

# **On Choice in Protocol Specification**

**Generalizing Projection in Asynchronous Multiparty Session Types**  
CONCUR 21, with Rupak Majumdar, Madhavan Mukund, and Felix Stutz

**On Channel Use in Protocols and General Point-to-Point Communication**  
under submission, with Felix Stutz

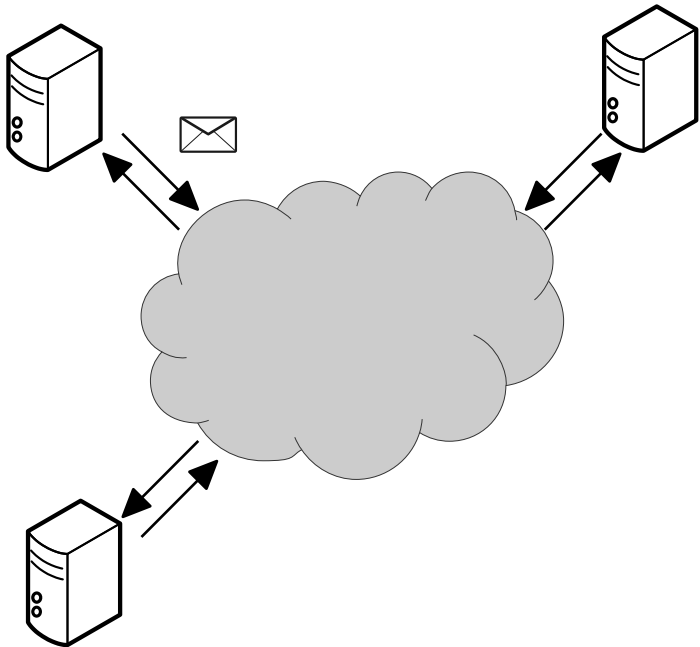
Damien Zufferey  
MPI-SWS  
2021.09.30

# Overview

- Detour: why it is hard to reason about CSM?
- Binary session types and half-duplex channels
- Binary to multiparty session types
- Directed to generalized choice
- Future work

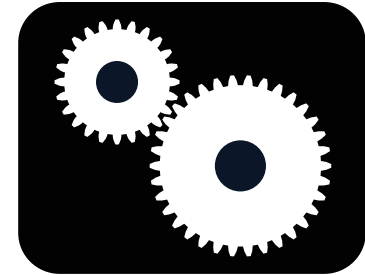
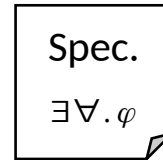
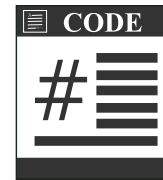
# What is this about ?

Distributed systems  
(message-passing)

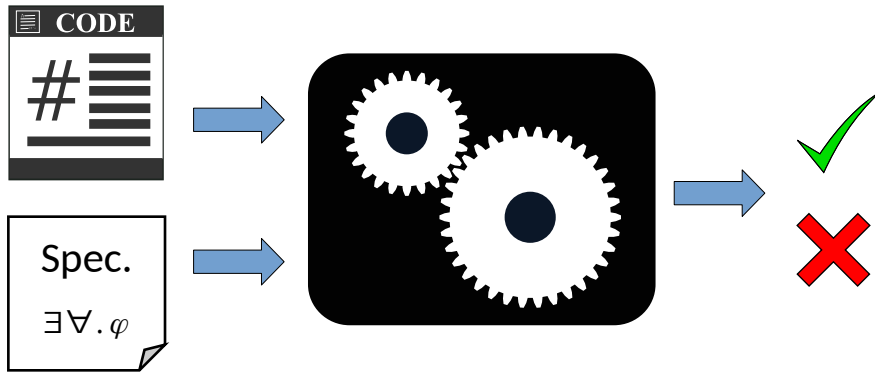


+

Verification



# What to Verify?



A communication protocol is correctly implemented:

- messages follow a prescribed order
- deadlock-free
- no dangling messages

# Two Approaches

## Type System

based on proof theory

+ effective

- not 'typeable'  $\neq$  incorrect

research toward more expressive

## Model Checking

based on automata theory

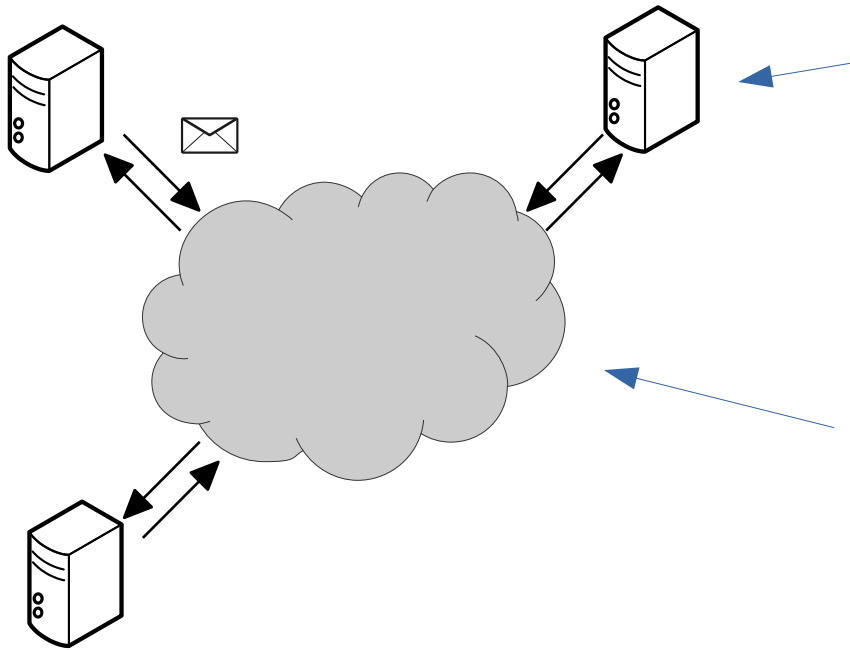
- expensive

+ counterexample

research toward more specific

We will try to see both approaches for verifying communicating systems.

# Model for the Software



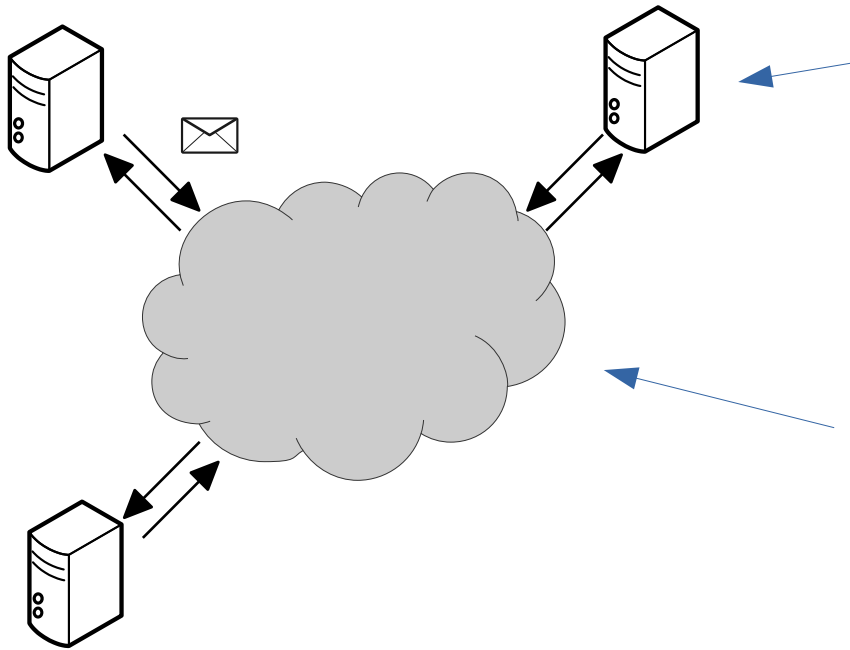
## Programs:

- Finite state machines
- Pushdown automata
- Turing machines

## Communication channels:

- routing: point-to-point, broadcast, ...
- capacity: unbounded, bounded
- reliability: reliable, lossy, fair, ...
- ordering: FIFO, bag

# Communicating State Machines (CSM)



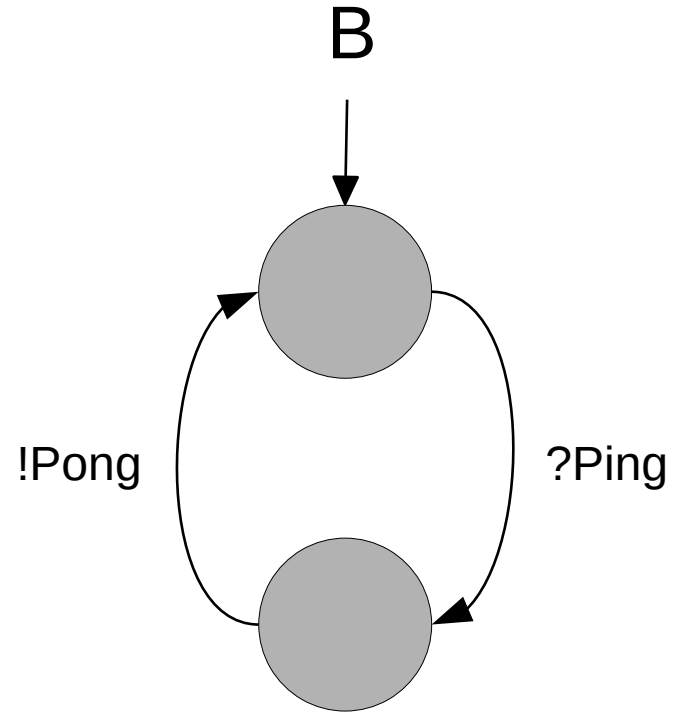
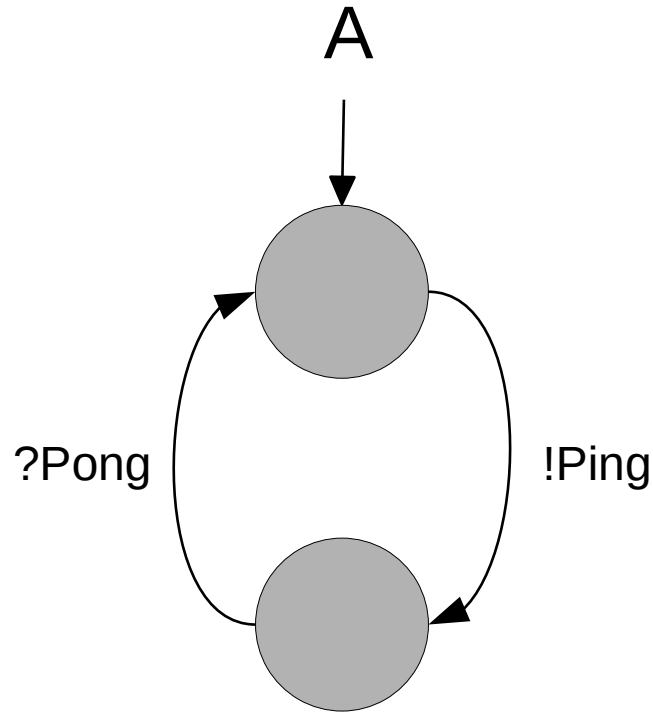
Programs:

- **Finite state machines**
- Pushdown automata
- Turing machines

Communication channels:

- routing: **point-to-point**, broadcast, ...
- capacity: **unbounded**, bounded
- reliability: **reliable**, lossy, fair, ...
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# “Hello World” of Message-Passing



CSP notation: '!' is send, '?' is receive



# CSM: Expressive Power

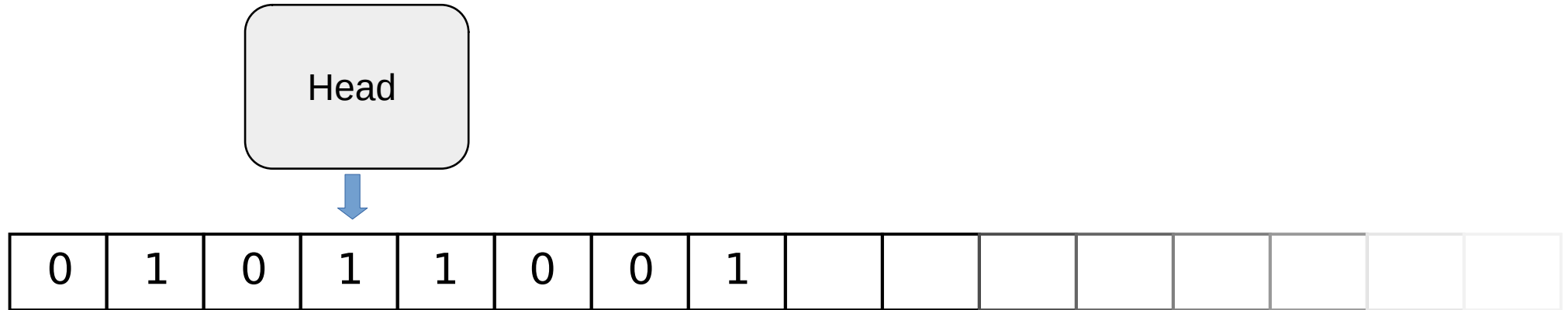
- Knowing the expressive power tells us what method can or cannot be applied.

(Don't try to solve undecidable problems)

- It can tell us what feature of the model is important.
- Unfortunately, CSM can simulate Turing machines.

