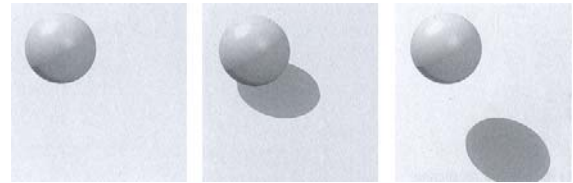


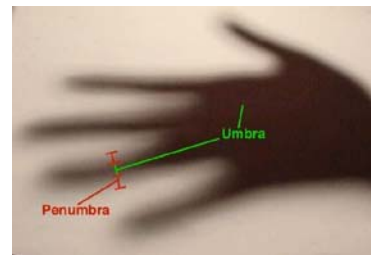
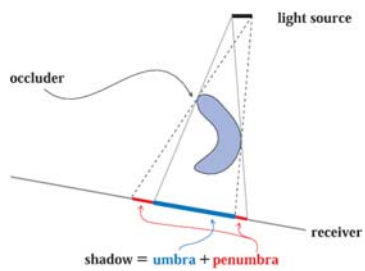
Shadows

Niels Jørgen Christensen
IMM . DTU

Effect of Shadows



Soft Shadows



Light source - Size



Anything like a shadow





Projection

$$\mathbf{P}_{ortho} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{P}_{oblique} = \begin{bmatrix} 1 & 0 & \cot \theta & 0 \\ 0 & 1 & \cot \phi & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{P}_{central} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & \frac{1}{d} & 0 \end{bmatrix}$$

Projection Shadows - Möller

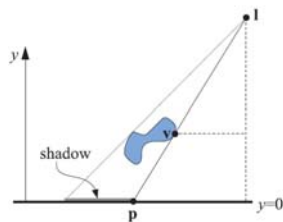
$$\frac{p_x - l_x}{v_x - l_x} = \frac{l_y}{l_y - v_y} \Rightarrow p_x = \frac{l_y v_x - l_x v_y}{l_y - v_y}$$

$$p_y = 0$$

$$p_z = \frac{l_y v_z - l_z v_y}{l_y - v_y}$$

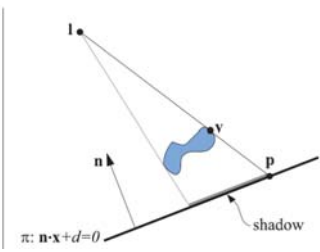
$$M = \begin{bmatrix} l_y & -l_x & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & -l_z & l_y & 0 \\ 0 & -1 & 0 & l_y \end{bmatrix}$$

$$p = Mv$$



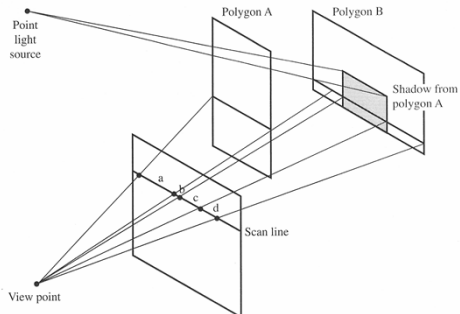
$$\pi :: y=0 \rightarrow \pi :: nx+d=0$$

$$p = l - \frac{d + n \cdot l}{n \cdot (v - l)} (v - l)$$

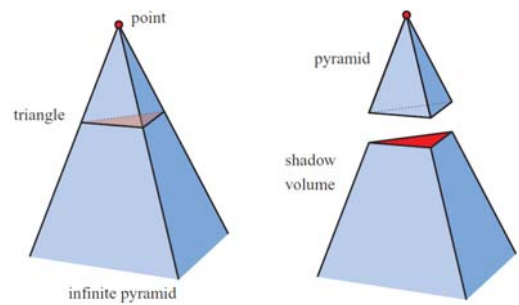


$$M = \begin{bmatrix} n \cdot l + d - l_x n_x & -l_x n_y & -l_x n_z & -l_x d \\ -l_y n_x & n \cdot l + d - l_y n_y & -l_y n_z & -l_y d \\ -l_z n_x & -l_z n_y & n \cdot l + d - l_z n_z & -l_z d \\ -n_x & -n_y & -n_z & n \cdot l \end{bmatrix}$$

