$$K^{\times}/\langle q \rangle \longrightarrow E_q(K)$$

$$\downarrow \qquad \qquad \downarrow$$

$$L^{\times}/\langle q \rangle \longrightarrow E_q(L)$$