# Turing Machine (TM)

- TM = finite control + unbounded tape (RAM)
- Operations: read/write memory, move left/right



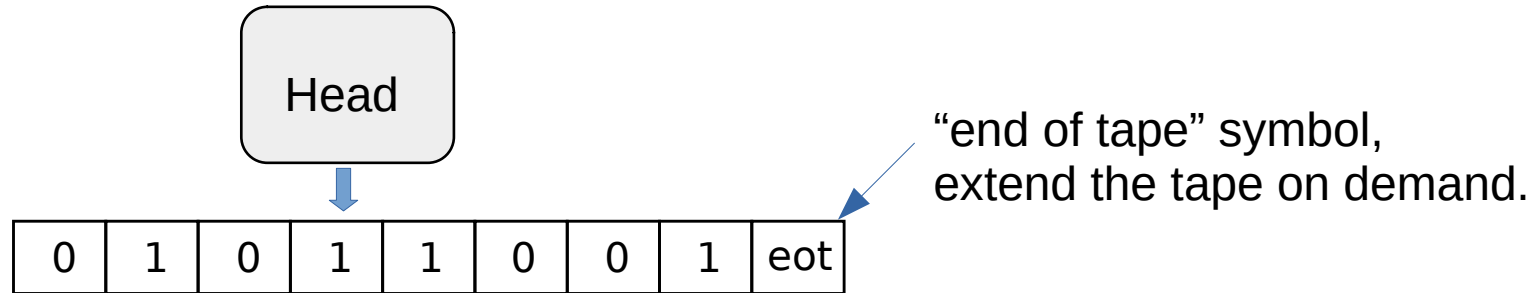
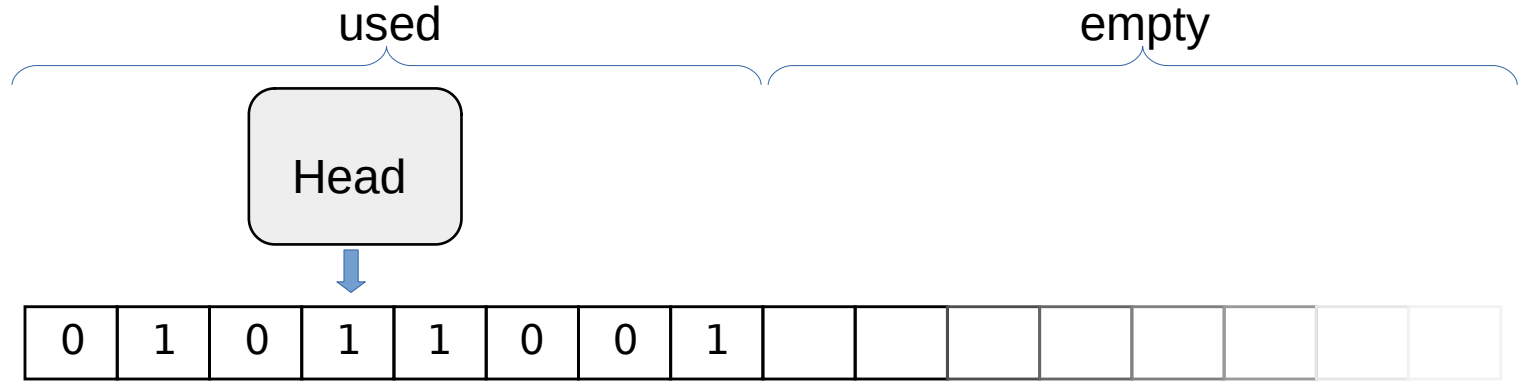
# TM → CSM

Idea:

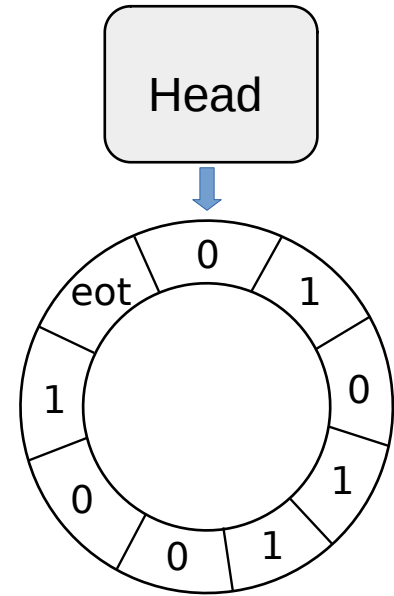
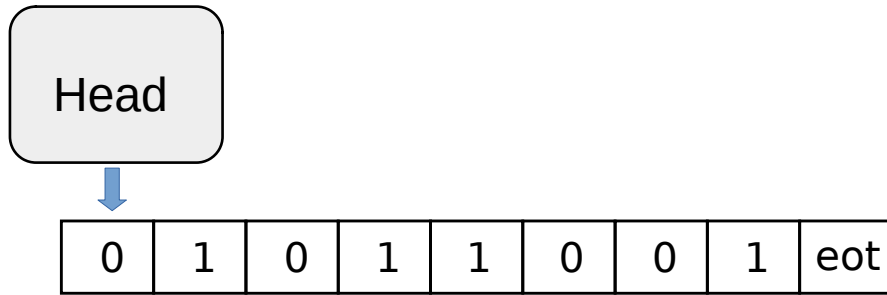
use the communication channels to store the content of the tape.

- 1) Store only the (finite) written part
- 2) Turn the tape into a loop
- 3) Extract the “Head part” of the tape
- 4) Split the loop in two parts (2 communication channels)

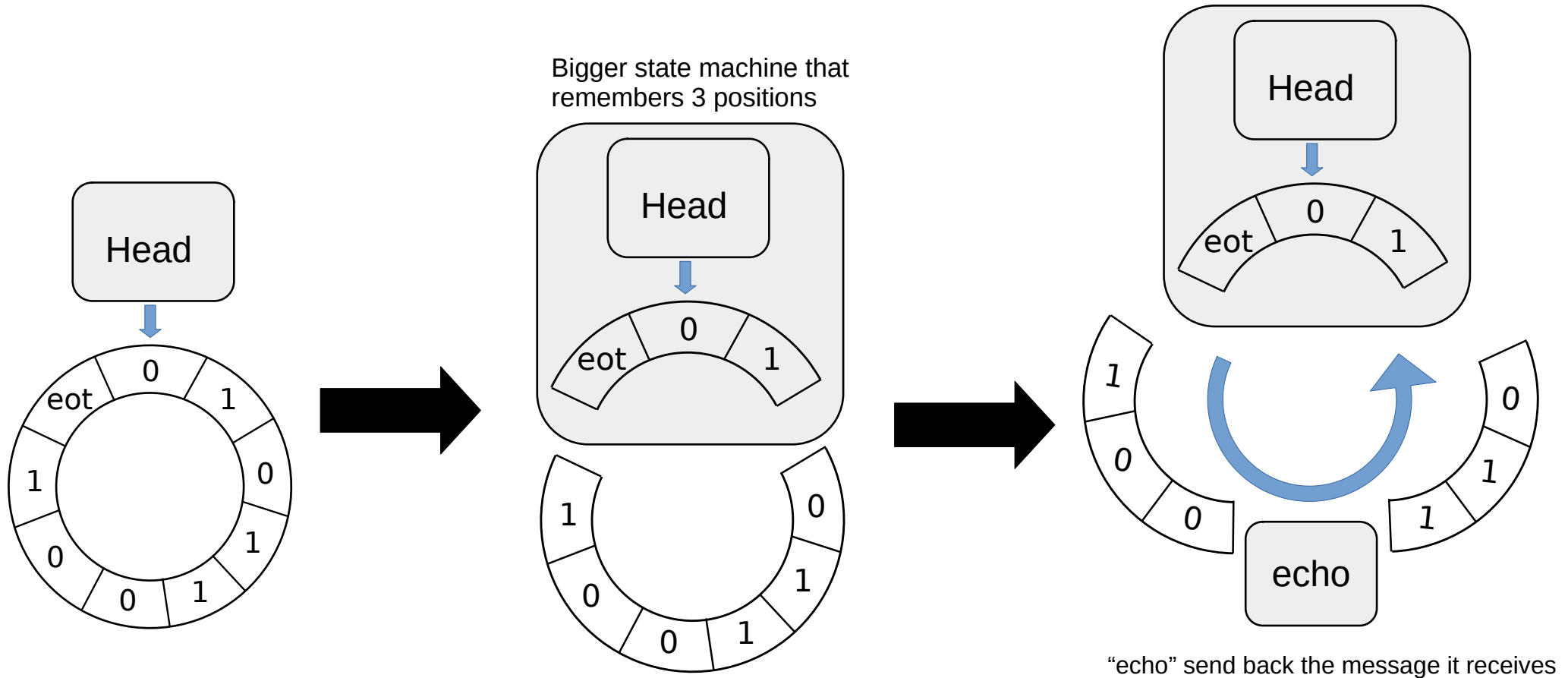
# TM → CSM



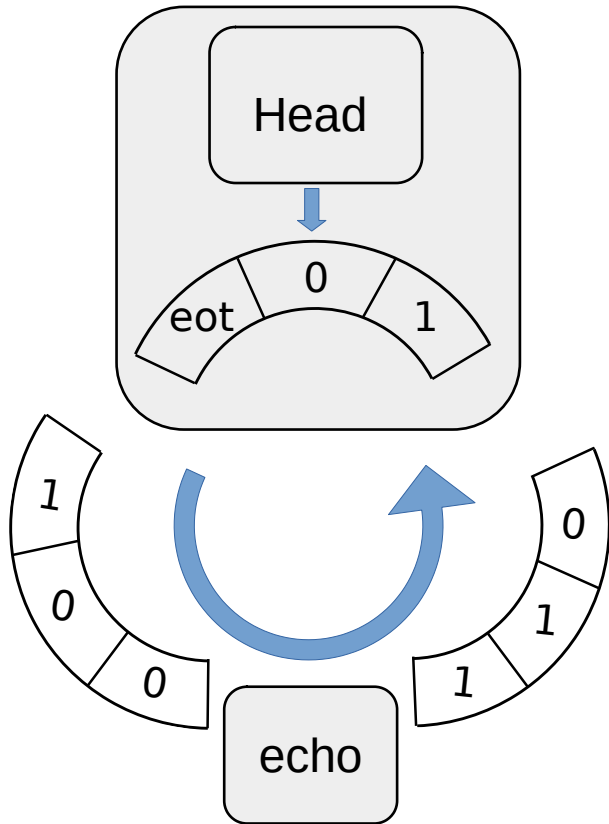
# TM $\rightarrow$ CSM



# TM → CSM



# TM → CSM



Emulating TM operations:

- 1) read/write: change local state of the head machine
- 2) move right: send to echo, receive from echo
- 3) move left:
  - insert position marker before current position
  - loop around the tape (move right) until the marker

# Other Channel Models

- capacity: unbounded, **bounded**
- reliability: reliable, lossy, ...
- ordering: FIFO, bag



Finite state machine

- capacity: **unbounded**, bounded
- reliability: reliable, lossy, ...
- ordering: FIFO, **bag**



Petri net

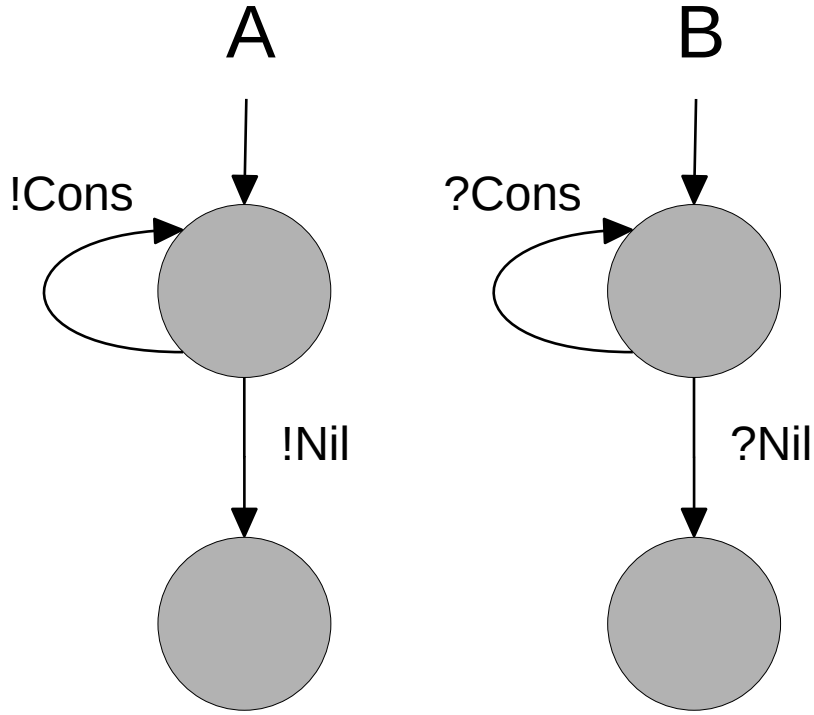
- capacity: **unbounded**, bounded
- reliability: reliable, **lossy**, ...
- ordering: **FIFO**, bag



WSTS



# Memory vs Communication Slack



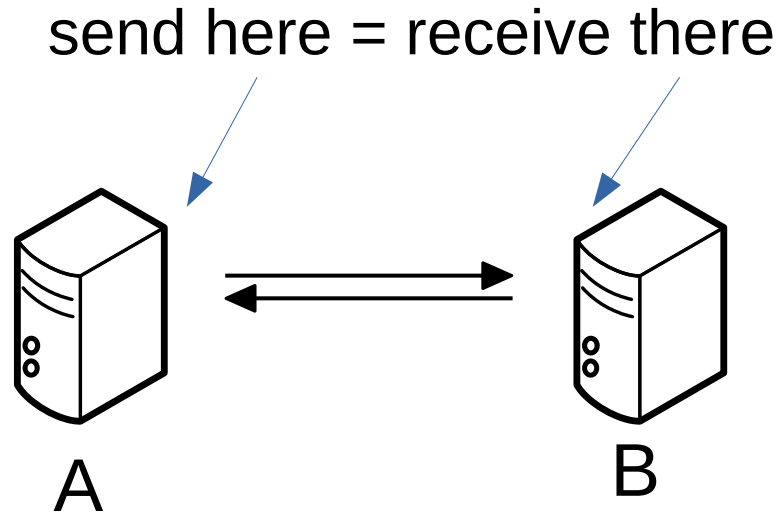
Some protocols using unbounded channels can be harmless.

