## **Title**

### D. Zack Garza

# Sunday 23<sup>rd</sup> August, 2020

### **Contents**

1	Frid	Friday, August 21																					
	1.1	Intro	and Definiti	ons .																 			
		1.1.1	Examples																	 			

### 1 Friday, August 21

#### 1.1 Intro and Definitions

**Definition 1.0.1** (Affine Variety).

Let  $k = \overline{k}$  be algebraically closed (e.g.  $k = \mathbb{C}, \overline{\mathbb{F}_p}$ ). A variety  $V \subseteq k^n$  is an affine k-variety iff V is the zero set of a collection of polynomials in  $k[x_1, \dots, x_n]$ .

Here  $\mathbb{A}^n := k^n$  with the Zariski topology, so the closed sets are varieties.

### **Definition 1.0.2** (Affine Algebraic Group).

An  $affine\ algebraic\ k$ -group is an affine variety with the structure of a group, where the multiplication and inversion maps

$$\mu:G\times G\longrightarrow G$$
 
$$\iota:G\longrightarrow G$$

are continuous.

### Example 1.1.

### 1.1.1 Examples

**1**  $G = \mathbb{G}_a \subseteq k$  the additive group of k is defined as  $\mathbb{G}_a := (k, +)$ . We then have a coordinate ring  $k[\mathbb{G}_a] = k[x]/I = k[x]$ .

**2** G = GL(n, k), which has coordinate ring  $k[x_{ij}, T] / \det(x_{ij}) \cdot T = 1$ .