

VE477

Introduction to Algorithms

Project (part 1)

Manuel — UM-JI (Fall 2017)

Goals of the project

- Know the common algorithmic problems
- Relate problems to real life applications
- Construct a catalog of the problems with their solutions

1 Setup

Important note: At the end of each part this document will be re-issued with completed tasks crossed out. Please do not forget to always refer to the latest version available. Please contact us if you think a problem has been misclassified, or if you feel any adjustment or clarification is needed.

1.1 Groups

Groups can be freely organised as long as the following rules are respected:

- No more than three students per group;
- Each group must register on Canvas (ve477 → People → Groups);
- A student must belong to exactly one group;

1.2 Problem selection

All the problems listed in section 3, are sorted by category and then by degree of difficulty. Solving an easy, not too hard, or hard problem will be rewarded by one, two, or three credits, respectively. No more than three credits can be selected from easy problems.

For each part of the project, students belonging to groups of one, two, or three students are expected to complete four, nine, or thirteen credits, respectively.

Each group needs to register on Canvas for each problem it selects. The group number used for registration is the one assigned on Canvas (cf. subsection 1.1).

No more than two groups can select a same problem. If four or more groups select a problem, the remaining groups will wait in a queue and be called upon if one of the three first groups decides to change problem. Freely changing problems is allowed until October 2, November 6, and December 4, for part 1, 2 and 3, respectively. Past the deadline a problem is considered to belong to the three first groups which registered for it. It should however be reminded that the final total number of credits of a group must remain unchanged. For instance changing a hard problem for an easy one is not permitted, while changing it for one easy and one “not too hard” is allowed, in the limit of three easy problems per group.

1.3 Catalog cover

This part of the project is not mandatory and only based on voluntary participations.

The goal of this project being the creation of a catalog it should feature a front page showing the following information: (i) a name, (ii) the course reference, and (iii) the academic year. All the rest of the design is left to your creativity. . .

You can freely propose covers by uploading a file on Canvas under the assignment “catalog cover” until December 15th. All the submissions will be made available for voting and the one with the most votes will be used as the official cover of the “Algorithm catalog” for the academic year 2017–2018. The designer(s) of the selected cover will be awarded a bonus.

2 Content

The goal being to construct a catalog listing problems together with their algorithmic solutions it is important that they are all treated following a similar pattern. Therefore a \LaTeX template has been posted on Canvas.

For each problem provide:

- A clear and brief description of the problem as well as of its input and complexity;
- Information on where it occurs or example applications;
- Some precise pseudocode of an efficient algorithm solving it;
- References where this problems is described, solved, or discussed;

Note that the goal is to be able to refer to the catalog over a long period of time. It is therefore better to provide several links or references, privileging links which are less likely to disappear (scientific articles, books, wikipedia. . .)

Important instructions regarding the template file:

- Do not change any line in the preamble unless it is to (un)comment the `\def\tcbox{}` line.
- Define the problem type on the line `\pbtype{type}`
- Do not include more than one problem per file
- Name the file after the problem number (e.g. `problem12.tex`).

3 Problems

3.1 Data structures

Easy to study:

1. Adjacency lists and adjacency matrices
2. Dictionaries (maps, multi-maps)
3. Priority queues
4. Union-Find

Not hard to study:

- | | |
|---|-----------------------------|
| 5. Bloom filters | 7. Generalized suffix trees |
| 6. Fibonacci heaps (note: hard, done in labs) | 8. Kd-Trees |

3.2 Combinatory

Easy to study:

- | | |
|-----------------------------|---|
| 9. Calendar generation | 12. SAT |
| 10. Generating graphs | 13. Searching |
| 11. Generating permutations | 14. Sorting (Merge sort, quick sort, heap sort) |

Not hard to study:

- | | |
|---------------------------|------------------------|
| 15. Generating Partitions | 16. Generating Subsets |
|---------------------------|------------------------|

3.3 Graph

Easy to study:

- | | |
|-------------------------------|-------------------------|
| 17. Graph traversal | 19. Prufer sequence |
| 18. Maximally-matchable edges | 20. Subtree isomorphism |

Not hard to study:

- | | |
|--------------------------------------|------------------------------------|
| 21. All-pairs shortest path | 30. Matching |
| 22. Clique problem | 31. Matching preclusion |
| 23. Closure problem | 32. Maximum cardinality matching |
| 24. Color coding | 33. Path finding |
| 25. Dulmage-Mendelsohn decomposition | 34. Single source shortest path |
| 26. Graduation problem | • Directed and non-directed graphs |
| 27. Graph coloring | • Non-negative and real weights |
| 28. Hitchcock Transport problem | 35. Traveling salesman problem |
| 29. Level ancestor problem | 36. Vertex independent set |

3.4 Mathematics

Easy to study:

- | | |
|-------------------------------------|------------------------------------|
| 37. Determinant of a matrix | 42. Matrix multiplication |
| 38. Fast/Discrete Fourier Transform | 43. Miller-Rabbin |
| 39. Gaussian elimination | 44. Modular exponentiation |
| 40. GCD and Bezout's identity | 45. Newton's method |
| 41. Karatsuba's multiplication | 46. Polynomial evaluation (Horner) |

Not hard to study:

- | | |
|--|---|
| 47. Interpolation | 50. Random number generation |
| 48. Intersection detection | 51. Square roots mod p (Tonelli-Shanks) |
| 49. Matrix inversion (Cholesky, Levinson-Durbin) | 52. Triangulation |

Hard to study:

- | | |
|---|---------------------|
| 53. Factorization (Multi Precision Quadratic Sieve) | 55. Shortest vector |
| 54. Primality testing (AKS) | |

3.5 Networks

Easy to study:

- | | |
|-----------------------------|-----------------------------------|
| 56. Back-pressure routing | 63. Maximum throughput scheduling |
| 57. Class-based queueing | 64. Max-min Fairness |
| 58. Deficit round robin | 65. MENTOR routing |
| 59. Distance-vector routing | 66. Random early detection |
| 60. Fair queueing | 67. Token bucket / leaky bucket |
| 61. Flood search routing | 68. Traffic shaping |
| 62. Link-state routing | |

3.6 Strings

Easy to study:

- | | |
|---------------------------|----------------------|
| 69. Edit distance problem | 72. String matching |
| 70. Set cover | 73. Text compression |
| 71. Set packing | |

Not hard to study:

- | | |
|---------------------------------------|---------------------------------|
| 74. Finite state machine minimization | 76. Shortest common superstring |
| 75. Longest common substring | |