2017 Integration Bee

Society for Undergraduate Mathematics Students

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Figure: May the odds be ever in your favor



Integral Calisthenics



$\sin x + \cos x + \csc x + \sec x \, \mathrm{d}x$



$$\int \frac{(9^3 + 10^3)x^{1728}}{\sin^2 x + \cos^2 x} \, \mathrm{d}x$$



 $\int \frac{x+1}{x^2+2x+3} \, \mathrm{d}x$



$$\int \frac{x^{2017} dx}{(x^{2018} + \pi^{2018})}$$



$$\int e^{e^X} e^X \, \mathrm{d} x$$



$\int \sin(\sin x) \cos x \, dx$



$\int \sin(x)\cos(x)\cot(x)\tan(x) dx$



$$\int 5x\sqrt{49-4x^2}\,\mathrm{d}x$$



$\int \cos^3(x) \sin(x) \, \mathrm{d}x$



$\int \sin^2(\sin(x))\cos(x)\,\mathrm{d}x$



 $\int \frac{4x+6}{2x^2+5x-3} \, \mathrm{d}x$



$$\int \frac{\cos(\ln(x))}{x} \, \mathrm{d}x$$



$\int \sin^2(x) \, \mathrm{d}x$



$\int xe^{x} dx$



 $\int \frac{2x^2 + 3}{x - 2} \, \mathrm{d}x$



$\int x \ln(x) \, \mathrm{d}x$



$$\int \frac{\ln(x) \, \mathrm{d}x}{x^2}$$



$\int_{-\pi}^{\pi} x \sin(x) dx$



$$\int \frac{\cos(x)}{\sqrt{1 + 16\sin^2(x)}} \, \mathrm{d}x$$



$$\int \frac{x}{\sqrt{1+x^2}} \, \mathrm{d}x$$



Intermediate Integrals



 $\int \frac{2x+6}{x^2+3x+2} \, \mathrm{d}x$



$$\int e^{12x} \sqrt{e^{12x} - \pi} \, \mathrm{d}x$$



$$\int \frac{\ln(\ln(x))}{x} \, \mathrm{d}x$$



$$\int x^3 \cos(2x) \, \mathrm{d}x$$



$$\int \frac{14 - 7x}{2x^2 + 5x - 3} \, \mathrm{d}x$$



 $\int \sin(\sqrt{x})$



$\int \tanh x \, \mathrm{d}x$



$\int \sec^8 x \tan x \, \mathrm{d}x$



$$\int x\sqrt{x+1}\,\mathrm{d}x$$



$\int \sin^2(x) \cos^2(x) \, \mathrm{d}x$



$\int \pi^{x} dx$



$$\int x^2 \ln(x) \, \mathrm{d}x$$



Spicy Integrals



$$\int \cos x \sqrt{\sin^2 x + 1} \, \mathrm{d}x$$



$\int \cosh^{-1}(x) \, \mathrm{d}x$



 $\int \frac{x^2}{1+x^2}$



$$\int \frac{1+\sin x}{1+\cos x}$$



$$\int \frac{1}{1 - x + x^2}$$



$\int_{-2017}^{2017} \sin\left(\sqrt[3]{x}\right) dx$



$$\int \frac{1}{1+e^x} \, \mathrm{d}x$$



 $\int (1+2x^2)e^{x^2}\,\mathrm{d}x$



 $\int \frac{e^{ix}}{x^2 + 1} \, \mathrm{d}x$



$$\int x(1-x)^{2017}$$



$$\int_{-\pi}^{\pi} \frac{x^3 - 2x}{\sqrt{x^4 + 1}}$$



 $\int \frac{1}{x(x^5+1)} \, \mathrm{d}x$



Challenge



 $\int \sinh x \sin x \, dx$



 $\int_{-\infty}^{\infty} \frac{1}{x^4 + 4} \, \mathrm{d}x$



$$\int \frac{\ln x \cos x - \frac{1}{x} \sin x}{\ln^2 x} \, \mathrm{d}x$$



 $\int_{-\infty}^{\infty} \frac{1}{1+x^2} \, \mathrm{d}x$



$$\int_0^\infty \frac{3\sqrt{3}}{1+x^3} \, \mathrm{d}x$$

