

# A Hybrid Quantum-Classical Algorithm for Robust Fitting

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## Robust fitting via consensus maximisation

Outliers exist in computer vision

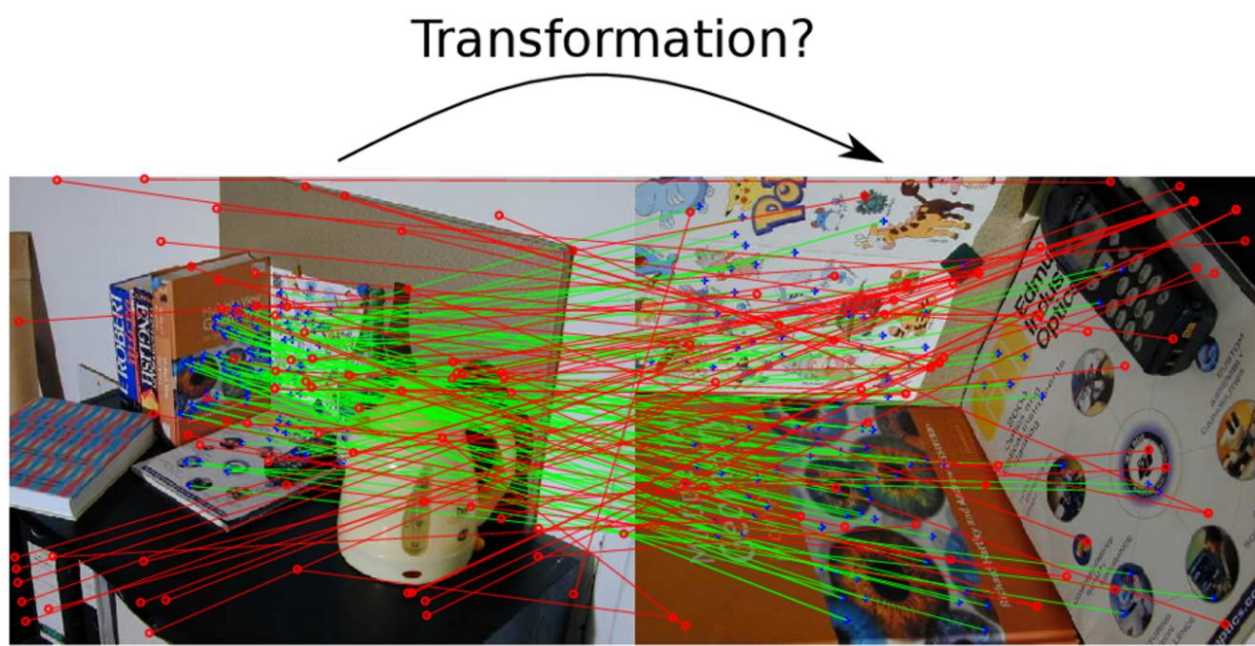


Figure 1 : Feature point matches containing outliers (red lines).

