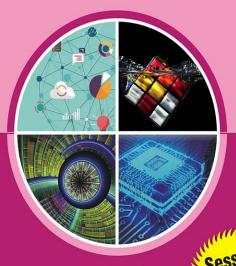


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By

Prashant Agarwal



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Array and Linked List

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PART-1

Questions-Answers Long Answer Type and Medium Answer Type Questions

Introduction: Basic Terminology, Elementary Data Organization Built in Data Types in C.

1-3 A (CS/IT-Sem-3)

Que 1.1. Define data structure. Describe about its need and types.

Why do we need a data type? AKTU 2014-15, Marks 05

Data structure:

Answer

1

- 1. A data structure is a way of organizing all data items that considers not only the elements stored but also their relationship to each other. Data structure is the representation of the logical relationship existing 2
- between individual elements of data. Data structure is define as a mathematical or logical model of particular 3. organization of data items.

It helps to understand the relationship of one element with the other.

- Data structure is needed because:
- 2 It helps in the organization of all data items within the memory.
- The data structures are divided into following categories:
- 1. Linear data structure :
- A linear data structure is a data structure whose elements form a a. sequence, and every element in the structure has a unique predecessor and unique successor.
 - Examples of linear data structure are arrays, linked lists, stacks b. and queues.
- 2. Non-linear data structure:
 - A non-linear data structure it is a data structure whose elements do not a. form a sequence. There is no unique predecessor or unique successor.
- Examples of non-linear data structures are trees and graphs.

Need of data type: The data type is needed because it determines what type of information can be stored in the field and how the data can be formatted.

Que 1.2. Discuss some basic terminology used and elementary data organization in data structures.

1-4 A (CS/IT-Sem-3)

-

- Basic terminologies used in data structure :
- 1. Data: Data are simply values or sets of values. A data item refers to a single unit of values.
- **2. Entity:** An entity is something that has certain attributes or properties which may be assigned values.
- 3. **Field:** A field is a single elementary unit of information representing an attribute of an entity.
- 4. Record : A record is the collection of field values of a given entity.
 5. File : A file is the collection of records of the entities in a given entity set.

Data organization: Each record in a file may contain many field items, but the value in a certain field may uniquely determine the record in the file. Such a field K is called a primary key, and the values $k_1, k_2,...$ in such a field are called keys or key values.

Que 1.3. Define data types. What are built in data types in C?

Explain.

ii.

Answer

- ${\bf 1.} \quad {\bf C} \ {\bf data} \ {\bf types} \ {\bf are} \ {\bf defined} \ {\bf as} \ {\bf the} \ {\bf data} \ {\bf storage} \ {\bf format} \ {\bf that} \ {\bf a} \ {\bf variable} \ {\bf can} \\ {\bf store} \ {\bf a} \ {\bf data} \ {\bf to} \ {\bf perform} \ {\bf a} \ {\bf specific} \ {\bf operation}.$
- 2. Data types are used to define a variable before to use in a program.3. There are two types of built in data types in C :
- a. **Primitive data types:** Primitive data types are classified as:
- i. Integer type: Integers are used to store whole numbers.

Size and range of integer type on 16-bit machine:

Туре	Size (bytes)	Range	Format specifier
int or signed int	2	-32,768 to 32,767	%d
unsigned int	2	0 to 65,535	%u
short int or signed short int	1	– 128 to 127	%hd
unsigned short int	1	0 to 255	%hu
long int or signed long int	4	- 2,147,483,648 to 2,147,483,647	%ld
unsigned long int	4	0 to 4,294,967,295	%lu

Floating point type: Floating types are used to store real numbers.

Size and range of floating point type on 16-bit machine:

Туре	Size (bytes)	Range	Format specifier
Float	4	3.4E – 38 to 3.4E+38	$\%\mathbf{f}$
double	8	1.7E – 308 to 1.7E+308	%lf
long double	10	3.4E – 4932 to 1.1E+4932	%lf

1-5 A (CS/IT-Sem-3)

Character type: Character types are used to store characters value.

Size and range of character type on 16-bit machine:				
Туре	Size (bytes)	Range	Format specifier	
char or signed char	1	- 128 to 127	%с	
unsigned char	1	0 to 255	%с	

- iv. Void type: Void type is usually used to specify the type of functions which returns nothing. h. Non-primitive data types:

Data Structure

- These are more sophisticated data types. These are derived from i. the primitive data types.
- The non-primitive data types emphasize on structuring of a group ii. of homogeneous (same type) or heterogeneous (different type) items. For example, arrays, lists and files.

PART-2

Questions-Answers

Algorithm, Efficiency of an Algorithm, Time and Space Complexity.

Long Answer Type and Medium Answer Type Questions

Define algorithm. Explain the criteria an algorithm must Que 1.4. satisfy. Also, give its characteristics.

Answer

- 1. An algorithm is a step-by-step finite sequence of instructions, to solve a well-defined computational problem.
- Every algorithm must satisfy the following criteria: 2.
- **Input:** There are zero or more quantities which are externally i. supplied.

Array and Linked List

1-6 A (CS/IT-Sem-3)

- iv. Finiteness: If we trace out the instructions of an algorithm then for all cases the algorithm will terminate after a finite number of
- stens. **Effectiveness:** Every instruction must be basic and essential.
- Characteristics of an algorithm:
- 1 It should be free from ambiguity.

It should be concise

3 It should be efficient

How the efficiency of an algorithm can be checked? Explain the different ways of analyzing algorithm.

Answer

2.

h.

Que 1.5.

2

- The efficiency of an algorithm can be checked by:
- Correctness of an algorithm 1
- Implementation of an algorithm 2. Simplicity of an algorithm 3
- Execution time and memory requirements of an algorithm 4
- Different ways of analyzing an algorithm: a.
 - Worst case running time: The behaviour of an algorithm with respect to the worst possible 1. case of the input instance.
 - The worst case running time of an algorithm is an upper bound on the running time for any input. Average case running time:
 - The expected behaviour when the input is randomly drawn from a 1. given distribution. 2.
 - The average case running time of an algorithm is an estimate of the running time for an "average" input.
- Best case running time: c.
 - 1 The behaviour of the algorithm when input is already in order. For example, in sorting, if elements are already sorted for a specific algorithm. The best case running time rarely occurs in practice comparatively 2.
 - with the first and second case.

Que 1.6. Define complexity and its types.

Answer

The complexity of an algorithm M is the function f(n) which gives the 1. running time and/or storage space requirement of the algorithm in terms of the size n of the input data.

of time it needs to run to completion.

Que 1.7. What do you understand by complexity of an algorithm? Compute the worst case complexity for the following C code:

The storage space required by an algorithm is simply a multiple of the

Worst case: The maximum value of f(n) for any possible input. **Average case:** The expected value of f(n) for any possible input.

Best case: The minimum possible value of f(n) for any possible

Space complexity: The space complexity of an algorithm is the amount

Time complexity: The time complexity of an algorithm is the amount

Following are various cases in complexity theory:

of memory it needs to run to completion.

main()
{
int s = 0, i, j, n;
for (j = 0; j < (3 * n); j++)
{
 for (i = 0; i < n; i++)
{
 s = s + i;
}
 printf("%d", i);
}}</pre>

Answer

Answer

Data Structure

h.

c.

data size n

input.

Types of complexity:

2

3

2.

AKTU 2014-15, Marks 05

1-7 A (CS/IT-Sem-3)

Complexity of an algorithm : Refer Q. 1.6, Page 1–6A, Unit-1. Worst case complexity : $\Omega(n) + \Omega(3n) = \Omega(n)$

Que 1.8. How do you find the complexity of an algorithm? What is the relation between the time and space complexities of an algorithm? Justify your answer with an example.

gorithm? Justify your answer with an example.

AKTU 2015-16, Marks 10

Complexity of an algorithm: Refer Q. 1.6, Page 1–6A, Unit-1.
Relation between the time and space complexities of an algorithm:

- 1. The time and space complexities of an algorithm
- 2. They are used to describe how much space/time our algorithm takes based on the input.
- 3. For example, when the algorithm has space complexity of :

objects based on the length of our input.

In contrast, the time complexity describes how much time our algorithm 4 consumes based on the length of the input. For example, when the algorithm has time complexity of: 5

of space which does not depend on the input. For every size of the input the algorithm will take the same (constant) amount of space. O(n), $O(n^2)$, $O(\log(n))$ - these indicate that we create additional

Array and Linked List

- O(1) i.e., constant then no matter how big is the input it always takes a constant time.
- O(n), $O(n^2)$, $O(\log(n))$ again it is based on the length of the input. h For example:

h.

1-8 A (CS/IT-Sem-3)

```
function(list 1) {
                                   function(list 1) {
     for (node in 1) {
                                   print("I got a list"); }
     print(node):
In this example, both take O(1) space as we do not create additional
```

objects which shows that time and space complexity might be different. PART-3

Asymptotic Notations: Big Oh. Big Theta, and Big Omega.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 1.9. What is asymptotic notation? Explain the big 'Oh'

notation.

Answer

1.

- Asymptotic notation is a shorthand way to describe running times for an algorithm.
- It is a line that stays within bounds. 2.
- These are also referred to as 'best case' and 'worst case' scenarios 3. respectively.

Big 'Oh' notation :

- Big-Oh is formal method of expressing the upper bound of an algorithm's 1. running time.
- It is the measure of the longest amount of time it could possibly take for 2. the algorithm to complete.
- More formally, for non-negative functions, f(n) and g(n), if there exists 3. an integer n_0 and a constant c > 0 such that for all integers $n > n_0$.

4

1-9 A (CS/IT-Sem-3)

- $f(n) \leq cg(n)$
- *i.e.*, the set of functions which, as n gets large, grow faster than a constant time f(n).

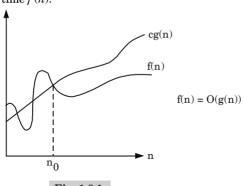


Fig. 1.9.1.

Que 1.10. What is complexity of an algorithm? Explain various notations used to express the complexity of an algorithm.

OR. What are the various asymptotic notations? Explain Big O notation.

AKTU 2017-18, Marks 07

Answer

Complexity of an algorithm: Refer Q. 1.6, Page 1-6A, Unit-1. Notations used to express the complexity of an algorithm:

θ-Notation (Same order): 1.

ล This notation bounds a function to within constant factors.

We say $f(n) = \theta g(n)$ if there exist positive constants n_0 , c_1 and c_2 b. such that to the right of n_0 the value of f(n) always lies between

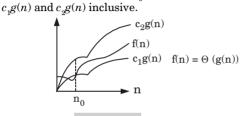
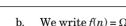


Fig. 1.10.1.

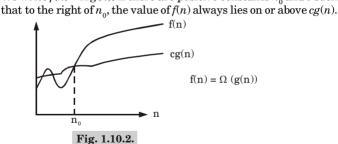
- Oh-Notation (Upper bound): Refer Q. 1.9, Page 1–8A, Unit-1. 3. Ω -Notation (Lower bound) :
 - This notation gives a lower bound for a function to within a constant factor.



1-10 A (CS/IT-Sem-3)

We write $f(n) = \Omega g(n)$ if there are positive constants n_c and c such

Array and Linked List



- Little Oh notation (o):
- 4
- It is used to denote an upper bound that is asymptotically tight because upper bound provided by O-notation is not tight. We write $o(g(n)) = \{f(n) : \text{ For any positive constant } c > 0, \text{ if a} \}$ b. constant $n_0 > 0$ such that $0 \le f(n) < cg(n) \ \forall \ n \ge n_0$
- 5. Little omega notation (\omega): It is used to denote lower bound that is asymptotically tight.
 - We write $\omega(g(n)) = \{f(n) : \text{ For any positive constant } c > 0, \text{ if a} \}$ h. constant $n_0 > 0$ such that $0 \le cg(n) < f(n)$

PART-4

Time-Space Trade-off, Abstract Data Types (ADT).

Questions-Answers Long Answer Type and Medium Answer Type Questions

Que 1.11. Explain time-space trade-off in brief with suitable example.

OR.

What do you understand by time and space trade-off? Define the various asymptotic notations. Derive the O-notation for linear AKTU 2018-19, Marks 07 search.

Time-space trade-off:

Answer

1. The time-space trade-off refers to a choice between algorithmic solutions of data processing problems that allows to decrease the running time of an algorithmic solution by increasing the space to store data and vice-versa.

with the probability p = 1/n. Then

1-11 A (CS/IT-Sem-3)

(performance efficiency) can be achieved at the cost of memory.

For Example: Suppose, in a file, if data stored is not compressed, it takes more space but access takes less time. Now if the data stored is

takes more space but access takes less time. Now if the data stored is compressed the access takes more time because it takes time to run decompression algorithm.

Various asymptotic notation: Refer Q. 1.10, Page 1–9A, Unit-1.

Various asymptotic notation: Refer Q. 1.10, Page 1–9A, Unit-1.

Derivation

2

Best case : In the best case, the desired element is present in the first position of the array, *i.e.*, only one comparison is made.

So. T(n) = O(1).

Average case: Here we assume that ITEM does appear, and that is equally likely to occur at any position in the array. Accordingly the number of comparisons can be any of the number 1, 2, 3,, n and each number occurs

$$= n \cdot (n+1)/2 \cdot (1/n)$$

$$= (n+1)/2$$

$$= O((n+1)/2) \simeq O(n)$$

 $T(n) = 1 \cdot (1/n) + 2 \cdot (1/n) + 3 \cdot (1/n) \dots + n \cdot (1/n)$

= (1 + 2 + 3 + + n) (1/n)

Worst case: Worst case occurs when ITEM is the last element in the array or is not there at all. In this situation n comparison is made

So. $T(n) = O(n+1) \approx O(n)$

Que 1.12. What do you understand by time-space trade-off?

Explain best, worst and average case analysis in this respect with

an example. AKTU 2017-18, Marks 07

Answer

Time-space trade-off: Refer Q. 1.11, Page 1–10A, Unit-1.

Best, worst and average case analysis: Suppose we are implementing an algorithm that helps us to search for a record amongst a list of records. We can have the following three cases which relate to the relative success our algorithm can achieve with respect to time:

1. Best case:

- a. The record we are trying to search is the first record of the list.
- b. If f(n) is the function which gives the running time and / or storage space requirement of the algorithm in terms of the size n of the input data, this particular case of the algorithm will produce a

complexity C(n) = 1 for our algorithm f(n) as the algorithm will run only 1 time until it finds the desired record.

Array and Linked List

2. Worst case:

- a. The record we are trying to search is the last record of the list.
- b. If f(n) is the function which gives the running time and / or storage space requirement of the algorithm in terms of the size n of the
 - input data, this particular case of the algorithm will produce a complexity C(n) = n for our algorithm f(n), as the algorithm will run n times until it finds the desired record.

3. Average case:

may run.

