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%% Header
% ES53 Pset 2
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%% Question 1
% 1a. Plotting Vmem, conductances, and gate probabilities at 100 uA/cm2
[t, y] = run_hh_model(8, 100, 0.1);

figure(1); hold on

% First subplot: Vmem
subplot(3,1,1);
plot(t, y(:,1));
title('Membrane Potential');
ylabel('Membrane Potential (mV)');
grid on;

% Second subplot: gNa & gK
subplot(3,1,2); hold on
gNa = y(:,2).^3 .* y(:,3) .* 120;
gK = y(:,4).^4 .* 36;
plot(t, gNa);
plot(t, gK);
title('Sodium & Potassium Conductances');
ylabel('Ionic Conductance (mS cm^2)');
legend('gNa', 'gK')
grid on;
hold off

% Third subplot: m, h, & n probabilities
subplot(3,1,3), hold on
plot(t, y(:,2));
plot(t, y(:,3));
plot(t, y(:,4));
title('m-gate, h-gate, & n-gate Open Probabilities');
xlabel('Time (ms)');
ylabel('Gate Probability');
legend('m-gate', 'h-gate', 'n-gate')
grid on;
hold off

hold off

%1b. Plotting Vmem from 0 to 100 uA/cm2

figure(2); hold on
title('Action Potentials at Amplitudes from 0 to 100 uA/cm2');
ylabel('Membrane Potential (mV)');
xlabel('Time (ms)')
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grid on;

% Loop starting at 0 uA/cm2 and ending at 100 uA/cm2
for i = 0:100
    [t1, y1] = run_hh_model(8, i, 0.1);
    % Plot membrane potential
    plot(t1, y1(:,1));
end

hold off

%1c. Plotting Peak Vmem vs. Pulse magnitude from 0 to 100 uA/cm2

figure(3); hold on
title('Maximum Membrane Voltage at Amplitudes from 0 to 100 uA/cm2 ');
ylabel('Membrane Potential (mV)');
xlabel('Stimulating Pulse Magnitude (uA/cm2)')
grid on;

for i = 0:100
    [t2, y2] = run_hh_model(8, i, 0.1);
    vMem = y2(:,1);

    % Find peaks in the membrane potential
    peaks = max(vMem);

    % Plot the peaks
    plot(i, peaks, 'ro');
end

hold off

%1d. Plotting barely-suprathreshold and above threshold action potentials

figure(4); hold on
title('Action Potentials at 16 and 100 uA/cm2 ');
ylabel('Membrane Potential (mV)');
xlabel('Time (ms)')
grid on;

% Plot action potential at 16 uA/cm2
[t3, y3] = run_hh_model(20, 16, 0.1);
plot(t3, y3(:,1));

% Plot action potential at 100 uA/cm2
[t4, y4] = run_hh_model(20, 100, 0.1);
plot(t4, y4(:,1));
legend("16 uA/cm2", "100 uA/cm2")
hold off
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%% Question 2

% tetany.m - simulates the summation of muscle twitches to reach tetany
% For ES 53, designed by L. Moyer
% Last modified 9/16/22

% Students - please add comments to show that you understand
% what is going on in each line of this code

clear all
close all

dt = 30; % time period between twitches in ms
frequency = 1/dt; % twitch frequency
numtwitches = 15; % number of twitches to initiate
x = [0:0.1:40]; % Time vector from 0 to 40 with periods of 0.1
twamp = zeros(1,2001); % Empty vector for fast twitch amplitudes
twamps = zeros(1,2001); % Empty vector for slow twitch amplitudes

% Generate time delayed twitches and sum

for i= 1:numtwitches;
y(i,:) = gampdf(x,3,1); %approximates a fast twitch response
start = round((i-1)*dt)+1; % calculate the start of the twitch based on time period
btwn twitches
twamp(i,start:(start+length(x)-1)) = y(i,:); % Place the twitch into the empty matrix
end
tetf = sum(twamp,1); % sum all twitches to represent twitch response/tetany

figure(5) % create a figure to plot twitches
subplot(211) % declare plot as 1st of 2 subplots
plot(tetf,'r') % plot the twitches in the color red
axis([0 500 0 1.1*max(max(tetf))]) % scale the axis according to the max twitch
magnitude
xlabel('Time (ms)')
ylabel('Twitch Force (a.u.)')
legend('Fast Twitch','location','southeast')

% Now you generate time delayed slow twitches and sum them.

% Write your own code (or modify below) and plot your results in subplot(212) in blue

for j= 1:numtwitches;
y2(j,:) = gampdf(x,3,2); %approximates a slow twitch response
star = round((j-1)*dt)+1;
twamps(j,star:(star+length(x)-1)) = y2(j,:);
end
tets = sum(twamps,1);

subplot(212)

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plot(tets, 'b')
axis([0 500 0 1.1*max(max(tets))])
xlabel('Time (ms)')
ylabel('Twitch Force (a.u.)')
legend('Slow Twitch', 'location', 'southeast')

%% Question 3
%3a. Force Velocity Relationship plot by Hill's Equation

% Constants
a = 20; % Newtons
b = 0.2; % m/s
T_max = 100; % Newtons

% Tension vector
T = linspace(0, T_max, 100);

% Hill's equation for velocity as a function of tension
v = b * ((T_max - T) ./ (T + a));

% Plot the force-velocity relationship
figure(6);
plot(T, v);
xlabel('Force (Tension) (N)');
ylabel('Velocity (m/s)');
title("Hill's Force-Velocity Relationship");
grid on;

%3b. Plotting the Force Velocity Relationship while varying a
figure(7); hold on

for a = 5:5:30 % 5 N to 30 N in steps of 5 N
    b = a / T_max; % vary b in accordance to v_max = 1 m/s
    v = b * ((T_max - T) ./ (T + a));
    plot(T, v);
end
xlabel('Force (Tension) (N)');
ylabel('Velocity (m/s)');
title("Hill's Force-Velocity Relationship (a = 5N to 30N)");
grid on
hold off
```