

# EE 511 Simulation Methods for Stochastic Systems

## Project #2

### Problem 1 [Waiting]

Use the inverse CDF method to generate independent samples,  $X_i$ , of the exponential random variable with average waiting time of 0.2 time units. Evaluate the quality of your generator with goodness of fit tests. poisson

### Problem 2 [Counting]

Each exponential random sample represents the waiting time until an event occurs. Implement a routine to count the number of events that occur in 1 unit of time. Generate such counts for 1000 separate unit time intervals. How are these counts distributed? Justify your answer

*You will need to learn to use functions for plotting networks in the next questions. Recent versions of MATLAB have built-in network plotting functions. Python and R have the iGraph library. Python also has the networkx library.*

### Problem 3 [Networking]

Given  $n=50$  people at a networking event. Imagine that any given unordered pair of two people connect at random and independently with probability  $p$ . Generate and plot sample networks for each value of  $p=\{0.02, 0.09\}$ . Briefly discuss the structure of these sample graphs.

### Problem 4 [Networking at larger scale]

Count the number of connections (edges) to a *vertex* (node) in one of your sample networks from Problem 3. This statistic is the *degree* of that vertex. The vertex degrees for all vertices in a random network are random. Vertex degree is a binomially distributed statistic for small networks.

Plot a histogram of vertex degrees for one of your sample networks in Problem 3. Repeat for the other sample network.

Generate a network with  $(n, p) = (250, 0.08)$  and plot the histogram of its vertex degrees. What distribution fits this data? Justify your claim with any probabilistic limit laws you know.

Turn in:

- A summary of your experiments including histograms of your data, any relevant plots, and relevant numerical results
- brief discussions of the results
- a print out of your code.