

Algebra

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Definition: A *group* is an ordered pair $(G, \cdot : G \times G \rightarrow G)$ where G is a set and \cdot is a binary operation, which satisfies the following axioms:

1. Associativity: $(g_1 g_2) g_3 = g_1 (g_2 g_3)$
2. Identity: $\exists e \in G \ni ge = eg = g$
3. Inverses: $g \in G \implies \exists h \in G \ni gh = gh = e$.

Some examples of groups:

- $(\mathbb{Z}, +)$
- $(\mathbb{Q}, +)$
- $(\mathbb{Q}^\times, \times)$
- $(\mathbb{R}^\times, \times)$
- $(\text{GL}(n, \mathbb{R}), \times)$
- (S_n, \circ)