
 - Can be produced by the interpreter, in which case it is certain no more solutions exist

■ We'll start again in five minutes.

Implementing Lists

- Compound terms can represent data structures
- Example: use pair(A, B) to represent a pair
 - This won't be a head or body term, so it will be treated as data
- Relations on pairs:

cons(A, B, pair(A, B)).
cdr(pair(_, B), B).
car(pair(A, _), A).
is_null(nil).

Relates a first and second item to a pair

Anonymous variable

```
?- cons(1, nil, X).
X = pair(1, nil).
?- car(pair(1, pair(2, nil)), X).
X = 1.
?- cdr(pair(1, pair(2, nil)), X).
X = pair(2, nil).
?- cdr(pair(1, pair(2, nil)), X),
   car(X, Y), cdr(X, Z).
X = pair(2, nil), Y = 2, Z = nil.
?- is null(nil).
true.
?- is null(pair(1, nil)).
false.
```

Prolog Lists

 Prolog also provides built-in linked lists, specified as elements between square brackets

```
[] [1, a] [b, 3, foo(bar)]
```

■ The pipe symbol acts like a dot in Scheme, separating some elements from the rest of the list

```
?- writeln([1, 2 | [3, 4]]). [1,2,3,4] true.
```

This allows us to write predicates like the following:

```
contains([X|_], X).
contains([_|Ys], X) :- contains(Ys, X).
```

Numbers and Comparisons

- Prolog includes integer and floating-point numbers
- Comparison predicates can be written in infix order

```
?- 3 =< 4. % less than or equal
true.
?- 4 =< 3.
false.
?- 3 =:= 3. % arithmetic equal
true.
?- 3 =\= 3. % arithmetic not equal
false.</pre>
```

The = operator specifies explicit unification, not equality

Arithmetic

 Arithmetic operators represent compound terms and are not evaluated

Comparisons perform evaluation on both operands

```
?- 7 =:= 3 + 4. 7 is equal to the result of evaluating +(3, 4)
```

■ The is operator unifies its first argument with the arithmetic result of its second argument

List Length

We can now define a predicate for length on our list representation:
 Unify L with the

```
len(nil, 0).
len(pair(_, B), L) :- len(B, M), L is M + 1.
```

```
?- len(nil, X).
X = 0.
?- len(pair(1, pair(b, nil)), X).
X = 2.
```

Must be second body term so that M is sufficiently instantiated for arithmetic

Built-in lists have a built-in length predicate

```
?- length([1, a, 3], X).
X = 3.
```

Side Effects

- Prolog provides I/O predicates, including reading from standard input and writing to standard output
- We will only use write and writeln:

```
?- X = 3, write('The value of X is: '),
   writeln(X).
The value of X is: 3
X = 3.
```

Unification and Search

- A logic solver is built around the processes of unification and search
- Search in Prolog uses backward chaining
 - Start with a set of goal terms
 - Look for a clause whose head can unify with a goal term
 - If unification succeeds, replace the old goal term with the body terms of the clause
 - Search succeeds when no more goal terms remain
- Unification attempts to unify two terms, which may require recursively unifying subterms
 - May require instantiating variables to values

Unification

- An atomic term only unifies with itself
- A variable unifies with any term
 - If the other term is not a variable, then the variable is instantiated with the value of the other term, i.e. all occurrences of the variable are replaced with the value
 - If the other term is a variable, the two variables are bound together such that later instantiating one with a value also instantiates the other with the same value
- A compound term unifies with another compound term if the functors and number of arguments are the same, and the arguments recursively unify

```
X = 3

Y = foo(1, Z)

foo(1, A) = foo(B, 3) % unifies B = 1, A = 3
```

Instantiation and Renaming

- Applying a clause involves renaming variables that occur in different contexts to be unique and can result in instantiation of variables
 - ightharpoonup Analogous to a- and β-reduction in λ-calculus
- Example:

```
foo(X, Y) :- bar(Y, X). ?- foo(3, X).
```

- 1. Rename rule to foo(X1, Y1) :- bar(Y1, X1).
- 2. Unify foo(3, X) with foo(X1, Y1), resulting in X1 = 3 and X <=> Y1
- 3. New goal term bar(X, 3)

