

2.

If n is even, then $(n + 3)^2$ is odd.

If n is even, then, by definition, there exists an integer k such that $n = 2k$.

We substitute this value of n into the expression $(n + 3)^2$ as follows:

$$(n + 3)^2 = (2k + 3)^2$$

$$= 4k^2 + 12k + 9 \text{ (expanding the term)}$$

$$= 2(2k^2 + 6k + 4) + 1 \text{ (factorizing 2 out of the terms with } k)$$

$$= 2t + 1, \text{ where } t = 2k^2 + 6k + 4$$

t is an integer because the product of integers is an integer, and the sum of integers is an integer.

An odd number, r , can be expressed in the form $2k + 1$, where k is an integer.

Therefore, $(n + 3)^2$ is an odd number.

3.

grandfather(X, Z) :-

father(X, Y), (mother(Y, Z) ; father(Y, Z)).

This rule is saying that X is the grandfather of Z if:

X is the father of some person Y and

Y is the mother or father of some Z

The , operator is used to combine two conditions, so the first condition is that X is the father of Y, and the second condition is that Y is either the mother or father of Z.

The ; operator is used to combine two possibilities: either Z is the mother of Y, or Z is the father of Y. So, the rule reads as follows: X is the grandfather of Z if there exists some person Y, who is the child of X and the parent of Z.