

Analysis and Application of Depth-Bounded Systems

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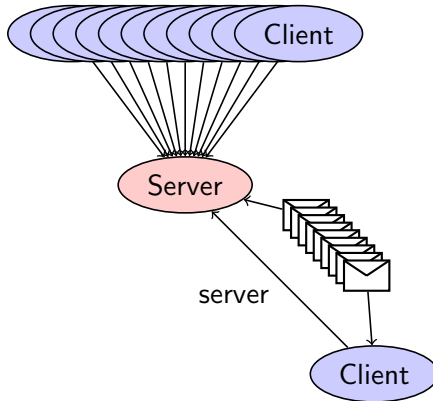
IST Austria

PUMA-RiSE workshop, Goldegg, 09.2012

Outline

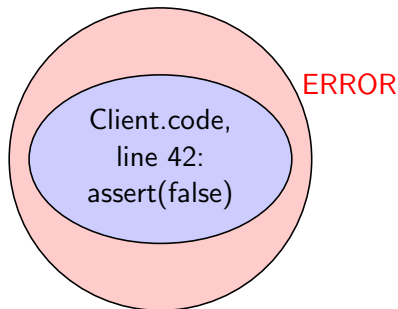
- 1 Where it all started
- 2 Computing the Covering Set for DBS
- 3 Using the Covering Set
 - Termination of DBS
 - Dynamic Package Interface

Example: client-server communication pattern



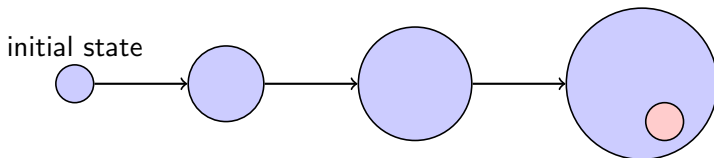
What kind of properties are we looking at ?

Safety properties, more precisely the control-state reachability problem (aka covering problem).



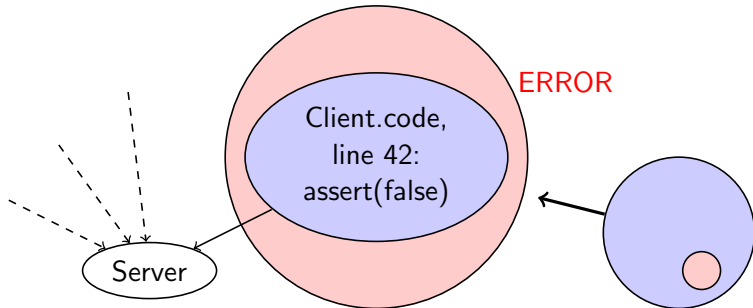
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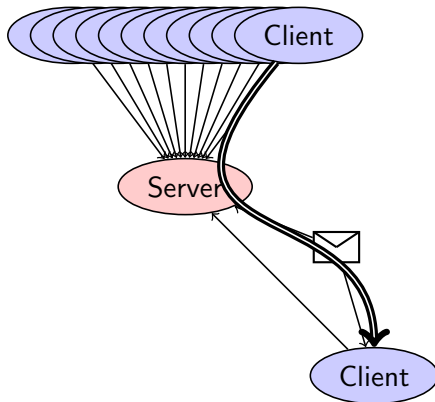
What kind of properties are we looking at ?

Safety properties, more precisely the control-state reachability problem (aka covering problem).



Depth-bounded systems: [Meyer, 2008]

System with a bound on the longest acyclic path.
(Concretely: it is not possible to encode an infinite memory.)