- a. The record we are trying to search can be any record in the list.
- b. In this case, we do not know at which position it might be.c. Hence, we take an average of all the possible times our algorithm
- d. Hence assuming for n data, we have a probability of finding any one of them is 1/n.
 e. Multiplying each of these with the number of times our algorithm might run for finding each of them and then taking a sum of all

those multiples, we can obtain the complexity C(n) for our algorithm

$$C(n) = 1 \cdot \frac{1}{2} + 2 \cdot \frac{1}{2} + \dots + n \cdot \frac{1}{2}$$
$$C(n) = (1 + 2 + \dots + n) \cdot \frac{1}{2}$$

f(n) in case of an average case as following:

$$C(n) = \frac{n(n+1)}{2} \cdot \frac{1}{n} = \frac{n+1}{2}$$

Hence in this way, we can find the complexity of an algorithm for average case as C(n) = O((n+1)/2)

Que 1.13. What do you mean by Abstract Data Type?

Answer

An Abstract Data Type (ADT) is defined as a mathematical model of the data objects that make up a data type as well as the functions that operate on these objects.

- 2. An Abstract Data Type (ADT) is the specification of the data type which specifies the logical and mathematical model of the data type.
- It does not specify how data will be organized in memory and what algorithm will be used for implementing the operations.

Description of the way in which components are related to each ล other Statements of operations that can be performed on the data type. h

An implementation chooses a data structure to represent the ADT.

The important step is the definition of ADT that involves mainly two

1-13 A (CS/IT-Sem-3)

PART-5

Array: Definition, Single and Multidimensional Array.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 1.14. Define array. How arrays can be declared?

An array can be defined as the collection of the sequential memory 1 locations, which can be referred to by a single name along with a number

Answer

h.

h.

Data Structure

narts ·

4

5

- known as the index, to access a particular field or data. 2. The general form of declaration is: type variable-name [sizel:
 - a. Type specifies the type of the elements that will be contained in the array, such as int. float or char and the size indicates the maximum of elements that can be stored inside the array. For example, when we want to store 10 integer values, then we can
- use the following declaration, int A[10]. Que 1.15. Write short note on types of an array.

Answer

There are two types of array:

- 1. One-dimensional array:
- An array that can be represented by only one-one dimension such a. as row or column and that holds finite number of same type of data items is called one-dimensional (linear) array.
 - of homogeneous data elements such as: i. The elements of the array are referenced respectively by an index set consisting of 'n' consecutive number.

One dimensional array (or linear array) is a set of 'n' finite numbers

ii

int

T-Sem-3) Array and Linked List

The elements of the array are stored respectively in successive

- 'n' number of elements is called the length or size of an array. The elements of an array 'A' may be denoted in C language as : A[0], A[1], A[2], ... A[n-1]
- A[0], A[1], A[2], ... A[n-1]2. Multidimensional arrays:

memory locations

a [50] [50] [50]:

- a. An array can be of more than one dimension. There are no restrictions to the number of dimensions that we can have.
 b. As the the dimensions increase the memory requirements increase.
 - drastically which can result in shortage of memory.

 c. Hence a multidimensional array must be used with utmost care.

 d. For example, the following declaration is used for 3-D array:

PART-6

Representation of Arrays: Row Major Order, and Column Major Order, Derivation of Index Formulae for 1-D, 2-D, 3-D and n-D Array.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 1.16. What is row major order? Explain with an example.

AKTU 2014-15, Marks 05

- In row major order, the element of an array is stored in computer memory as row-by-row.
- Under row major representation, the first row of the array occupies the first set of memory locations reserved for the array, the second row occupies the next set, and so forth.
 In row major order, elements of a two-dimensional array are ordered
 - In row major order, elements of a two-dimensional array are ordered as: $A_{11}, A_{12}, A_{13}, A_{14}, A_{15}, A_{16}, A_{21}, A_{22}, A_{23}, A_{24}, A_{25}, A_{26}, A_{31},, A_{46}, A_{51}, A_{52}, A_{54}, A_{55}, A_{55$

....., A₅₆ Example :

Let us consider the following two-dimensional array :

Γ			c	
	e	f	g	h

i j k l

1-15 A (CS/IT-Sem-3)

have a single row of elements. This is the row major representation. By application of above mentioned process, we get С.

When this step is applied to all the rows except for the first row, we

{a, b, c, d, e, f, g, h, i, i, k, l}

Que 1.17. Explain column major order with an example.

Answer

ล

h

- 1 In column major order the elements of an array is stored as column-bycolumn, it is called column major order.
- Under column major representation, the first column of the array 2
- occupies the first set of memory locations reserved for the array, the second column occupies the next set, and so forth. 3. In column major order, elements are ordered as:
 - $A_{11}, A_{21}, A_{31}, A_{41}, A_{51}, A_{12}, A_{22}, A_{32}, A_{42}, A_{52}, A_{13}, \ldots, A_{55}, A_{16}, A_{26}, \ldots, A_{56}$ **Example:** Consider the following two-dimensional array:

$$\begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \end{bmatrix}$$
 Transpose the elements of the array. Then, the representation will

- be same as that of the row major representation. Then perform the process of row-major representation. h
- By application of above mentioned process, we get c.
- $\{a, e, i, b, f, j, c, g, k, d, h, l\}.$

Que 1.18. Write a short note on address calculation for 2D array.

Determine addressing formula to find the location of (i, j)th element of a $m \times n$ matrix stored in column major order.

Derive the index formulae for 1-D and 2-D array.

Answer

a.

Let us consider a two-dimensional array A of size $m \times n$. Like linear 1. array system keeps track of the address of first element only, i.e., base address of the array (Base (A)).

Using the base address, the computer computes the address of the 2. element in the i^{th} row and j^{th} column *i.e.*, LOC (A[i][j]). Formulae:

a.

Column major order: LOC(A[i][j]) = Base(A) + w[m(j - lower bound for column index) h.

Row major order:

LOC(A[i][i]) = Base(A) + w[mi + i] in C/C++

the array.

LOC(A[i][i]) = Base(A) + w[ni + i] in C/C++where w denotes the number of words per memory location for the

Que 1.19. Explain the formulae for address calculation for 3-D array with example.

array A or the number of bytes per storage location for one element of

LOC(A[i][i]) = Base(A) + w[n(i - lower bound for column index)]+ (i - lower bound for row index)]

Answer

In three-dimensional array, address is calculated using following two methods:

Row major order:

Location (A[i, j, k]) = Base(A) + mn(k-1) + n(i-1) + (j-1)

Column major order:

Location (A[i, i, k]) = Base(A) + mn(k-1) + m(i-1) + (i-1)

For example : Given an array [1..8, 1..5, 1..7] of integers. If Base (A) = 900then address of element A[5, 3, 6], by using rows and columns methods are:

The dimensions of *A* are : M = 8, N = 5, R = 7, i = 5, i = 3, k = 6Row major order:

Location (A[i, j, k]) = Base(A) + mn(k-1) + n(i-1) + (j-1)

Location $(A[5, 3, 6]) = 900 + 8 \times 5(6 - 1) + 5(5 - 1) + (3 - 1)$

 $= 900 + 40 \times 5 + 5 \times 4 + 2$ = 900 + 200 + 20 + 2 = 1122

Column major order:

Location (A[i, j, k]) = Base(A) + mn(k-1) + m(j-1) + (i-1)Location $(A[5, 3, 6]) = 900 + 8 \times 5(6 - 1) + 8(3 - 1) + (5 - 1)$

> $= 900 + 40 \times 5 + 8 \times 2 + 4$ = 900 + 200 + 16 + 4 = 1120

Que 1.20. Consider the linear arrays AAA [5:50], BBB [-5:10] and

CCC [1:8]. Find the number of elements in each array. a.

Suppose base (AAA) = 300 and w = 4 words per memory cell for b.

AAA. Find the address of AAA [15], AAA [35] and AAA [55].

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Answer

The number of elements is equal to the length; hence use the formula:

Length = UB - LB + 1

Length (AAA) = 50 - 5 + 1 = 46

Length (BBB) = 10 - (-5) + 1 = 16

Length (CCC) = 8 - 1 + 1 = 8h. Use the formula

LOC(AAA[i]) = Base(AAA) + w(i - LB)

LOC (AAA [15]) = 300 + 4 (15 - 5) = 340LOC (AAA [35]) = 300 + 4 (35 - 5) = 420

AAA [55] is not an element of AAA, since 55 exceeds UB = 50.

 $\overline{ ext{Que 1.21.}}$ Suppose multidimensional arrays P and Q are declared

as P(-2:2,2:22) and Q(1:8,-5:5,-10:5) stored in column major order

i. Find the length of each dimension of P and Q.
ii. The number of elements in P and Q.
iii. Assuming base address (Q) = 400, W = 4, find the effective indices

Assuming base address (Q) = 400, W = 4, find the effective indices E_1, E_2, E_3 and address of the element Q[3, 3, 3].

AKTU 2018-19. Marks 07

1-17 A (CS/IT-Sem-3)

Answer

ii.

The length of a dimension is obtained by

Length = Upper Bound – Lower Bound + 1 Hence, the lengths of the dimension of P are,

$$L_1 = 2 - (-2) + 1 = 5;$$
 $L_2 = 22 - 2 + 1 = 21$

The lengths of the dimension of Q are,

$$L_1 = 8 - 1 + 1 = 8$$
; $L_2 = 5 - (-5) + 1 = 11$; $L_3 = 5 - (-10) + 1 = 16$
Number of elements in $P = 21 \times 5 = 105$ elements

Number of elements in $I = 21 \times 3 = 100$ elements

Number of elements in $Q = 8 \times 11 \times 16 = 1408$ elements

 $E_1 = 3 - 1 = 2;$ $E_2 = 3 - (-5) = 8;$ $E_3 = 3 - (-10) = 13$

The address depends on whether the programming language stores Q in row major order or column major order. Assuming Q is stored in

column major order. $E_3L_2 = 13 \times 11 = 143$

$$E_3L_2 = 13 \times 11 = 143$$

 $E_3L_2 + E_2 = 143 + 8 = 151$

 $E_3L_2 + E_2 = 143 + 8 = 151$ $(E_3L_2)L_1 = 151 * 8 = 1208$

$$(E_2L_2 + E_2)L_1 + E_1 = 1208 + 2 = 1210$$

Therefore, LOC(Q[3,3,3]) = 400 + 4(1210) = 400 + 4840 = 5240

PART-7

Application of Arrays, Sparse Matrices and their Representation.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Write a short note on application of arrays.

Answer

Que 1.22.

- Arrays are used to implement mathematical vectors and matrices, as well as other kinds of rectangular tables. Many databases, small and large, consist of one-dimensional arrays whose elements are records.
- Arrays are used to implement other data structures, such as lists, heaps, hash tables, queues and stacks.
- 3. Arrays are used to emulate in-program dynamic memory allocation, particularly memory pool allocation.
- 4. Arrays can be used to determine partial or complete control flow in programs, as a compact alternative to multiple "if" statements.5. The array may contain subroutine pointers (or relative subroutine

numbers that can be acted upon by SWITCH statements) that direct the

Que 1.23. What are sparse matrices? Explain.

path of the execution.

Answer

- Sparse matrices are the matrices in which most of the elements of the matrix have zero value.
- 2. Two general types of n-square sparse matrices, which occur in various applications, as shown in Fig. 1.23.1.
- 3. It is sometimes customary to omit block of zeros in a matrix as in Fig. 1.23.1. The first matrix, where all entries above the main diagonal are zero or, equivalently, where non-zero entries can only occur on or below the main diagonal, is called a lower triangular matrix.
- 4. The second matrix, where non-zero entries can only occur on the diagonal or on elements immediately above or below the diagonal, is called tridiagonal matrix.



1-19 A (CS/IT-Sem-3)

 $\begin{pmatrix} 4 & 3 & -5 & 1 & 0 & 6 \\ 1 & 0 & 6 & -7 & 8 & -1 & 3 \\ (a) \text{ Triangular matrix} \end{pmatrix}$

 $\begin{pmatrix}
5 & -3 & & & \\
1 & 4 & 3 & & \\
9 & -3 & 6 & & \\
2 & 4 & -7
\end{pmatrix}$ (b) Tridiagonal matrix

Fig. 1.23.1.

Que 1.24. Write a short note on representation of sparse matrices.

Answer

There are two ways of representing sparse matrices:

- 1. Array representation:
 - i. In the array representation of a sparse matrix, only the non-zero elements are stored so that storage space can be reduced.
 - ii. Each non-zero element in the sparse matrix is represented as (row, column, value).
 - iii. For this a two-dimensional array containing three columns can be used. The first column is for storing the row numbers, the second column is for storing the column numbers and the third column represents the value corresponding to the non-zero element at (row, column) in the first two columns.
 - iv. For example, consider the following sparse matrix:

 $\begin{bmatrix} 2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 4 & 3 & 0 \end{bmatrix}$

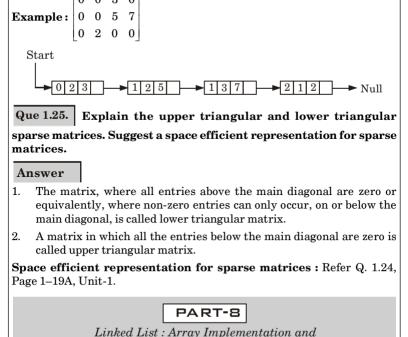
The above matrix can be represented as:

_						
	Row	Column	Value			
	0	0	2			
	1	1	1			
	2	1	4			
	2	2	3			

2. Linked representation :

- i. In the linked list representation each node has four fields. These four fields are defined as :
 - **a.** Row: Index of row, where non-zero element is located.
 - $\textbf{b.} \quad \textbf{Column:} \\ \textbf{Index of column, where non-zero element is located.}$
 - c. Value: Value of non-zero element located at index (row, column).
 - **d.** Next node: Address of next node.

Node structure: Row Column Value Address



Array and Linked List

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Pointer Implementation of Singly Linked List.

Que 1.26. Define the term linked list. Write a C program to

- implement singly linked list for the following function using array:
- i. Insert at beginning
 ii. Insert at end
 iii. Insert at end
 iv. Delete at end
- v. Delete at beginning vi. Delete after element

vii. Display in reverse order

1-20 A (CS/IT-Sem-3)

i. Linked list :

Answer

1. A linked list, or one-way list, is a linear collection of data elements, called nodes, where the linear order is given by means of pointers.

1-21 A (CS/IT-Sem-3)

Fig. 1.26.1. 2.