What is the difference between

- channel as memory  
(store information for later)
- communication slack  
(delay in the propagation of information)

# Looking at the Channels

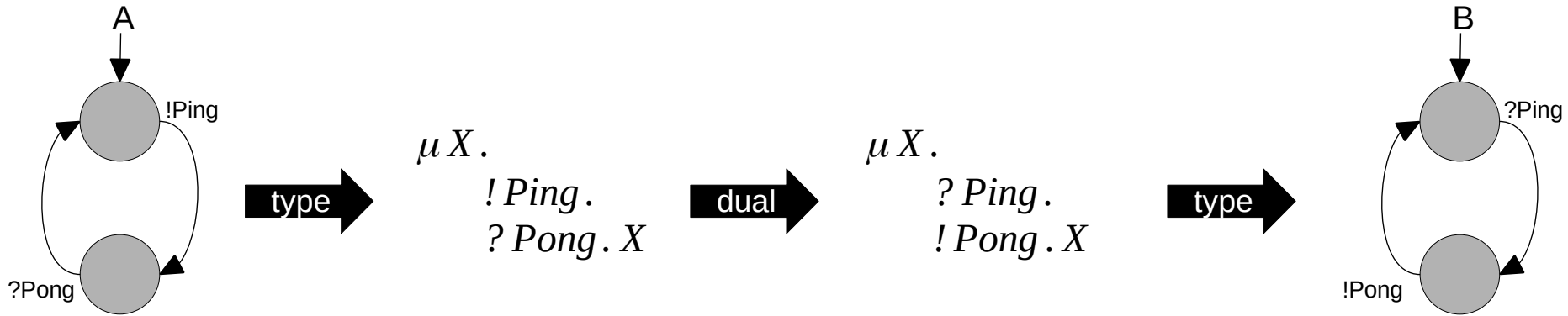
Operations on channel endpoints are **dual**.



# Binary Session Types (BST)

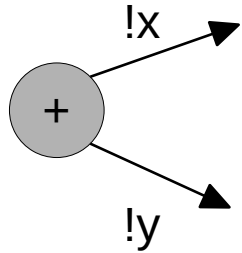
Idea: one side of the channel determines the operation on the other side.

- 1) get the operations for A
- 2) compute the operations for B using duality
- 3) check B executes the specified operations

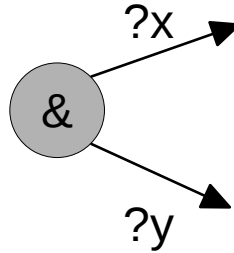


# Duality in Choice

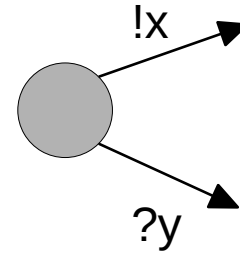
Internal



External



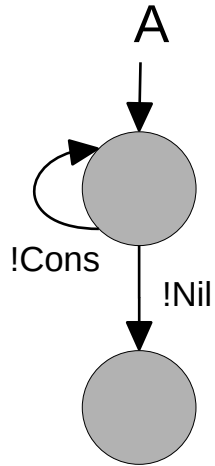
Mixed



dual

**deterministic** choice: all outgoing transitions have different labels

# BST Example with Choice



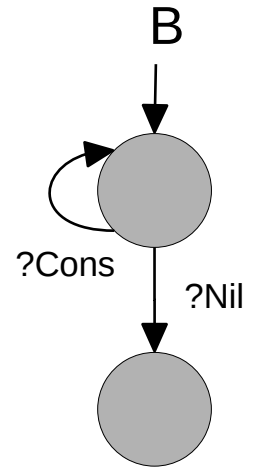
**type**

$$\mu X. \\ \quad !Cons.X \\ \quad \oplus !Nil.0$$

**dual**

$$\mu X. \\ \quad ?Cons.X \\ \quad \& ?Nil.0$$

**type**



# BST and Model Checking

BST specifies only **half-duplex** protocols. [Cécé05]

Half-duplex:

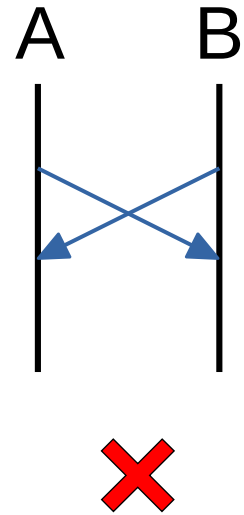
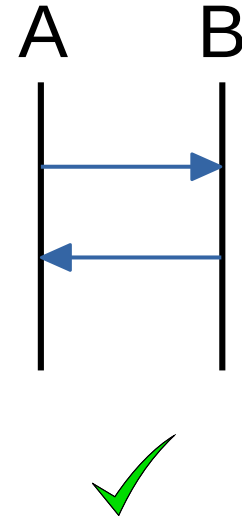
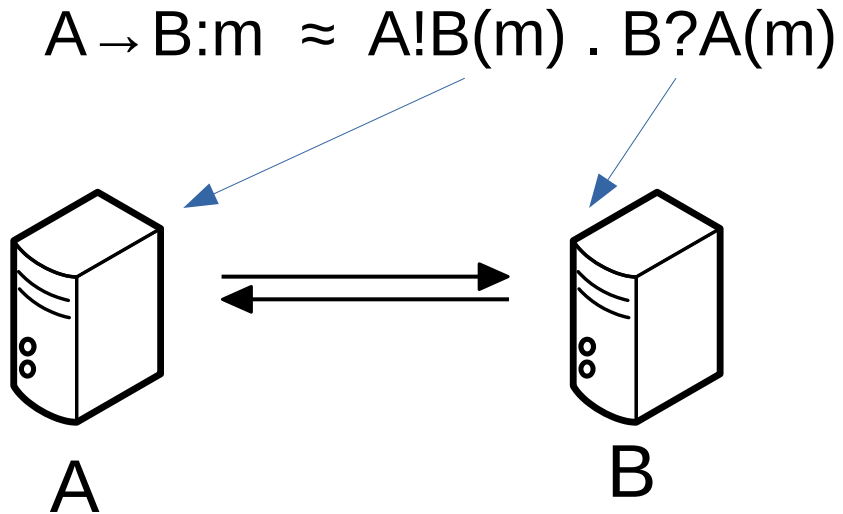
- Buffers are empty when communication switch direction
- With 2 processes: not Turing complete

BST enforce this restriction on the protocol: runs the same on half- and full-duplex systems.

[Cécé05] Gérard Cécé and Alain Finkel. Verification of programs with half-duplex communication. Inf. Comput., 2005.

# Duality and Message Spec.

Dual operations are easily **specified together**.



# More than two Processes...

- 2 processes: well understood
- 3+ processes: badly understood
  - Projection of global description is lossy. It can introduce non-determinism.
  - Messages sent by different processes are independent.



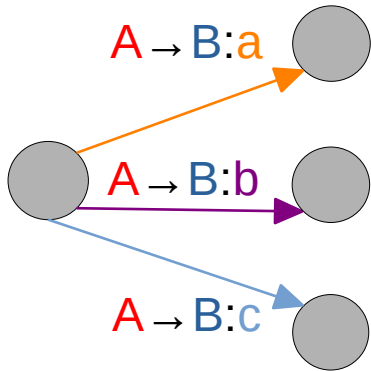
# Binary to Multiparty

Find some restriction to keep protocol “well-behaved”.  
Keep track of choices without getting confused.

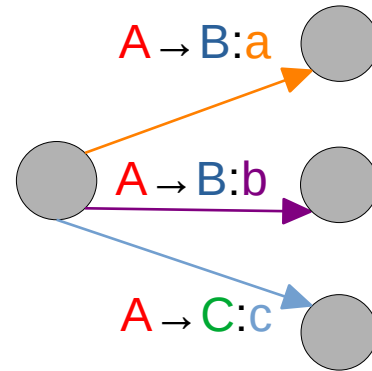
- First with directed choice (classical MST)
- Then with generalized choice (CONCUR paper)

# Directed vs Generalized Choice

Globally



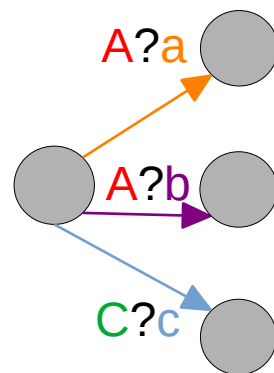
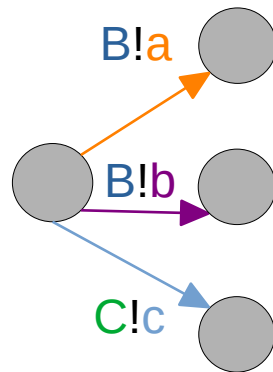
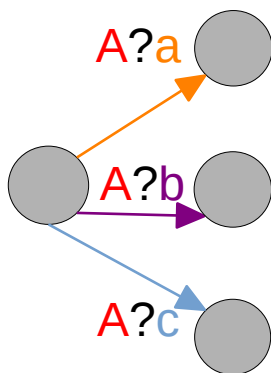
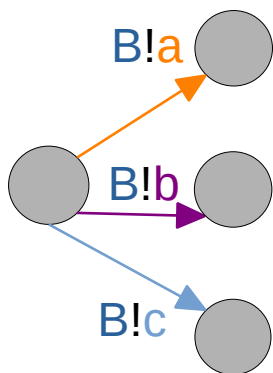
$A, B$  are constant.  
Only the messages ( $a, b, c$ ) change



Sender  $A$  is constant.  
The receivers ( $B, C$ ) and messages changes

# Directed vs Generalized Choice

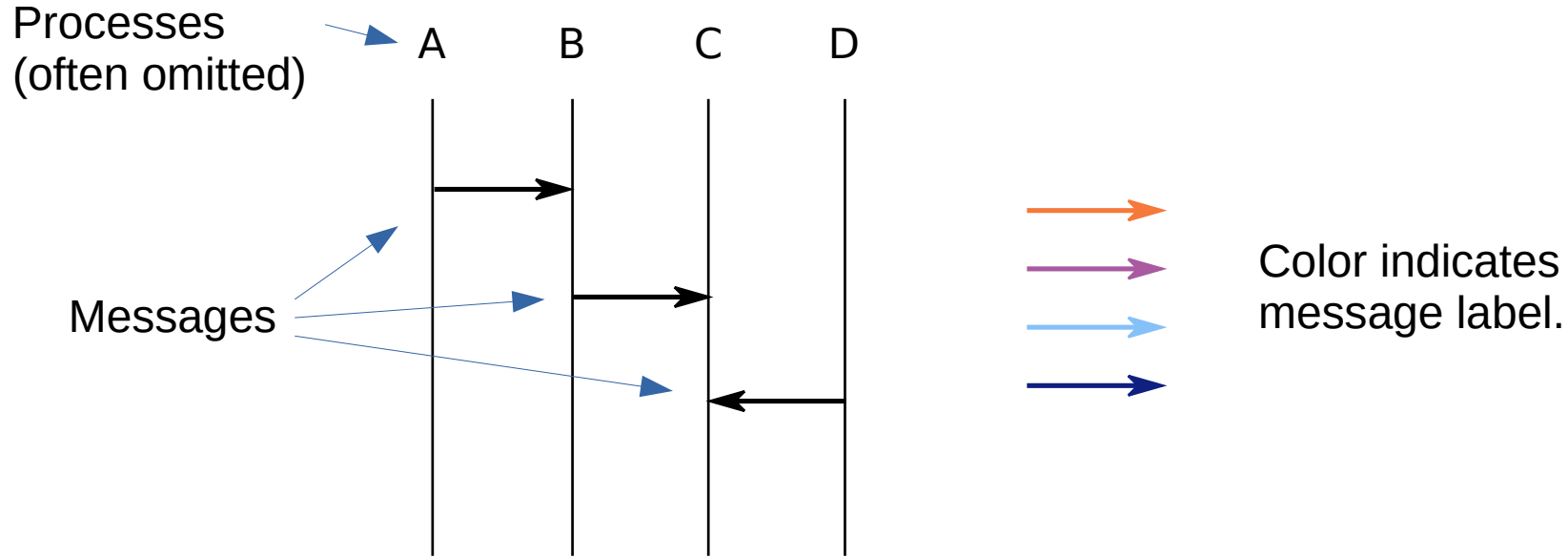
Locally



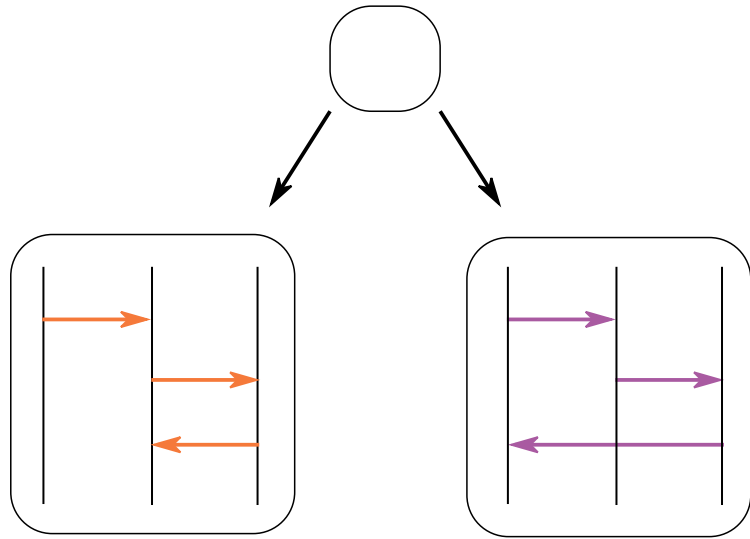
$A, B$  are constant.  
Only the messages ( $a, b, c$ ) change

Everything can change.

