#### Verification of Concurrent Asynchronous Message-passing Programs

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Outline Introduction Actor Systems Deadlock Freedom of *Static* Actor Systems

Outline

#### Introduction

- Actor System
- Aπ-calculus
- General Actor Systems
- Deadlock Freedom of Static Actor Systems
- Static Actor System
- a Potri Note
- Structural Analysis of Petri Nets
- Extensions to Dynamic Actor Systems
  - Parametric Systems
  - Star Topologies

# Outli Introductic Actor System Deadlock Freedom of Static Actor System Extensions to Dynamic Actor System

- Introduction
- Actor Systems
  - Aπ-calculus
  - General Actor Systems
- Deadlock Freedom of Static Actor Systems
  - Static Actor Systems
  - Petri Nets
  - · Structural Analysis of Petri Nets
- Extensions to Dynamic Actor Systems
  - Parametric Systems
  - Star Topologies



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#### Shared memory

Communication using a memory that every process can access (read and write).



- + Fast
- Limited scaling
- Hard to program (deadlocks, races, ...)

## Introduction Actor Systems Readllock Freedom of Static Actor Systems Extensions to Dynamic Actor Systems

#### Message passing

## Example (1): scala/docs/examples/actors/pingpong.scala



+ Scales well

- Slower

~ Hard to program (easier than shared memory ?)

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Actor Systems adlock Freedom of Static Actor Systems Extensions to Dynamic Actor Systems class Ping(count: Int, pong: Actor) extends Actor { var pingsLeft = count - 1 class Pong extends Actor ( pong ! Ping def act() { loop { var pongCount = 0 react { loop f case Pong => react { if (pingsLeft % 1000 == 0) case Ping => if (pongCount % 1000 == 0) println("Ping: pong") if (pingsLeft > 0) { println("Pong: ping "+pongCount) pong ! Ping sender ! Pong pingsLeft -= 1 pongCount += 1 } else { case Stop => println("Ping: stop") println("Pong: stop") pong ! Stop exit() exit()

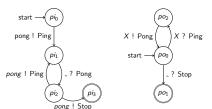
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Deadlock Freedom of Static Actor Systems
Extensions to Dynamic Actor Systems

Objectives and Contributions

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## ${\sf Example~(2):~scala/docs/examples/actors/pingpong.scala}$



#### Objectives

- · Identifying fragments:
  - interesting for the programmer;
  - where verification related problems are decidable.
- Algorithms fast enough to check properties of those fragments.

#### Contributions

- . An heuristic to check for Deadlock freedom of static systems.
- A new kind of system: Star Topologies
- A semi-algorithm for control reachability in Star Topologies.

#### Outline

- Actor Systems
  - Aπ-calculus
  - General Actor Systems

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#### $A\pi$ -calculus: Syntax

x(y).P(input prefix)  $\overline{x}(y)$ (output)  $\sum_i a_i(b_i).P_i$ (external choice) (parallel composition) 1P (replication)  $(\nu x)P$ (name creation) (unit process)

#### $A\pi$ -calculus: Concepts

The  $\pi$ -calculus [Milner et al., 1992a, Milner et al., 1992b] is a process calculus able to describe concurrent computations whose configuration may change during the computation.

The asynchronous π-calculus [Honda & Tokoro, 1991, Boudol et al., 1992] is a restriction of the  $\pi$ -calculus.

It is build around the notions of

Names : channels as first class values

Threads: concurrent execution of parallel threads:  $P \mid Q$ .

i/o prefixes : sending/receiving messages.