Data Structure

Each node is divided into two parts: the first part contains the information of the element, and the second part, called the link field or next pointer field, contains the address of the next node in the list Program:

#include<stdio h> #include<conio.h> #include<alloc.h>

struct_node { int info: struct node *link;

struct node *first:

void main() i. Insert at beginning:

void insert beginning() { struct node *ptr: ptr = (struct node*)malloc(sizeof(struct node)):

if (ptr == NULL) { printf ("overflow\n"); return:

scanf ("%d", &ptr -> info); $ptr \rightarrow link = first$: first = ptr: ii. Insert at end:

void insert end() { struct node *ptr; *cpt; if (ptr == NULL) {

return;

cot = first:

cpt = cpt -> link;

while (cpt -> link != NULL)

ptr = (struct node*)malloc(sizeof(struct node)); printf ("Link list is overflow\n"):

printf ("input new node information");

printf ("input new node information"): scanf ("%d", &ptr -> info);

```
ptr \rightarrow link = NULL:
iii. Insert after element :
    void insert given node( ) {
    struct node *ptr. *cpt:
    int data:
    ptr = (struct node*)malloc(sizeof(struct node));
    if(ptr == NULL)
```

Array and Linked List

1-22 A (CS/IT-Sem-3)

cpt -> link = ptr:

```
printf ("overflow\n"):
return:
printf ("input new node information");
scanf("%d", &ptr -> info):
```

```
printf ("input information of node after which insertion will be made");
scanf ("%d", &data):
cot = first:
while (cpt -> info != data)
cpt = cpt -> link;
```

```
ptr \rightarrow link = cpt \rightarrow link:
cpt -> link = ptr:
```

```
void delete end( ) {
struct node *ptr, *cpt;
if(first == NULL) {
```

```
iv. Delete at end:
    printf ("underflow \n"):
    return:
```

```
ptr = first:
while (ptr -> link != NULL) {
```

```
cpt = ptr;
ptr = ptr -> link;
```

```
cpt -> link = NULL;
free (ptr);
Delete at beginning:
void delete_beginning( ) {
struct node *ptr;
if (first == NULL) {
```

```
v.
     printf ("underflow \n"):
     return:
     ptr = first:
     first = ptr -> link;
     free (ptr);
```

```
void delete given info( ) {
struct node *ptr, *cpt;
int data:
if (first == NULL) {
printf("underflow\n"):
return:
ptr = first:
```

printf ("input information of node to be deleted"):

while (ptr != NULL) { cot = otr -> link: $ptr \rightarrow link = tpt$:

1-23 A (CS/IT-Sem-3)

Data Structure

Delete after element:

scanf ("%d", & data): while (ptr -> info != data) {

cpt -> link = ptr -> link;

cpt = ptr: ptr = ptr -> link:

free (ptr):

Deletion at end

Exit.

5.

v.

vi

vii. Display in reverse order: reverse list() { ptr = First:cot = NULL:

```
cpt = ptr:
                 ptr = cpt;
             } }
Que 1.27. Write algorithm of following operation for linear linked
```

list:

Traversal i. ii. Insertion at beginning iii. Search an element iv. Delete node at specified location

Answer Traversing a linked list: Let LIST be a linked list in memory. This i. algorithm traverses LIST, applying an operation PROCESS to each element of LIST. The variable PTR points to the node currently being

- processed. 1. Set PTR := START [Initializes pointer PTR]
- Repeat Steps 3 and 4 while PTR != NULL 2. Apply PROCESS to PTR -> INFO 3.
- Set PTR := PTR -> LINK (PTR now points to the next node) 4. [End of Step 2 loop]

1-2	4A((CS/IT-Sem-3)	Array and Linked List		
ii.	Ins	Insertion at beginning: Here START is a pointer variable which			
			ode. ITEM is the value to be inserted.		
	1. If (START == NULL) Then				
	2.	START = New Node	[Create a new node]		
	3.	START->INFO = ITEM	[Assign ITEM to INFO field]		
	4.	START->LINK = NULL Else	[Assign NULL to LINK field]		
	5.	Set PTR = START	[Initialize PTR with START]		
	6.	START = New Node	[Create a new node]		
	7.	START->INFO = ITEM	[Assign ITEM to INFO field]		
	8.	START->LINK = PTR	[Assign PTR to LINK field]		
	9.	[End of If] Exit			
iii.	Sea	arch an element : Here STA	ART is a pointer variable which contains		
			I is the value to be searched.		
	1.	Set $PTR = START$, $LOC =$			
	2.	Repeat While (PTR != NUI			
	3.		Then [Check if ITEM matches with INFO field]		
	4.	Print: ITEM is present at l	-		
	4. 5.	Return	ocation Loc		
	6.	Else			
	7.	PTR = PTR -> LINK	[Move PTR to next node]		
	7. 8.	LOC = LOC + 1	[Increment LOC]		
	o. 9.	[End of If]	Interement 100		
		[End of While Loop]			
		Print: ITEM is not present	in the list		
		Exit	in the list		
iv.			sition : Here START is a pointer variable		
ıv.			erst node. PTR is a pointer variable which		
	con	tains address of node to be d	leleted. PREV is a pointer variable which		
	-	nts to previous node. ITEM			
	1.	If $(START == NULL)$ Then			
	2.	Print: Linked-List is empty			
	3.	Else If $(START \rightarrow INFO =$			
		· - <u>-</u>	[Check if ITEM is in 1st node]		
	4.	PTR = START			
	5.	START = START -> LINK	[START now points to 2nd node		
	6.	Delete PTR			
	7.	Else			
	8.	PTR = START, PREV = ST			
	9.	Repeat While (PTR != NU)	LL)		

11. PREV -> LINK = PTR -> LINK [Assign LINK field of PTR to PREV]

[If ITEM matches with PTR->INFO]

10. If $(PTR \rightarrow INFO == ITEM)$ Then

12.

13. Else

Delete PTR

Dat	a Str	ructure		1-25 A (CS/IT-Sem-3)
		PREV = PTR PTR = PTR -> LINK [End of Step 10 If] [End of While Loop]		[Assign PTR to PREV] [Move PTR to next node]
		Print: ITEM deleted [End of Step 1 If]		
		Exit		
v.	add	ress of first node. PTR is a po	ointe	pointer variable which contains the er variable which contains address of er variable which points to previous
	nod	e. ITEM is the value to be d		
	1. 2.	If (START == NULL) Then Print: Linked-List is empty		[Check whether list is empty]
	3.	Else		
	4.	PTR = START, PREV = ST	'AR'	
	5.	Repeat While (PTR -> LIN		
	6.	PREV = PTR		[Assign PTR to PREV]
	7.	$PTR = PTR \rightarrow LINK$		[Move PTR to next node]
		[End of While Loop]		
	8.	ITEM = PTR -> INFO		[Assign INFO of last node to ITEM]
	9.	If (START -> LINK == NU	ILI.)	- 0
	0.			[If only one node is left]
	10	START = NULL		[Assign NULL to START]
		Else		[Assign NOLL to START]
	9.	PREV -> LINK = NULL		
	Э.		. NITI	TI to link field of accord lost model
		_	INU	LL to link field of second last node
	10	[End of Step 9 If] Delete PTR		
	11.	Print: ITEM deleted		
	10	[End of Step 1 If]		
	12.	Exit		
Qu	ie 1.2	28. Implement linear li	ıked	l list using pointer for following
un	ctio			
i.	Ins	ert at beginning	ii.	Insert at end
ii.	Ins	ert after element	iv.	Delete at end
v.	Del	ete at beginning	vi.	Delete after element
⁄ii.	Dis	play in reverse order		
Ar	iswe	er		
		<stdio.h></stdio.h>		
		<conio.h></conio.h>		
		<pre><pre><pre><pre><pre><pre><pre><pre></pre></pre></pre></pre></pre></pre></pre></pre>		
		struct simplelink {		
	lata;			
stru	ict si	mplelink *next;		

```
} node:
i.
    Function to insert at beginning:
    node *insert_begin(node *p)
    node *temp:
    temp = (node *)malloc(sizeof(node));
    printf("\nEnter the inserted data:"):
    scanf("%d".&temp->data):
    temp->next = p:
    p = temp:
    return(p):
ii.
    Function to insert at end .
    node *insert end(node *p){
    node *temp, *a:
    \alpha = p:
    temp=(node*)malloc(sizeof(node));
    printf("\nEnter the inserted data:"):
    scanf("%d",&temp->data):
    while(p->next!=NULL)
    p = p - \text{next}:
```

printf("\nEnter the data(after which you want to enter data):");

Array and Linked List

1-26 A (CS/IT-Sem-3)

p->next = temp:

node temp, *a:

scanf("%d",&x); while(p->data != x) { p = p->next;

return(a):

int x; q = p;

temp->next = (node *)NULL:

iii. Function to insert after element:
 node *insert after(node *p) {

temp = (node *)malloc(sizeof(node));
printf("\nEnter the inserted data:");

scanf("%d",&temp->data);
temp->next = p->next;
p->next = temp;
return (q);

iv. Function to delete last node :
 node *del end(node *p) {

```
Data Structure
                                                   1-27 A (CS/IT-Sem-3)
    node * a. *r:
    r = p:
    q = p;
    if(p->next == NULL)
    r = (node *)NULL:
    واجو
    while(p->next := NULL)
    q = p;
    p = p - next;
    q > next = (node *)NULL:
    free(p):
    return(r):
    Function to delete first node:
v.
    node *delete begin(node *p) {
    node *a;
    q = p;
    q = p - next;
    free(q);
    return(p);
vi. Function to delete node after element:
    node "delete after(node, *p)
    node *temp, *q;
    int x;
    printf("\nEnter the data(after which you want to delete):");
    scanf("%d" .&x):
    while(p->data != x) {
    p = p - next;
    temp = p-next;
    p->next = temp->next;
    free(temp);
    return (q);
vii. Function to reverse the list:
    node *reverse(node *p) {
    node *q, *r;
```

	q = (node *)NULL;					
	while(p!= NULL) {					
	r = q;					
	q = p; p = p - next;					
	p-next=r;					
	}					
	return(q);					
	}					
Qı	e 1.29. What are the advantages and disadvantages of single					
lin	ed list?					
Aı	swer					
Ad	antages:					
1.	Linked lists are dynamic data structures as it can grow or shrink during the execution of a program. $ \\$					
2.	The size is not fixed.					
3.	Data can store non-continuous memory blocks.					
4.	Insertion and deletion of nodes are easier and efficient. Unlike array a linked list provides flexibility in inserting a node at any specified position and a node can be deleted from any position in the linked list.					
5.	Many more complex applications can be easily carried out with linked lists.					
Dis	dvantages :					
1.	More memory: In the linked list, there is a special field called link field which holds address of the next node, so linked list requires extra space.					
2.	Accessing to arbitrary data item is complicated and time consuming task.					
Qı	Que 1.30. Write an algorithm that reverses order of all the					
ele	elements in a singly linked list.					
Aı	swer					
1.	To reverse a linear linked list, three pointer fields are used.					
2.	_					
	Algorithm:					
1.	PTR = FIRST					

Array and Linked List

1-28 A (CS/IT-Sem-3)

TPT = NULL

REV = PREV

Repeat step 4 while PTR != NULL

3.

4.

Data Structure 1–29 A (CS/IT-Sem-				
5. PREV = PTR 6. PTR = PTR -> LINK 7. PREV -> LINK = REV [End of while loop] 8. START = PREV 9. Exit Que 1.31. Write difference between array and linked list. AKTU 2014-15, Marks 05				
Answe	er			
S. No.	Array	Linked list		
1.	An array is a list of finite number of elements of same data type <i>i.e.</i> , integer, real or string etc.	A linked list is a linear collection of data elements called nodes which are connected by links.		
2.	Elements can be accessed randomly.	Elements cannot be accessed randomly. It can be accessed only sequentially.		
3.	Array is classified as: a. 1-D array b. 2-D array c. n-D array	A linked list can be linear, doubly or circular linked list.		
4.	Each array element is independent and does not have a connection with previous element or with its location.	Location or address of element is stored in the link part of previous element or node.		
5.	Array elements cannot be added, deleted once it is declared.	The nodes in the linked list can be added and deleted from the list.		
6.	In array, elements can be modified easily by identifying the index value.	In linked list, modifying the node is a complex process.		
7.	7. Pointer cannot be used in Pointers are used in linked list. array.			
	PART-9 Time-Space Trade Off, Abstract Data Types (ADT).			

1-30 A (CS/IT-Sem-3)

Array and Linked List

Long Answer Type and Medium Answer Type Questions

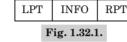
Questions-Answers

Que 1.32. Explain doubly linked list.

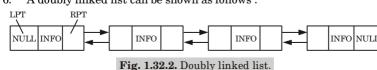
any arbitrary node within the list.

Answer 1

- The doubly or two-way linked list uses double set of pointers, one pointing to the next node and the other pointing to the preceding node. 2. In doubly linked list, all nodes are linked together by multiple links which help in accessing both the successor and predecessor node for
- 3. Every node in the doubly linked list has three fields:



- LPT will point to the node in the left side (or previous node) i.e., LPT will hold the address of the previous node. RPT will point to the node in the right side (or next node) i.e.. RPT will hold the address of the next node.
- INFO field store the information of the node 5 A doubly linked list can be shown as follows: 6.



7. The structure defined for doubly linked list is: struct node

```
int info:
struct node *rpt;
struct node *lpt:
node:
```

Que 1.33. What are doubly linked lists? Write C program to create

doubly linked list.

AKTU 2015-16, Marks 10

Answer **Doubly linked list:** Refer Q. 1.32, Page 1–30A, Unit-1.

Program:

include<stdio.h>

4

```
Data Structure
                                                        1-31 A (CS/IT-Sem-3)
     # include<conio h>
     #include<alloc h>
     struct node
          int info:
          struct node *lpt;
          struct node *rpt;
     struct node *first :
     void main()
     create():
     getch():
     void create ( )
     struct node *ptr. *cpt :
     char ch:
     ptr = (struct node *) malloc (size of (struct node));
     printf ("Input first node information"):
    scanf ("%d", & ptr \rightarrow info);
     ptr \rightarrow lpt = NULL:
     first = ptr:
     dо
    cpt = (struct node *) malloc (size of (struct node));
     printf("Input next node information");
     scanf ("%d", & cpt \rightarrow info):
     ptr \rightarrow rpt = cpt;
     cpt \rightarrow lpt = ptr;
    ptr = cpt;
     printf ("Press <Y/N> for more node");
     ch = getch():
     while (ch == 'Y'):
    ptr \rightarrow rpt = NULL;
Que 1.34. Implement doubly linked list using pointer for following
functions:
```

i.

ii.

v.