Formal model: WSTS

A well-structured transition system (WSTS) is a transition system $\langle S, \rightarrow, \leq \rangle$ such that:

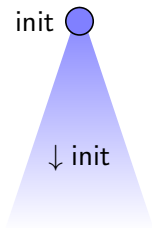
- \leq is a well-quasi-ordering (wqo),
 i.e. well-founded + no infinite antichain.
- compatibility of \leq w.r.t. \rightarrow

$$\forall \begin{array}{c} t \xrightarrow{*} t' \\ s \xrightarrow{\quad} s' \end{array} \quad \begin{array}{c} \vee \\ \vee \end{array} \quad \exists$$

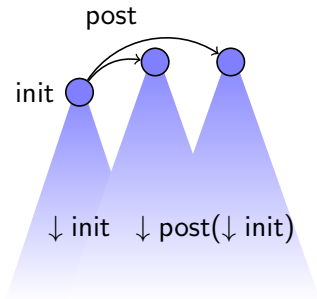
For more detail see:

[Finkel and Schnoebelen, 2001, Abdulla et al., 1996]

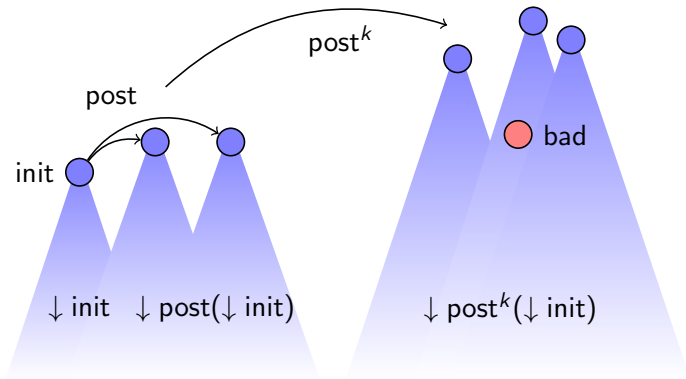
Forward algorithm for covering



Forward algorithm for covering



Forward algorithm for covering



Computes the covering set rather than answering only a single coverability query.

Representing downward-closed sets with ideals

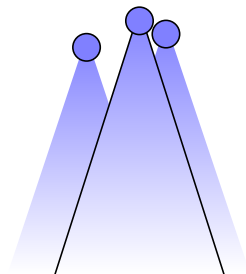
Given a wqo-set (X, \leq) .

A subset of X is **directed** if it is non-empty and closed under upper bounds.

An **ideal** of X is a directed downward-closed subset of X .

The ideal completion $Idl(X)$ of X is the set of all ideals of X .

A downward-closed subset is a finite union of ideals.

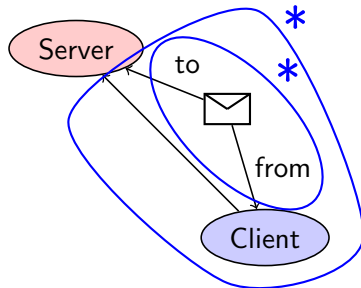
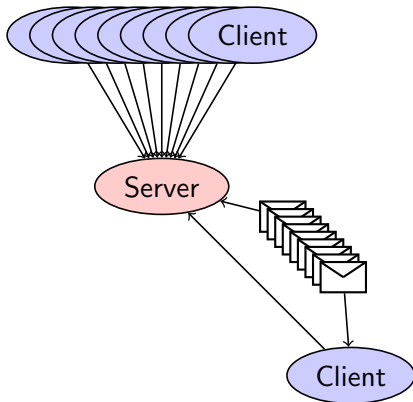


Ideal for representing downward-closed sets.

ADL: [Geeraerts et al., 2006]

Further developed in [Finkel and Goubault-Larrecq, 2009]

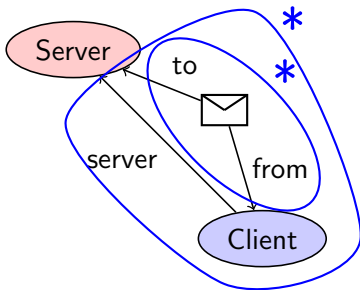
Applied to DBP in [Wies et al., 2010]



When does acceleration work ? (flat systems)

DBP are intrinsically non-flat.

covering set:

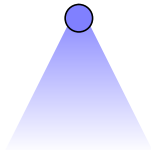


ω^2 steps from the initial state and the final state.