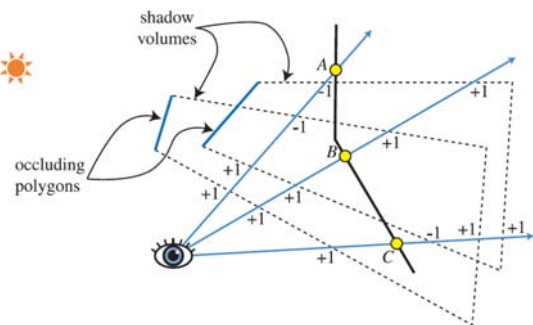
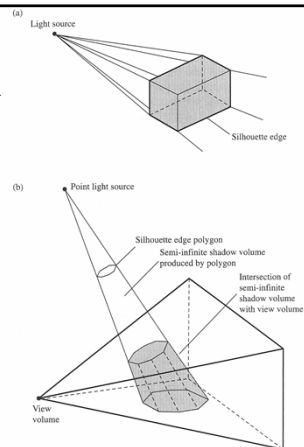
Scanline



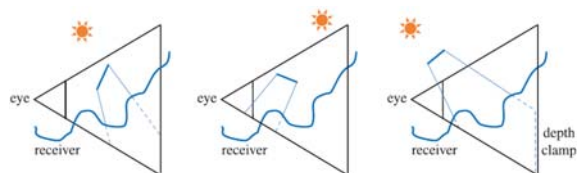
Shadow Volume



Shadow Volum



Shadow Volume - Problems



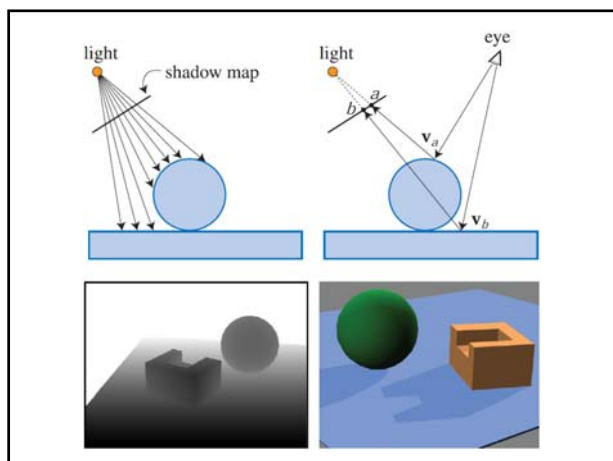
Contours



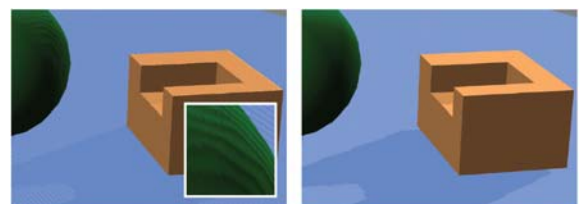
Shadow Volume - Properties

- General purpose HW
- No sampling problems – not image based
- Fill rate limited – SV polygons big
 - Rasterizing bottleneck
- Stencil buffer needed
 - or modified method
- Soft shadows from blending multiple SV
 - Expensive
- No HW shadows from curved surfaces