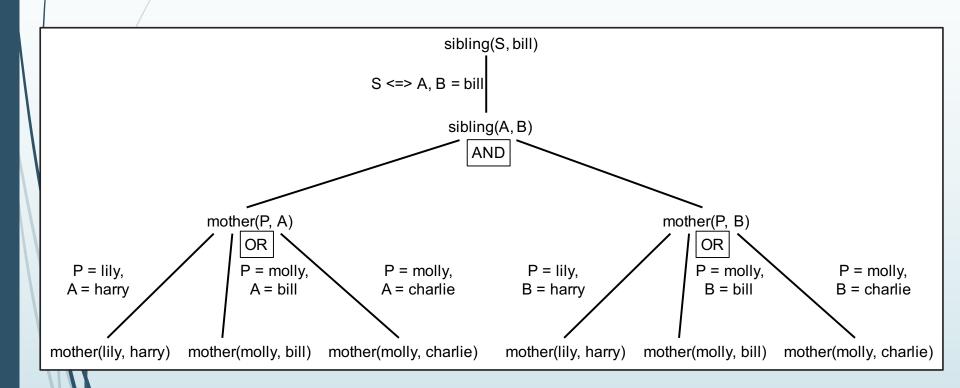
Search Order

- In pure logic programming, search order is irrelevant as long as the search terminates
- In Prolog, clauses are applied in program order, and terms within a body are resolved in left-to-right order
- Example:

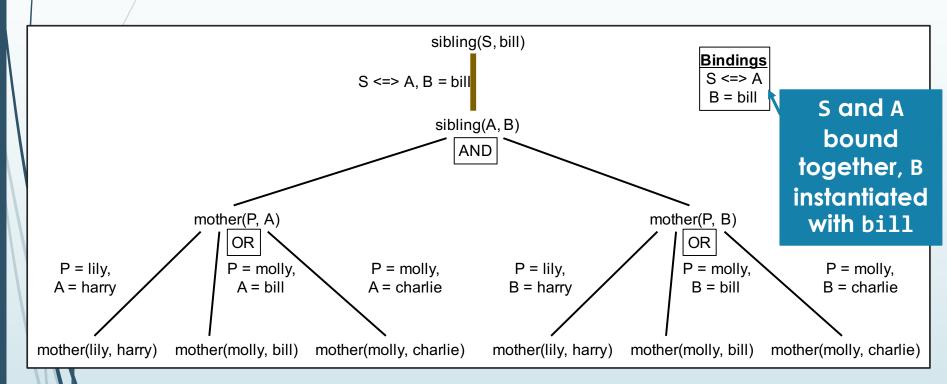
```
sibling(A, B) :- mother(P, A), mother(P, B).
mother(lily, harry).
mother(molly, bill).
mother(molly, charlie).
```

```
?- sibling(S, bill)
S = bill
```

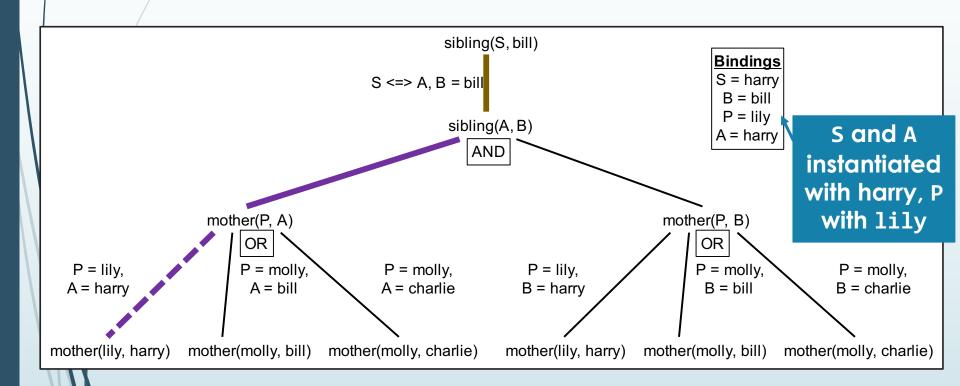
 Search encounters choice points, and backtracking is required on failure or if the user asks for more solutions



