

Title

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Remark 1.

There is a natural action of $\mathrm{MCG}(\Sigma)$ on $H_1(\Sigma; \mathbb{Z})$, i.e. a *homology representation* of $\mathrm{MCG}(\Sigma)$:

$$\begin{aligned}\rho : \mathrm{MCG}(\Sigma) &\rightarrow \mathrm{Aut}_{\mathrm{Grp}}(H^1(\Sigma; \mathbb{Z})) \\ f &\mapsto f_*.\end{aligned}$$

Theorem 1.1 (*Mapping Class Group of the Torus*).

There is a group isomorphism

$$\sigma : \mathrm{MCG}(\Sigma_2) \rightarrow \mathrm{SL}(2, \mathbb{Z})$$

which is given by sending any self-homeomorphism f