



# EECS 490 – Lecture 21

Logic, Constraints, and Dependencies

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# Announcements

- ▶ Project 4 due tonight at 8pm
- ▶ HW5 due Tue 12/5 at 8pm
- ▶ Project 5 due Tue 12/12 at 8pm

# Prolog Example: Quicksort

## ► Partition:

```
partition(_, [], [], []).  
partition(Pivot, [Item|Rest], [Item|Less], NotLess) :-  
    Item < Pivot,  
    partition(Pivot, Rest, Less, NotLess).  
partition(Pivot, [Item|Rest], Less, [Item|NotLess]) :-  
    Item >= Pivot,  
    partition(Pivot, Rest, Less, NotLess).
```

## ► Sort:

```
quicksort([], []).  
quicksort([Item|Rest], Sorted) :-  
    partition(Item, Rest, Less, NotLess),  
    quicksort(Less, SortedLess),  
    quicksort(NotLess, SortedNotLess),  
    append(SortedLess, [Item|SortedNotLess], Sorted).
```

# Prolog Example: Primes

- Sieve of Eratosthenes:

```
numbers(2, [2]).
numbers(Limit, Numbers) :-
    M is Limit - 1, numbers(M, NumbersToM),
    append(NumbersToM, [Limit], Numbers).

is_not_multiple(N, D) :- R is mod(N, D), R =\= 0.

filter_not_multiple(_, [], []).
filter_not_multiple(Factor, [First|Rest],
    [First|FilteredRest]) :-
    is_not_multiple(First, Factor),
    filter_not_multiple(Factor, Rest, FilteredRest).
filter_not_multiple(Factor, [_|Rest], FilteredRest) :-
    filter_not_multiple(Factor, Rest, FilteredRest).

sieve([]).
sieve([First|Rest], [First|SievedRest]) :-
    filter_not_multiple(First, Rest, FilteredRest),
    sieve(FilteredRest, SievedRest).

primes(Limit, Primes) :-
    numbers(Limit, Numbers), sieve(Numbers, Primes).
```

# Constraint Logic Programming

- Extension of logic programming to include constraints on variables
- Basic Prolog includes limited arithmetic constraints that require variables to be instantiated

```
square_sum([N, X, Y, Z]) :-  
    N == Z * Z, N == X * X + Y * Y,  
    X > 0, Y > 0, Z > 0, X < Y, N < 1000.
```

```
?- square_sum(S).  
ERROR: ==/2: Arguments are not sufficiently  
instantiated
```

# CLP(FD)

- The CLP family of libraries provide constraint logic programming as extensions to Prolog
- CLP(FD) is included in SWI-Prolog and works on finite domains (integer subsets)

Import  
CLP(FD)  
module

```
:- use_module(library(clpfd)).
```

CLP(FD)  
constraint  
operator

```
square_sum_c([N, X, Y, Z]) :-  
    N #= Z * Z, N #= X * X + Y * Y,  
    X #> 0, Y #> 0, Z #> 0, X #< Y, N #< 1000,  
    label([N, X, Y, Z]).
```

Require given  
variables to  
be *grounded*

```
?- square_sum_c(S).  
S = [25, 3, 4, 5] ;  
S = [100, 6, 8, 10] ;  
S = [169, 5, 12, 13] ;  
...
```

# Search in CLP

- Search follows the same general strategy as Prolog, except that a *constraint store* keeps track of the set of constraints
  - Start with a set of goal terms
  - For first goal term, find a clause whose head can be unified with the term
    - Unification can instantiate or bind variables
  - Insert body terms that are not constraints into the front of the set of goal terms
  - Insert body terms that are constraints into the constraint store
  - Check whether the constraint store is unsatisfiable
    - If so, backtrack
- Search succeeds when no more goal terms remain, and the constraint store is not unsatisfiable

# Example: Verbal Arithmetic

- Find a solution to the following such that each digit is distinct, and leading digits are non-zero:

	S	E	N	D	
+		M	O	R	E
	-----				
=	M	O	N	E	Y

- Plain Prolog:

```
money([S, E, N, D, M, O, R, Y]) :-
    is_digit(S), is_digit(E), is_digit(N), is_digit(D),
    is_digit(M), is_digit(O), is_digit(R), is_digit(Y),
    S \= 0, M \= 0,
    S \= E, S \= N, S \= D, S \= M, S \= O, S \= R, S \= Y,
    E \= N, E \= D, E \= M, E \= O, E \= R, E \= Y,
    N \= D, N \= M, N \= O, N \= R, N \= Y,
    D \= M, D \= O, D \= R, D \= Y,
    M \= O, M \= R, M \= Y,
    O \= R, O \= Y,
    R \= Y,
```

$$\begin{aligned}
 &1000 * S + 100 * E + 10 * N + D \\
 + &1000 * M + 100 * O + 10 * R + E \\
 =: &10000 * M + 1000 * O + 100 * N + 10 * E + Y.
 \end{aligned}$$