Nested loops are required to compute the covering set.

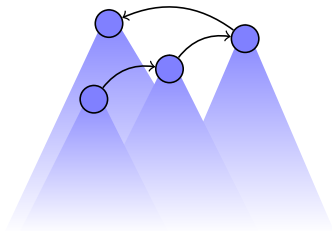
From acceleration to widening

Acceleration considers transitions - widening only states.



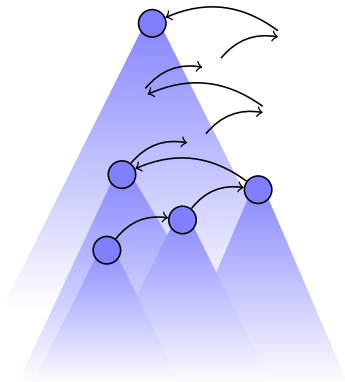
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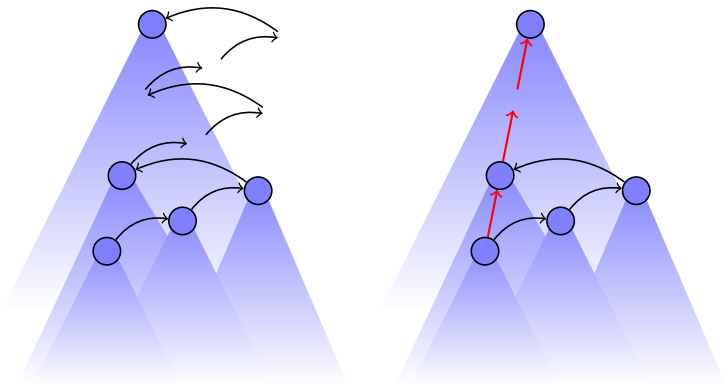
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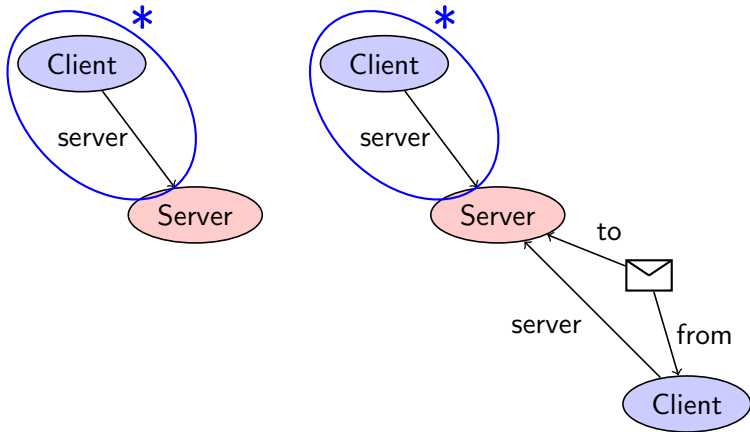


From acceleration to widening

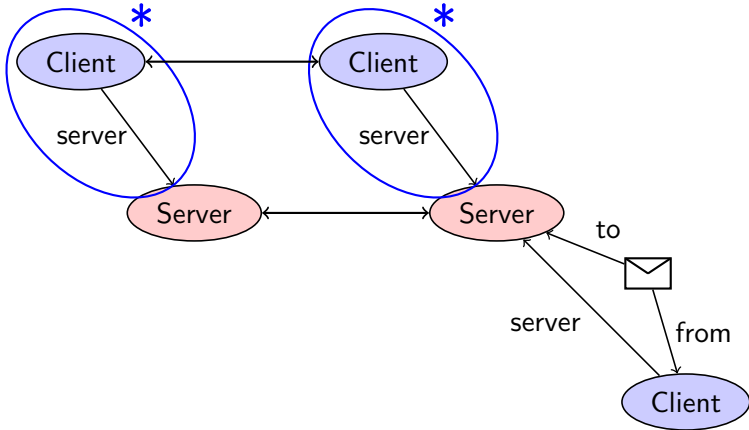
Acceleration considers transitions - widening only states.



