

Discrete Structures and Theory (Spring 2023)Discussion 8Date: 24/03/2023Exercise 1:

Find the values of these expressions.

- a) $1 \cdot \bar{0}$
- b) $1 + \bar{1}$
- c) $\bar{0} \cdot 0$
- d) $\overline{(1 + 0)}$

Exercise 2:

The Boolean operator \oplus , called the *XOR* operator, is defined by $1 \oplus 1 = 0$, $1 \oplus 0 = 1$, $0 \oplus 1 = 1$, and $0 \oplus 0 = 0$. Simplify these expressions.

- a) $x \oplus 0$
- b) $x \oplus 1$
- c) $x \oplus x$
- d) $x \oplus \bar{x}$

Exercise 3:What values of the Boolean variables x and y satisfy $xy = x + y$?Exercise 4:

Prove the second absorption law $x(x + y) = x$ using the other Boolean identities. Do not use the first absorption law.

Exercise 5:Use a table to express the values of the Boolean function $F(x, y, z) = x\bar{y}z + \overline{(xyz)}$ Exercise 6:

Find the sum-of-products expansions of these Boolean functions.

- a) $F(x, y) = x + y$
- b) $F(x, y) = xy$
- c) $F(x, y) = 1$
- d) $F(x, y) = y$