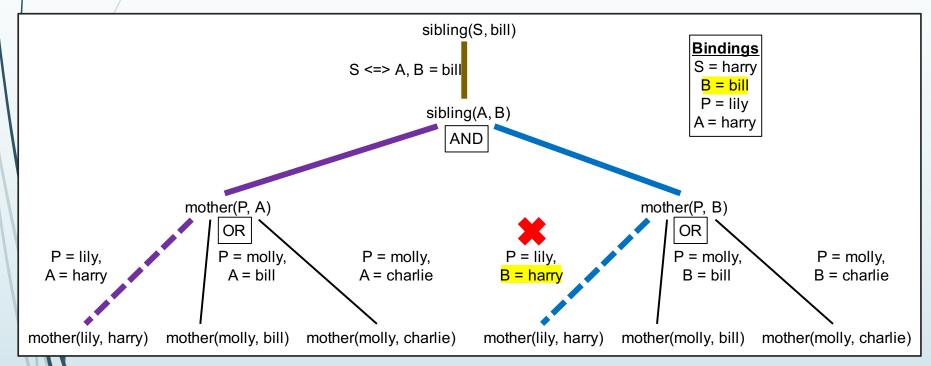
First, sibling(S, bill) is unified with the head term sibling(A, B), and the body terms of the clause are added to the goals



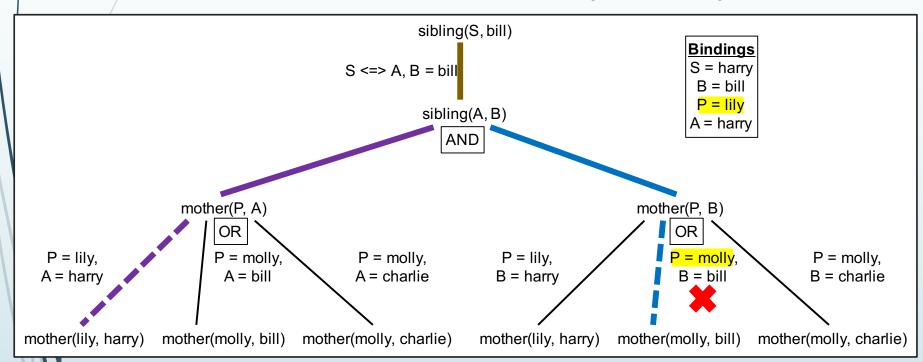
■ The goal mother(P, A) is solved first, with an initial choice of applying the fact mother(lily, harry)



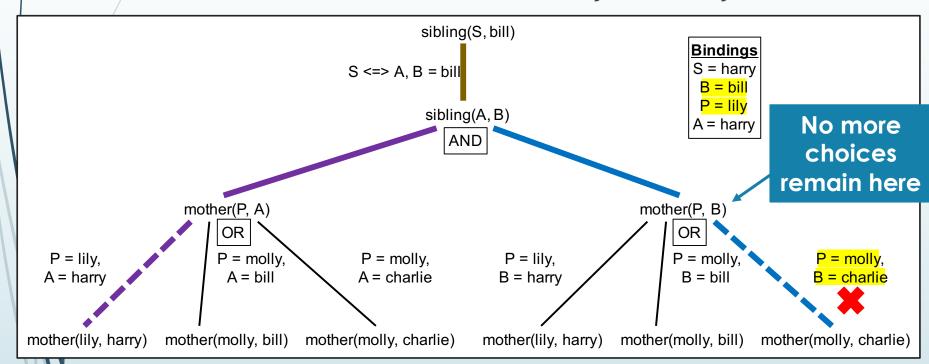
- Then the goal mother(P, B) is solved, with an initial choice of applying the fact mother(lily, harry)
- However, unification of B = bill with harry fails



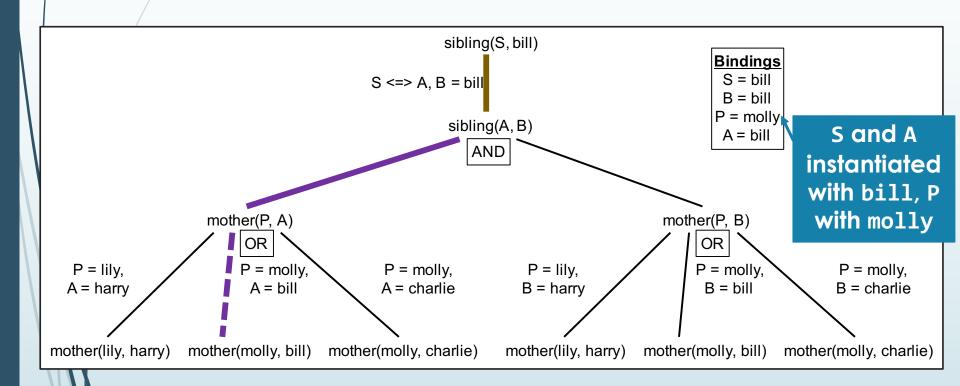
- The search backtracks to the previous choice point, attempting to apply the fact mother(molly, bill)
- However, unification of P = lily with molly fails