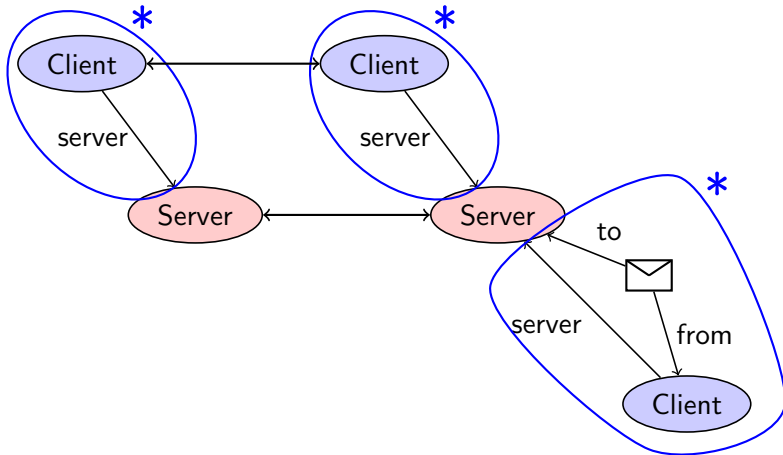
Set-widening for DBP (1)



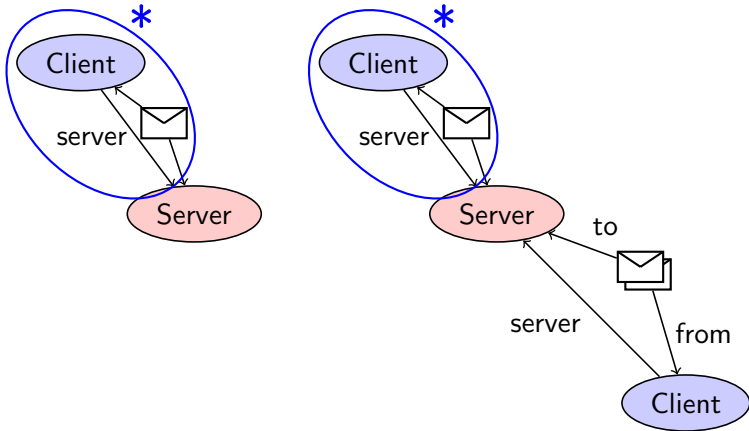
Set-widening for DBP (1)



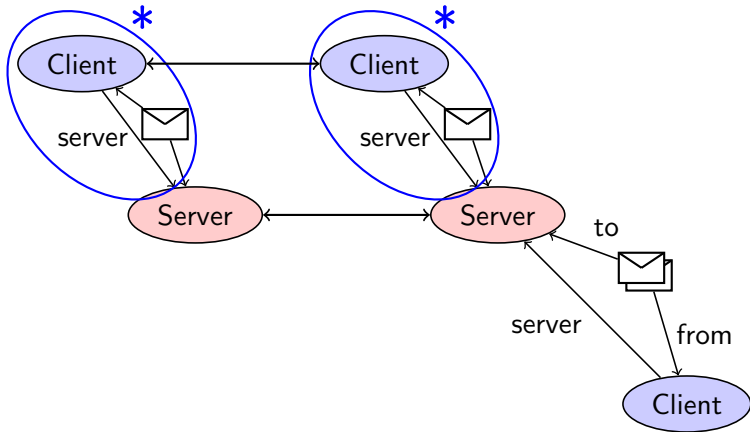
Set-widening for DBP (1)



