

Title

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Tuesday 29th September, 2020

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Exercise 1.1 (?).

Show that the 3 natural coordinate charts on \mathbb{CP}^2 given by e.g. $\varphi_{U_0}([z_0 : z_1 : z_2]) = \left[\frac{z_1}{z_0}, \frac{z_2}{z_0} \right]$ yield a smooth atlas.

Exercise 1.2 (?).

Consider the map

$$\pi : \mathbb{CP}^2 \rightarrow \mathbb{R}^2$$
$$[z_0 : z_1 : z_2] \mapsto \left[\frac{|z_1|^2}{|z_0|^2 + |z_1|^2 + |z_2|^2}, \frac{|z_2|^2}{|z_0|^2 + |z_1|^2 + |z_2|^2} \right].$$

Show that π is smooth and $\text{im}\pi = \{p_1, p_2 \geq 0, p_1 + p_2 \leq 1\}$.

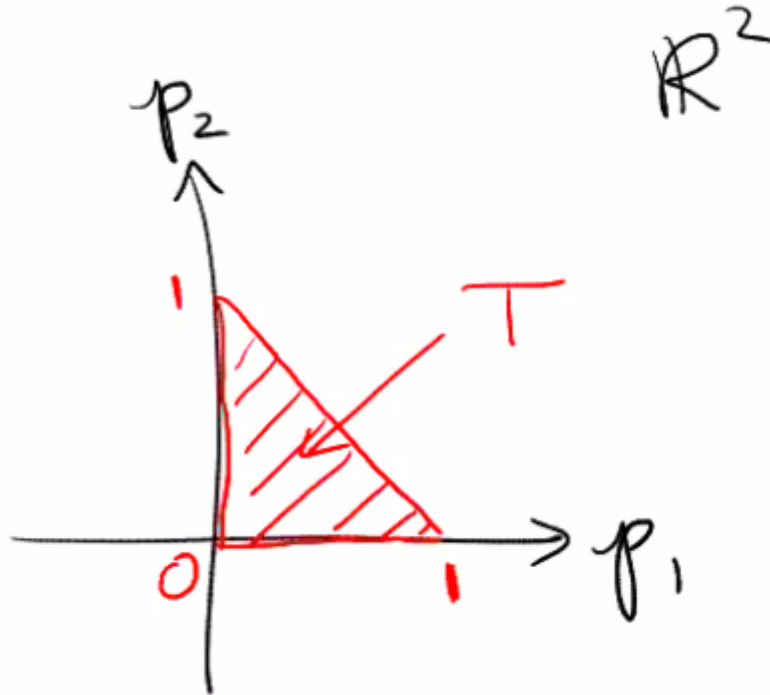


Figure 1: O

Exercise 1.3 (?).

Show that if $[p_1, p_2] \in T^\circ$ is in the interior of the above triangle, then $\pi^{-1}(p_1, p_2) \cong S^1 \times S^1$ is diffeomorphic to a torus. If instead the point is on an edge, the