

$$f(x)=\prod_i\left(\frac{1}{\sigma_i\sqrt{2\pi}}e^{-\frac{(x-\mu_i)^2}{2\sigma_i^2}}\right)$$

$$=\prod_i\left(\frac{1}{\sqrt{2\pi}\sigma_i}e^{-\frac{(x-\mu_i)^2}{2\sigma_i^2}}\right)$$

$$\log\left(f(x)\right)=\log\left(\prod_i\frac{1}{\sqrt{2\pi}\sigma_i}\right)-\frac{(x-\mu_i)^2}{2\sigma_i^2}$$

$$=-\frac{1}{2}\left(n\log(2\pi)+\sum_i\log(\sigma_i^2)\right)-\sum_i\frac{(x-\mu_i)^2}{2\sigma_i^2}$$

$$=-\frac{1}{2}G_{const}-\sum_i\frac{(x-\mu_i)^2}{2\sigma_i^2}$$

$$=-\frac{1}{2}G_{const}-\frac{1}{2}\sum_i\frac{(x-\mu_i)^2}{\sigma_i^2}$$

$$G_{const}=n\log(2\pi)+\sum_i\log(\sigma_i^2)$$

$$E=\sum_{n=1}^n||g\left(x_n\right)-d\left(x_n\right)||$$

$$d\left(x_n\right)=\left(d_1\left(x_n\right),...,d_K\left(x_n\right)\right)^t$$

$$g\left(x_n\right)=\left(g_1\left(x_n\right),...,g_K\left(x_n\right)\right)^t$$

$$KN$$