

2. Using the simple imperative language shown in lecture, write out the derivation trees for the following expressions and statements using operational semantics

$P \rightarrow S$ $S \rightarrow \text{skip} \mid S; S \mid V = A$   <b>if</b> $B$ <b>then</b> $S$ <b>else</b> $S$ <b>end</b>   <b>while</b> $B$ <b>do</b> $S$ <b>end</b> $A \rightarrow N \mid V \mid (A + A) \mid (A - A) \mid (A * A)$ $B \rightarrow \text{true} \mid \text{false} \mid (A \leq A) \mid (B \text{ and } B) \mid \text{not } B$ $V \rightarrow \text{Identifier}$ $N \rightarrow \text{IntegerLiteral}$	$x = -1$  1. $((x * 3) - 2)$ 2. $((x \leq 3) \text{ and } (0 \leq x))$
---	---

$$\begin{array}{r}
 \langle x, \sigma \rangle \rightarrow -1 \quad \langle 3, \sigma \rangle \rightarrow 3 \\
 \hline
 \langle (x * 3), \sigma \rangle \rightarrow -3 \quad \langle 2, \sigma \rangle \rightarrow 2 \\
 \hline
 \langle ((x * 3) - 2), \sigma \rangle \rightarrow -5
 \end{array}$$

$$\begin{array}{r}
 \langle x, \sigma \rangle \rightarrow -1 \quad \langle 3, \sigma \rangle \rightarrow 3 \quad \langle 0, \sigma \rangle \rightarrow 0 \quad \langle x, \sigma \rangle \rightarrow -1 \\
 \hline
 \langle (x \leq 3), \sigma \rangle \rightarrow \text{true} \quad \langle (0 \leq x), \sigma \rangle \rightarrow \text{false} \\
 \hline
 \langle ((x \leq 3) \text{ and } (0 \leq x)), \sigma \rangle \rightarrow \text{false}
 \end{array}$$

3. Suppose we wanted to add the ternary conditional ( $B ? A : A$ ) to our language, where  $(b ? a_1 : a_2)$  evaluates to  $a_1$  if  $b$  evaluates to true and  $a_2$  otherwise. Write rules for the evaluating a ternary conditional using big-step operational semantics.

$$\begin{array}{r}
 \langle b, \sigma \rangle \rightarrow \text{true} \quad \langle a_1, \sigma \rangle \rightarrow n_1 \\
 \hline
 \langle (b ? a_1 : a_2), \sigma \rangle \rightarrow n_1
 \end{array}$$

$$\begin{array}{r}
 \langle b, \sigma \rangle \rightarrow \text{false} \quad \langle a_2, \sigma \rangle \rightarrow n_2 \\
 \hline
 \langle (b ? a_1 : a_2), \sigma \rangle \rightarrow n_2
 \end{array}$$