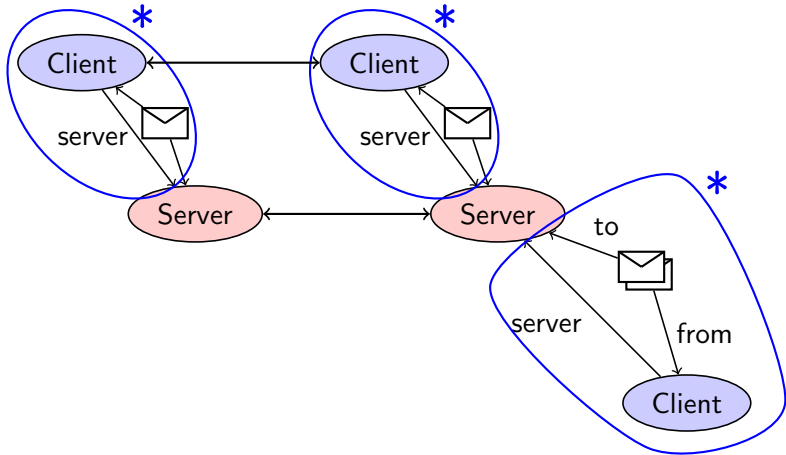
Set-widening for DBP (2)



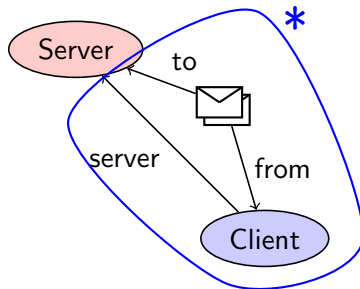
Set-widening for DBP (2)



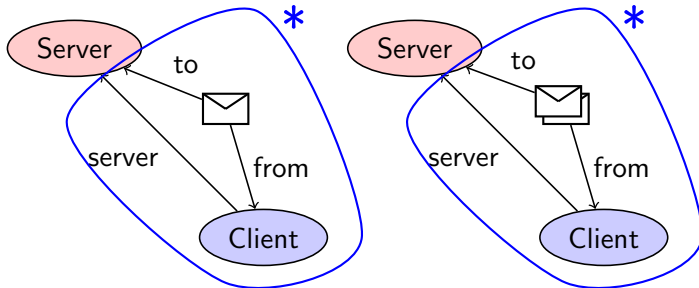
Set-widening for DBP (2)



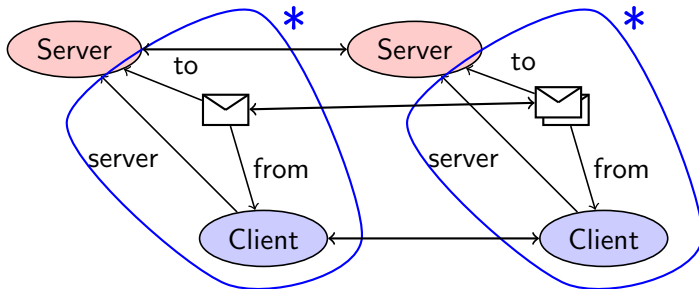
Set-widening for DBP (3)



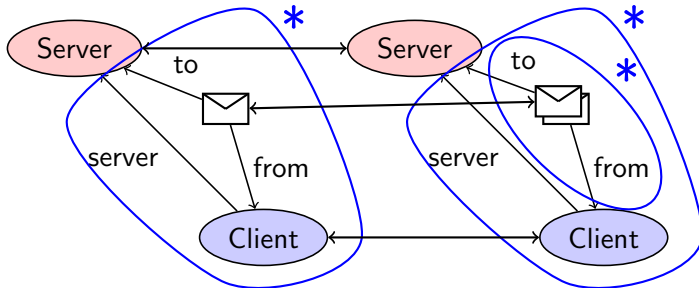
Set-widening for DBP (3)



Set-widening for DBP (3)



Set-widening for DBP (3)



How the Covering Set Grows ?