Least square is sensitive to outliers

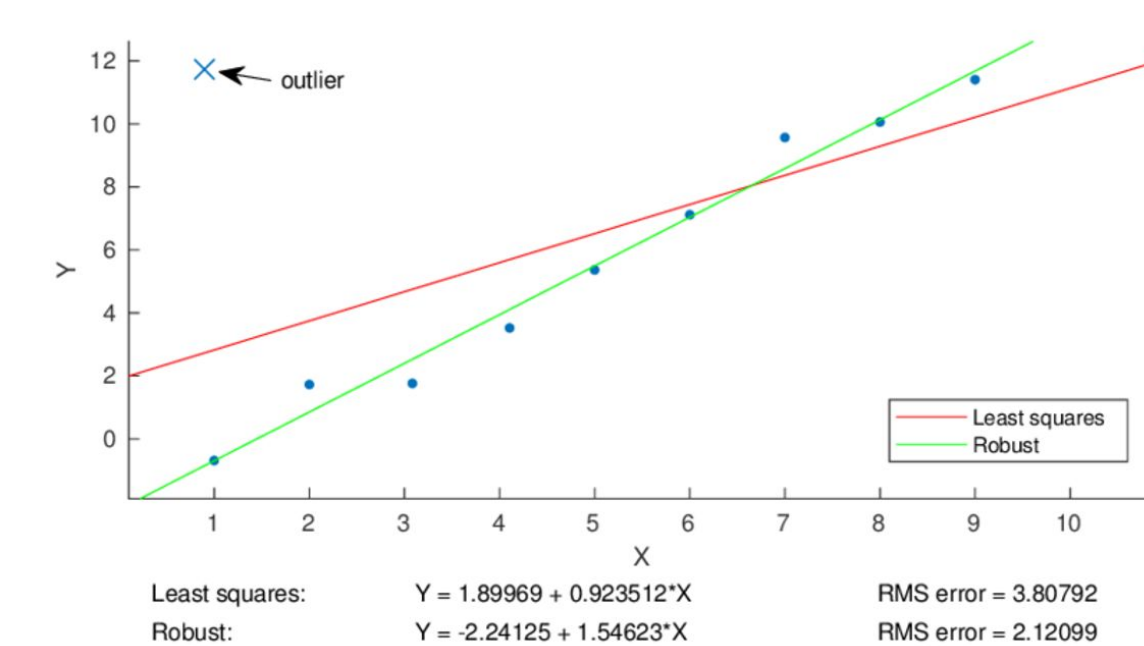