Insert at beginning Insert at end

iii. Searching an element iv. Delete at beginning

Delete at end vi. Delete entire list

```
1-32 A (CS/IT-Sem-3)
                                                   Array and Linked List
Answer
#include<stdio h>
#include<conio h>
typedef struct n{
int data:
struct n *prev:
struct n *next:
}node:
node *head = NULL, *tail = NULL;
    Function to insert at beginning:
    void insert beg(node*h, int d) {
    node *temp:
    temp = (node *)malloc(sizeof(node)):
    temp->data = d:
    temp->prev = NULL:
    if(head == NULL)
    temp->next = NULL:
    head = tail = temp;
    return:
    temp->next = h:
    h->prev = temp:
    h = h - prev;
    head = h:
ii.
    Function to insert at end:
    void insert end(node *t, int d) {
    node *temp:
    temp = (node*)malloc(sizeof(node));
    temp->data = d:
    temp->next = NULL;
    if(head == NULL) {
    temp->prev = NULL:
    head = tail = temp;
    return:
    temp->prev = t;
    t->next = temp:
    t = t->next;
    tail = t;
iii. Function to search an element:
    node *find(node *h, int aft) {
    while(h->next != head && h->data != aft)
```

```
Data Structure
                                                    1-33 A (CS/IT-Sem-3)
    h = h > next
    if(h->next == head && h->data != aft)
    return (node*) NULL:
    else
    return h:
iv. Function to delete at beginning:
    void delete beg(node *h, node *t) {
    if(head == (node*)NULL) {
    printf("\nList is empty."):
    getch():
    return:
    if(head == tail) {
    free(h):
    head = tail = (node *)NULL:
    return:
    if(h>next == t)
    tail->prev = NULL:
    head = tail:
    else {
    head = head->next:
    head->prev = NULL:
    free(h);
    Function to delete at end:
v.
    void delete end(node *h, node *t) {
    if(head == (node *)NULL) {
    printf("\nList is empty.");
    getch():
    return;
    if(head == tail) {
    free(h):
    head = tail = (node*)NULL:
    return;
    if(t->prev == h) {
    head > next = NULL;
    tail = head:
    else {
    tail = tail->prev:
```

tail->next = NULL;

```
1-34 A (CS/IT-Sem-3)
                                                    Array and Linked List
    free(t):
    void display(node *h) {
    while(h != NULL) {
    printf(n"/%d", h->data):
    h = h > next:
vi. Function to delete entire list:
    void free_list(node *list) {
    node *t:
    while(list != NULL) {
    t = list:
    list = list->next:
    free(t):
Que 1.35. Write algorithm of following operation for doubly linked
list:
i.
    Traversal
ii.
    Insertion at beginning
iii. Delete node at specific location
iv. Deletion from end.
                                   OR.
Write an algorithm or C code to insert a node in doubly link list in
beginning.
                                             AKTU 2014-15, Marks 05
Answer
    Traversing of two-way linked list:
i.
    Forward Traversing:
я.
    1.
         PTR \leftarrow FIRST.
    2
         Repeat step 3 to 4 while PTR != NULL.
    3
        Process INFO (PTR).
        PTR \leftarrow RPT (PTR).
    4.
    5.
         STOP.
h.
    Backward Traversing:
         PTR \leftarrow FIRST.
    1.
    2.
        Repeat step (3) while RPT (PTR) != NULL.
        PTR \leftarrow RPT(PTR)
    3.
    4.
        Repeat step (5) to (6) while PTR != NULL.
    5.
        Process INFO (PTR).
    6.
        PTR \leftarrow LPT (PTR).
    7.
        STOP.
```

7 $SET HEAD \rightarrow PREV = NEW NODE$ SET HEAD = NEW NODE 8.

IF PTR - NIII.I. then Write OVERFLOW

9 EXIT iii. Delete node at specific location:

IF HEAD = NULL then Write UNDERFLOW 1 Go to Step 9

IEND OF IFI SET TEMP = HEAD 2.

Repeat Step 4 while TEMP -> DATA != ITEM 3. SET TEMP = TEMP -> NEXT 4

IEND OF LOOPI 5. SET PTR = TEMP -> NEXT

SET TEMP -> NEXT = PTR -> NEXT 6 SET PTR -> NEXT -> PREV = TEMP 7.

FREE PTR

Deletion from end:

IF HEAD = NULL

Write UNDERFLOW Go to Step 7

IEND OF IFI SET TEMP = HEAD

Repeat Step 4 WHILE TEMP -> NEXT!= NULL SET TEMP = TEMP -> NEXT

IEND OF LOOP! 5. SET TEMP -> PREV -> NEXT = NULL

FREE TEMP 6. 7. EXIT

Data Structure

1

8.

9

2. 3.

4

iv. 1 EXIT

Insertion at beginning:

Go to Step 9 IEND OF IFI

ii.

Write a program in C to delete a specific element in Que 1.36.

single linked list. Double linked list takes more space than single linked list for sorting one extra address. Under what condition, could a double linked list more beneficial than single linked list.

AKTU 2018-19, Marks 07

1-35 A (CS/IT-Sem-3)

Answer

Program to delete a specific element from a single linked list: #include <stdio.h>

// the given node

```
#include <stdlib h>
// A linked list node
struct Node
int data:
struct Node *next:
/* Given a reference (pointer to pointer) to the head of a list
and an int, inserts a new node on the front of the list. */
void push(struct Node** head ref. int new data)
struct Node* new node = (struct Node*) malloc(sizeof(struct Node));
new node->data = new data:
new node->next = (*head ref):
(*head ref) = new node:
/* Given a reference (pointer to pointer) to the head of a list
and a position, deletes the node at the given position */
void deleteNode(struct Node **head_ref. int position)
// If linked list is empty
if (*head ref == NULL)
return:
// Store head node
struct Node* temp = *head ref:
// If head needs to be removed
if(position == 0)
*head ref = temp->next; // Change head
free(temp): // free old head
return:
// Find previous node of the node to be deleted
for (int i = 0; temp!= NULL && i < position - 1; i++)
temp = temp -> next:
// If position is more than number of nodes
if (temp == NULL || temp->next == NULL)
return:
// Node temp->next is the node to be deleted
// Store pointer to the next of node to be deleted
struct Node *next = temp->next->next:
// Unlink the node from linked list
free(temp->next): // Free memory
temp->next = next; // Unlink the deleted node from list
// This function prints contents of linked list starting from
```

Da	ta Structure 1–37 A (CS/IT-Sem-3)
	void printList(struct Node *node)
	{
	while (node != NULL)
	printf("%d", node->data);
	node = node->next;
	}
	} /* Decree 4 to 4 to 4 to 5 co 5
	/* Program to test above functions*/ int main()
	int main()
	/* Start with the empty list */
	struct Node* head = NULL;
	push(&head, 7);
	push(&head, 1);
	push(&head, 3);
	push(&head, 2);
	push(&head, 8);
	puts("Created Linked List: ");
	printList(head);
	deleteNode(&head, 4);
	<pre>puts("\nLinked List after Deletion at position 4: ");</pre>
	printList(head);
	return 0;
ĺ	}
l	uble linked list is more beneficial than single linked list because :
1.	A double linked list can be traversed in both forward and backward
	direction.
2.	The delete operation in double linked list is more efficient if pointer to
	the node to be deleted is given.
3.	In double linked list, we can quickly insert a new node before a given node.
4.	In double linked list, we can get the previous node using previous pointer
	but in singly liked list we traverse the list to get the previous node.

PART-10 Circular Linked List.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 1.37. What is meant by circular linked list? Write the

functions to perform the following operations in a doubly linked list

Insertion after a specified node. Delete the node at a given position.

Creation of list of nodes.

d. Sort the list according to descending order Display from the beginning to end.

AKTU 2016-17, Marks 15

Answer

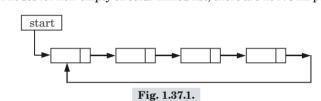
a.

h.

c.

Δ.

Circular linked list: A circular list is a linear linked list, except that the last element points to the first element. Fig. 1.37.1 shows a circular linked list with 4 nodes for non-empty circular linked list, there are no NULL pointers.



Functions:

To create a list: Refer Q. 1.33, Page 1-30A, Unit-1. я.

```
To insert after a specific node:
h.
    void insert given node()
```

struct node *ptr, *cpt, *tpt, *rpt, *lpt;

ptr = (struct node *) malloc (size of (struct node)): if (ptr == NULL)

printf ("OVERFLOW"); return: printf ("input new node information");

scanf("%d", & ptr -> info);printf ("input node information after which insertion");

scanf ("%d", & m); cpt = first;

while (cpt -> info != m)

cpt = cpt -> rpt;tpt = cpt -> rpt;

 $cpt \rightarrow rpt = ptr;$

```
Data Structure
                                                     1-39 A (CS/IT-Sem-3)
    ptr \rightarrow lpt = cpt:
    ptr \rightarrow rpt = tpt:
    tnt \rightarrow lpt = ptr;
    printf ("Insertion is done\n"):
    To delete the node at a given position:
c.
    void deleteNode(int data) {
    struct dllNode *nPtr. *tmp = head:
    if (head == NULL) {
    printf("Data unavailable \n"):
    return:
    } else if (tmp->data == data) {
    nPtr = tmp->next:
    tmp->next = NULL:
    free(tmp):
    head = nPtr:
    totNodes--:
    } else {
    while (tmp->next != NULL && tmp->data != data) {
    nPtr = tmp:
    tmp = tmp - next:
    if(tmp->next == NULL \&\& tmp->data != data) {
    printf("Given data unavailable in list\n"):
    return:
    } else if (tmp->next != NULL && tmp->data == data) {
    nPtr->next = tmp->next;
    tmp->next->previous = tmp->previous:
    tmp->next = NULL;
    tmp->previous = NULL;
    free(tmp);
    printf("Data deleted successfully\n");
    totNodes --:
    } else if (tmp->next == NULL && tmp->data == data) {
    nPtr->next = NULL:
    tmp->next = tmp->previous = NULL;
    free(tmp);
    printf("Data deleted successfully\n");
```

To sort the list according to descending order:

totNodes--:

int i. i. tmp:

void insertionSort() {

nPtr1 = nPtr2 = head;

struct dllNode *nPtr1. *nPtr2:

d.

```
for (i = 0; i < totNodes; i++)
tmn = nPtr1->data:
for (i = 0; i < i; i++)
nPtr2 = nPtr2 - > next:
for (i = i: i > 0 \&\& nPtr2 -> previous -> data < tmp; i--) {
```

Array and Linked List

```
nPtr2->data = nPtr2->previous->data;
nPtr2 = nPtr2->previous:
nPtr2->data = tmp:
nPtr2 - head
nPtr1 = nPtr1 - > next
```

To display from the beginning to end: e.

void display() if(head == NULL)printf("\nList is Empty!!!"); else struct Node *temp = head; printf("\nList elements are: \n"):

1-40 A (CS/IT-Sem-3)

 $printf(\text{"%d} \leq \text{===> ".temp -> data})$: printf("%d ---> NULL", temp -> data);

printf("NULL <--- "): while(temp -> next != NULL)

Que 1.38. Write a C program to implement circular linked list for following functions: i.

Searching of an element Insertion at specified position ii. iii. Deletion at the end

```
iv. Delete entire list
```

Answer #include<stdio.h>

#include<conio.h> typedef struct n{

int data: struct n *next:

}node: node *head = NULL;

```
Data Structure
                                                    1-41 A (CS/IT-Sem-3)
void insert cir end node *h, int d) {
node *temp:
temp = (node*)malloc(sizeof(node)):
temp->data = d:
if(head == NULL) {
head = temp:
temp->next = head:
return:
while(h->next != head)
h = h > next
temp->next = h->next:
h->next = temp:
i.
    Function to search an element:
    node *find(node *h. int aft) {
    while(h->next != head && h->data != aft)
    h = h - next:
    if(h-next == head & h-next == aft)
    return (node*)NULL:
    else
    return h:
ii.
    Function to insert node at specified position:
    void insert cirsp pos(node *h. int pos. int d)
    node *temp, *loc;
    int p = 0:
    while(h->next != head && p < pos - 1)
         loc = h;
         p++;
         h = h - next;
    if(pos > pos + 1 \&\& h->next == head) || pos < 0)
    printf("\nPosition does not exists.");
    getch();
    if((p + 2) == pos) {
    loc = h:
    temp = (node*)malloc(sizeof(node));
    temp->data = d;
    temp->next = loc->next;
```

if(pos == 1) { h = head;

```
1-42 A (CS/IT-Sem-3)
                                                    Array and Linked List
         while(h->next != head)
         h = h > next
         h->next = temp:
         head = temp:
    واجو
         loc->next = temp:
    void display (node *h) {
    while (h->next != head) {
    printf("%d", h->data):
    h = h > next:
    printf("%d", h->data):
iii. Function to delete at the end:
    void delete cir end(node *h) {
    node *temp:
    if(head == NULL) {
    printf("\nList is empty");
    getch():
    if(h->next == head) {
    printf("\nNode deleted. List is empty");
    getch():
    head = NULL:
```

free(h);
return;

temp = h;h = h->next;

free(h);

node *t:

t = list;
list = list->next;

while(h->next != head) {

temp->next = h->next;

while(list != NULL) {

iv. Function to delete entire list:
 void free list(node *list) {

Data Structure	1-43 A (CS/IT-Sem-3)		
Que 1.39. Write an algorithm to inse	rt a node at the end in a		
circular linked list.	AKTU 2017-18, Marks 07		
Answer			
1. If PTR = NULL 2. Write OVERFLOW			
3. Go to Step 1			
[END OF IF] 4. SET NEW_NODE = PTR			
5. SET PTR = PTR -> NEXT			
6. SET NEW_NODE -> DATA = VAL 7. SET NEW_NODE -> NEXT = HEAD			
8. SET TEMP = HEAD			
9. Repeat Step 10 while TEMP -> NEXT !=	HEAD		
10. SET TEMP = TEMP -> NEXT END OF LOOP			
11. SET TEMP -> NEXT = NEW_NODE			
12. EXIT			
PART-11			
Operation on a Linked List, Insertic	on, Deletion, Traversal		
Polynomial Representation and Add			
Multiplications of Single Variable and '	Iwo variable Polynomiai.		
O			
Questions-Answe	ers		
Long Answer Type and Medium An	swer Type Questions		
Que 1.40. Write an algorithm to implement insertion, deletion			
and traversal on a singly linked list.			
Answer			
Refer Q. 1.27, Page 1–23A, Unit-1.			
Que 1.41. Write a C program to impl	ement insertion, deletion		
operation on a doubly linked list.			
Answer			
Refer Q. 1.34, Page 1–31A, Unit-1.			

void htraverse ()

#include<stdio.h>
#include<conio.h>
#include<alloc.h>
struct_node

struct node * ptr:

ptr = first:

printf ("Backward traversing :\n")

printf ("% $d \$ ", ptr -> info);

Que 1.43. Write a program in C to implement insertion, deletion

while (ptr → rpt != NULL)

ptr = ptr → rpt;

while (ptr != NULL)

ptr = ptr -> lpt;

and traversal in circular linked list.

struct node *link;

int info:

struct node *first;

```
Data Structure
```

void create(), traverse(), insert beg(), insert end().