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#### $A\pi$ -calculus: Example (1)

 $\overline{pong_{Pin\sigma}} \langle ping_{Pon\sigma} \rangle | pi_1$ ping<sub>Pong</sub>().pi<sub>2</sub> pi22 + pi2h  $\overline{pong_{Ping}} \langle ping_{Pong} \rangle | pi_1$ pong Stop () pi3 0

pong! Ping pong! Ping ? Pong pong! Stop

Dia

#### $A\pi$ -calculus: Example (2)

$$\begin{array}{rcl}
\rho o_0 &=& \operatorname{pong}_{Stop}().\rho o_1 \\
&+& \operatorname{pong}_{Ping}(X).\rho o_2 \\
\rho o_1 &=& 0 \\
\rho o_2 &=& \overline{X}\langle\rangle|\rho o_0
\end{array}$$



### $A\pi$ -calculus: Semantics

Evaluating a formula in  $A\pi$ -calculus reduces to applying the rule:

$$\overline{a}\langle b
angle \mid \sum_{i=1}^n a_i(b_i).Q_i \ o \ Q_{\scriptscriptstyle X}[b/b_{\scriptscriptstyle X}] \quad ext{ where } a_{\scriptscriptstyle X}=a$$

#### What happens:

- channel a carries b:
- b is sent through a and replace b<sub>x</sub> in the continuation Q<sub>x</sub>.

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Tom Henzinger, Thomas Wies, Verifying actors  $A\pi$ -calculus: Semantics

 $A\pi$ -calculus: Semantics

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Evaluating a formula in  $A\pi$ -calculus reduces to applying the rule:

$$\overline{a}\langle b \rangle \mid \sum_{i \in I} a_i(b_i).Q_i \quad o \quad Q_{\scriptscriptstyle X}[b/b_{\scriptscriptstyle X}] \quad ext{ where } a_{\scriptscriptstyle X} = a$$

#### What happens:

- channel a carries b:
- b is sent through a and replace by in the continuation Qv.

Evaluating a formula in  $A\pi$ -calculus reduces to applying the rule:

$$\overline{a}\langle b \rangle \mid \sum_{i \in I} a_i(b_i).Q_i \rightarrow Q_x[b/b_x]$$
 where  $a_x = a$ 

#### What happens:

- channel a carries b:
- b is sent through a and replace by in the continuation Qv.

#### Overview

#### General Actor Systems

The Actor Model [Hewitt et al., 1973, Clinger, 1981, Agha, 1986] uses actors and their interactions to build concurrent softwares.

An actor can:

- · send finitely many messages to other actors.
- create a finite number of new actors
- receive a message from its mailbox and continue with a specified behaviour.

What can an actor do ?

Receive 
$$P(\vec{a}_I; \vec{a}_O) = \sum_{i \in I} a_i(\vec{b}_i).P_i(\vec{a}_I; \vec{a}_O, \vec{b}_i) \quad \forall i \in I, a_i \in \vec{a}_I$$

Send 
$$P(\vec{a}_I; \vec{a}_O) = \overline{a} \langle \vec{b} \rangle | P'(\vec{a}_I; \vec{a}_O)$$
  
Branch  $P(\vec{a}_I; \vec{a}_O) = A(\vec{a}_I; \vec{a}_O) \oplus B(\vec{a}_I; \vec{a}_O)$ 

New channel 
$$P(\vec{a}_I; \vec{a}_O) = (\nu \vec{a}) \cdot P'(\vec{a}_I, \vec{a}; \vec{a}_O)$$

New actor 
$$P(\vec{a}_I; \vec{a}_O) = (\nu \vec{n})(Q(\vec{n}; \emptyset)|P'(\vec{a}_I; \vec{a}_O, \vec{n}))$$

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Unique Receiver Condition [Amadio, 2000]

In  $\pi$ -calculus threads and names are independent. In the actor model an actor does not share its mailbox

The unique receiver condition links channels with a thread. It is a syntactic restriction where names that belong to a thread are kept separately.

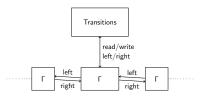
General Actor Systems What can an actor do ?