Name	tree size	cov. set size	time
ping-pong	17	14	0.6 s
client-server	25	2	1.9 s
client-server-with-T0	184	5	12.8 s
genericComputeServer	57	4	4.6 s
genericComputeServer-fctAsActor	98	8	14.8 s
liftChatLike	1846	21	1830.9 s
round_robin_2	830	63	48.8 s
round_robin_3	3775	259	737.8 s

Table: Experimental results: the columns indicate the number of nodes in the Karp-Miller tree, the number of ideals in the covering set, and the running time.

Interesting Properties of the Cover

The covering set:

- can answer an covering question (control-state reachability),
- has a compact representation,
- is an inductive invariant.

The first point was the original motivation for this work.

The last two points allows us to do much more.

PICASSO is available at

<http://pub.ist.ac.at/~zufferey/picasso/>.

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Termination Proofs and Counter Abstractions

Termination proof:

finite union of ranking function [Podelski and Rybalchenko, 2004]

Counter abstraction:

counts the number of occurrences of some elements in a system.

Typically one counts the number of processes in a state/control-location.

In this work we automatically infer complex termination proof using a flexible counter abstraction. The number of counters is not fixed a priori, but depends on the reachable states in the system. This is joint work with Kshitij Bansal, Eric Koskinen, and Thomas Wies (work in progress).

Treiber's stack: code

```
struct node {
    struct node *next;
    value data;
};
struct stack { struct node *Top; };
struct stack *S;
```

```
value pop() {
    struct node *t, *x;
    do {
        t = S->Top;
        if (t == NULL) return EMPTY;
        x = t->next;
    } while (!CAS(&S->Top,t,x));
    return t->data;
}
```

```
void init() {
    S = alloc();
    S->Top = NULL;
}
```

```
void push(value v) {
    struct node *t, *x;
    x = alloc();
    x->data = v;
    do {
        t = S->Top;
        x->next = t;
    } while (!CAS(&S->Top,t,x));
}
```

Treiber's stack: as DBS and Covering Set

Encoding:

- push and pop are a single operation.
- Operation: first read the top of stack, then CAS.

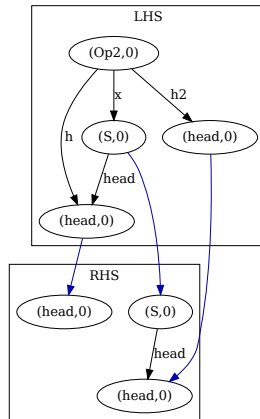
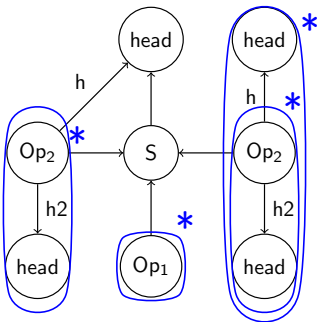
Invariant for termination:

A process cannot fail twice unless someone else did succeed.

Show PICASSO output: rewrite rules, cover, and cover + post.

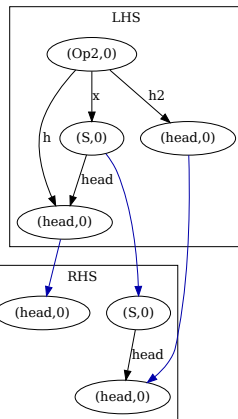
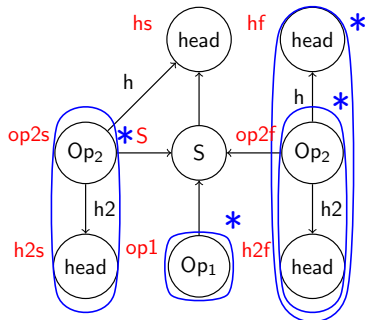
Numerical Abstraction from the Covering Set