**Takes 90  
seconds to  
solve on  
Macbook**



# Example: Verbal Arithmetic

- Find a solution to the following such that each digit is distinct, and leading digits are non-zero:

$$\begin{array}{r}
 \text{S E N D} \\
 + \quad \text{M O R E} \\
 \hline
 = \text{M O N E Y}
 \end{array}$$

- Prolog + CLP(FD):

```

money_c([S, E, N, D, M, O, R, Y]) :-
    L = [S, E, N, D, M, O, R, Y],
    L ins 0 .. 9, S #\= 0, M #\= 0, all_distinct(L),

```

Takes 0.2  
seconds to  
solve on  
Macbook

Require variables in L to  
be members of set [0, 9]

Constrain variables in L  
to have distinct values

```

1000 * S + 100 * E + 10 * N + D
+
1000 * M + 100 * O + 10 * R + E
#= 10000 * M + 1000 * O + 100 * N + 10 * E + Y,
label(L).

```

# Example: Sudoku

## ► Sudoku solver:

```
sudoku(Rows) :-
    length(Rows, 9), maplist(same_length(Rows), Rows),
    append(Rows, Values), Values ins 1..9,
    maplist(all_distinct, Rows),
    transpose(Rows, Columns),
    maplist(all_distinct, Columns),
    Rows = [Row1, Row2, Row3, Row4, Row5, Row6, Row7, Row8, Row9],
    blocks(Row1, Row2, Row3),
    blocks(Row4, Row5, Row6),
    blocks(Row7, Row8, Row9),
    maplist(label, Rows).
```

Higher-order predicate

Partial application

```
blocks([], [], []).
blocks([N1, N2, N3 | RestRow1],
      [N4, N5, N6 | RestRow2],
      [N7, N8, N9 | RestRow3]) :-
    all_distinct([N1, N2, N3, N4, N5, N6, N7, N8, N9]),
    blocks(RestRow1, RestRow2, RestRow3).
```

- ▶ We'll start again in five minutes.

# Make

- Tool for automating the building of software packages, tracking dependencies between components
- Programming model is a combination of declarative and imperative
- A *rule* declares a relation between a target and its dependencies, specifies commands to build the target

target: dependencies  
commands

**Zero or more  
targets or files**

**Tab  
indentation**

**Sequence of zero or  
more commands, usually  
each on its own line**

# Simple Example

- Rule contained within Makefile:

```
hello:
    echo "Hello world!"
```

**No dependencies**

**Build hello  
target**

**Build first  
target in  
Makefile**

```
> make hello
echo "Hello world!"
Hello world!
> make
echo "Hello world!"
Hello world!
```

**Target has no  
dependencies, so  
it will always build**

# Building an Executable

- More complex dependency trees can be specified

```
main: a.o b.o c.o
      g++ -o main a.o b.o c.o

a.o: a.cpp
     g++ --std=c++14 -Wall -pedantic -c a.cpp

b.o: b.cpp
     g++ --std=c++14 -Wall -pedantic -c b.cpp

c.o: c.cpp
     g++ --std=c++14 -Wall -pedantic -c c.cpp
```

```
> make
g++ --std=c++14 -Wall -pedantic -c a.cpp
g++ --std=c++14 -Wall -pedantic -c b.cpp
g++ --std=c++14 -Wall -pedantic -c c.cpp
g++ -o main a.o b.o c.o
```

# Rebuilding a Target

- A target is only rebuilt when one of its dependencies has been modified

Modify timestamp  
on b.cpp

```
> touch b.cpp
> ls -l
-rw-r--r--  1 kamil  staff    229 Nov 17 01:01 Makefile
-rw-r--r--  1 kamil  staff     90 Nov 17 00:57 a.cpp
-rw-r--r--  1 kamil  staff   6624 Nov 17 01:01 a.o
-rw-r--r--  1 kamil  staff     31 Nov 17 01:12 b.cpp
-rw-r--r--  1 kamil  staff    640 Nov 17 01:01 b.o
-rw-r--r--  1 kamil  staff     33 Nov 17 00:58 c.cpp
-rw-r--r--  1 kamil  staff    640 Nov 17 01:01 c.o
-rwxr-xr-x  1 kamil  staff  15268 Nov 17 01:01 main
> make
g++ --std=c++14 -Wall -Werror -pedantic -c b.cpp
g++ -o main a.o b.o c.o
```

# Example: Makefile for Notes

```
all: foundations functional theory data declarative
foundations: foundations.html foundations.tex
functional: functional.html functional.tex
theory: theory.html theory.tex
data: data.html data.tex
declarative: declarative.html declarative.tex
asynchronous: asynchronous.html asynchronous.tex
metaprogramming: metaprogramming.html metaprogramming.tex

%.html: %.rst
    rst2html.py --stylesheet=../style/style.css $< > $@

%.tex: %.rst
    rst2latex.py --stylesheet=../style/style.sty $< > $@
    pdflatex $@
    pdflatex $@
    pdflatex $@

clean:
    rm -vf *.html *.tex *.pdf *.aux *.log *.out
```

**Not currently built**

**Pattern rule**

**Build PDF file**

**Dependencies**

**Target**