$$K^{\times}/\langle q \rangle \xrightarrow{\cong \phi_K} E_q(K)$$

$$\downarrow \qquad \qquad \downarrow$$

$$K^{\times}/\langle q \rangle \xrightarrow{\cong \phi_L} E_q(L)$$