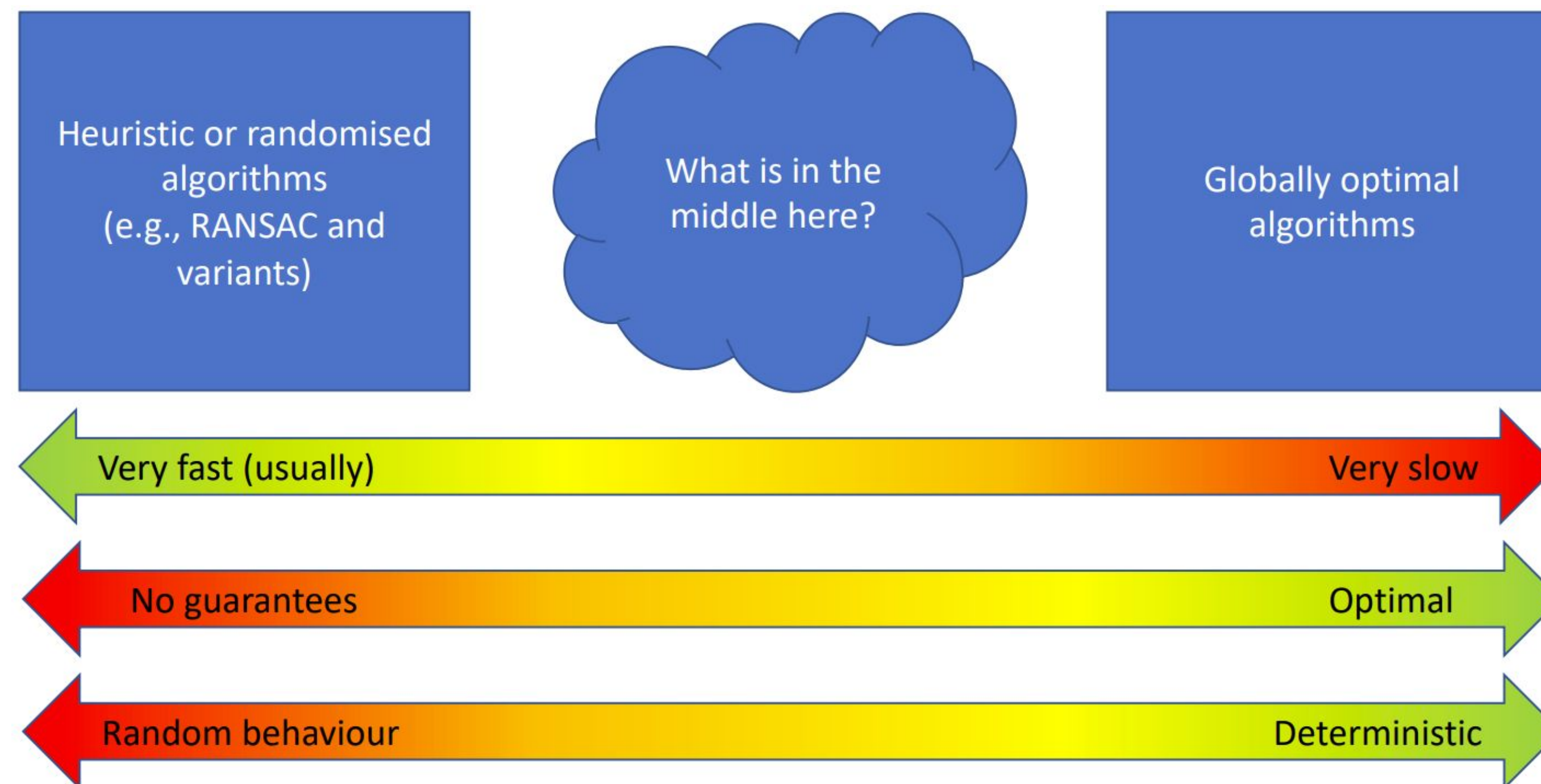