Receive 
$$P(\vec{a}_I; \vec{a}_O) = \sum_i a_i(\vec{b_i}) \cdot P_i(\vec{a}_I; \vec{a}_O, \vec{b}_i) \quad \forall i \in I, a_i \in \vec{a}_I$$

Send 
$$P(\vec{a}_i; \vec{a}_O) = \vec{a}(\vec{b})|P'(\vec{a}_i; \vec{a}_O)$$
  
Branch  $P(\vec{a}_i; \vec{a}_O) = A(\vec{a}_i; \vec{a}_O) \oplus B(\vec{a}_i; \vec{a}_O)$   
New channel  $P(\vec{a}_i; \vec{a}_O) = (\nu\vec{a}).P'(\vec{a}_i, \vec{a}_i; \vec{a}_O)$   
New actor  $P(\vec{a}_i; \vec{a}_O) = (\nu\vec{a})(Q(\vec{a}_i; \vec{a}_O; \vec{a}_O), \vec{a}_O)$ 

#### Reachability is undecidable for General Actor Systems.

Encoding a Turing machine into an actor system.



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Static Actor Systems Petri Nets Structural Analysis of Petri Net

#### Static Actor Systems

Systems of actors without creation of channels or actors are *static*. It corresponds to  $A\pi$ -calculus without creation of names. This fragment of  $A\pi$ -calculus reduces to Petri nets [Amadio & Meyssonnier, 2002].

#### Remark

Without name creation, a general !? + reply mechanism is not possible. However, we can emulate it when there is no more than one reply per received message.

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  - Parametric Syster
  - Star Topologi

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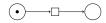
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#### Petri Nets

Petri nets are modeling language for discrete distributed systems. A Petri net (S, T, F, M) is a directed bipartite graph where

- S a finite set of places;
- T a finite set of transitions;
- F is the flow relation,  $F \subseteq (S \times T) \bigcup (T \times S) \rightarrow \{0,1\}$ ;
- ullet M is a marking,  $M:\mathcal{S} 
  ightarrow \mathbb{N}$  .

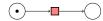
Places may contain some tokens, that are consumed and created by transitions.



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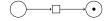


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Deadlock Freedom of Static Actor Systems

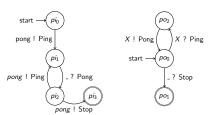
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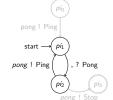
Tom Henzinger, Thomas Wies, Deadlock Freedom of Static Actor System

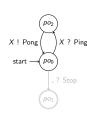
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Reachability: Static Actor Systems to Petri Nets (1)

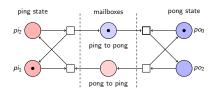
Reachability: Static Actor Systems to Petri Nets (1)







#### Reachability: Static Actor Systems to Petri Nets (2)



#### Structural Properties

Siphon: Set of places S such that  $\bullet S \subseteq S \bullet$ 



Trap : Set of places T such that  $T \bullet \subseteq \bullet T$ .



P-Invariant: (nonzero integer vector I, integer X) such that

$$\forall M \text{ marking}, M_0 \rightarrow^* M : \sum_{p \in P} I(p) \cdot M(p) = X$$

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Necessary Condition for Deadlock [Commoner, 1972]

Deadlock: at least one incoming place per transition is empty.

Deadlock: at least one incoming place per transition is empty.

Necessary Condition for Deadlock [Commoner, 1972]







#### Necessary Condition for Deadlock [Commoner, 1972]



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Structural Analysis of Petri Nets

Deadlock Freedom of Static Actor Systems Trap. Invariant, ILP, SAT

Algorithm 1 Check Petri net for deadlock freedom

Require: P = (S, T, F, M) a petri net Ensure: returns Yes if P is deadlock free s∈S t∈⊕s p∈⊕t / while  $R = \text{solve}(\phi)$  do if is maximal trap in R marked ? then

Trap, Invariant, ILP, SAT

 $t \leftarrow \text{smallest marked trap in } R$ else if  $\exists (I, X)$  controlling R then  $t \leftarrow \bigwedge_{s \in R} s$ ∆I(x):z/0

