# Title

D. Zack Garza

## **Table of Contents**

### **Contents**

Table of Contents										2							
1	Lect	ture 12															3
	1.1	Brauer Groups								 	 		 	 			3

Table of Contents

Lecture 12

# 1 | Lecture 12

#### 1.1 Brauer Groups

Goal: for C a curve over  $k = \overline{k}$ , we've computed

$$H^{i}(C, \mathbb{G}_{m}) = \begin{cases} \mathcal{O}_{C}^{\times}(C) & i = 0 \\ \operatorname{Pic}(C) & i = 1 \\ 0 & i > 1 \end{cases}$$

Currently i > 1 is a mystery, so today we'll look at i = 2. Recall that we've reduced this to the Galois cohomology of the function field  $H^i(k(C), \mathbb{G}_m)$  and of the strict Henselization  $H^i(K_{\overline{x}}, \mathbb{G}_m)$ .

Today we'll try to understand the Galois cohomology of a field with coefficient in  $\bar{k}^{\times}$ , or  $\mathbb{G}_m$  thought of as a sheaf on the étale site. We'll discuss i = 2, and a general principle in group cohomology is that if one understands i = 1, 2 then one can often understand all degrees.

In general,  $H^1$  has a geometric interpretation: torsors.

 $H^2$  is much harder: they classify more general objects called **gerbes** 

Lecture 12 3

<sup>&</sup>lt;sup>1</sup>The stalk of the structure sheaf,  $\mathcal{O}_{C,x}$ .