Figure 2 : Sensitivity of least squares to outliers.

**Objective:** make model fitting robust (insensitive) to outliers

## Research gap in consensus maximisation

Theoretical results on classical computers [1]

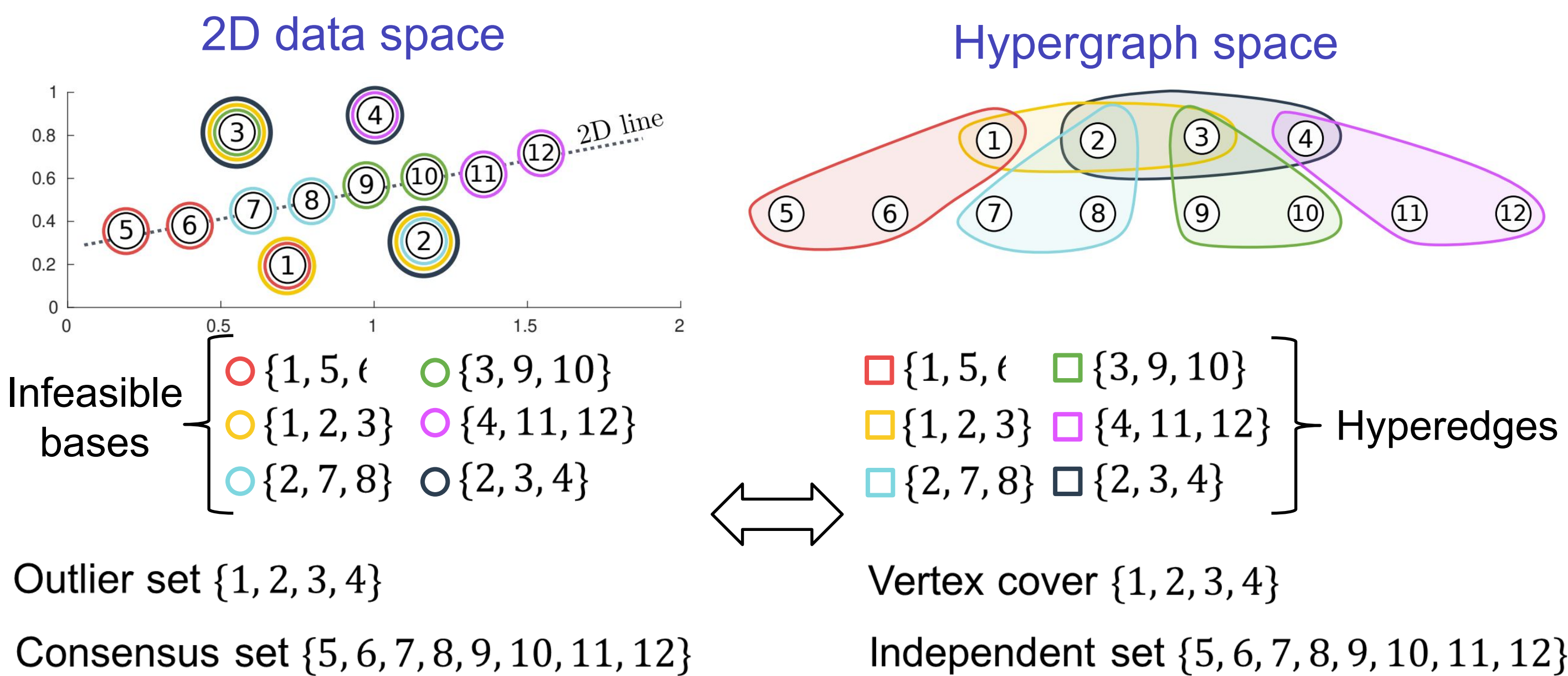


### Motivation

- Investigate a new type of computer → A hybrid quantum-classical algorithm
- Address the random behaviour → An error bound  $|J^*| - |\tilde{J}| \leq \rho$

### Contributions

## Maximise consensus as minimise vertex cover



## Hybrid quantum-classical robust fitting

Hypergraph vertex cover as 0-1 ILP

$$I(A) = \min_{z \in \{0,1\}^N} \|z\|_1 \quad s.t. \quad A^T z \geq 1_M,$$

where  $z_i = 1$  implies vertex  $i \in$  vertex cover

can be solved by quantum annealer

Hypergraph vertex cover as QUBO

$$Q_\lambda(A) = \min_{v \in \{0,1\}^{N+\delta'M}} [v^T \quad 1](J + \lambda H_A^T H_A)[v^T \quad 1]^T$$

where,  $v = [z^T \quad t_{(1)}^T \quad \dots \quad t_{(M)}^T]$

Relaxation

$$LP(A) = \min_{z \in [0,1]^N} \|z\|_1 \quad s.t. \quad A^T z \geq 1_M,$$

### Hybrid quantum-classical robust fitting

1.  $A \leftarrow$  Sample new hyperedge
2. Decay penalty  $\lambda$
3. Solve  $Q_\lambda(A)$  with *quantum annealing*
4. If  $J \leftarrow \mathcal{V}_{C_z}$  is a consensus set
5. If  $\|z\|_1 < \|z_{best}\|_1$ , then
6.  $z_{best} \leftarrow z$  and  $J_{best} \leftarrow J$
7. Repeat step 1