 $\phi \leftarrow \phi \wedge \neg t$ else if ILP approximation has a solution then  $\phi \leftarrow \phi \wedge \neg R$ 

return NO end if end while return Yes

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Structural Analysis of Petri Nets

#### Trap, Invariant, ILP, SAT

#### Algorithm 2 Check Petri net for deadlock freedom

Require: P = (S, T, F, M) a petri net Ensure: returns Yes if P is deadlock free Enumerating siphons with SAT solver V p ∧ finish ← while  $R = \text{solve}(\phi)$  do if is maximal trap in R marked ? then t ← smallest marked trap in R  $\phi \leftarrow \phi \wedge \neg t$ else if  $\exists (I, X)$  controlling R then  $t \leftarrow \bigwedge_{s \in R} s$ ^I(s);≠0  $\phi \leftarrow \phi \wedge \neg t$ else if ILP approximation has a solution then  $\phi \leftarrow \phi \wedge \neg R$ else return NO

Algorithm 3 Check Petri net for deadlock freedom

Require: P = (S, T, F, M) a petri net Ensure: returns Yes if P is deadlock free  $\phi \leftarrow \bigwedge \{s \Rightarrow \bigwedge$ V p ∧ finish x∈S \ t∈•x \p∈•t / while  $R = \text{solve}(\phi)$  do if is maximal trap in R marked ? then . t ← smallest marked trap in R  $\phi \leftarrow \phi \wedge \neg t$ else if  $\exists (I, X)$  controlling R then  $\bullet$ Checking siphon for emptiness  $t \leftarrow \bigwedge_{s \in R} s$ ∧I(x);r0  $\phi \leftarrow \phi \wedge \neg t$ else if ILP approximation has a solution then  $\phi \leftarrow \phi \wedge \neg R$ else return NO end if

end if

end while

return Yes

end while

return Yes

#### Trap, Invariant, ILP, SAT

#### Algorithm 4 Check Petri net for deadlock freedom

Require: P = (S, T, F, M) a petri net Ensure: returns Yes if P is deadlock free t ∈ • x while  $R = \text{solve}(\phi)$  do if is maximal trap in R marked ? then t ← smallest marked trap in R  $\phi \leftarrow \phi \wedge \neg t$ else if  $\exists (I, X)$  controlling R then  $t \leftarrow \bigwedge_{\substack{s \in R \\ \land I(s) \neq 0}} s$  $\phi \leftarrow \phi \wedge \neg t$ else if ILP approximation has a solution then Refining enumeration  $\phi \leftarrow \phi \wedge \neg R$ return NO



Example

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Deadlock Freedom of Static Actor Systems

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Structural Analysis of Petri Nets

Example

Deadlock Freedom of Static Actor Systems

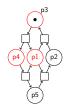
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Structural Analysis of Petri Nets

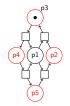
#### Example

end if end while return Yes



#### Siphon p1,p3,p4

- has no marked trap.
- has no place invariant.
- has no ILP solution.

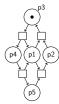


#### Siphon p2,p3,p4,p5

 has marked trap p2,p3,p4,p5.

Results

#### Example



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#### No more siphon.

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Petri net is deadlock free.

Name	#places	#transitions	Deadlock	Tina <sup>1</sup>	heuristic
Philo 2	129	232	Yes	0.4 s	0.4s
Philo 3	265	650	Yes	62.4s	0.4s
Philo 4	449	1398	Yes	_	0.6s
Philo 8	1665	9610	Yes	_	28 s
Pi approx 3	130	260	No	0.2 s	5.8 s
Pi approx 4	204	490	No	1s	137 s
Pi approx 5	294	822	No	11 s	_
Pi approx 6	400	1274	No	121 s	l —
Pi approx 8	660	2610	No	_	_
Cell safe	34	38	No	_	0.1s
Cell safe compact	4	26	No	6.1 s	0.1s
Cell unsafe	34	29	Yes	0.1 s	0.1s
Cell unsafe compact	4	17	Yes	0.1 s	0.1s

1 [Berthomieu & Vernadat, 2006] Tom Henzinger, Thomas Wies,

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Outline

- Extensions to Dynamic Actor Systems
  - Parametric Systems
  - Star Topologies

Static Actor Systems: Too Restrictive

Unfortunately, most real life programs are not static.