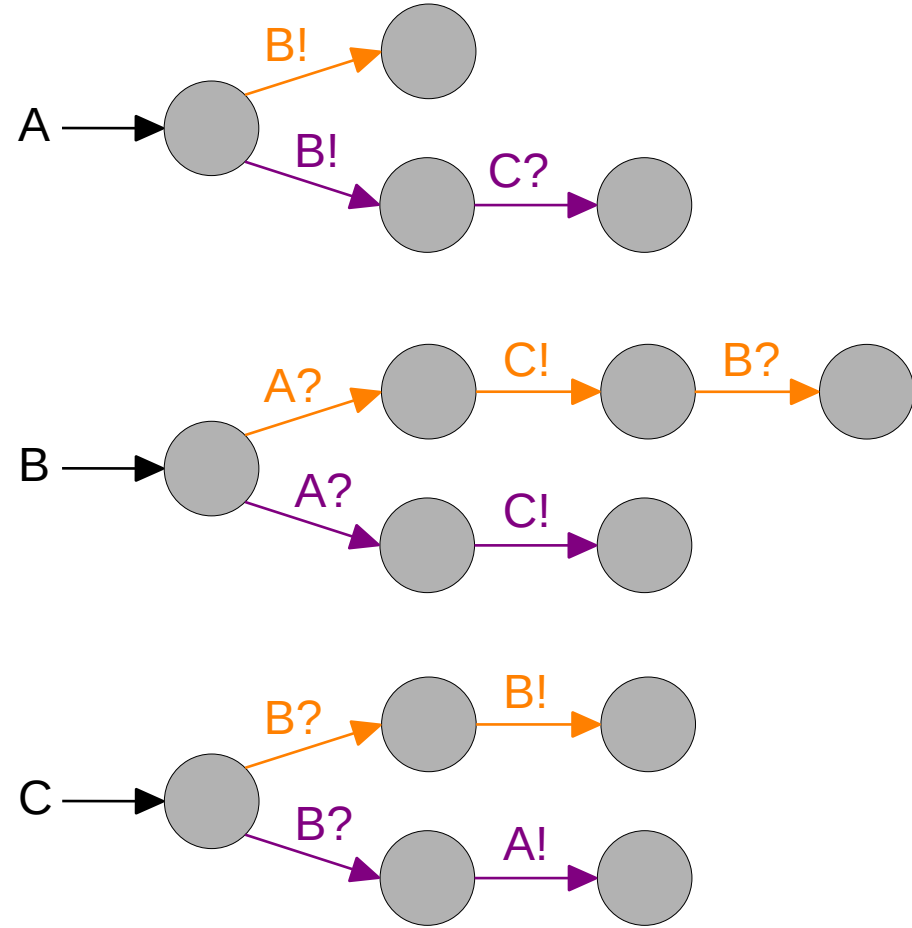
# High Level Message Sequence Charts Notation



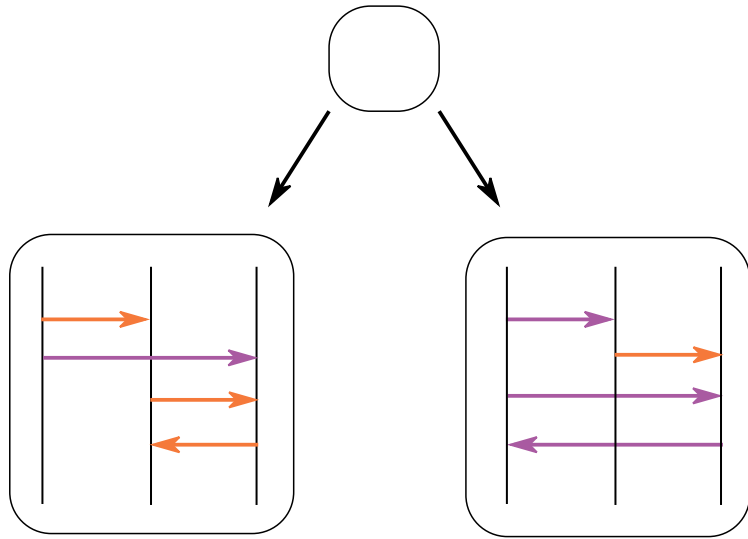
# From Duality to Projection



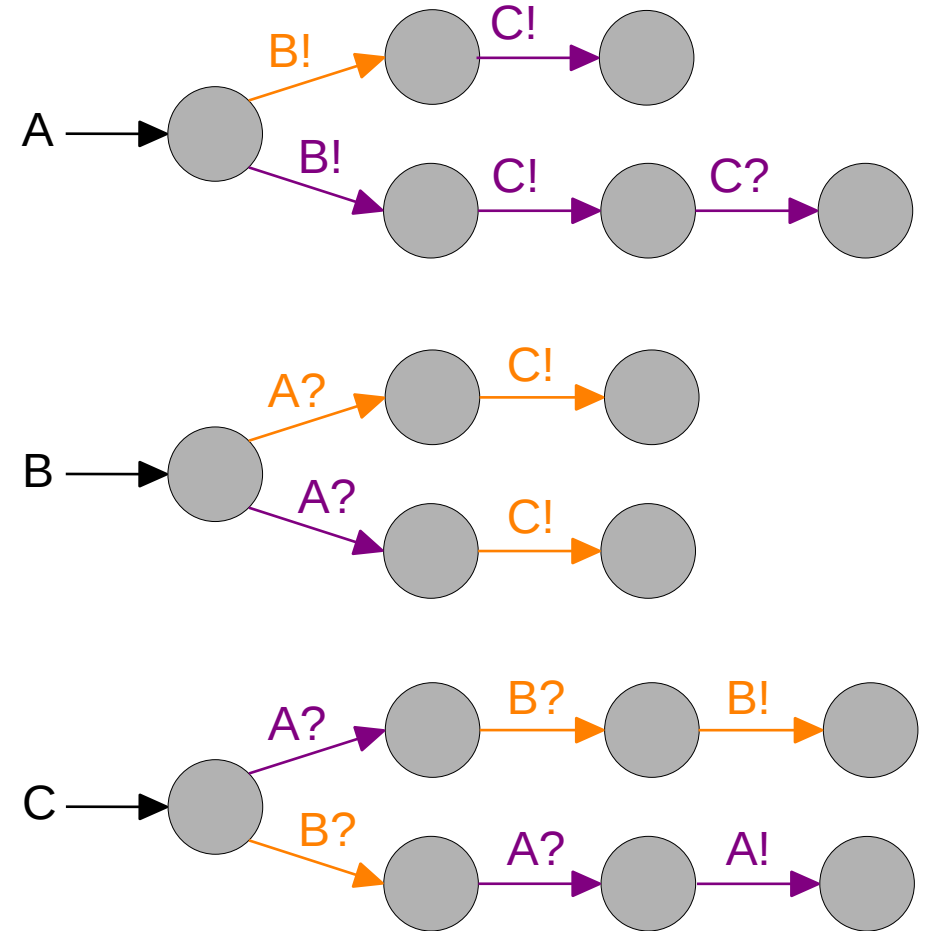
project



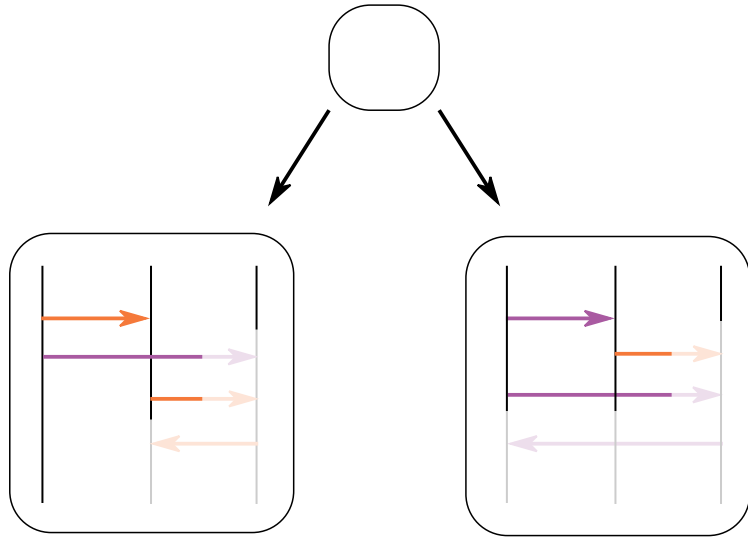
# Another Example



project

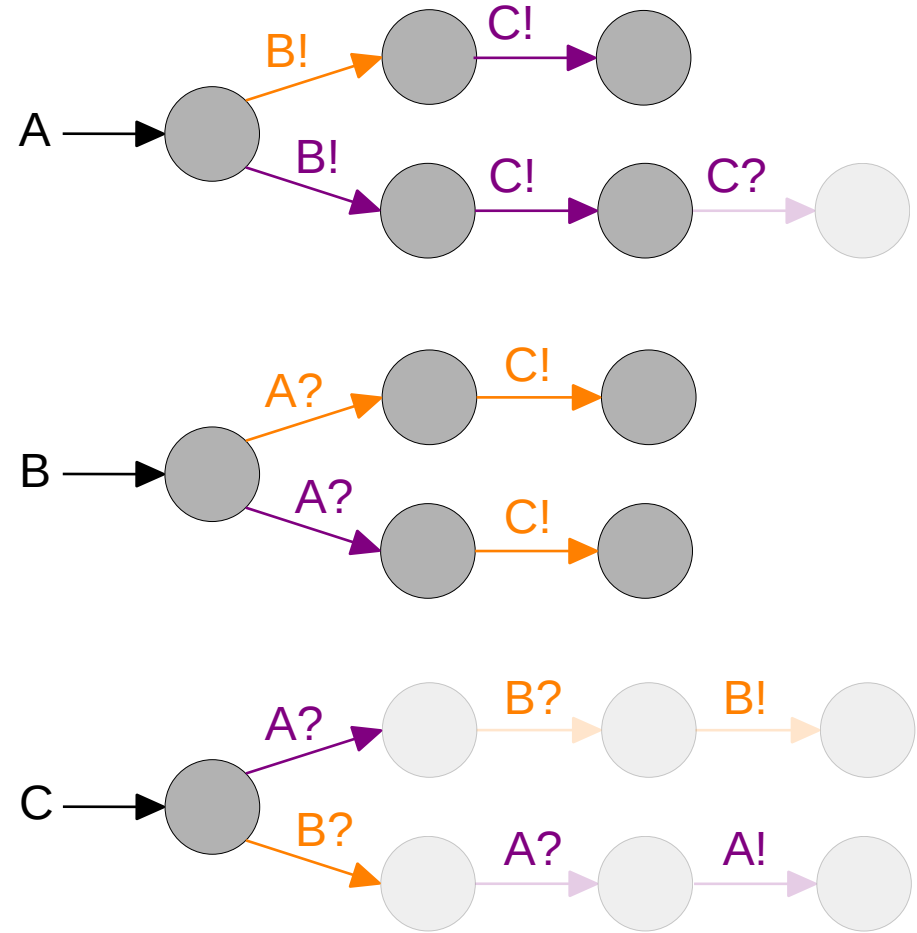


# Which is Wrong



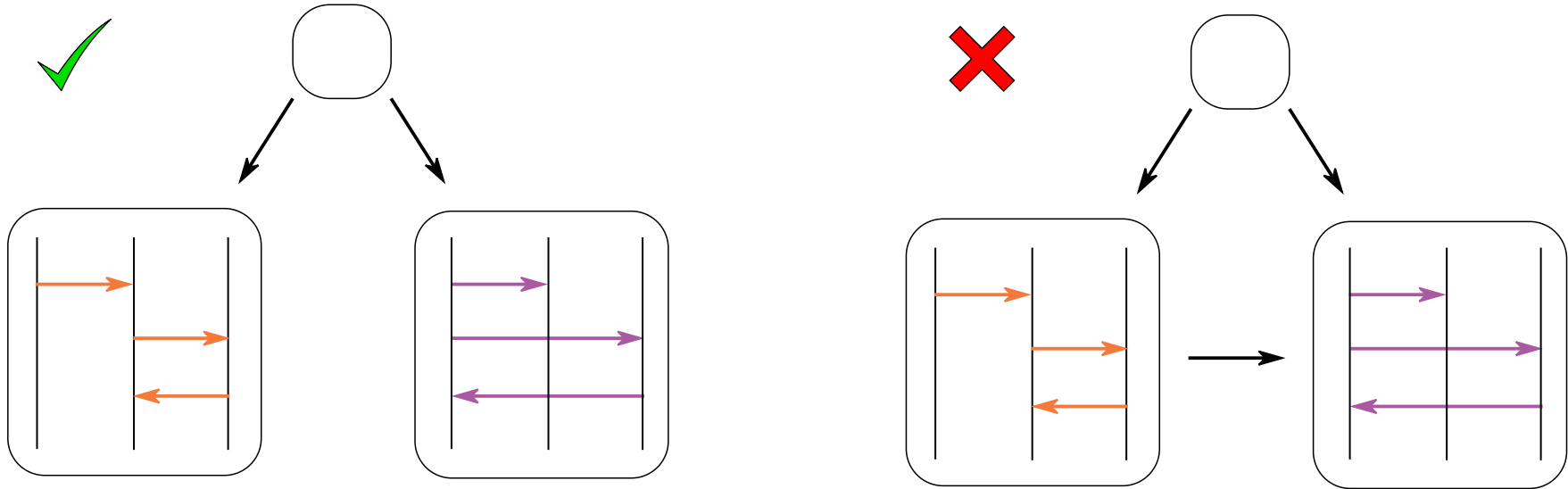
project

The messages from A,B are independent.  
C cannot rely on their ordering.



