

$$\begin{array}{ccc}
 K^\times / \langle q \rangle & \longrightarrow & E_q(K) \\
 \downarrow & & \downarrow \\
 L^\times / \langle q \rangle & \longrightarrow & E_q(L)
 \end{array}$$