1-45 A (CS/IT-Sem-3)

```
delete beg(), delete end():
     clrscr():
     create():
     traverse():
     insert beg():
     traverse():
    insert end():
     traverse():
     delete beg():
     traverse():
    getch():
void create()
     struct node *ptr. *cpt:
    char ch:
     ptr = (struct node *) malloc (size of (struct node));
     printf("input first node") :
    scanf("%d" & ptr -> info);
     first = ptr:
     3 ob
     cpt = (struct node *) malloc (size of (struct node)):
     printf("Input next node"):
     scanf ("%d" & cpt -> info):
     ptr \rightarrow link = cpt;
     ptr = cpt:
     print f ("Press < Y/N > for more node"):
     ch = getch();
while (ch == "Y"):
ptr \rightarrow link = first :
void traverse ()
     struct node *ptr;
    printf("Traversing of link list; \n");
     ptr = first;
    while = (ptr != first)
     printf ("%d \n", ptr -> info):
     ptr = ptr -> link;
void insert_beg ( )
```

```
ptr = (struct node*) malloc (sizeof (struct node)):
if (ptr == NULL)
    printf ("overflow\n"):
    return :
printf ("Input New Node"):
scanf ("%d", &ptr -> info);
cpt = first :
```

Array and Linked List

1-46 A (CS/IT-Sem-3)

struct node *ptr:

```
while (cpt -> link != first)
     cpt = cpt -> link:
ptr \rightarrow Link = first:
first = ptr:
cpt -> link = first :
void insert end()
```

```
struct node *ptr: *cpt:
ptr = (struct node*) malloc (sizeof (struct node)):
if (ptr == NULL)
printf("overflow\n"):
return:
printf ("Input New Node information");
scanf ("%d", &ptr -> info);
```

cpt = first: while (cpt -> link != first); cpt = cpt -> link; $cpt \rightarrow link = ptr;$

 $ptr \rightarrow link = first :$ void delete_beg() struct node *ptr, *cpt; if (first == NULL) printf ("underflow\n"); return: cpt = first;

while (cpt -> link != First) cpt = cpt -> link; first = ptr -> link;cpt -> link = first;

Fig. 1.44.1.

Fig. 1.44.2.

The link coming out of the last node is NULL pointer.

For example : Let us consider the polynomial of degree 4 i.e., $3x^4 + 8x^2 + 6x + 8$ can be written as 3 * power(x, 4) + 8 * power(x, 2) + 6 * power

In case of polynomial of 3 variables *i.e.*, x, y, z can also be represented as

Explain the method to represent the polynomial

1-47 A (CS/IT-Sem-3)

Data Structure

free (ptr):

void delete end()

return:

ptr -> link = first; free (cpt);

equation using linked list.

(x, 1) + 8 * power (x, 0)

It can be represented as linked list as

linked list as shown in Fig. 1.44.3.

cot = first:

ptr = cpt; cpt = cpt -> link:

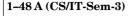
Que 1.44.

3.

struct node *ptr, *cpt; if (first -- NIII.I.)

while (cpt -> link != first)

printf ("underflow\n"):



Array and Linked List

power x | power y | power z | coeff | next

Fig. 1.44.3.

For example : Let us consider the following polynomial of 3 variable $3x^2 + 2xy^2 + 5y^3 + 7yz$.

We can replace each term of the polynomial with node of the linked list as

2 - 0 3 0 5 - 0 1 1 7 NULL

Fig. 1.44.4.

Que 1.45. Explain the method to represent the polynomial equation using linked list. Write and explain method to add two polynomial equations using linked list.

Answer

Representation of polynomial: Refer Q. 1.44, Page 1–47A, Unit-1.

Addition of two polynomials using linked lists:

- Let p and q be the two polynomials represented by the linked list.
- 1. While p and q are not null, repeat step 2.
- 2. If powers of the two terms are equal then,

in powers of the two terms are equal then,

if the terms do not cancel then insert the sum of the terms into the sum

Polynomial

(resultant)

Update p

 $\operatorname{Update} q$

Else if the (power of the first polynomial) > (power of second polynomial)

Then insert the term from first polynomial into sum polynomial

Then insert the term from first polynomial into sum polynomial Update p

Else insert the term from second polynomial into sum polynomial Update a

3. Copy the remaining terms from the non-empty polynomial into the sum polynomial.

Example : Let us consider the addition of two polynomials of single variable $5x^4 + 6x^3 + 2x^2 + 10x + 4$ and $7x^3 + 3x^2 + x + 7$. We can visualize this as follows :

$$5x^{4} + 6x^{3} + 2x^{2} + 10x + 4$$
$$+7x^{3} + 3x^{2} + x + 7$$
$$5x^{4} + 13x^{3} + 5x^{2} + 11x + 11$$

 $\it i.e.$, to add two polynomials, compare their corresponding terms starting from the first node and move towards the end node.

Que 1.46. Write and explain method to multiply polynomial equation using linked list.

Answer

c

- The multiplication of polynomials is performed by multiplying coefficient and adding the respective power.
- To produce the multiplication of two polynomials following steps are performed:a. Check whether two given polynomials are non-empty. If anyone
 - polynomial is empty then polynomial multiplication is not possible. So exit.
 - b. Second polynomial is scanned from left to right.

 $3x^2 + x + 2$ and perform multiplication as

scanned from left to right and its each term is multiplied by the term of the second polynomial, *i.e.*, find the coefficient by multiplying the coefficients and find the exponent by adding the exponents.

d. If the product term already exists in the resulting polynomial then

For each term of the second polynomial, the first polynomial is

its coefficients are added, otherwise a new node is inserted to represent this product term.

For example: Let us consider two polynomial $8x^4 + 6x^2 + 5x + 2$ and

$$\begin{array}{r}
8x^{4} + 6x^{2} + 5x + 2 \\
 \times 3x^{2} + x + 2
\end{array}$$

$$24x^{6} + 18x^{4} + 15x^{3} + 6x^{2} \\
+ 8x^{5} + 6x^{3} + 5x^{2} + 2x \\
 + 16x^{4} + 12x^{2} + 10x + 4$$

$$24x^{6} + 8x^{5} + 34x^{4} + 21x^{3} + 23x^{2} + 12x + 4$$

VERY IMPORTANT QUESTIONS

Following questions are very important. These questions may be asked in your SESSIONALS as well as UNIVERSITY EXAMINATION.

Q. 1. Define data structure. Describe about its need and types. Why do we need a data type?

Ans. Refer Q. 1.1.

· ahoo main()

s = s + i:

Ans. Refer Q. 1.7.

Ans. Refer Q. 1.8.

order

Ans. Refer Q. 1.21.

Ans. Refer Q. 1.31.

notation. Ans. Refer Q. 1.10.

int s = 0, i, j, n;

printf("%d", i):

for (i = 0; i < n; i++)

for (i = 0; i < (3 * n); i++)

Q. 5. What do you understand by time and space trade-off? Define the various asymptotic notations. Derive the O-notation for linear search. Ans. Refer Q. 1.11. Q. 6. What do you understand by time-space trade-off? Explain best, worst and average case analysis in this respect with an example. Ans. Refer Q. 1.12.

i. Find the length of each dimension of P and Q.

Q. 8. Write difference between array and linked list.

ii. The number of elements in P and Q.

Q.3. How do you find the complexity of an algorithm? What is the relation between the time and space complexities of an

Q. 4. What are the various asymptotic notations? Explain Big Q

Q. 7. Suppose multidimensional arrays P and Q are declared as P(-2:2,2:22) and Q(1:8,-5:5,-10:5) stored in column major

iii. Assuming base address (Q) = 400, W = 4, find the effective indices E_1, E_2, E_3 and address of the element Q[3, 3, 3].

algorithm? Justify your answer with an example.

- Q.9. What are doubly linked lists? Write C program to create doubly linked list. Ans. Refer Q. 1.33.
- Q. 10. Write an algorithm or C code to insert a node in doubly link list in beginning. Ans Refer Q. 1.35.
- Q.11. Write a program in C to delete a specific element in single linked list. Double linked list takes more space than single linked list for sorting one extra address. Under what condition, could a double linked list more beneficial than single linked list. Ans Refer Q. 1.36.
- Q. 12. What is meant by circular linked list? Write the functions to perform the following operations in a doubly linked list. a. Creation of list of nodes.
 - Insertion after a specified node.
 - c. Delete the node at a given position.
 - d. Sort the list according to descending order
 - e. Display from the beginning to end.
 - Ans. Refer Q. 1.37.
- Q. 13. Write an algorithm to insert a node at the end in a circular linked list.

Ans. Refer Q. 1.39.





Stacks and Queues

CONTENTS

Part-1	:	Stacks: Abstract Data Type 2-2A to 2-3A Primitive Stack Operations: Push and Pop
Part-2	:	Arrays and Linked 2–3A to 2–9A Implementation of Stack in C
Part-3	:	Application of Stack :
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Part-6	:	Circular Queues, Array 2-27A to 2-34A and Linked Implementation of Queue in C

Part-7: Dequeue and Priority Queue 2-34A to 2-36A

PART-1

Stacks: Abstract Data Type, Primitive Stack Operations: Push and Pop.

Questions-Answers

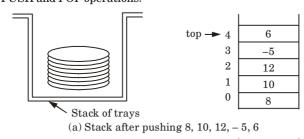
Long Answer Type and Medium Answer Type Questions

Que 2.1. What do you mean by stack? Explain all its operation with suitable example.

Answer

from the top only.

- 1. A stack is one of the most commonly used data structure.
- 2. A stack, also called Last In First Out (LIFO) system, is a linear list in which insertion and deletion can take place only at one end, called top.
- 3. This structure operates in much the same way as stack of trays.4. If we want to remove a tray from stack of trays it can only be removed
- 5. The insertion and deletion operation in stack terminology are known as PUSH and POP operations.



	l 1
4 0	10
top → 2	12
1	10
0	8
(b) S	tack after no

(b) Stack after poping	
elements $6, -5$	

 $\begin{array}{c|cccc}
4 & 11 \\
3 & 7 \\
2 & 12 \\
1 & 10 \\
0 & 8 \\
\end{array}$

9

top -> 5

(c) Stack after pushing elements 7, 11, 9

Fig. 2.1.1.

2-3 A (CS/IT-Som-3)

2 READ DATA $TOP \leftarrow TOP + 1$

3 4

5.

4.

STOP

STOP

Data Structure

STACK [TOP] ← DATA

POP operation: In pop operation, we remove an element from stack. After

every pop operation top of stack is decremented by 1.

Algorithm: POP (STACK, TOP, ITEM)

1. If TOP < 0 then write "STACK UNDERFLOW and STOP"

2. STACK [TOP] ← NULL

 $TOP \leftarrow TOP - 1$ 3.

PART-2

Arrays and Linked Implementation of Stack in C.

Stacks and Queues

Long Answer Type and Medium Answer Type Questions

Questions-Answers

Que 2.4. Write a C function for array implementation of stack.

Write all primitive operations. AKTU 2015-16, Marks 10

```
Answer
#include<stdio.h>
#include<conio h>
#define MAX 50
    int stack [MAX + 1], top = 0;
    void main()
```

```
clrscr();
void create( ), traverse( ), push( ), pop( );
create():
printf("\n stack is:\n");
traverse():
```

push(): printf("After Push the element in the stack is:\n"): traverse(): :()gog

```
printf("After Pop the element in the stack is :\n");
    traverse():
    getch();
void create()
```

```
char ch:
    do
    top ++;
    printf("Input Element");
    scanf("%d", stack[top]);
    printf("Press<Y>for more element\n");
    ch = getch();
while (ch == 'Y')
```

void traverse()

```
Data Structure
                                                    2-5 A (CS/IT-Sem-3)
         int i
         for(i = top; i > 0; --i)
         printf("%d\n", stack[i]);
    void push()
         int m:
         if(top == MAX)
         printf("Stack is overflow"):
         return:
         printf("Input new element to insert"):
         scanf("%d", &m):
         top++:
         stack[top] = m:
    void pop()
         if(top == 0)
         printf("Stack is underflow \n"):
         return:
         stack[top] = '\0':
         top --:
Que 2.5.
             Write a C function for linked list implementation of
stack. Write all the primitive operations.
                                             AKTU 2015-16, Marks 10
Answer
#include<stdio.h>
#include<conio.h>
#include<alloc.h>
    struct node
    int info;
    struct node *link;
    };
         struct node *top;
         void main()
         void create(), traverse(), push(), pop();
         create();
```

if(ptr == NULL)

2-6 A (CS/IT-Sem-3)

```
printf("\n stack is:\n"):
     traverse().
     pop():
     printf("After push the element in the stack is : \n"):
     traverse():
     pop():
     printf("After pop the element in the stack is: \n")
     traverse():
     getch():
     void create()
     struct node *ptr. *cpt:
     char ch:
     ptr = (struct node *) malloc (sizeof (struct node)):
     printf("Input first info"):
     scanf("%d", &ptr -> info):
    ptr \rightarrow link = NULL:
οĥ
    cpt = (struct node *) malloc (sizeof (struct node));
     printf("Input next information");
     scanf("%d", &cpt -> info):
     cot \rightarrow link = otr:
     ptr = cpt:
     printf("Press < Y/N > for more information"):
     ch = getch();
     while (ch == 'Y')
     top = ptr;
void traverse()
     struct node *ptr;
     printf("Traversing of stack: \n");
     ptr = top:
     while (ptr != NULL)
     printf ("%d \n", ptr -> info);
     ptr = ptr -> link;
void push()
     struct node *ptr:
     ptr = (struct node *) malloc (sizeof (struct node));
```

Stacks and Queues

```
Data Structure
                                                    2-7 A (CS/IT-Sem-3)
         printf("Overflow\n");
         return:
         printf("Input New node information"):
         scanf("%d", &ptr -> info);
         ptr -> link = top:
         top = ptr:
    ()qoq biov
         struct node *ptr:
         if(top == NULL)
         printf("Underflow \n"):
         return:
         ptr = top;
         top = ptr -> link;
         free (ptr);
Que 2.6.
            What is stack? Implement stack with singly linked list.
                                             AKTU 2014-15, Marks 05
Answer
Stack: Refer Q. 2.1, Page, 2-2A Unit-2.
Implementation using singly linked list:
typedef struct stack
    int *data:
    struct stack *next;
    }stack:
void push(stack **top, int *data)
    stack *newn;
    newn = (stack *)malloc(sizeof(stack));
    newn->data = data:
    newn->next = (stack *)NULL;
    if(*top == NULL)
    *top = newn;
    return;
    newn->next = (*top);
    *top = newn;
```

```
2-8 A (CS/IT-Sem-3)
                                                      Stacks and Queues
    int *pop(stack **top)
    int *rval = (int *)NULL:
    stack *tmp:
    if(*top!= NULL)
         tmp = *top:
         *top = (*top)->next:
         rval = tmp->data:
         free(tmp):
    }
         return(rval):
            Write a function in C language to reverse a string using
Que 2.7.
stack
                                             AKTU 2014-15, Marks 05
                                   OR
What is a stack? Write a C program to reverse a string using stack.
                                             AKTU 2017-18, Marks 07
Answer
Stack: Refer Q. 2.1, Page 2-2A, Unit-2.
#include<stdio.h>
#include<conio h>
#include<string.h>
#define MAX 20
    int top = -1;
    char stack [MAX]:
    char pop();
    push(char);
    main()
         clrscr():
         char str [20];
         int i:
         printf("Enter the string:");
         gets(str);
         for(i = 0; i < strlen(str); i++)
         push (str [i]);
         for(i = 0; i < strlen(str); i++)
         str[i] = pop();
         printf("Reversed string is :");
```

```
stack[++top] = item:
    char pop()
        if(top == -1)
        printf("Stack underflow \n"):
        return stack [top - -];
                             PART-3
        Application of Stack: Prefix and Postfix Expression
                  Evaluation of Postfix Expression.
                        Questions-Answers
     Long Answer Type and Medium Answer Type Questions
Que 2.8.
            Write a short note on the application of stack.
Answer
Applications of stack are as follows:
1.
    Expression evaluation: Stack is used to evaluate prefix, postfix and
```

Expression conversion : An expression can be represented in prefix, postfix or infix notation. Stack can be used to convert one form of

Syntax parsing: Many compilers use a stack for parsing the syntax of expressions, program blocks etc. before translating into low level code.