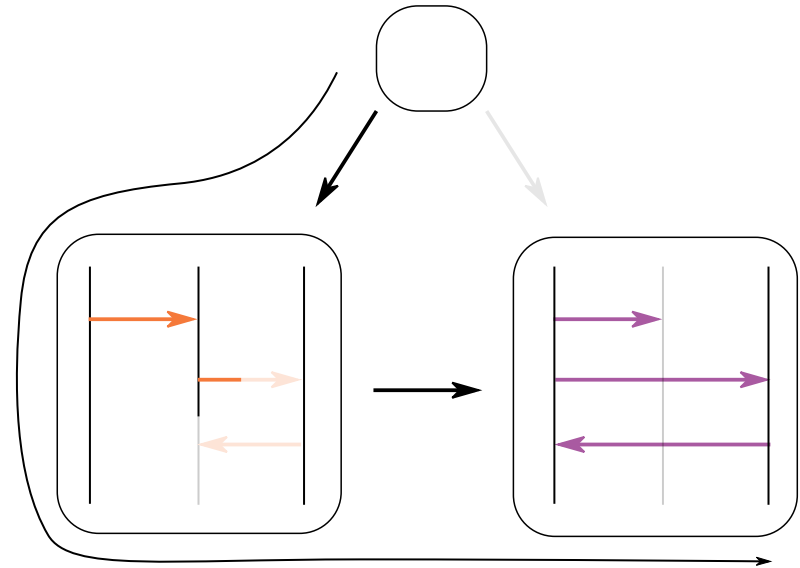
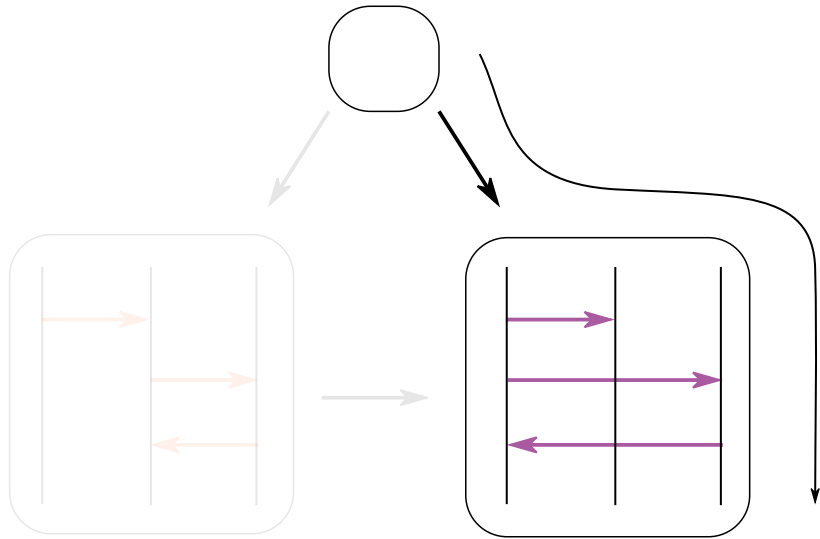
# No Compositionality

Composing two correct subprotocols can result in an incorrect one...

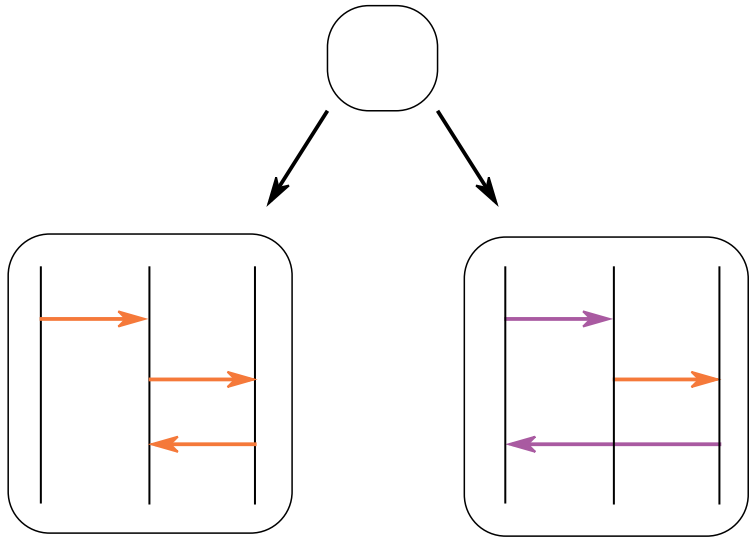




# Counterexample

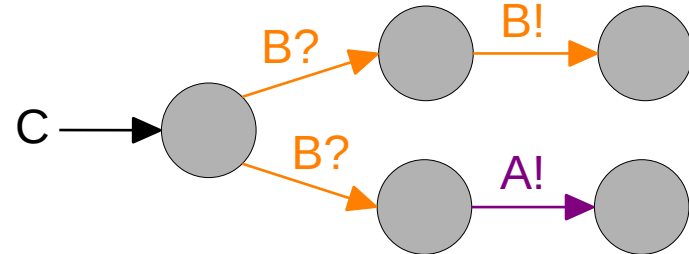
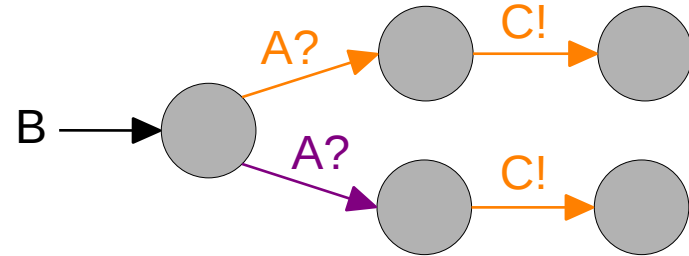
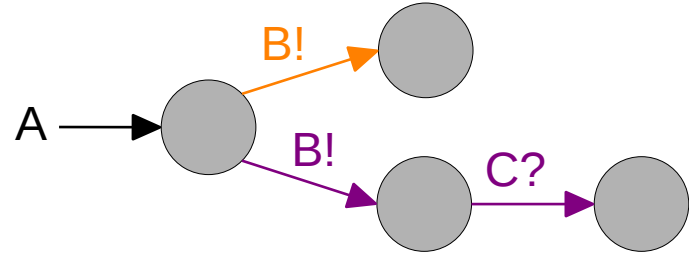


# Determinism does not carry over



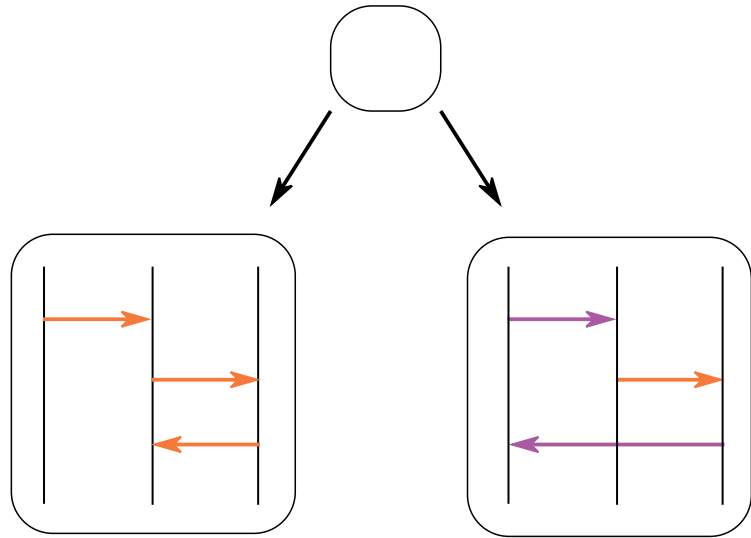
A makes the choice,  
B is deterministic,  
but C is not...

project

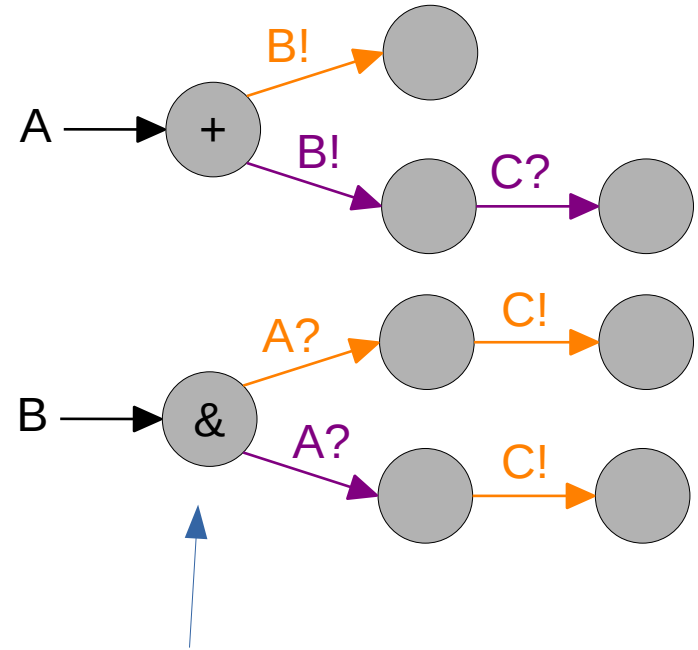


# MST in a Nutshell (1)

Projects the protocol and checks the projection does not introduce unwanted nondeterminism.



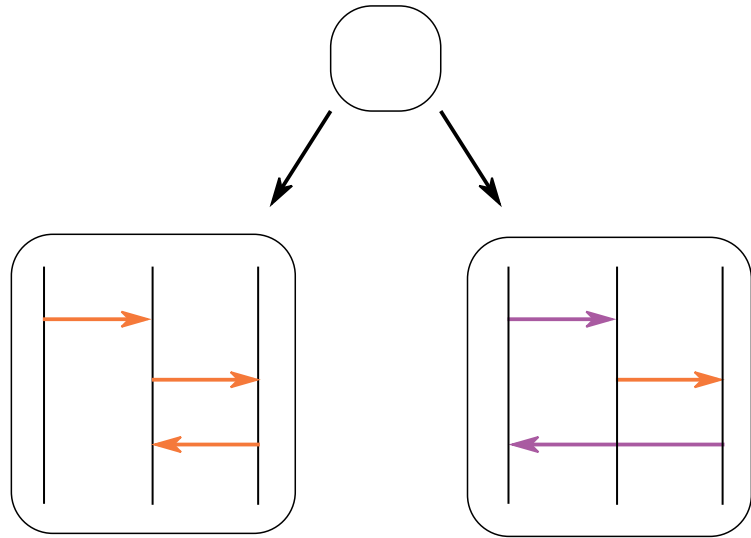
project



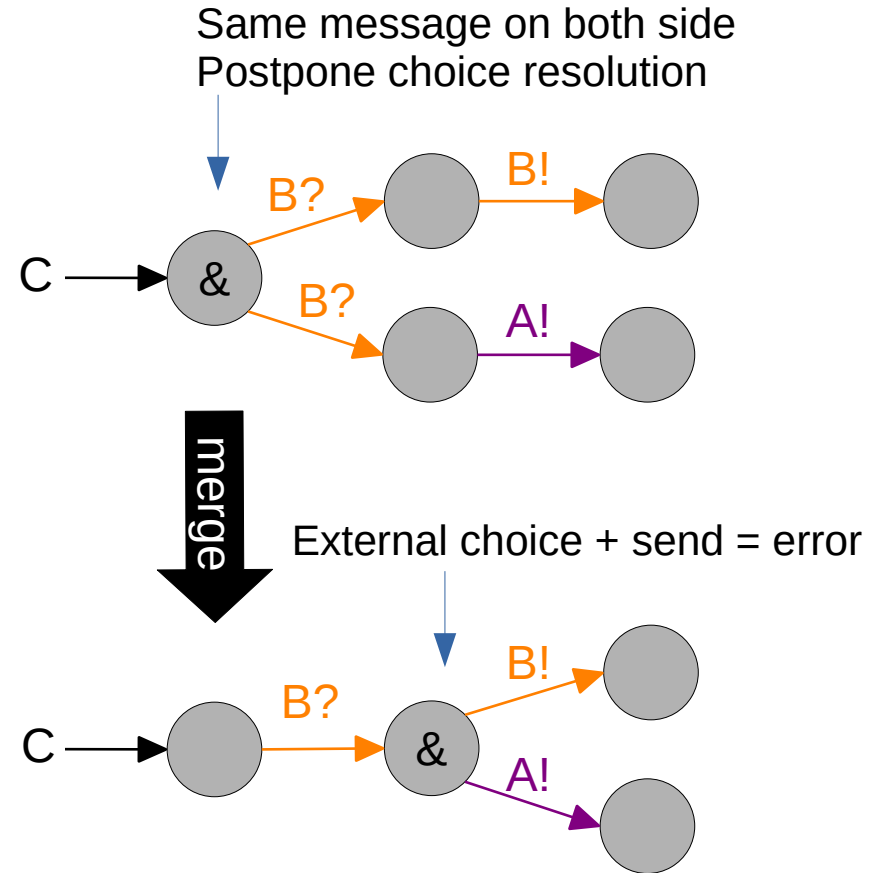
Keep track of internal/external choice

# MST in a Nutshell (2)

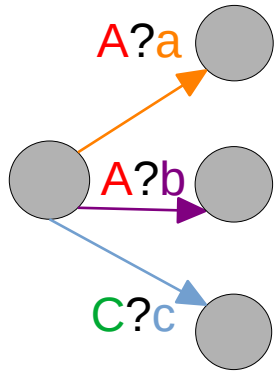
Projects the protocol and checks the projection does not introduce unwanted nondeterminism.