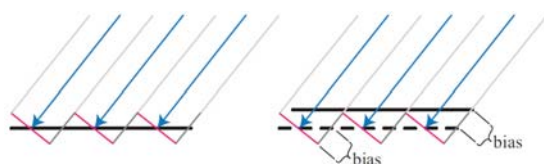
Shadow Map



Shadow Map - problems

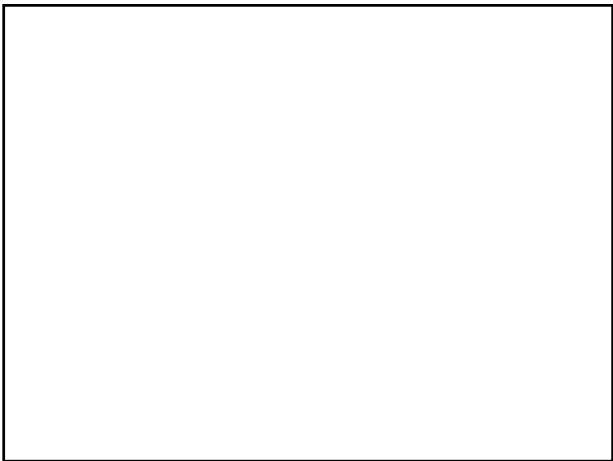
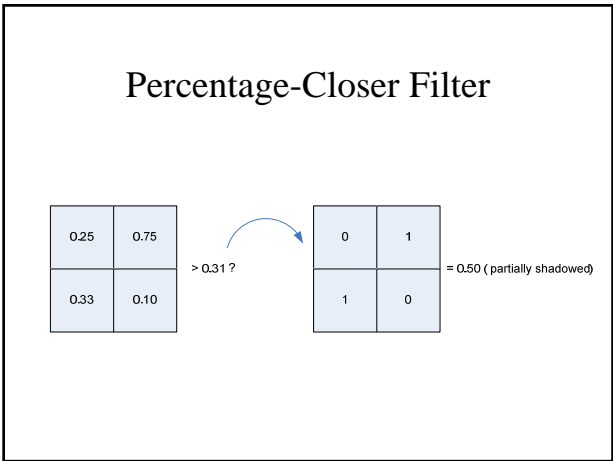
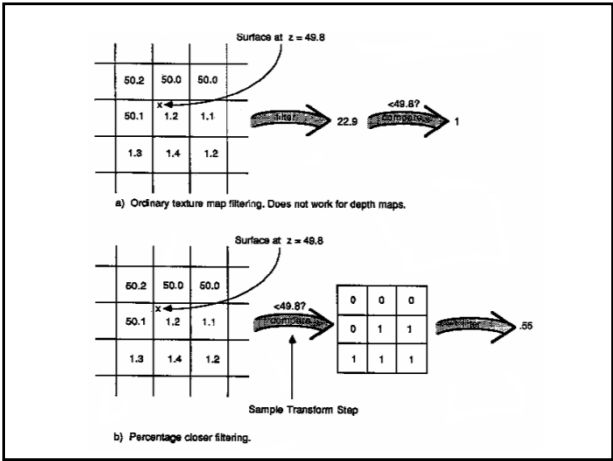
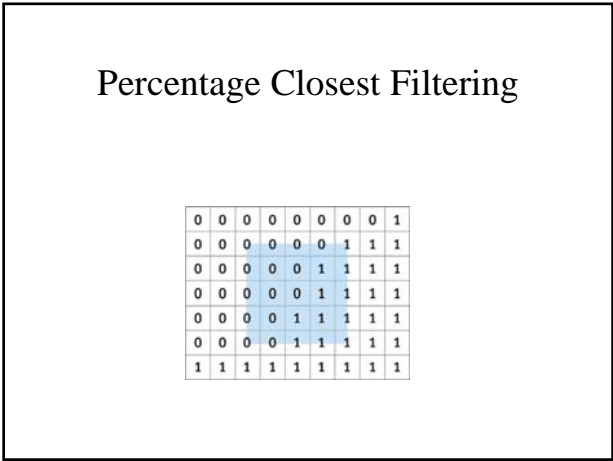
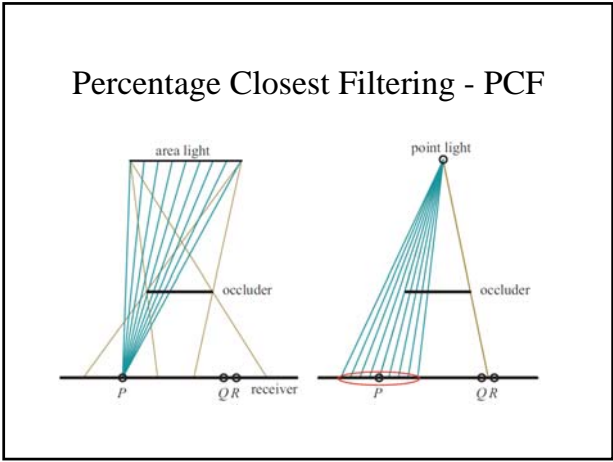
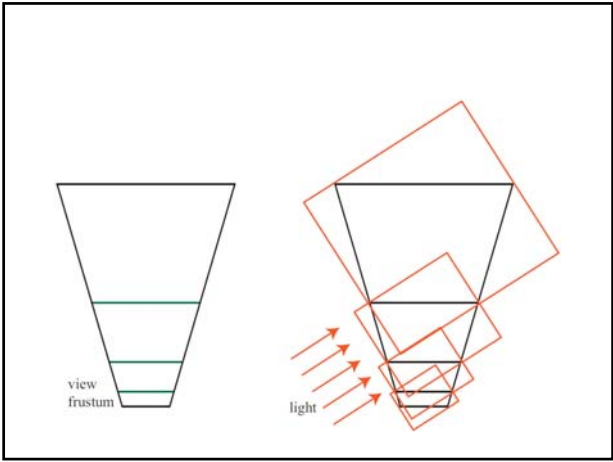


