## **Title**

## D. Zack Garza

## Tuesday $15^{th}$ September, 2020

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1.1 Review	
Let $k = \bar{k}$ , we're setting up correspondences	
Polynomial functions	Affine space
· ·	$\mathbb{A}^n/k \coloneqq \{[a_1, \cdots, a_n] \in k^n\}$
Maximal ideals $\langle x_1 - a_1, \cdots, x_n - a_n \rangle$	Points $[a_1, \cdots, a_n] \in \mathbb{A}^n/k$
Radical ideals $I \leq k[x_1, \cdots, x_n]$	Affine varieties $X \subset \mathbb{A}^n/k$ , vanishing locii of polynomial
I	$\mapsto V(I) \coloneqq \left\{ a \mid f(a) = 0 \forall f \in I \right\}$
$I(X) := \left\{ f \mid f _X = 0 \right\}$	$\leftarrow X$
Radical ideals containing $I(X)$ , i.e. ideals in $A(X)$	closed subsets of $X$ , i.e. affine subvarieties
A(X) is a domain	X irreducible
A(X) is not a direct sum	X connected
Prime ideals in $A(X)$	Irreducible closed subsets of $X$
Krull dimension $n$ (longest chain of prime ideals)	$\dim X = n$ , (longest chain of irreducible closed subsets)
Ring Theory	Geometry/Topology of Affine Varieties.

Recall that we defined the coordinate ring  $A(X) := k[x_1, \cdots, x_n]/I(X)$ , which contained no nilpotents.

We had some results about dimension

- 1.  $\dim X < \infty$  and  $\dim \mathbb{A}^n = n$ .
- 2.  $\dim Y + \mathrm{codim}_X Y = \dim X$  when  $Y \subset X$  is irreducible.

3.