Parenthesis checking: Stack is used to check the proper opening and

2-9 A (CS/IT-Sem-3)

Data Structure

puts (str);
getch();

push (char item)

واجو

infix expressions.

expression to another.

closing of parenthesis.

2.

3.

4.

if(top == MAX - 1)
printf("Stack overflow\n"):

of STACK) which has the same precedence as or higher precedence

Repeatedly pop from STACK and add to *P* each operator (on the top

Convert following infix expression into postfix

AKTU 2014-15, Marks 05

of STACK) until a left parenthesis is encountered. Remove the left parenthesis [Do not add it to *P*]

String reversal: Stack is used to reverse a string. We push the characters of string one by one into stack and then pop character from

Function call: Stack is used to keep information about the active

Write down the algorithm to convert infix notation into

Stacks and Queues

2-10 A (CS/IT-Sem-3)

functions or subroutines

than ⊗

[End if]

[End if]

[End of step 2]

expression A + (B * C + D)/E.

 $Add \otimes to STACK$.

If a right parenthesis is encountered, then:

b.

ล

b.

End. Que 2.10.

6

7.

stack

Que 2.9.

postfix.

5.

ß

((
A	(A
+	(+	A
((+(A
В	(+(AB
*	(+(*	AB
C	(+(*	ABC
+	(+(+	ABC*
D	(+(+	ABC*D
)	(+	ABC*D+
/	(+/	ABC*D+
E	(+/	ABC*D+E
)	(ABC*D+E/+
	15005	

Resultant postfix expression : ABC * D + E/+

Que 2.11. | Consider the following infix expression and convert

into reverse polish notation using stack. $A + (B * C - (D/E ^ F) * H)$

AKTU 2018-19, Marks 07

Answer A + (B*C - C)

Data Structure

r			
- ($D/E \wedge F)*H$		
	Character	Stack	Postfix
	A	(A
	+	(+	A
	((+(A
	В	(+(AB
	*	(+(*	AB
	\mathbf{C}	(+(*	ABC
	_	(+ (- (ABC*
	((+(-(ABC*
	D	(+ (- (ABC*D
	/	(+(-(/	ABC*D
	${f E}$	(+ (- (/	ABC*DE
	^	(+ (- (/^	ABC*DE
	\mathbf{F}	(+ (- (/^	ABC*DEF
)	(+ (- (/^	ABC*DEF
	*	(+ (- *	ABC*DEF ^/
	H	(+ (- *	ABC*DEF ^/ H

Resultant reverse polish expression : ABC * DEF ^ / H

2-11 A (CS/IT-Sem-3)

2-12 A (CS/IT-Sem-3)

expression.

c.

Answer

5

Stacks and Queues

Write down the algorithm to convert postfix to infix.

Answer

This algorithm finds the value of an arithmetic expression P written in postfix notation 1 Add a right parenthesis ")" to P.

[This acts as a sentinel] 2. Scan P from left to right and repeat step 3 and 4 for each element of Puntil the sentinel ")" is encountered.

3. If an operand is encountered, put it on STACK.

4. If an operator \otimes is encountered then: Remove the top two elements of STACK, where A is the top element and B is the next-to-top element. h. Evaluate $B \otimes A$.

[End of if structure] [End of step 2 loop] Set value equal to top element on STACK.

Place the result of (b) back on STACK.

6. End.

Que 2.13. | Consider the following arithmetic expression written

in infix notation: E = (A + B) * C + D / (B + A * C) + D

 $\mathbf{E} = \mathbf{A}/\mathbf{B} \wedge \mathbf{C} + \mathbf{D} * \mathbf{E} - \mathbf{A} * \mathbf{C}$

Convert the above expression into postfix and prefix notation.

E = (A + B) * C + D / (B + A * C) + D

Postfix: $E = (A + B) * C + D / (B + T_1) + D$ $T_1 = AC *$ $= (A + B) * C + D / T_0 + D$ $T_2 = BT_1 +$ $= T_3 * C + D / T_2 + D$ = $T_3 * C + T_4 + D$ $T_3 = AB +$ $T_4 = DT_9/$ $= T_5 + T_4 + D$ $T_5 = T_3 C *$

 $= T_6 + D$ $T_6 = T_5 T_4 +$ $T_7 = T_6 D +$ $= T_7$ On putting the values of T's

= AB + C * DBAC * + / + D +

 $= T_6D +$ $= T_5 T_4 + D +$ $= T_3 C * DT_2 / + D +$ $= AB + C * DBT_1 + / + D +$

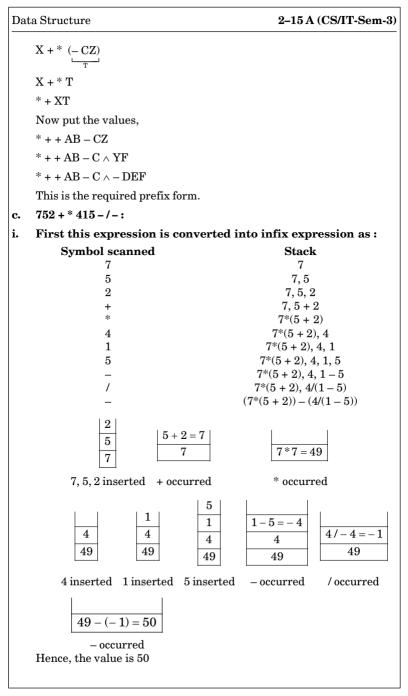
Data Structure	2-13 A (CS/IT-Sem-3)
Prefix: $E = (A + B) * C + D / (B + A * C) +$	D
$= (A + B) * C + D / (B + T_1) + D$	$T_1 = *AC$
$= (A + B) * C + D / T_2 + D$	$T_2 = + BT_1$
$= T_3 * C + D / T_2 + D$	$T_3 = + AB$
$= T_3 * C + T_4 + D$	$T_4 = /DT_2$
$= T_5 + T_4 + D$	$T_5 = *T_3C$
$= T_6 + D$	$T_6^5 = + T_5^T T_4$
$= T_7$	$T_7 = + T_6D$
On putting the values of T's	7 6
$E = + T_6 D$	
$= + + T_5 T_4 D$	
$= + + *T_3C / DT_2D$	
$= + + * + ABC / D + B T_1D$	
= + + * + ABC / D + B * ACD	
b. $E = A/B \wedge C + D * E - A * C$	
Postfix: $E = A / T_1 + D * E - A * C$	$T_1 = BC^{\wedge}$
$= T_2 + D * E - A * C$	$T_2 = AT_1/$
$= T_2 + T_3 - A * C$	$T_3 = DE^*$
$= T_2 + T_3 - T_4$	$T_4 = AC *$
$= T_5 - T_4$	$T_5 = T_2 T_3 +$
= T ₆	$T_6 = T_5 T_4 -$
On putting the values of T's	0 0 1
$= T_5 T_4 -$	
$= T_2 T_3 + AC *$	
$= AT_1/DE * + AC *$	
= ABC \(\triangle \text{/DE * + AC *}	
Prefix: $E = A/B \wedge C + D * E - A * C$	
$= A / T_1 + D * E - A * C$	$T_1 = \wedge BC$
$= T_2 + D * E - A * C$	$T_2 = /AT_1$
$= T_2 + T_3 - A * C$	$T_3 = *DE$
$= T_2 + T_3 - T_4$	$T_4 = *AC$
$= T_5 - T_4$	$T_5 = + T_2 T_3$
= T ₆	$T_6 = -T_5 T_4$
On putting the values of T's	
$=-T_5T_4$	
$= - + T_2 T_3 * AC$	

This is the required postfix form. $(A + B) + *C - (D - E) \wedge F$

 $(\underbrace{+ \ AB}_x) + * \ C - (D - E) \wedge F$

 $X + *C - (D - E) \wedge F$ $X + *C - (\underline{DE}) \wedge F$ $X + *C - (Y \wedge F)$ $X + *C - (Y \wedge F)$ $X + *C - (\underline{Y} \wedge F)$ X + *(C - Z)

h.



Stacks and Queues

PART-4 Iteration and Recursion, Principles of Recursion, Tail Recursion.

Removal of Recursion Problem Solving Using Iteration and Recursion with Examples such as Binary Search, Fibonacci Number and Hanoi Towers. Trade off between Iteration and Recursion.

Questions-Answers Long Answer Type and Medium Answer Type Questions

Que 2.15. What is iteration? Explain.

Answer

1

6.

7

Answer

to run indefinitely.

- Iteration is the repetition of a process in order to generate a (possibly unbounded) sequence of outcomes.
- 2 The sequence will approach some end point or end value.
- 3 Each repetition of the process is a single iteration, and the result of each iteration is then the starting point of the next iteration. Iteration allows us to simplify our algorithm by stating that we will 4
- repeat certain steps until told. 5 This makes designing algorithms quicker and simpler because they do not have to include lots of unnecessary steps.

Iteration is used in computer programs to repeat a set of instructions. Count controlled iteration will repeat a set of instructions upto a specific

number of times, while condition controlled iteration will repeat the instructions until a specific condition is met.

Que 2.16. What is recursion? Explain.

- 1. Recursion is a process of expressing a function that calls itself to perform specific operation.
- Indirect recursion occurs when one function calls another function that 2. then calls the first function.
- 3. Suppose *P* is a procedure containing either a call statement to itself or
- a call statement to a second procedure that may eventually result in a call statement back to the original procedure P. Then *P* is called recursive procedure. So the program will not continue 4.

sum of digits of the given number. Also, calculate the time AKTU 2016-17, Marks 10 complexity.

Answer Recursion: Refer Q. 2.16, Page 2–16A, Unit-2.

```
Program:
    #include<stdio h>
    #include<conio.h>
    int sum(int n)
         if(n < 10)
         return(n):
         else
         return(n \% 10 + sum (n / 10)):
    main()
    int s.n:
    printf("\nEnter any number:");
    scanf("%d",&n);
    s = sum(n):
```

printf(" \n Sum of digits = %d", s);

getch(); return 0: length of the digit of the input number n.

So, we can conclude that time taken by program is linear in terms of the

T(n) = O(length of digit of (n)) where n is the number whose sum of

Stacks and Queues

2-18 A (CS/IT-Sem-3)

So, time complexity is,

 $\{ if (x \le 0) \}$ return x:

individual digit is to be found.

ii

iii

Que 2.18. Explain all types of recursion with example.

Answer

Answer
Types of recursion:

a. Direct recursion: A function is directly recursive if it contains an

Direct recursion: A function is directly recursive if it contains at explicit call to itself.
 For example: int foo (int x)

{ if (x <= 0) return x; return foo (x - 1); }

b. Indirect recursion: A function is indirectly recursive if it contains a call to another function.
 For example:
 int foo (int x)

return bar (x);
}
int bar (int y)
{ return foo (y-1);

tail recursion:
Tail recursion (or tail-end recursion) is a special case of recursion in which the last operation of the function, the tail call is a recursive call. Such recursions can be easily transformed to iterations.

call. Such recursions can be easily transformed to iterations.
Replacing recursion with iteration, manually or automatically, can drastically decrease the amount of stack space used and improve efficiency.

efficiency.

3. Converting a call to a branch or jump in such a case is called a tail continuous and continuous actions.

 Converting a call to a branch or jump in such a case is called a tal call optimization.
 For example:

For example :Consider this recursive definition of the factorial function in C : factorial (n)

This definition is tail recursive since the recursive call to factorial is not the last thing in the function (its result has to be multiplied by

return n * factorial (n - 1):

factorial (n. accumulator)

return accumulator:

return factorial (n-1):

return factorial $(n-1, n^*)$ accumulator):

operation involves another recursive call to the function.

if(n == 0)

2-19 A (CS/IT-Sem-3)

```
recursive) when the pending operation does involve another recursive call to the function.

3. The Fibonacci function fib provides a classic example of tree recursion. The Fibonacci numbers can be defined by the rule:
```

2. A recursive function is said to be tree recursive (or non-linearly

int fib (int n) { /* n >= 0 */ if (n == 0) return 0:

1. A recursive function is said to be linearly recursive when no pending

factorial (n)

Data Structure

4

n

d. Linear and tree recursive:

if (n == 1)return 1; return fib (n - 1) + fib (n - 2);

fib is tree recursive.

Que 2.19. Explain Tower of Hanoi.

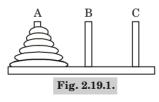
```
Answer
```

1. Suppose three pegs, labelled A, B and C is given, and suppose on peg A, there are finite number of n disks with decreasing size.

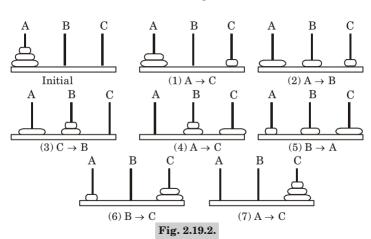
2. The object of the game is to move the disks from peg A to peg C using peg B as an auxiliary.

The pending operation for the recursive call is another call to fib. Therefore,

- 3 The rule of game is follows:
- Only one disk may be moved at a time. Specifically only the top disk on any peg may be moved to any other peg.
 - At no time, can a larger disk be placed on a smaller disk. h.



The solution to the Tower of Hanoi problem for n = 3.



Total number of steps to solve Tower of Hanoi problem of n disk $= 2^{n} - 1 = 2^{3} - 1 = 7$

Que 2.20. What is Tower of Hanoi problem? Write the recursive AKTU 2014-15, Marks 05

Answer

Tower of Hanoi problem: Refer Q. 2.19, Page 2–19A, Unit-2.

Recursive code for Tower of Hanoi:

code in C language for the problem.