### Error bound

$$|J^*| - |J_{best}| \leq \|z_{best}\|_1 - LP(A)$$

Current best solution

Relaxation

## Experiments

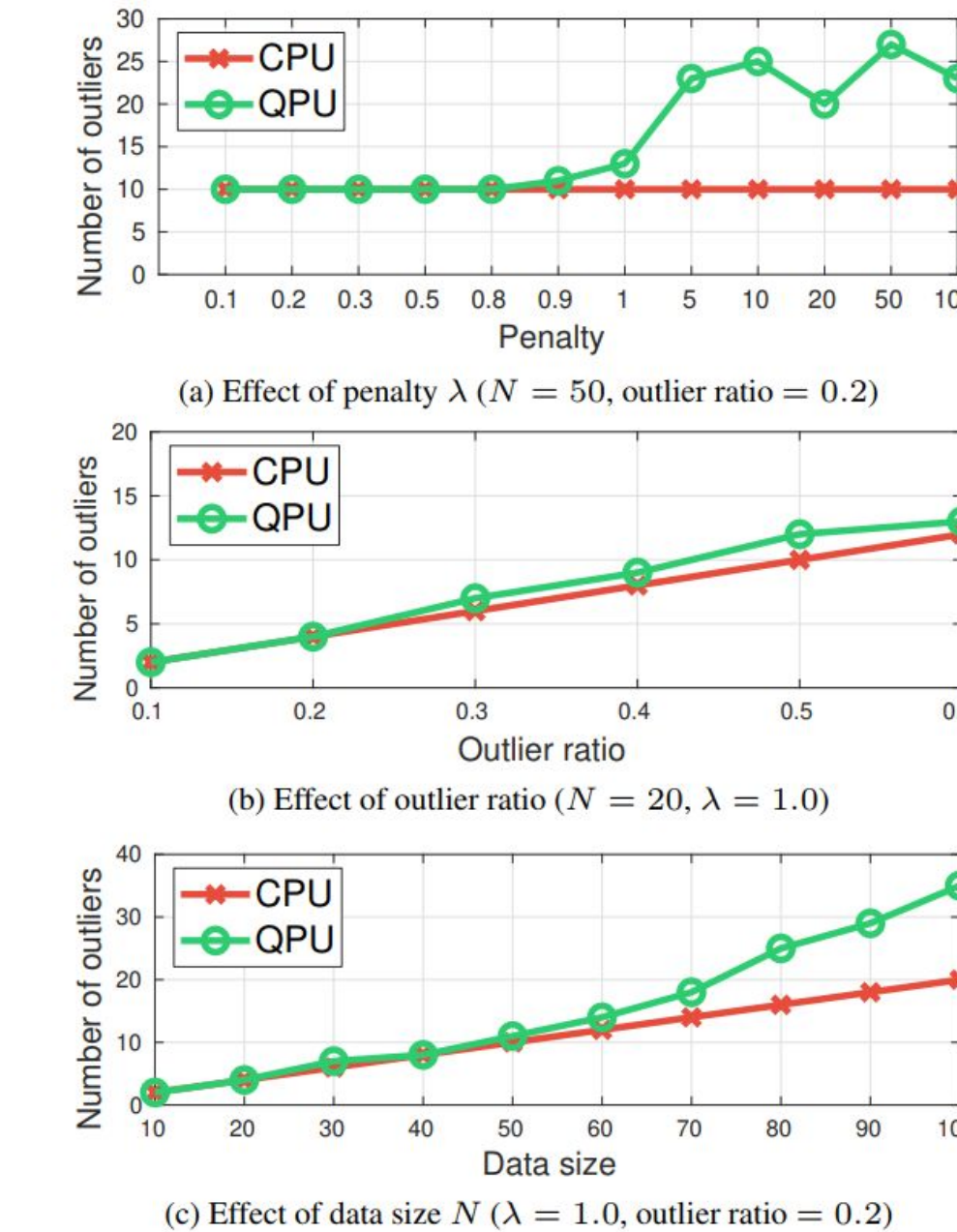


Figure 3. Comparison between CPU and QPU in solving QUBO

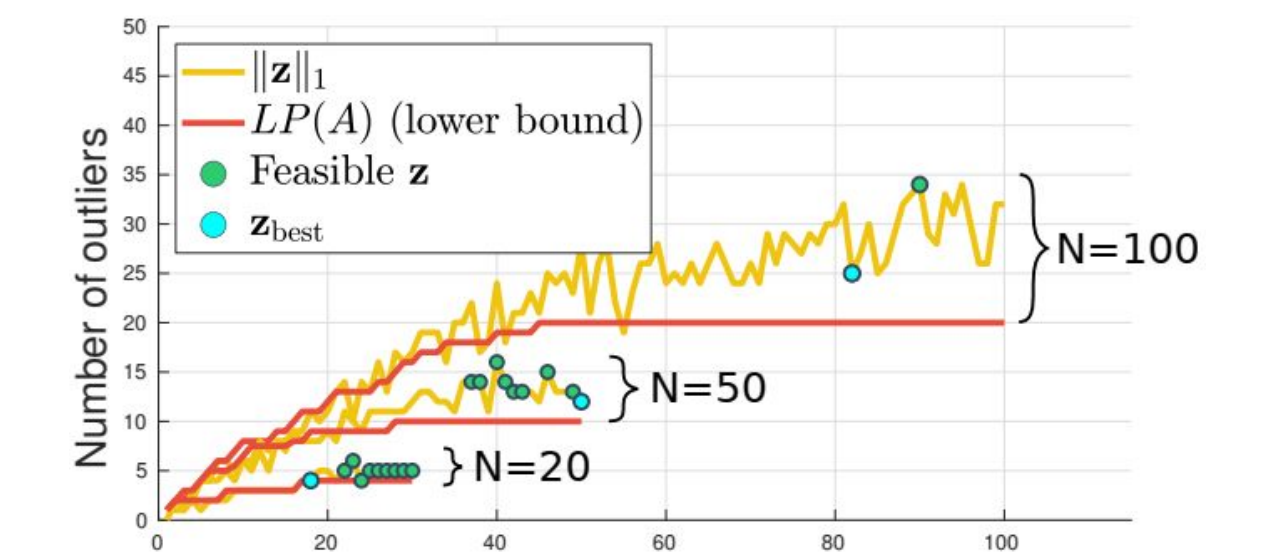