Op2: CAS succeed



Numerical Abstraction from the Covering Set

Op2: CAS succeed



$$S' = S$$

$$op1' = op1$$

$$op2s' = 0$$

$$op2f' = op2f + op2s - 1$$

$$h2f' = h2f + h2s - 1$$

$$hf' = hf + 1$$

$$hs' = 1$$

$$h2s' = 0$$

Implementation

Example	Cov size	Cov+ \mathcal{N} (sec)	ARMC (sec)	Total (sec)
split/merge	3	3.5	4.5	8.0
Work stealing, 3 processors	3	5.4	1.0	6.4
Parameterized work stealing	1	3.7	0.9	4.6
Compute server job queue	1	3.9	1.2	5.1
Map reduce	4	5.6	0.9	6.5
Map reduce with failure	5	7.9	6.0	13.9
Treiber's stack	1	3.8	0.5	4.3
Treiber's stack (fine-grained)	3	10.3	4.7	15.0
Herlihy Wing queue	2	20.4	85.9	106.3

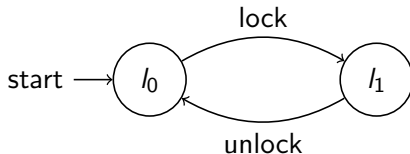
Table: Experimental results. Columns indicate the size of the cover, the running time for its construction and the construction of the numerical abstraction, the running time of the final termination, and the total time of our method.

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Object Interfaces

Example: one should invoke the lock and unlock methods of a lock object in alternation, starting by lock.



In this work we use the covering set to extract interface for *groups of objects* in a non-concurrent setting. This is joint work with Shahram Esmailsabzali, Rupak Majumdar, and Thomas Wies (submitted to ICSE).

Example: Sets and Iterators

```
class Set {
    protected int sver, size;
    public Set() {
        sver := size := 0;
    }
    public void add(int elem) {
        if (!duplicate) {
            sver++; size++;
        }
    }
    protected void delete(int pos) {
        sver++; size--;
    }
    public Iterator iterator() {
        return (new Iterator(this));
    }
}
```

```
class Iterator {
    int iver, pos;
    Set it_of;
    protected Iterator(Set s) {
        it_of := s; pos := 0;
        iver := s.sver;
    }
    public int next() {
        if (iver == S.sver) then pos++;
        else throw new Exception();
    }
    public void remove() {
        if (iver == S.sver) then {
            it_of.delete(pos);
            iver := S.sver;
        } else {
            throw new Exception();
        }
    }
}
```


Predicate Abstraction and DBS Encoding

How do we get from the code to the DBS ?

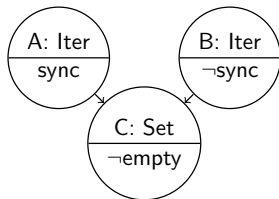
We use predicates abstraction and symbolic execution.

- unary predicate for Set:
empty (size = 0)
- binary predicates for Set and Iterator:
sync (iver = it_of.sver)

Rewriting rule for `Iterator.remove`

We have to consider a few cases:

- An iterator can be either synchronized or not.
- An iterator can be either the caller or part of the frame.



$$\varphi(A, A) \Rightarrow wp(A.remove, sync_{A'})$$

$$\varphi(A, A) \Rightarrow wp(A.remove, \neg sync_{A'})$$

$$\varphi(B, A) \Rightarrow wp(A.remove, sync_{B'})$$

$$\varphi(B, A) \Rightarrow wp(A.remove, \neg sync_{B'})$$

$$\varphi(C, A) \Rightarrow wp(A.remove, empty_{C'})$$

$$\varphi(C, A) \Rightarrow wp(A.remove, \neg empty_{C'})$$

To know what cases we must consider, we go back and forth between the cover computation and the symbolic execution.

Extracting the DPI

- compute the covering set and the DBS
- apply the post operator once more
- track each transition to get the DPI

Show PICASSO output for the Set and Iterators example.
http://pub.ist.ac.at/~zufferey/picasso/dpi/set_iterator_report.html

Conclusion

We present an analysis to compute an over-approximation of the covering set for BDS.

Then we show that on top of answering coverability question the covering set can be used as starting point for more advanced analysis:

- numerical abstraction to prove (weak-fair) termination;
- interfaces for groups of objects.

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