#include<stdio.h>

#include<conio.h>

void main()

```
Data Structure
                                               2-21 A (CS/IT-Sem-3)
        clrscr():
        int n:
        char A = A' B = B' C = C'
        void hanoi (int. char. char. char):
        printf("Enter number of disks:"):
        scanf("%d", &n):
        printf("\n\n Tower of Hanoi problem with %d disks\n", n);
        printf("Sequence is : \n"):
         hanoi (n. A. B. C):
              printf("\n"):
                  getch():
    void hanoi (int n, char A, char B, char C)
        If(n! = 0)
        hanoi (n-1, A, C, B):
        printf("Move disk %d from %c to %c\n, n, A, C,");
        hanoi (n-1, B, A, C):
Que 2.21. Write a recursive algorithm for solving the problem of
Tower of Hanoi and also explain its complexity. Illustrate the
solution for four disks and three pegs.
Explain Tower of Hanoi problem and write a recursive algorithm
to solve it.
                                          AKTU 2018-19, Marks 07
                                OR.
Write an algorithm for finding solution to the Tower
of Hanoi problem. Explain the working of your algorithm (with 4
                                         AKTU 2015-16, Marks 15
disks) with diagrams.
Answer
```

Tower of Hanoi problem: Refer Q. 2.19, Page 2–19A, Unit-2.

Algorithm:

TOWER (N, BEG, AUX, END)

Stacks and Queues

Write: BEG → END ล

h

2.

3

4

5

2-22 A (CS/IT-Sem-3)

Return [End of If structure]

[Move N – 1 disk from peg BEG to peg AUX] Call TOWER (N - 1, BEG, END, AUX)

Write: BEG → END

[Move N-1 disk from peg AUX to peg END]

Call TOWER (N – 1, AUX, BEG, END)

Time complexity:

Let the time required for n disks is T(n).

There are 2 recursive calls for n-1 disks and one constant time operation to move a disk from 'from' peg to 'to' peg. Let it be k_i .

Therefore. $T(n) = 2 T(n-1) + k_1$

Return

 $T(0) = k_0$, a constant. $T(1) = 2k_2 + k_1$

 $T(2) = 4k_2 + 2k_1 + k_1$ $T(2) = 8k_2 + 4k_1 + 2k_1 + k_1$ Coefficient of $k_1 = 2^n$ Coefficient of $k_0 = 2^n - 1$

Time complexity is $O(2^n)$ or $O(a^n)$ where a is a constant greater than 1. So, it has exponential time complexity. Space complexity:

Space for parameter for each call is independent of *n i.e.*, constant. Let it be k.

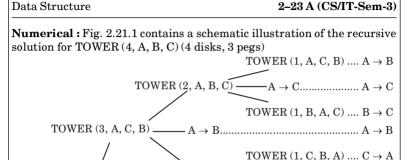
When we do the 2nd recursive call 1st recursive call is over. So, we can reuse the space of 1st call for 2nd call. Hence, T(n) = T(n-1) + k

T(1) = 2kT(2) = 3k

T(0) = k

T(3) = 4k

So, the space complexity is O(n).



TOWER (3, B, A, C) \longrightarrow B \rightarrow C B \rightarrow C

TOWER (1, C, B, A) ..., $C \rightarrow A$

TOWER (1, A, C, B) ..., $A \rightarrow B$

TOWER (2, A, B, C) $A \to C$ $A \to C$ TOWER (1, B, A, C) $B \to C$ Fig. 2.21.1. Recursive solution to Tower of Hanoi problem for n = 4.

Observe that the recursive solution for n = 4 disks consist of the following 15 moves:

Que 2.22. Discuss the principle of recursion.

Answer

a solution.

- 1. Recursion is implemented through the use of function.
- 2. A function that contains a function call to itself or a function call to a second function which eventually calls the first function, is known as a recursive function.
- 3. Two important conditions must be satisfied by any recursive function:

 a. Each time a function calls itself it must be closer, in some sense to
 - b. There must be a discussion criterion for stopping the process or computation.

There are two ways to remove recursion:

2-24 A (CS/IT-Sem-3)

1. By iteration : All tail recursion function can be removed by iterative method.

Stacks and Queues

- 2. By using stack: All non-tail recursion method can be removed by using stack.
- Que 2.24. Define the recursion. Write a recursive and non-recursive program to calculate the factorial of the given number.

 AKTU 2017-18, Marks 07

printf("The factorial of a given number using nonrecursion is

Answer

Program:

Recursion: Refer Q. 2.16, Page 2–16A, Unit-2.

```
#include <stdio.h>
#include <conio.h>
yoid main()
```

int n, a, b;
clrscr();
printf("Enter any number\n");
scanf("%d", &n);

```
printf("The factorial of a given number using recursion is %d \n", a);
b = nonrecfactorial(n);
```

%d", b); getch(); }

a = recfactorial(n):

```
int recfactorial(int x)
{
  int f;
  if(x == 0)
```

return(1);
}
else

f = x * recfactorial(x - 1);

```
Data Structure
                                                  2-25 A (CS/IT-Sem-3)
    return(f):
    int nonrecfactorial(int x)
    int i. f = 1:
    for(i = 1: i \le x: i++)
    f = f * i:
    return(f);
                              PART-5
 Queues: Operation on Queue: Create, Add, Delete, Full and Empty.
                         Questions-Answers
     Long Answer Type and Medium Answer Type Questions
Que 2.25. Discuss queue.
Answer
    Queue is a linear list which has two ends, one for insertion of elements
1
    and other for deletion of elements
    The first end is called 'Rear' and the later is called 'Front'.
2.
3
    Elements are inserted from Rear end and deleted from Front end.
4
    Queues are called First In First Out (FIFO) list, since the first element in
    a queue will be the first element out of the queue.
5.
    The two basic operations that are possible in a queue are:
         Insert (or add) an element to the queue (push) or Enqueue.
    h.
         Delete (or remove) an element from a queue (pop) or Dequeue.
Example:
    Suppose we have an empty queue, with 5 memory cells such as:
    Front = -1
    Rear = -1 i.e., Empty gueue.
```

Stacks and Queues

AKTU 2014-15, Marks 05 traversal of a queue. ΛR

Discuss various algorithms for various operation of queue.

2-26 A (CS/IT-Sem-3)

2.

3.

Answer 1. Insertion:

Insert in Q (Queue, Max, Front, Rear, Element)

Let Queue is an array. Max is the maximum index of array. Front and

Rear to hold the index of first and last element of Queue respectively and Element is value to be inserted.

Step 1: If Front = 1 and Rear = Max or if Front = Rear + 1 Display "Overflow" and Return

Step 2: If Front = NULL [Queue is empty]

Set Front = 1 and Rear = 1 else if Rear = N then Set Rear = 1

موام Set Rear = Rear + 1

[End of if Structure] Step 3: Set Queue [Rear] = Element [This is new element] Step 4: End

Deletion: Delete from Q (Queue, Max. Front, Rear, Item) Step 1: If Front = NULL [Queue is empty]

display "Underflow" and Return Step 2: Set Item = Queue [Front]

Step 3: If Front = Rear [Only one element] Set Front = Rear and Rear = NIII.L.

Else if Front = N, then Set Front = 1Else

Set Front = Front + 1

[End if structure] Step 4: End Traversal of a queue: Here queue has Front End FE and Rear End

RE. This algorithm traverse queue applying an operation PROCESS to

each element of queue : Step 1: [Initialize counter] Set K = FE

Step 2: Repeat step 3 and 4 while $K \le RE$ **Step 3:** [Visit element] Apply PROCESS to queue [K] **Step 4:** [Increase counter] Set K = K + 1

[End of step 2 loop]

Step 5: Exit

PART-6

Circular Queue, Array and Linked Implementation of Queue in C.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 2.27. What is circular queue? Write a C code to insert an element in circular queue. Write all the condition for overflow.

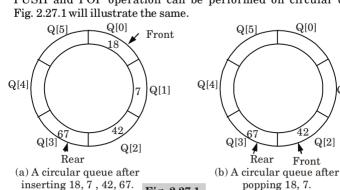
AKTU 2014-15, Marks 05

Q[1]

2-27 A (CS/IT-Sem-3)

Answer

- A circular queue is one in which the insertion of a new element is done at the very first location of the queue if the last location at the queue is full
- 2 In circular queue, the elements Q[0], Q[1], Q[2] ... Q[n-1] is represented in a circular fashion.
- **For example:** Suppose *Q* is a queue array of six elements. 3. PUSH and POP operation can be performed on circular queue.



C code to insert an element in circular queue: void insert ()

```
int item:
if((front == 0 \&\& rear == Max - 1) | | ((front == rear + 1))|
printf("Queue is overflow\n");
return;
```

Fig. 2.27.1.

```
front = 0:
         rear = 0:
        else
        if (rear == Max - 1) /*rear is at last position of queue*/
        rear = 0:
        else
        rear = rear + 1:
         printf("Input the element for insertion:"):
         scanf("%d", &item):
         cqueue [rear] = item:
Conditions for overflow: There are two conditions:
    (front = 0) and (rear = Max - 1)
1
    front = rear + 1
If any of these two conditions is satisfied, it means that overflow occurs.
Que 2.28. Write an algorithm to insert and delete an item from the
circular linked list.
Answer
Insertion in circular linked list:
i.
    At the beginning:
        If AVAIL = NULL then linked list is OVERFLOW and STOP
    1
    2
        PTR ← AVAIL
```

if(front == -1) /*If queue is empty*/

 $AVAIL \leftarrow LINK (AVAIL)$ Read INFO (PTR)
3. $CPT \leftarrow FIRST$

 $CPT \leftarrow LINK(CPT)$

PTR ← AVAIL

CPT ← FIRST

 $CPT \leftarrow LINK(CPT)$ $LINK(CPT) \leftarrow PTR$

LINK (PTR) \leftarrow FIRST FIRST \leftarrow PTR LINK (CPT) \leftarrow FIRST

 $AVAIL \leftarrow LINK (AVAIL)$ Read INFO (PTR)

4. Repeat step 5 while LINK (CPT) != FIRST

Repeat step 5 while LINK (CPT) != FIRST

If AVAIL = NULL then linked list is OVERFLOW and STOP

4

5. 6.

7.

1.

2

3.

5.

6.

ii.

STOP

At the end

Stacks and Queues

2-28 A (CS/IT-Sem-3)

Dat	ta Stı	ructure	2-29 A (CS/IT-Sem-3)
	7.	$\operatorname{LINK}\left(\operatorname{PTR}\right) \leftarrow \operatorname{FIRST}$	
	8.	STOP	
Del		n in circular linked list :	
i.	Fro	om the beginning	
	1.	If FIRST = NULL then linked list is	UNDERFLOW and STOP
	2.	$CPT \leftarrow FIRST$	
	3.	Repeat step 4 while LINK (CPT) $!= F$	FIRST
	4.	$CPT \leftarrow LINK(CPT)$	
	5.	$PTR \leftarrow FIRST$	
		$FIRST \leftarrow LINK (PTR)$	
		$LINK(CPT) \leftarrow FIRST$	
	6.	$LINK(PRT) \leftarrow AVAIL$	
		$AVAIL \leftarrow PTR$	
	7.	STOP	
ii.		om the end	
	1.	If FIRST = NULL then linked list is	UNDERFLOW and STOP.
	2.	$CPT \leftarrow FIRST$	
	3.	Repeat step 4 while LINK (CPT) $!= F$	FIRST
	4.	$PTR \leftarrow CPT$	
		$CPT \leftarrow LINK(CPT)$	
	5.	$LINK(PTR) \leftarrow FIRST$	
	6.	$LINK(CPT) \leftarrow AVAIL$	
		$AVAIL \leftarrow CPT$	
	7.	STOP	
Qu	ıe 2.	29. Write a C program to	implement the array
rep	rese	entation of circular queue.	AKTU 2016-17, Marks 10
Α			
	nswe		
#ind	clude	<stdio.h></stdio.h>	
		<conio.h></conio.h>	
		<pre><pre>c<pre>c<pre>c<pre>process.h></pre></pre></pre></pre></pre>	
#de		MAX 10	
	$_{\mathrm{typ}}$	edef struct {	
		int front, rear;	
		int elements [MAX];	
		} queue;	
	voi	d createqueue (queue *aq) {	
		$aq \rightarrow front = aq \rightarrow rear = -1$	
	}		
	int {	isempty (queue *aq)	
		$if(aq \rightarrow front = = -1)$	
		return 1;	
		else	
		return 0;	
1		i cuai i c,	

```
int isfull (queue *aq) {
     if(((aq -> front = = 0) && (aq -> rear = = MAX - 1))
                             ||(aq - > front == aq - > rear + 1)||
                 return 1:
     else
                 return 0:
void insert (queue *ag, int value) {
     if(aq \rightarrow front = = -1)
                 aq \rightarrow front = aq \rightarrow rear = 0;
     else
                 aq \rightarrow rear = (aq \rightarrow rear + 1) \% MAX:
                 aq -> element [aq -> rear] = value:
int delete (queue *aq) {
     int temp:
     temp = aq -> element [aq -> front];
     if(aq \rightarrow front = aq \rightarrow rear)
     aq \rightarrow front = aq \rightarrow rear = -1:
     else
     aq \rightarrow front = (aq \rightarrow front + 1) \% MAX:
     return temp:
void main()
     int ch, elmt;
     queue q;
     create queue (&q);
     while (1) {
     printf("1. Insertion \n");
     printf("2. Deletion \n");
     printf("3. Exit \n"):
     printf("Enter your choice");
      scanf("%d",&ch):.
               switch (ch)
                            case 1:
                             if(isfull (&q))
                             printf("queue is full");
                             getch();
                             else
                             printf("Enter value");
```

Stacks and Queues

2-30 A (CS/IT-Sem-3)

printf("4. Exit\n");

scanf("%d", &ch);

printf("Enter your choice :");

```
2-32 A (CS/IT-Sem-3)
                                                        Stacks and Queues
            switch(ch)
             case 1 ·
               insert():
               break:
             case 2 ·
               delete():
               break:
             case 3 ·
               display():
               break:
             case 4 ·
               exit(0):
               default:
                  printf("Please enter correct choice \n"):
           getch();
         void insert( )
             struct node *ptr;
             ptr = (struct node*)malloc(sizeof (struct node)):
             int item:
             printf("Input the element for inserting :\n");
             scanf("%d",&item):
             prt-> info = item;
             ptr->link = NULL:
             if (front == NULL)
                                                         /* queue is empty*/
             front = ptr;
             else
             rear->link = ptr;
             rear = ptr;
    void delete()
           struct node *ptr;
           if (front == NULL)
         {
            printf("Queue is underflow \n");
           return:
         if (front == rear) {
```

```
Data Structure
                                                     2-33 A (CS/IT-Sem-3)
           free(front):
           rear = NULL:
         else
           ptr = front:
           front = ptr->link:
           free (ptr):
    void display()
    struct node *ptr:
    ptr = front:
    if (front == NULL)
         printf("Queue is empty\n");
    else
         printf("\n Elements in the Queue are :\n");
         while(ptr != NULL)
             printf("%d\n", ptr->info);
             ptr = ptr - link;
```

Que 2.31. Explain how a circular queue can be implemented using arrays. Write all functions for circular queue operations.