Figure 4. Number of outliers  $\|z\|_1$  optimised by QPU and lower bound  $LP(A)$ , plotted across the iterations of the proposed algorithm

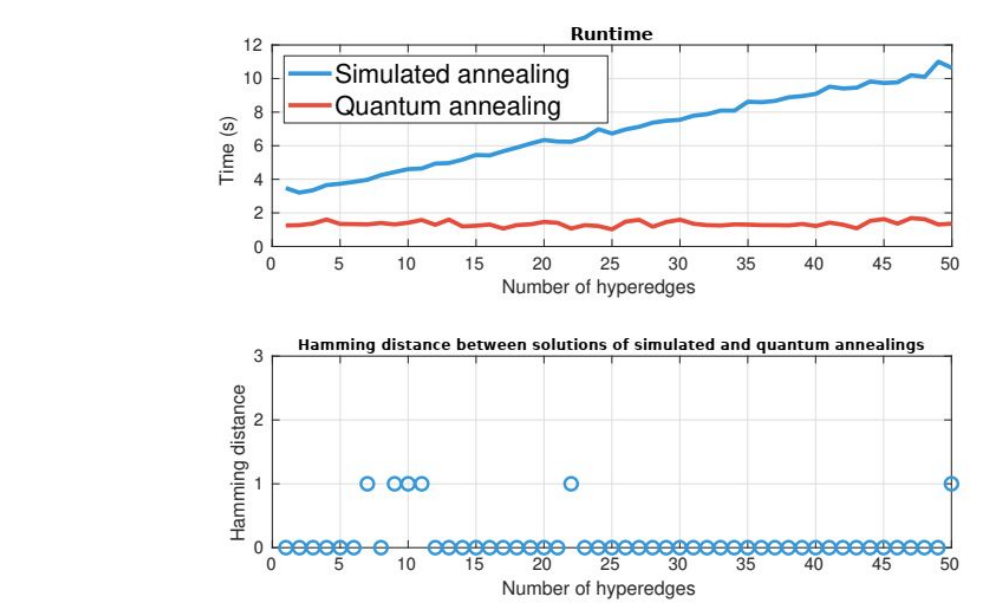


Figure 5. Comparison between quantum annealing (on D-Wave Advantage) and simulated annealing (on classical computer)