Shadow Map - Bias



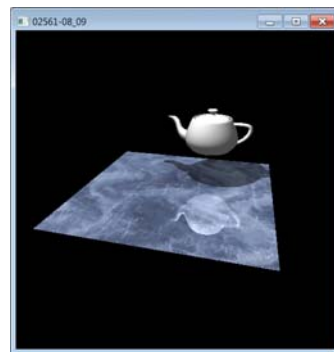
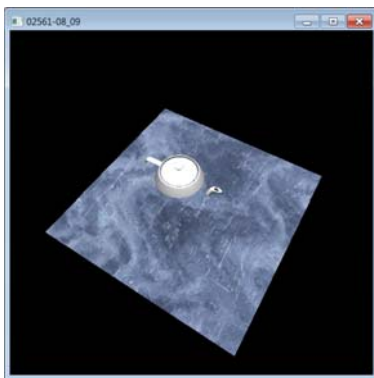
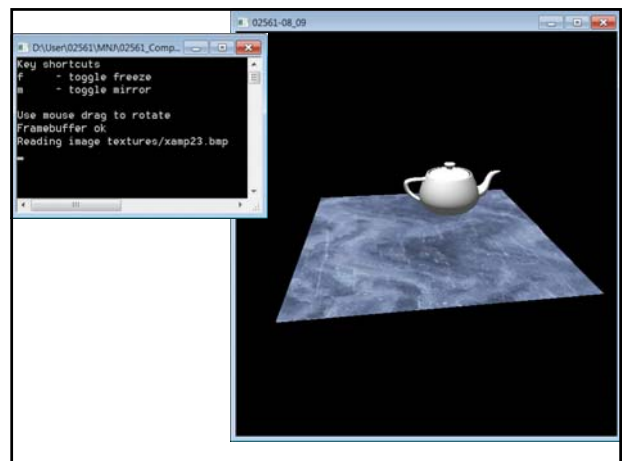
Shadow Map - Problem



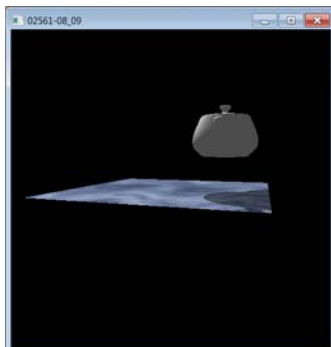


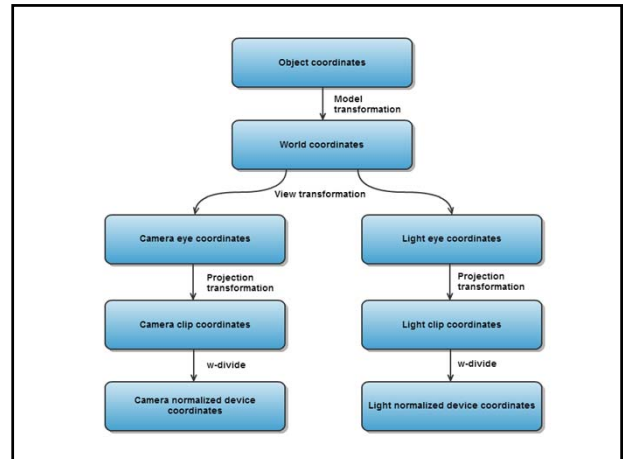
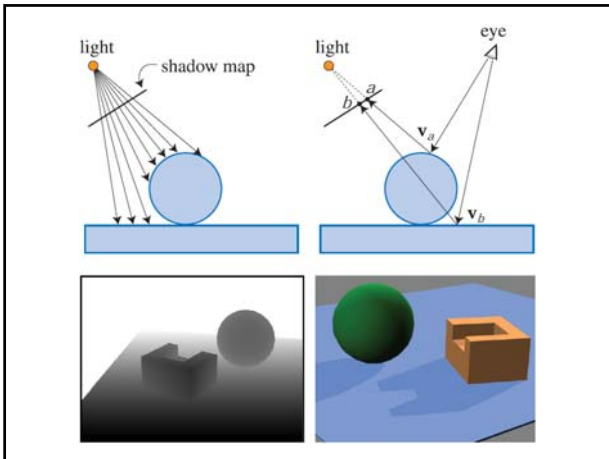
Shadow Map - Exercise

- Shadow maps - week 8
- Reflections – week 9 (continuation)



