Title

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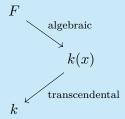
1.1 Chapter 1



Let k be a field, not necessarily algebraically closed.

Definition 1.1.1 (Algebraic Function Field).

An one variable algebraic function field F/K is a field extension F of K which factors as



where $x \in \bar{k}$ is some element that is not algebraic over k.

Definition 1.1.2 (Field of Constants).

The subfield

$$\tilde{k} := \left\{ z \in F \cap K^{\text{alg}} \right\} \le F,$$

consisting of elements that are algebraic over F is denoted the **field of constants**.

Definition 1.1.3 (Algebraically Closed).

If $\tilde{k} = k$, we say that k is algebraically closed in F.

Definition 1.1.4 (Rational Function Field).

An extension F/k is **rational** iff F = k(y) for some $y \in k^{\text{transc}}$ which is transcendental over k.

Definition 1.1.5 (Valuation Ring).

A ring $\mathcal{O} \subseteq F$ is a valuation ring for F iff $k \subset \mathcal{O} \subseteq F$ and $z \in F \implies z \in \mathcal{O}$ or $z^{-1} \in \mathcal{O}$.

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Definition 1.1.6 (Discrete Valuation Ring).

A ring local R (thus with a unique maximal ideal) which is a PID but not a field is a **discrete** valuation ring.

Definition 1.1.7 (Place).

A place of a function field F/K is the maximal ideal of a valuation ring of \$Fk

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