project

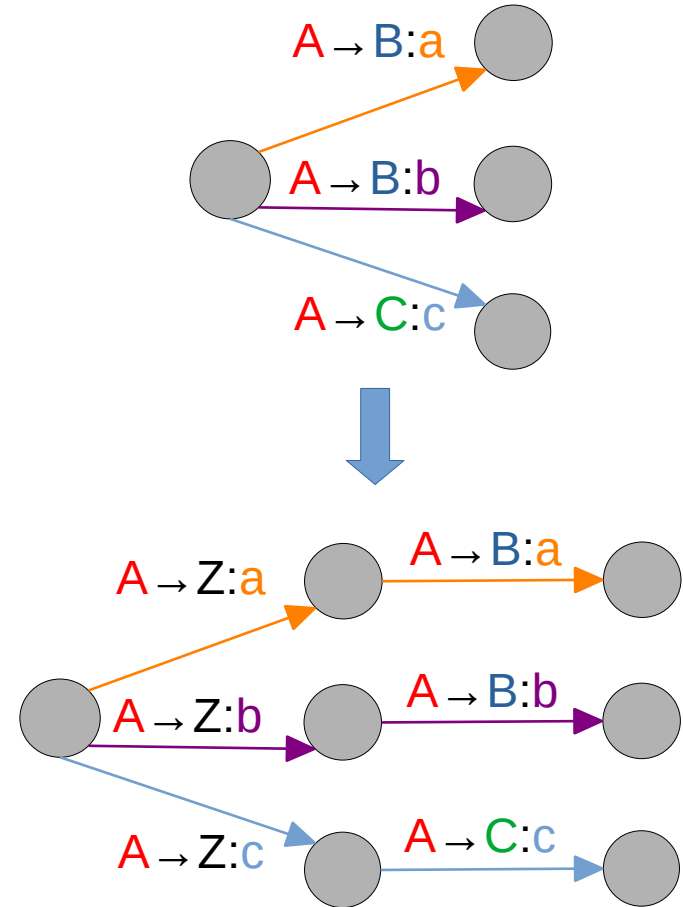


# Generalized Choice

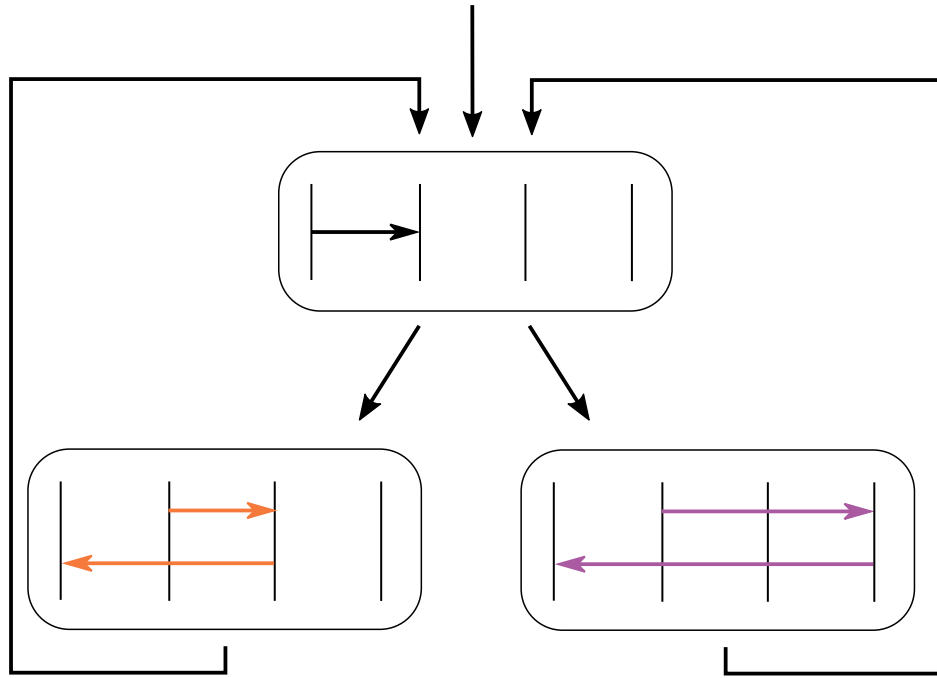


Local generalize receive that matters.

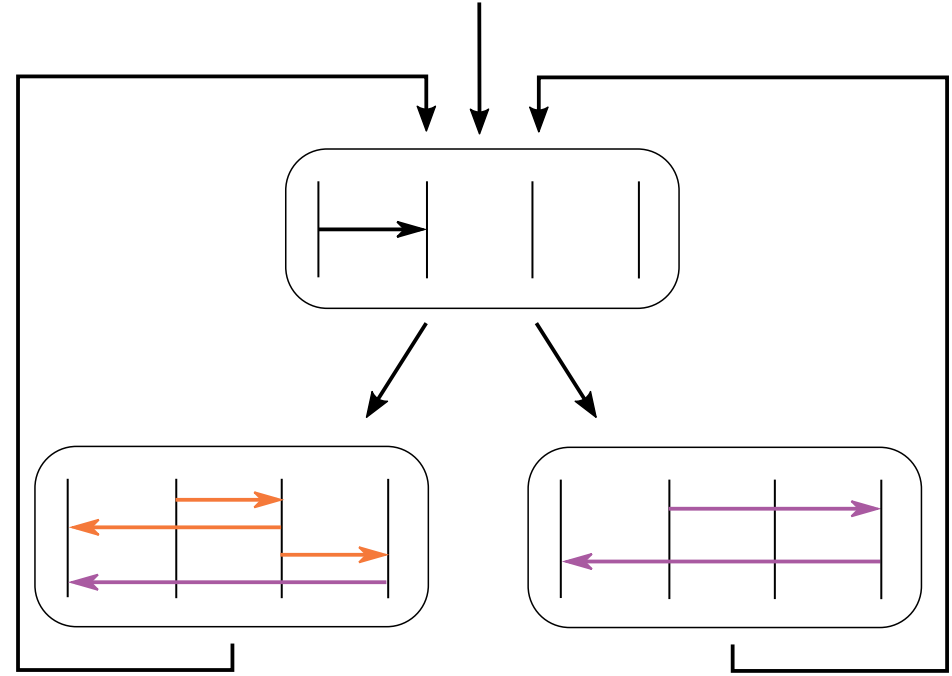
Global and sending can be simulated with an extra process.



# Partial Order Across Channels

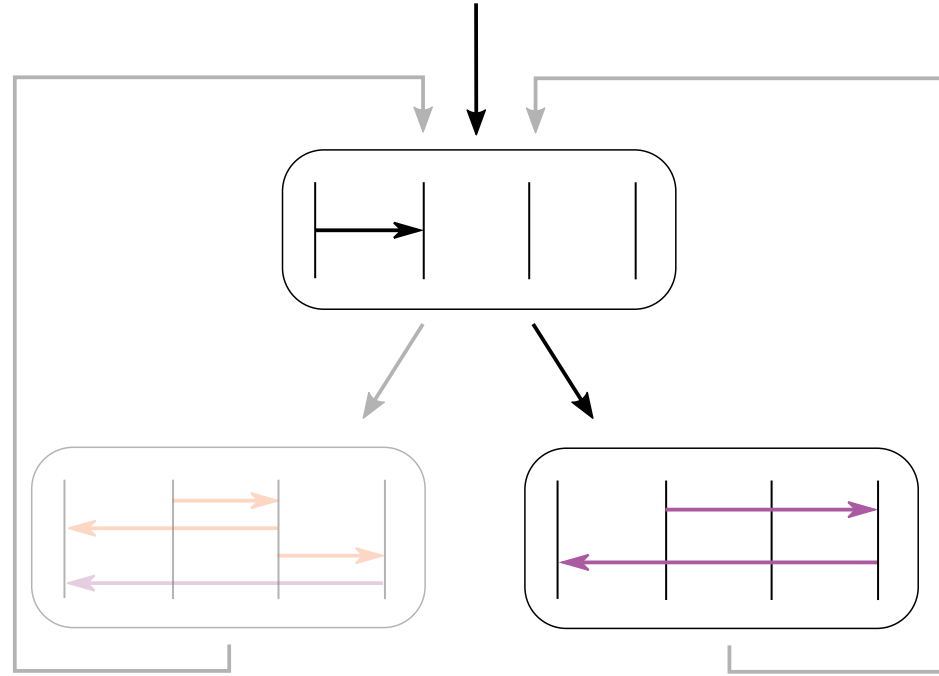
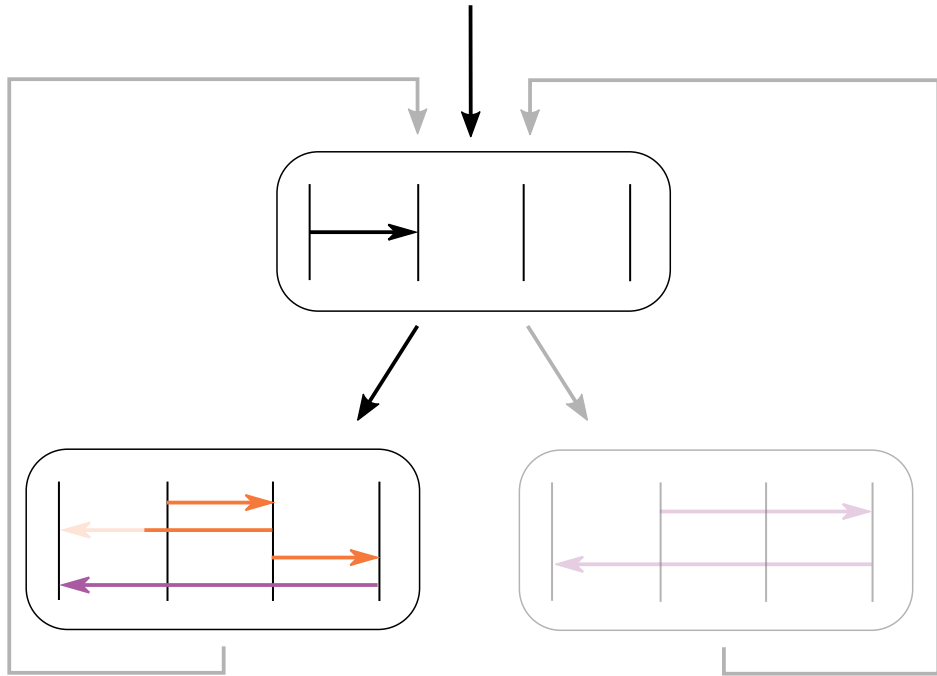


Well-formed



Wrong

# Wrong Example



# Projection and Merge

- Projection is similar to MST
- Merge checks for potential confusion

$$\begin{aligned}
 & \langle \&_{i \in I} \mathbf{q}_i?m_i.AL_{1,i} , Msg_1 \rangle \sqcap \langle \&_{i \in J} \mathbf{q}_i?m_i.AL_{2,i} , Msg_2 \rangle = \\
 & \&_{i \in I \setminus J} \mathbf{q}_i?m_i.AL_{1,i} \quad \& \quad \text{if } \begin{cases} \forall i \in I \setminus J. \mathbf{r} \triangleleft \mathbf{q}_i?m_i \notin Msg_2, \\ \forall i \in J \setminus I. \mathbf{r} \triangleleft \mathbf{q}_i?m_i \notin Msg_1 \end{cases} \\
 & \&_{i \in I \cap J} \mathbf{q}_i?m_i.(AL_{1,i} \sqcap AL_{2,i}) \quad \& \quad \text{No confusion} \\
 & \&_{i \in J \setminus I} \mathbf{q}_i?m_i.AL_{2,i}
 \end{aligned}$$