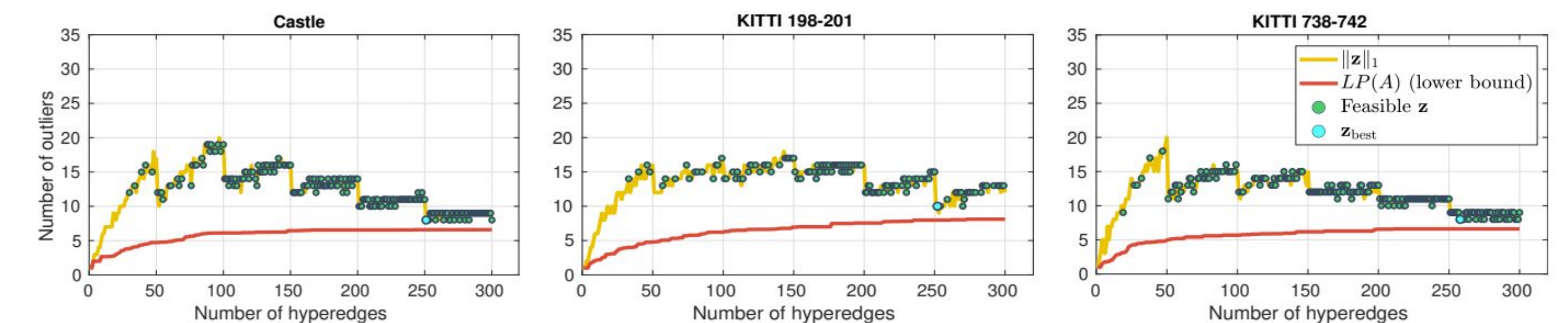


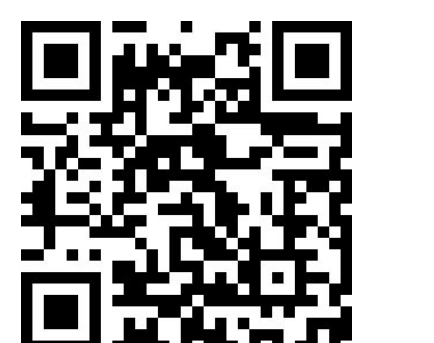
Figure 5. . Fundamental matrix estimation, where number of outliers  $\|z\|_1$  and lower bound  $LP(A)$

Method	RS [36]	LRS [21]	FLRS [47]	EP [45]	IBCO [15]	QRF [20]	Alg. 1-E	Alg. 1-F
Castle $N = 84$	$ Z $ (Error bound) Time (s)	74 (—) 0.20	74 (—) 0.11	74 (—) 0.20	70 (—) 0.25	76 (—) 0.34	72 (8.17) 18.07	76 (1.41) 1998.87
Valbonne $N = 45$	$ Z $ (Error bound) Time (s)	34 (—) 0.21	36 (—) 0.20	36 (—) 0.31	33 (—) 0.34	38 (—) 0.44	36 (6.00) 110.30	36 (4.00) 1915.82
Zoom $N = 108$	$ Z $ (Error bound) Time (s)	90 (—) 0.31	91 (—) 0.29	91 (—) 0.14	92 (—) 0.21	95 (—) 0.35	89 (—) 257.03	93 (9.91) 92.35
KITTI 104-108 $N = 337$	$ Z $ (Error bound) Time (s)	309 (—) 0.04	313 (—) 0.04	312 (—) 0.07	318 (—) 0.28	321 (—) 0.39	256 (—) 799.33	320 (9.91) 137.26
KITTI 198-201 $N = 322$	$ Z $ (Error bound) Time (s)	306 (—) 0.05	308 (—) 0.13	307 (—) 0.07	308 (—) 0.23	312 (—) 0.42	309 (—) 774.06	308 (10.00) 36.15
KITTI 738-742 $N = 501$	$ Z $ (Error bound) Time (s)	481 (—) 0.05	483 (—) 0.18	483 (—) 0.23	491 (—) 0.53	492 (—) 0.61	447 (—) 1160.12	492 (5.88) 22.46

Figure 5. Fundamental matrix estimation. Only our algorithm amongst all methods returns error bounds

## Conclusions

- A hybrid quantum-classical algorithm for consensus maximisation
- The algorithm is terminated with an error bound



Paper



Code

## References

[1] Tat-Jun Chin, Zhipeng Cai, and Frank Neumann. “Robust fitting in computer vision: Easy or hard?.” ECCV 2018.