They also create actors.

We explore two cases:

- Parametric systems
- · Systems with creation of actors

A parametric system is a function  $\mathcal{F}$  that for any  $n \in \mathbb{N}$  maps to a static system  $\mathcal{F}(n)$ . The type of problem we are interested in is:

Given  $\mathcal{F}: \mathbb{N} \to \mathsf{Static}$  System. P a safety property, prove:

$$\forall n \in \mathbb{N}, \ \mathcal{F}(n) \text{ verifies } P$$

Unfortunately, deciding such problem is in general not possible [Apt & Kozen, 1986].



#### Dynamic Creation of Actors

#### What we want

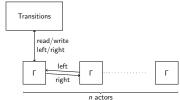
Adding equations of the kind:

$$P(\vec{a}_I;\vec{a}_O) = (\nu \vec{n})(Q(\vec{n};\emptyset)|P'(\vec{a}_I;\vec{a}_O,\vec{n}))$$

Consequence: Without any restriction, we can still apply the Turing machine construction for general actors systems.

#### $\lim_{n\to\infty} \mathcal{F}(n)$ is Turing Complete

It is possible to encode a n-bounded Turing machine within  $\mathcal{F}(n)$ .



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#### Restrictions

#### Restrictions

- Limiting name mobility (1 hop)
- Only a finite subset of all actors are allowed to create actors.

What it does: Created actors are isolated from each other. (i.e. no recursive infinite structure)

#### Star Topologies: Definition

$$\begin{split} P(\vec{a}_l; \vec{a}_O) &= \sum_{i \in I} a_i(\vec{b}_i).P_i(\vec{a}_l; \vec{a}_O, \vec{b}_i) \qquad \forall i \in I, a_i \in \vec{a}_l \quad (1) \\ P(\vec{a}_l; \vec{a}_O) &= \vec{a}(\vec{b})|P'(\vec{a}_l; \vec{a}_O) \qquad \qquad \forall b \in \vec{b}, b \notin \vec{a}_O \quad (2) \end{split}$$

$$P(\vec{a}_I; \vec{a}_O) = \bar{a} \langle \vec{b} \rangle | P'(\vec{a}_I; \vec{a}_O)$$

$$\forall b \in \vec{b}, b \notin \vec{a}_O$$
 (2)

$$P(\vec{a}_I; \vec{a}_O) = A(\vec{a}_I; \vec{a}_O) \oplus B(\vec{a}_I; \vec{a}_O)$$

$$P(\vec{a}_I; \vec{a}_O) = (\nu \vec{n})(Q(\vec{n}; \emptyset)|P'(\vec{a}_I; \vec{a}_O, \vec{n}))$$

Static actors can have all types of equations, but they cannot be created

Dynamic actors are created. However, they cannot have equations of type (4).



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Star Topologies: Issues

2 dimensions of unboundedness:

- unbounded number of actors:
- · unbounded number of messages in each actor's mailbox.

Static actor systems have only the message dimension.

If we can remove one dimension, we can use algorithms similar to the static case

#### Star Topologies: Analysis

#### Definition (Control Flow Reachability)

Given a system of equation in  $A\pi$ -calculus containing an equation identifier A and an initial configuration P, the control flow reachability problem asks whether it is possible to reach a configuration P' containing A:

 $P \rightarrow^* P'$  where P' is a process of the shape ... |A(...)| ....