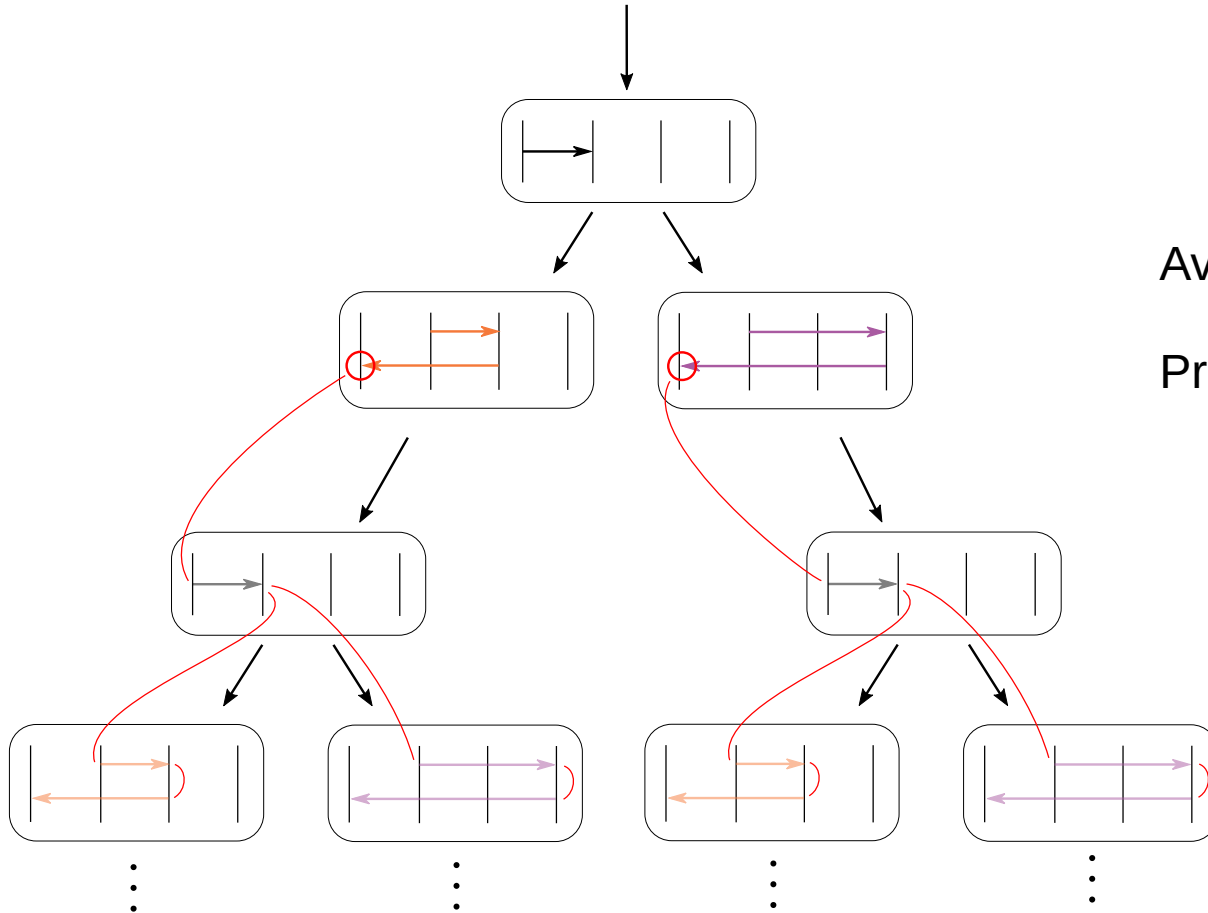
Available messages



# Available Messages

- 1<sup>st</sup> message in the channels (FIFO)
- Messages indep. from the receptions to merge
- Effectively computable (unfold recursion once)

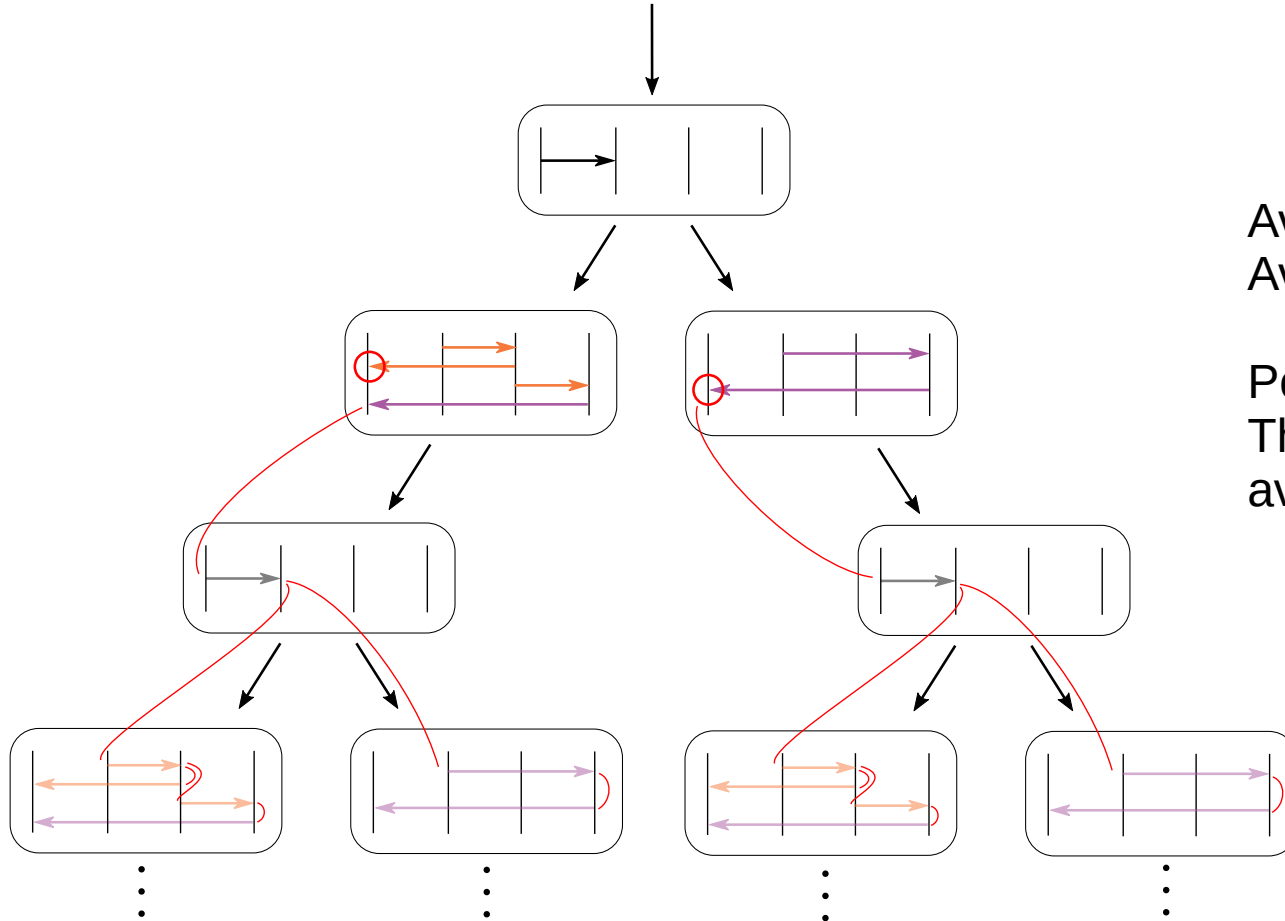
# Computing Available Messages 1



Available messages are  $\emptyset$ .

Protocol is one long causal chain.

# Computing Available Messages 2



Available left branch:  $\{\leftarrow\}$

Available right branch:  $\emptyset$

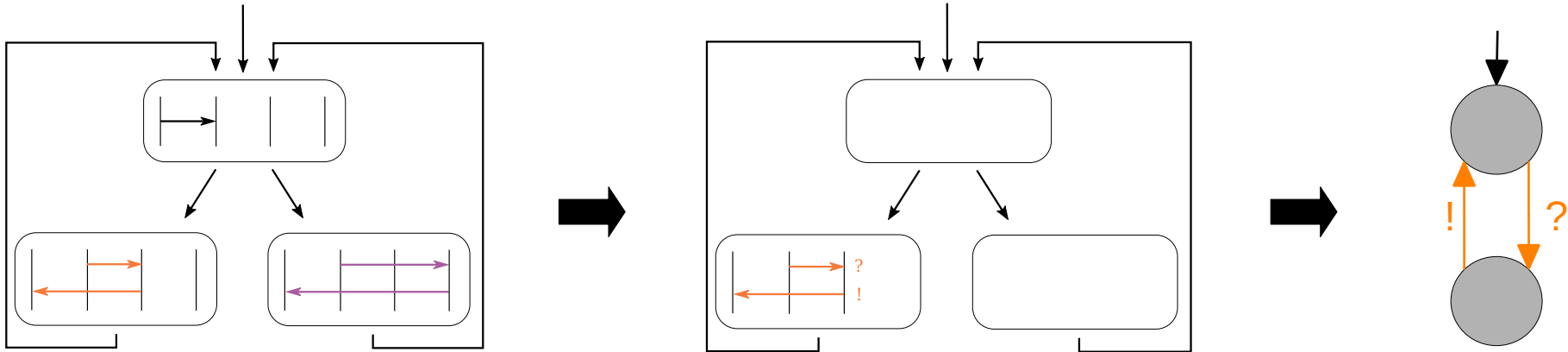
Potential confusion:

The right receive  $\leftarrow$  but it is also available on the left branch.

# Empty Paths (Loops) Elimination

Each worker only appears in one branch.

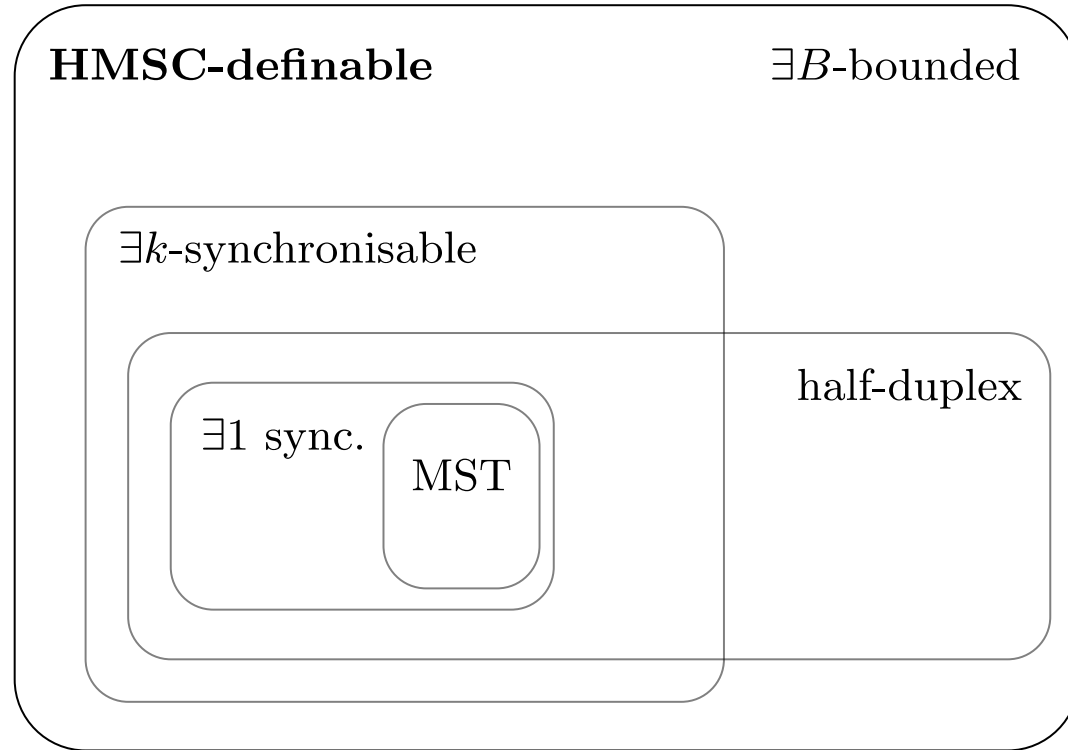
More general projection that allows loops where a process is not involved.



