Title

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Exercise 1.1 (?)**.**

Show that the 3 natural coordinate charts on $\mathbb{CP}^2$ given by e.g. $\varphi_{U_0}([z_0 : z_1 : z_2]) = \left[\dfrac{z_1}{z_0}, \dfrac{z_2}{z_0} \right]$ yield a smooth atlas.

Exercise 1.2 (?)**.**
Consider the map

$$\pi : \mathbb{CP}^2 \to \mathbb{R}^2$$

$$[z_0 : z_1 : z_2] \mapsto \left[\frac{|z|_1^2}{|z|_0^2 + |z|_1^2 + |z|_2^2}, \frac{|z|_2^2}{|z|_0^2 + |z|_1^2 + |z|_2^2} \right].$$

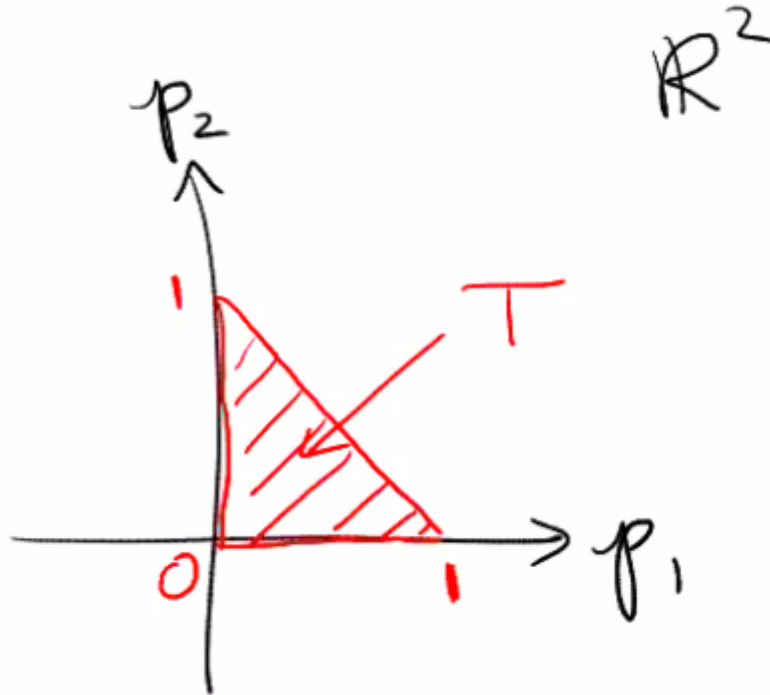Show that π is smooth and $\text{im}\pi = \{p_1, p_2 \geq 0, p_1 + p_2 \leq 1\}$.

Figure 1: O

Exercise 1.3 (?).
Show that

- If $[p_1, p_2] \in T^\circ$ is in the interior of the above triangle, then $\pi^{-1}(p_1, p_2) \cong S^1 \times S^1$ is diffeomorphic to a torus.
- If the point is on an edge, the fiber is diffeomorphic to S^1,
- If the point is on a vertex, the fiber is diffeomorphic to a single point.