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Star Topologies: Dual Abstraction

Remove the messages related source of unboundedness with counter abstractions.

drop-counter: 0 to bound then drop ∞-counter : 0 to bound then ∞

drop-abstraction counts the messages of dynamic actors with drop-counters.

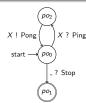
∞-abstraction counts the messages of dynamic actors with ∞-counters

#### Star Topologies: Equivalence Classes of Dynamic Actors

Transforming a dynamic actor d with an unbounded number of messages into a finite object.

- From dynamic actors to equivalence classes:
  - Fetch all messages containing a channel owned by d.
  - Substitute owned channels by Self. It corresponds to alpha-conversion in the  $\pi$ -calculus congruence relation.
- Apply the counter abstraction on each message kind to abstract infinitely many configuration into a finite number of possibilities.

#### Star Topologies: Example of Equivalence Classes



- At location pos
- Parameter X = ping
- Messages: From Type ping pong, pongn ping

One static ping actor Many dynamic pong; actors

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DOO

X ? Ping

? Stop

X ! Pong

start  $po_0$  Verifying actors

#### Star Topologies: Example of Equivalence Classes Star Topologies: Example of Equivalence Classes



- At location no.

viessages			
From	Type	То	#
ping	Ping	Self	1
Self	Pong	ping	5

One static ping actor Many dynamic pong; actors

- Parameter X = ping

One static ping actor Many dynamic pong; actors

 $po_1$ 

 At location pos Parameter X = ping

Messages:

From Type ping Self

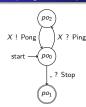
Pong Bound of abstraction is 3

Ping Self

To

ping

#### Star Topologies: Example of Equivalence Classes



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drop-abstraction

- At location po<sub>2</sub>
- Parameter X = ping

One static ping actor

Bound of abstraction is 3.

Many dynamic pone; actors

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Parametric Systems

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Extensions to Dynamic Actor Systems

Well Structured Transition System (WSTS)

WSTS are a generalisation of Petri nets that keep the monotonicity properties of Petri nets [Abdulla et al., 1996, Finkel & Schnoebelen, 2001].

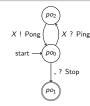
The transition relation →, wgo <:

$$A \leq B \land A \rightarrow A' \Rightarrow \exists B', B \rightarrow B' \land A' \leq B'$$

The property p also needs to satisfy some monotonicity condition:

A satisfies  $p \land A \leq B \Rightarrow B$  satisfies p

#### Star Topologies: Example of Equivalence Classes



 $\infty$ -abstraction

- At location po2
- Parameter X = ping
- Messages: <u>From Type To #</u> <u>ping Ping Self 1</u> Self Pong ping ∞

One static ping actor Many dynamic pong; actors Bound of abstraction is 3.

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Parametric System
Star Topologies

tems

Star Topologies: Coverability Tree

Coverability Trees are used to analyse Petri nets [Karp & Miller, 1969, Finkel, 1991]. The idea was generalized to WSTS [Finkel, 1987].



(1, 0)

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Star Topologies: <

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Verifying actors Star Topologies

Star Topologies: Coverability Tree

Coverability Trees are used to analyse Petri nets [Karp & Miller, 1969, Finkel, 1991]. The idea was generalized to WSTS [Finkel, 1987].



We need a < relation that is a well-quasi-ordering, such that the control flow reachability is monotonic w.r.t. < and the transition relation is also monotonic w.r.t. <.

< is oriented around two axes:

- · A configuration with more dynamic actor can do more.
- · A configuration with more messages can do more.

t

**Idea:** With the *drop*-counters some messages are removed, the rest is identical. Furthermore, a configuration with less messages is covered by one with more messages.

#### Lemma

For all realisable paths  $p_a$  in the drop-abstraction A, there is a path  $p_c$  in the corresponding concrete system C such that the configurations of  $p_c$  cover the configurations in  $p_a$ .

**Idea:** With the  $\infty$ -counters messages can be added, the rest is identical. Furthermore, a configuration were messages are added covers the original one.