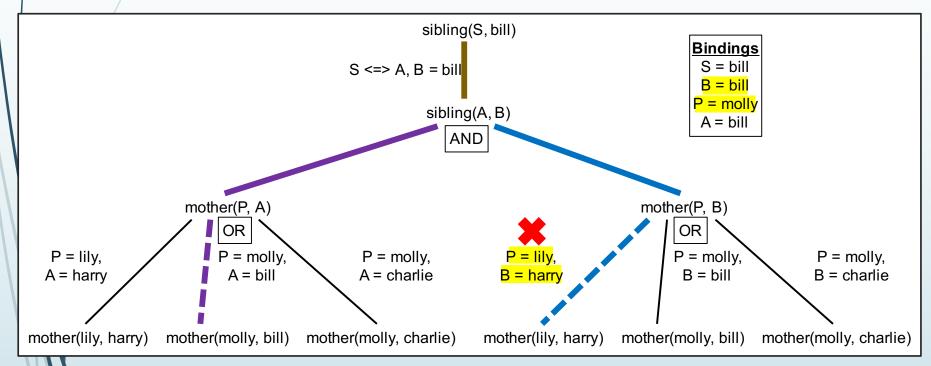
- The search backtracks once again, attempting to apply the fact mother(molly, charlie)
- However, unification of P = lily with molly fails



The search backtracks to the preceding choice point, unifying mother(P, A) with mother(molly, bill)

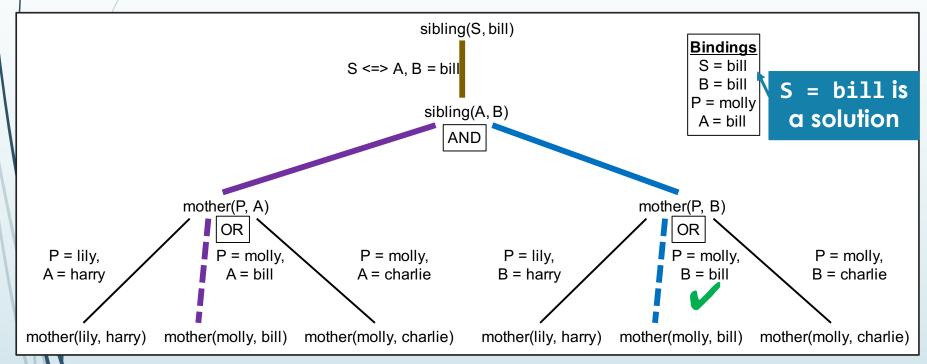


- Then the goal mother(P, B) is solved, with an initial choice of applying the fact mother(lily, harry)
- However, unification of B = bill with harry fails



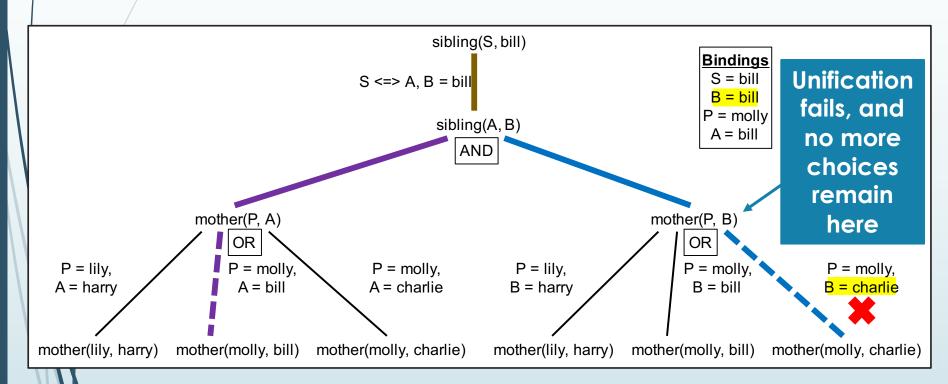
First Solution

- The search backtracks to the previous choice point, attempting to apply the fact mother(molly, bill)
- Unification succeeds, and no goal terms remain