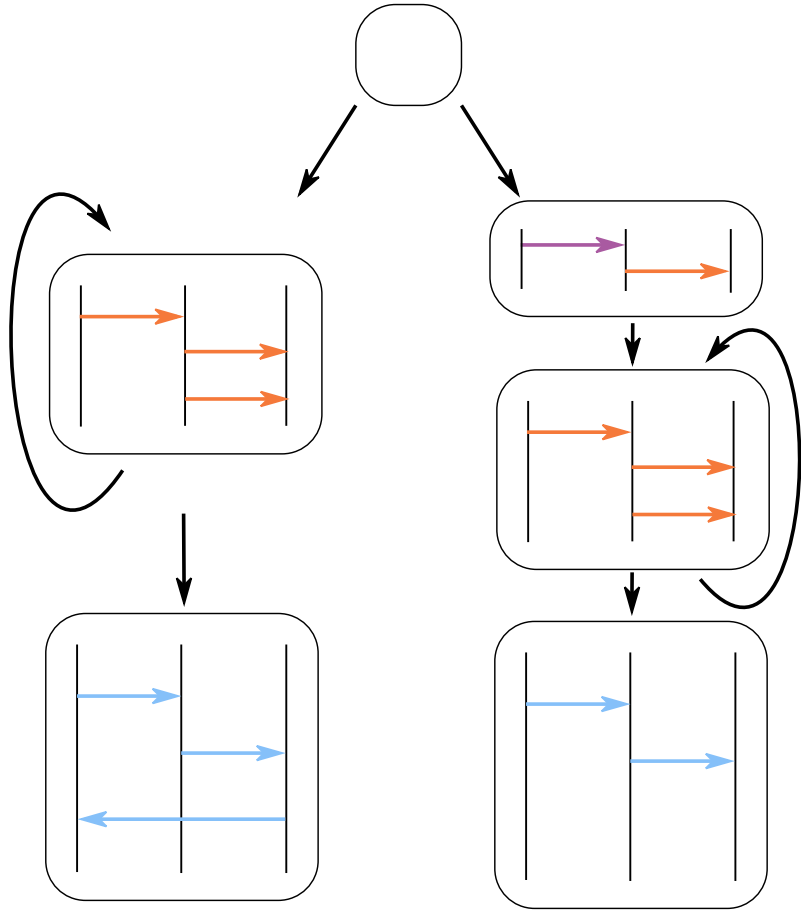
# Future Work

- Understanding MST languages
- Completeness and loops
- Reordering of independent receive
- Subtyping

# Understanding MST Languages



# Completeness and Loops

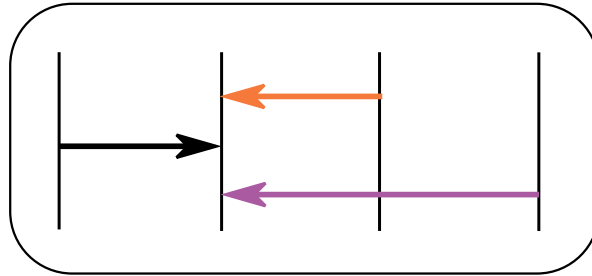


Implementable but rejected by MST.

directed choice  
 $\exists 1$ -bounded  
 $\exists 1$ -sync  
half-duplex

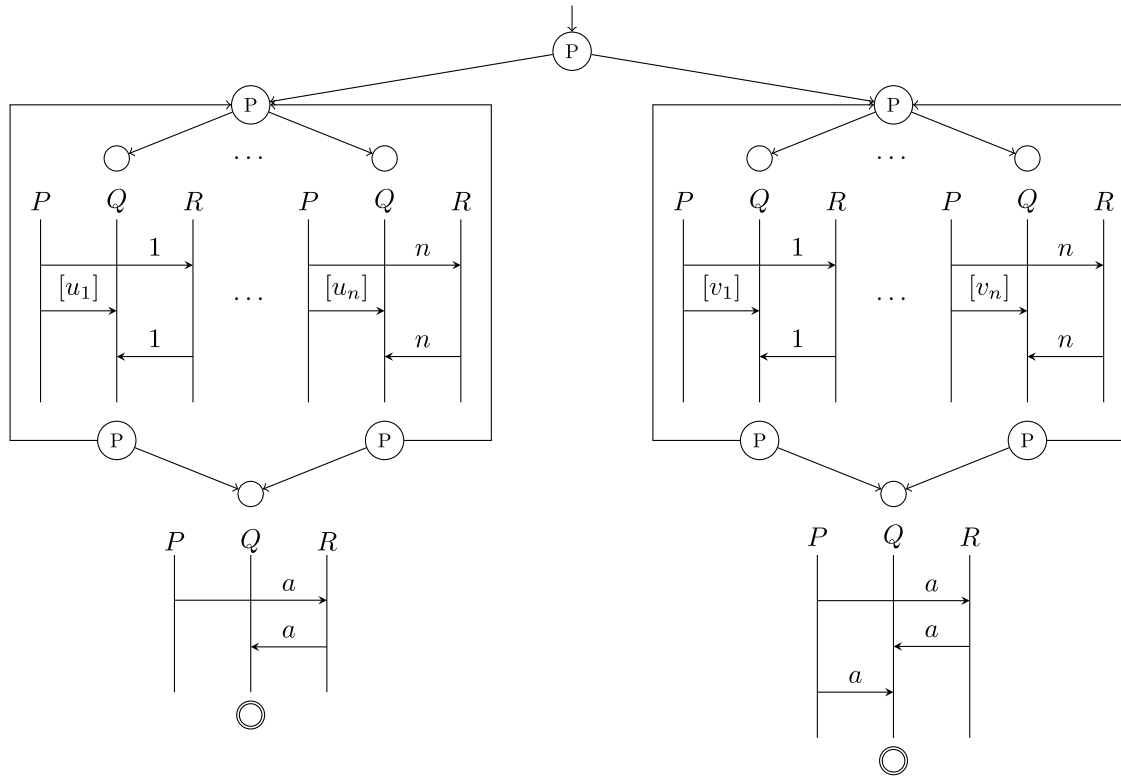
# Intra-Process Reordering

- Somewhat similar to precise subtyping
- Motivation: performance, process independent messages in their order of arrival





# Unfolding with Reordering ...



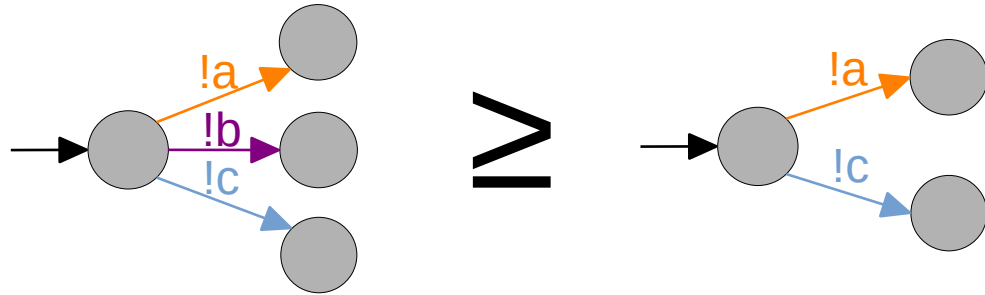
PCP encoding

... is hard.

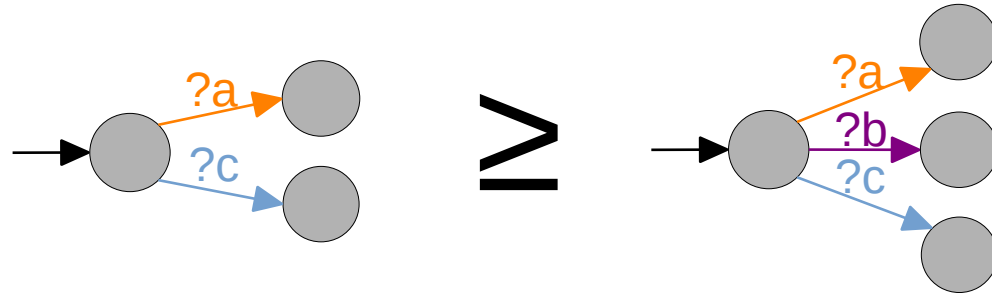
# Subtyping

What we expect for “typical” subtyping rules

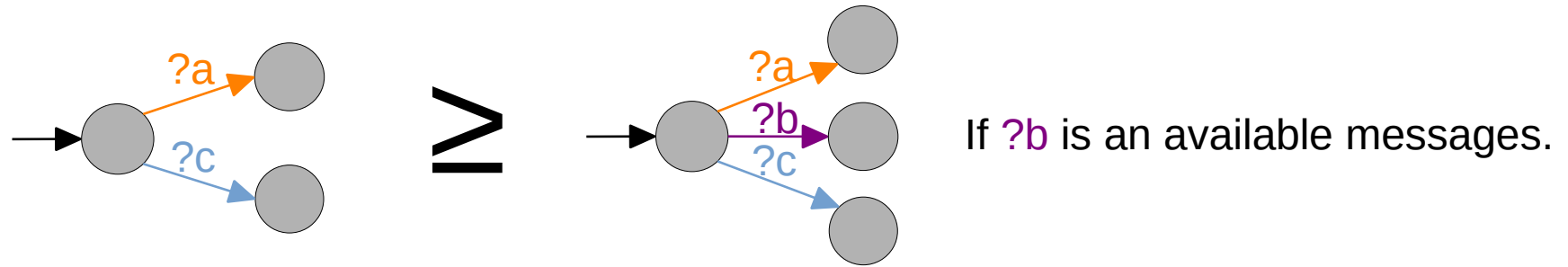
Send



Receive

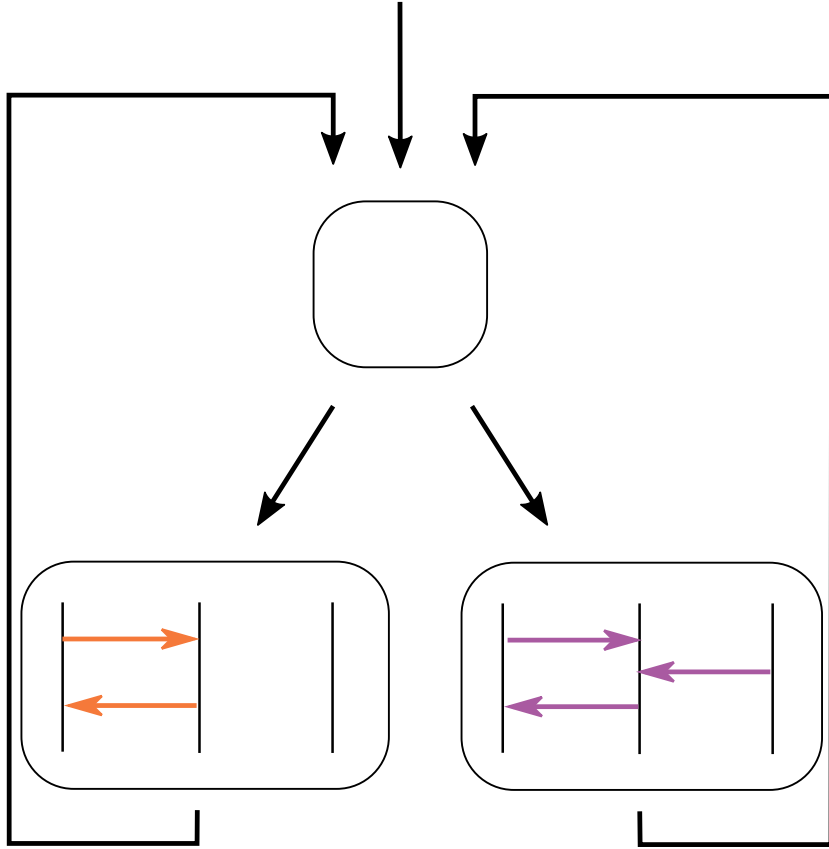


# Subtyping: Receive

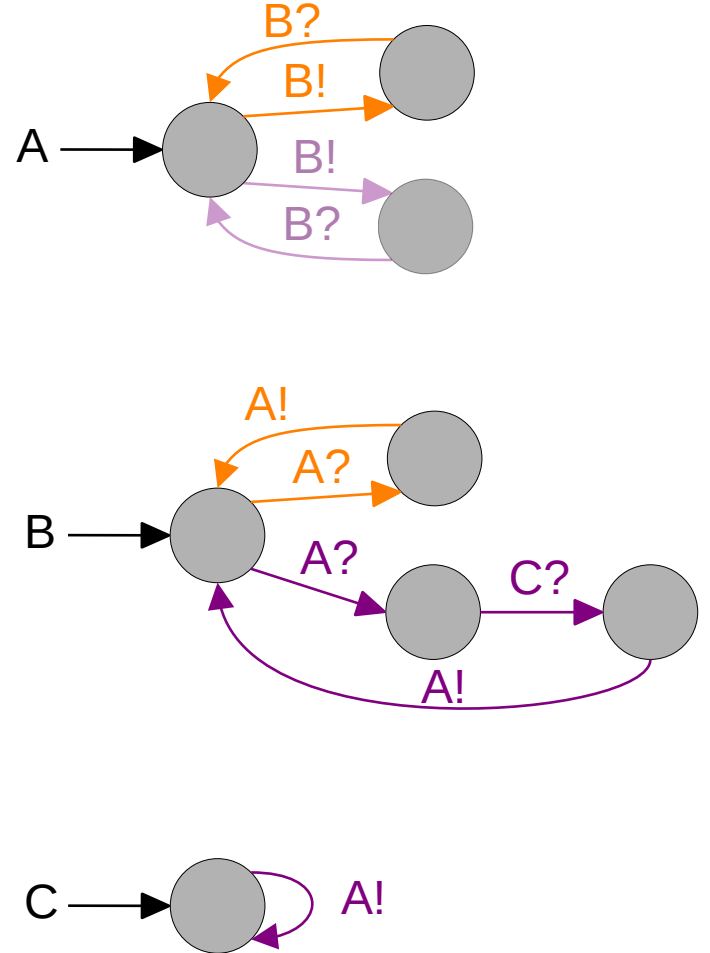


Subtyping is not local but needs global information.

# Subtyping: Send



project



# Conclusion

- Understanding how to specify communication protocols
- Finding the balance between expressiveness and complexity
- Generalized choice with projection that computes the available messages.