#### Lemma

For all realisable paths  $p_c$  in a concrete system C, there is a path  $p_a$  in the corresponding  $\infty$ -abstraction A such that the configurations of  $p_a$  cover the configurations in  $p_c$ .

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drop-abstraction  $\leq$  concrete system  $\leq \infty$ -abstraction

We need a condition for:

We have

 $\infty$ -abstraction  $\leq drop$ -abstraction

To prove that the analysis has enough precision.



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#### Algorithm 5 Control flow reachability

return a ∈ treen

#### Star Topologies: Agreement of Abstractions

#### tree<sub>D</sub> ≈ tree<sub>l</sub> when:

for all path  $p_i$  in the coverability tree of I, there is a path  $p_d$  in the coverability tree of D such that

- both p<sub>i</sub> and p<sub>d</sub> have length k;
- $\forall i \in [0, k-1]$ ,  $i^{th}$  transition  $\varphi_i$  is the same for  $p_i$  and  $p_d$ ;
- $\forall i \in [0, k-1]$ , i<sup>th</sup> configuration  $I_i$ ,  $D_i$  are similar  $(I_i \sim D_i)$ .

#### Remark

We use  $I_i \sim D_i$  and not  $\leq$ .  $\sim$  is defined to ignore messages of dynamic actors.

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- Making the agreement condition more flexible
- (i.e. more robust w.r.t. optimisation in building the tree)
- · Proving the completeness of the algorithm
- Reachability problem for star topologies
- Other communication topologies
- Is is possible to find restrictions for parametric systems?

# Star Topologies: Soundness

#### Theorem (Soundness)

Given a system C, a bound  $n \in \mathbb{N}$ , the corresponding drop-abstraction D and  $\infty$ -abstraction I, and a control flow location q to cover. If the coverability trees of D and I agree then the answer to whether q is covered can be accurately computed from the tree of D.



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#### References I



Agha, G. (1986).

ACTORS: A Model of Concurrent Computation in Distributed Systems.
PhD thesis, MIT CSAIL.

Amadio, R. M. (2000).

Theor. Comput. Sci. 240, 147-176.

Amadio, R. M. & Meyssonnier, C. (2002).

Nord. J. Comput. 9, 70-101.

Apt. K. R. & Kozen. D. (1986).

Inf. Process. Lett. 22, 307–309

Berthomieu, B. & Vernadat, F. (2006). In OEST pp. 123–124. IEEE Computer Society.

Boudol, G., Laneve, C., Laneve, C. & Meije, P. (1992)

Technical report INRIA Report 1702, INRIA, Sophia Antipolis.

Clinger, W. (1981).

Foundations of Actor Semantics.
PhD thesis, MIT CSAIL.

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#### References II

#### Commoner, F. (1972).

Technical Report CA-7206-2311 Applied Data Research, Inc. Wakefield, Massachusetts.

In ICALP, (Ottmann, T., ed.), vol. 267, of Lecture Notes in Computer Science pp. 499-508. Springer.

Finkel, A. (1991).

In Applications and Theory of Petri Nets. (Rozenberg, G., ed.), vol. 674, of Lecture Notes in Computer Science pp. 210-243. Springer.

Finkel, A. & Schnoebelen, P. (2001). Theor. Comput. Sci. 256, 63-92.

Hewitt, C., Bishop, P. & Steiger, R. (1973).

In IJCAI pp. 235-245...

Honda, K. & Tokoro, M. (1991).

In ECOOP, (America, P., ed.), vol. 512, of Lecture Notes in Computer Science pp. 133-147, Springer.

Karp, R. M. & Miller, R. E. (1969). J. Comput. Syst. Sci. 3, 147-195. References III





Milner, R., Parrow, J. & Walker, D. (1992a). Inf. Comput. 100. 1-40.



Milner, R., Parrow, J. & Walker, D. (1992b). Inf. Comput. 100, 41-77.