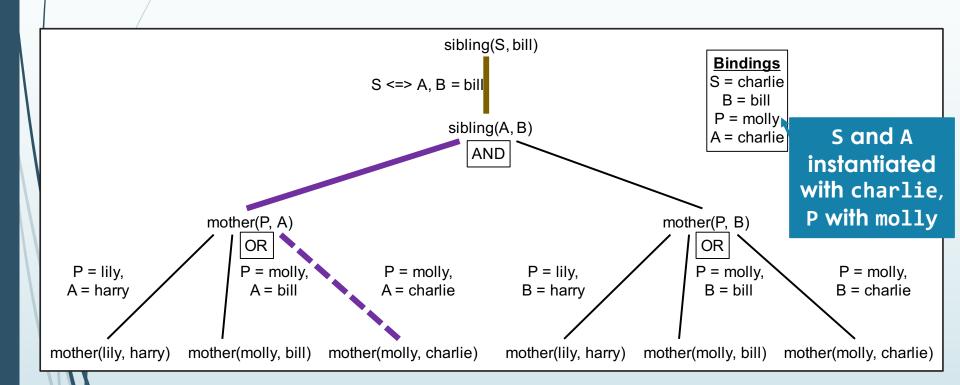


Continuing the Search

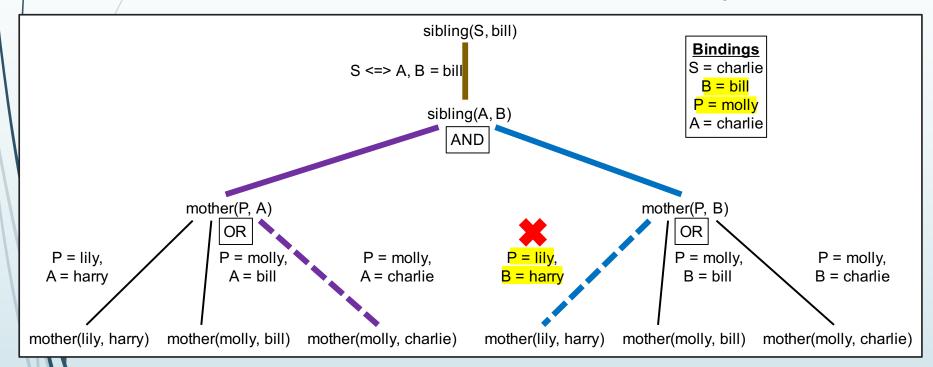
■ If we ask the interpreter for another solution, it backtracks to the previous choice point, attempting to apply the fact mother(molly, charlie)



The search backtracks to the preceding choice point, unifying mother(P, A) with mother(molly, charlie)

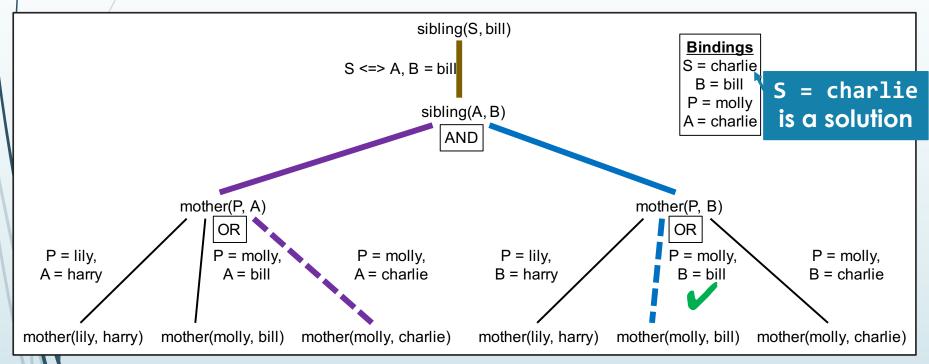


- Then the goal mother(P, B) is solved, with an initial choice of applying the fact mother(lily, harry)
- However, unification of B = bill with harry fails



Second Solution

- The search backtracks to the previous choice point, attempting to apply the fact mother(molly, bill)
- Unification succeeds, and no goal terms remain



No More Solutions

If we ask the interpreter for another solution, it backtracks to the previous choice point, attempting to apply the fact mother(molly, charlie)