To do





```

getLightProjection() {
  // todo implement
  return mat4();
}

mat4 getLightView() { mat4
  // todo implement
  return mat4();
}

mat4 getLightViewProjection(){
  return getLightProjection() * getLightView();
}

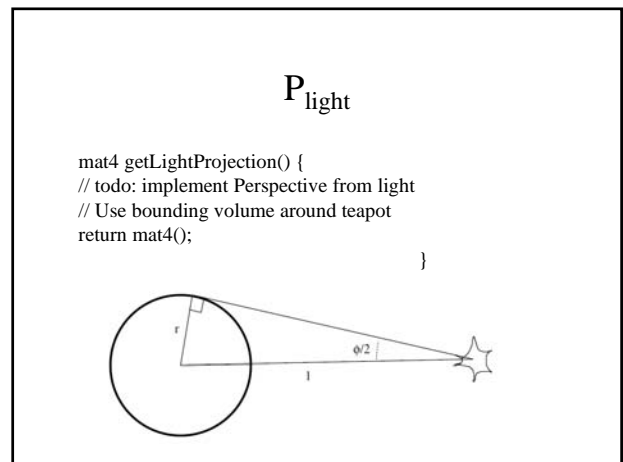
void updateProjShadowTexture() {
  // todo bind framebuffer, set viewport to shadowmap and clear to white

  mat4 projection = getLightProjection();
  mat4 view = getLightView();
  mat4 model = Translate(teapotPosition);

  // todo render black teapot

  // todo release framebuffer, setviewport to window
}

```



V_{light}

```

mat4 getLightView() {
  // todo : use LookAt
  return mat4();
}

```

$P_{light} * V_{light}$

```

mat4 getLightViewProjection(){
  return getLightProjection() * getLightView();
}

```

updateProjShadowTexture

```
void updateProjShadowTexture() {
// todo bind framebuffer, set viewport to shadowmap, clear to white

mat4 projection = getLightProjection();
mat4 view = getLightView();
mat4 model = Translate(teapotPosition);

// todo render black teapot

// todo release framebuffer, setviewport to window
}
```

LookAt - V

```
mat4 LookAt( const vec4& eye, const vec4& at, const vec4& up )
{
    vec4 n = normalize(eye - at);
    vec4 u = vec4(normalize(cross(up,n)),0.0);
    vec4 v = vec4(normalize(cross(n,u)),0.0);
    vec4 t = vec4(0.0, 0.0, 0.0, 1.0);
    mat4 c = mat4(u, v, n, t);
    return c * Translate( -eye );
}
```

In Angel/mat.h

Perspective P_{per}

```
mat4 Perspective( const GLfloat fovy, const GLfloat aspect,
const GLfloat zNear, const GLfloat zFar ) {
    GLfloat top = tan(fovy*DegreesToRadians/2) * zNear;
    GLfloat right = top * aspect;
    mat4 c;
    c[0][0] = zNear/right;
    c[1][1] = zNear/top;
    c[2][2] = -(zFar + zNear)/(zFar - zNear);
    c[2][3] = -2.0*zFar*zNear/(zFar - zNear);
    c[3][2] = -1.0;
    c[3][3] = 0.0;
    return c;
} //In Angel/mat.h
```

updateProjShadowTexture

```
void updateProjShadowTexture() {
// todo bind framebuffer, set viewport to shadowmap,clear to white

mat4 projection = getLightProjection();
mat4 view = getLightView();
mat4 model = Translate(teapotPosition);

// todo render black teapot

// todo release framebuffer, setviewport to window
}
```

```
GLuint buildFramebufferObject(int width, int height, GLuint textureId)
{
    GLuint framebufferObjectId, renderBufferId;
    glGenFramebuffers(1, &framebufferObjectId);
    glGenRenderbuffers(1, &renderBufferId);
    glBindRenderbuffer(GL_RENDERBUFFER, renderBufferId);
    glRenderbufferStorage(GL_RENDERBUFFER, GL_DEPTH_COMPONENT24, width,
height);
    glBindFramebuffer(GL_FRAMEBUFFER, framebufferObjectId);
    glFramebufferTexture2D(GL_FRAMEBUFFER, GL_COLOR_ATTACHMENT0,
GL_TEXTURE_2D, textureId, 0);
    glFramebufferRenderbuffer(GL_FRAMEBUFFER, GL_DEPTH_ATTACHMENT,
GL_RENDERBUFFER, renderBufferId);
    GLenum frameBufferRes = glCheckFramebufferStatus(GL_DRAW_FRAMEBUFFER);
    cout << getFramebufferStatusString(frameBufferRes)<<endl;
    glBindFramebuffer(GL_DRAW_FRAMEBUFFER, 0);
    return framebufferObjectId;
}
```