AKTU 2018-19, Marks 07 Answer

```
Implementation of circular queue using array:
```

printf("\n");

Refer Q. 2.29, Page 2-29A, Unit-2. Function to create circular queue:

void Queue :: enQueue(int value)

```
2-34 A (CS/IT-Sem-3)
```

```
if((front == 0 \&\& rear == size - 1) || (rear == (front - 1)\%(size - 1)))
    printf("\nQueue is Full");
     return:
    else if (front == -1)/* Insert First Element */
     front = rear = 0:
     arr[rear] = value:
     else if (rear == size - 1 && front != 0)
     rear = 0:
     arr[rear] = value:
     else
     rear++;
     arr[rear] = value;
Function to delete element from circular queue:
     int Queue :: deQueue()
    if (front == -1)
    printf("\nQueue is Empty");
    return INT MIN:
     int data = arr[front];
     arr[front] = -1;
     if (front == rear)
     front = -1;
     rear = -1:
     else if (front == size -1)
     front = 0:
     else
     front++;
     return data;
                                PART-7
```

Stacks and Queues

2-35 A (CS/IT-Sem-3)

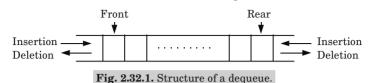
Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 2.32. Explain dequeue with its types.

Answer

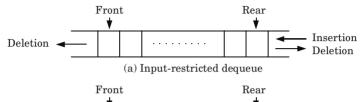
1. In a dequeue, both insertion and deletion operations are performed at either end of the queues. That is, we can insert an element from the rear end or the front end. Also deletion is possible from either end.



- 2. This dequeue can be used both as a stack and as a queue.
- 3. There are various ways by which this dequeue can be represented. The most common ways of representing this type of dequeue are:
 - a. Using a doubly linked list
 - b. Using a circular array

Types of dequeue:

- 1. Input-restricted dequeue: In input-restricted dequeue, element can be added at only one end but we can delete the element from both ends.
- 2. Output-restricted dequeue: An output-restricted dequeue is a dequeue where deletions take place at only one end but allows insertion at both ends



Insertion — Insertion — Insertion

(b) Output-restricted dequeue

Fig. 2.32.2.

Stacks and Queues

applications.

Answer

- 1 A priority queue is a data structure in which each element has been assigned a value called the priority of the element and an element can be inserted or deleted not only at the ends but at any position on the
- 2 A priority queue is a collection of elements such that each element has been assigned an explicit or implicit priority and such that the order in which elements are deleted and processed comes from the following rules:
 - An element of higher priority is processed before any element of lower priority. Two elements with the same priority are processed to the order in h

which they were inserted to the queue. Types of priority queues are:

- Ascending priority queue: In ascending priority queue, elements 1. can be inserted in an order. But, while deleting elements from the queue, always a small element to be deleted first.
- **Descending priority queue:** In descending priority queue, elements 2. are inserted in any order but while deleting elements from the queue always a largest element to be deleted first.

Applications of priority queue: 1

- The typical example of priority queue is scheduling the jobs in operating system. Typically operating system allocates priority to jobs. The jobs are placed in the queue and position 1 of the job in priority queue determines their priority.
- 2 In network communication, to manage limited bandwidth for transmission, the priority queue is used.
- 3. In simulation modelling, to manage the discrete events the priority queue is used.

VERY IMPORTANT QUESTIONS

Following questions are very important. These questions may be asked in your SESSIONALS as well as UNIVERSITY EXAMINATION.

Q. 1. Write a C function for array implementation of stack. Write all primitive operations. Ans. Refer Q. 2.4.

Q. 2. Write a C function for linked list implementation of stack.

Q. 3. What is stack? Implement stack with singly linked list.

Write all the primitive operations.

2-37 A (CS/IT-Sem-3)

Data Structure

Ans. Refer Q. 2.5.

Q. 7. Solve the following:

Ans. Refer Q. 2.20.

b. (A+B)+*C-(D-E) ∧ F [Infix to prefix]
c. 752+*415-/- [Evaluate the given postfix expression]
Ans. Refer Q. 2.14.

a. ((A - (B + C) * D) / (E + F)) [Infix to postfix]

in C language for the problem.

Q. 8. What is recursion? Write a recursive program to find sum of digits of the given number. Also, calculate the time complexity.

Ans. Refer Q. 2.17.

Q. 9. What is Tower of Hanoi problem? Write the recursive code

Q.10. Explain Tower of Hanoi problem and write a recursive algorithm to solve it.

Ans. Refer Q. 2.21.

Q.11. Define the recursion. Write a recursive and non-recursive program to calculate the factorial of the given number.Ans. Refer Q. 2.24.

Q. 12. Write the procedures for insertion, deletion and traversal of a queue.

Ans. Refer Q. 2.26.

2-38 A (CS/IT-Sem-3)

- in circular queue. Write all the condition for overflow. Ans. Refer Q. 2.27.
- Q. 14. Write a C program to implement the array representation of circular queue. Ans. Refer Q. 2.29.
- Q.15. Explain how a circular queue can be implemented using arrays. Write all functions for circular queue operations.

Ans. Refer Q. 2.31.



Part-1

Part-5 :



Searching and Sorting

CONTENTS

Searching, Sequential Search, Index Sequential Search, Binary Search

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Searching and Sorting

Searching : Concept of Searching, Sequential Search, Index Sequential Search, Binary Search.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 3.1. What do you mean by searching? Explain.

- Answer
- Searching is the process of finding the location of given element in the linear array.
 The search is said to be successful if the given element is found, *i.e.*, the
- element does exists in the array; otherwise unsuccessful.

 There are two searching techniques:
- a. Linear search (sequential) b. Binary search
- 4. The algorithm which we choose depends on organization of the array
- technique, and if the array elements are sorted, then it is preferable to use binary search.

 Que 3.2. Write a short note on sequential search and index

If the elements are in random order, then we have to use linear search

Answer

sequential search.

elements.

5.

3-2 A (CS/IT-Sem-3)

Sequential search:

- In sequential (or linear) search, each element of an array is read oneby-one sequentially and it is compared with the desired element. A search will be unsuccessful if all the elements are read and the desired element is found.
- Linear search is the least efficient search technique among other search techniques.
- techniques.
 3. It is used when the records are stored without considering the order or when the storage medium lacks the direct access facility.
- 4. It is the simplest way for finding an element in a list.
 5. It searches the elements sequentially in a list, no matter whether list is
- a. In case of sorted list in ascending order, the search is started from

1st element and continued until desired element is found or the element whose value is greater than the value being searched.

Index sequential search:

specified group.

h

c.

1.

2.

3.

3.

1st element and continued until the desired element is found or the element whose value is smaller than the value being searched. If the list is unsorted searching started from 1st location and

continued until the element is found or the end of the list is reached.

In index sequential search, an index file is created, that contains some

specific group or division of required record, once an index is obtained, then the partial searching of element is done which is located in a

In indexed sequential search, a sorted index is set aside in addition to the

Each element in the index points to a block of elements in the array or

3-3 A (CS/IT-Sem-3)

- 4.
- another expanded index. First the index is searched that guides the search in the array. Indexed sequential search does the indexing multiple times like creating 5.
 - the index of an index. When the user makes a request for specific records it will find that index 6. group first where that specific record is recorded.

Que 3.3. Write down algorithm for linear/sequential search

technique. Give its analysis.

Answer

LINEAR (DATA, N, ITEM, LOC) Here DATA is a linear array with N elements, and ITEM is a given item of information. This algorithm finds the location LOC of ITEM in DATA, or sets

- LOC := 0 if the search is unsuccessful. [Insert ITEM at the end of DATA] Set DATA[N + 1] := ITEM 1.
- 2. [Initialize counter] Set LOC := 1
 - Set LOC := LOC + 1[End of loop]
- [Successful?] If LOC = N + 1, then : Set LOC := 0 4.
- Exit 5.

Repeat while DATA[LOC] ≠ ITEM

Analysis of linear search:

[Search for ITEM]

Best case: Element occur at first position. Time complexity is O(1). **Worst case:** Element occur at last position. Time complexity is O(n).

Que 3.4. Write down the algorithm of binary search technique.

Write down the complexity of algorithm.

Answer Binary search (A, n, item, loc)

Let *A* is an array of '*n*' number of items, item is value to be searched.

3-4 A (C	CS/IT-Sem-3)	Searching and Sorting				
 Set: beg = 0, Set: end = n - 1, Set: mid = (beg + end) / 2 While ((beg ≤ end) and (a [mid]!= item)) If (item < a[mid]) then Set: end = mid - 1 else Set: beg = mid + 1 endif Set: mid = (beg + end) / 2 endwhile If (beg > end) then Set: loc = -1 // element not found else Set: loc = mid endif Exit Analysis of binary search: The complexity of binary search is O(log₂ n). Que 3.5. What is difference between sequential (linear) search and binary search technique? 						
S. No.	Sequential (linear) search	Binary search				
1.	No elementary condition <i>i.e.</i> , array can be sorted or unsorted.	Elementary condition <i>i.e.</i> , array should be sorted.				
2.	It takes long time to search an element.	It takes less time to search an element.				
3.	Complexity is $O(n)$.	Complexity is $O(\log_2 n)$.				
4.	It searches data linearly.	It is based on divide and conquer method.				
Concept of Hashing and Collision Resolution Techniques used in Hashing.						
Questions-Answers Long Answer Type and Medium Answer Type Questions						
Que 3.6. What do you mean by hashing?						

Answer

- Hashing is a technique that is used to uniquely identify a specific object from a group of similar objects.
 Hashing is the transformation of a string of characters into a usually
- shorter fixed-length value or key that represents the original string.

 In hashing, large keys are converted into small keys by using hash functions.
- The values are then stored in a data structure called hash table.
 The task of hashing is to distribute entries (key/value pairs) uniformly across an array.
- Each element is assigned a key (converted key). By using that key we can access the element in O(1) time.
 Using the key, the algorithm (hash function) computes an index that
- 7. Using the key, the algorithm (hash function) computes an index that suggests where an entry can be found or inserted.
- 8. Hashing is used to index and retrieve items in a database because it is faster to find the item using the shorter hashed key than to find it using the original value.
- 9. The element is stored in the hash table where it can be quickly retrieved using hashed key which is defined by

 Hash Key = Key Value % Number of Slots in the Table

Que 3.7. Discuss types of hash functions.

Answer

h.

Types of hash functions:

- a. Division method:
 - Choose a number m larger than the number n of key in K. (The number m is usually chosen to be a prime number or a number without small divisors, since this frequently minimizes the number of collisions.)
 - 2. The hash function H is defined by :

$$H(k) = k \pmod{m} \quad \text{or} \quad H(k) = k \pmod{m} + 1$$

- 3. Here $k \pmod{m}$ denotes the remainder when k is divided by m.
- 4. The second formula is used when we want the hash addresses to range from 1 to m rather than from 0 to m-1.
- Midsquare method:
 - 1. The key k is squared.
 - 2. The hash function H is defined by : H(k) = l where l is obtained by deleting digits from both end of k^2 .
 - where t is obtained by deleting digits from both end of k^2 .

 3. We emphasize that the same positions of k^2 must be used for all of
- c. Folding method:

the keys.

1. The key k is partitioned into a number of parts, k_1, \ldots, k_r , where each part, except possibly the last, has the same number of digits as the required address.

- Searching and Sorting
- 2. Then the parts are added together, ignoring the last carry *i.e.*, $H(k) = k_1 + k_2 + \dots + k_n$
- where the leading-digit carries, if any, are ignored.

 4. Now truncate the address upto the digit based on the size of hash table.

Que 3.8. What is collision? Discuss collision resolution

techniques.

OR

Write a short note on hashing techniques.

AKTU 2017-18, Marks 3.5

Answer

Collision :

2

5

1. Collision is a situation which occur when we want to add a new record R with key k to our file F, but the memory location address H(k) is already occupied.

A collision occurs when more than one keys map to same hash value in

the hash table.

Collision resolution technique:

- Hashing with open addressing:
- In open addressing, all elements are stored in the hash table itself.
 While searching for an element, we systematically examine table slots until the desired element is found or it is clear that the element is not in
- the table.
- Thus, in open addressing, the load factor λ can never exceed 1.
 The process of examining the locations in the hash table is called probing.
 - Following are techniques of collision resolution by open addressing:
 - a. Linear probing: i. Given an ordinary hash function h': U [0, 1,, m-1], the

method of linear probing uses the hash function. $h(h, i) = (h'(h) + i) \mod m$

 $h(k, i) = (h'(k) + i) \mod m$ where 'm' is the size of the hash table and $h'(k) = k \mod m$ (basic hash function).

b. Quadratic probing:

- i. Suppose a record R with key k has the address H(k) = h then instead of searching the locations with address h, h + 1, h + 2,, we linearly search the locations with addresses h, h + 1, h + 4, h + 9,, $h + i^2$.
- ii. Quadratic probing uses a hash function of the form

 $h\left(k,i\right)=\left(h'\left(k\right)+c_{1}i+c_{2}i^{2}\right)\bmod m$ where (as in linear probing) h' is an auxiliary hash function, c_{1} and $c_{2}\neq0$ are auxiliary constants, and $i=0,\,1,\,....,\,m-1$.

c. Double hashing:

Double hashing:
 Double hashing is one of the best methods available for open addressing because the permutations produced have many of the characteristics of randomly chosen permutations.

3-7 A (CS/IT-Sem-3)

- ii Double hashing uses a hash function of the form:
 - $h(k, i) = (h_1(k) + ih_2(k)) \mod m$,

where h_1 and h_2 are auxiliary hash functions and m is the size of the hash table.

Hashing with separate chaining:

- This method maintains the chain of elements which have same hash 1 address.
- 2 We can take the hash table as an array of pointers.
- Size of hash table can be number of records. 3 4 Here each pointer will point to one linked list and the elements which have same hash address will be maintained in the linked list.
- We can maintain the linked list in sorted order and each elements of 5. linked list will contain the whole record with key.
- For inserting one element, first we have to get the hash value through 6. hash function which will map in the hash table, then that element will be inserted in the linked list.
- Searching a key is also same, first we will get the hash key value in hash 7. table through hash function, then we will search the element in corresponding linked list.
- Deletion of a key contains first search operation then same as delete 8. operation of linked list.

What do you mean by hashing and collision? Discuss Que 3.9. the advantages and disadvantages of hashing over other searching AKTU 2014-15, Marks 10

Hashing: Refer Q. 3.6, Page 3-4A, Unit-3.

techniques.

Answer

Collision: Refer Q. 3.8, Page 3-6A, Unit-3.

- Advantages of hashing over other search techniques:
- The main advantage of hash tables over other table data structures is 1. speed. This advantage is more apparent when the number of entries is large (thousands or more).
- Hash tables are particularly efficient when the maximum number of 2. entries can be predicted in advance, so that the bucket array can be allocated once with the optimum size and never resized.
- If the set of key-value pairs is fixed and known ahead of time (so insertions 3. and deletions are not allowed), one may reduce the average lookup cost by a careful choice of the hash function, bucket table size, and internal data structures.

Disadvantages of hashing over other search techniques: Hash tables can be more difficult to implement than self-balancing binary

search trees. Choosing an effective hash function for a specific application is more an art than a science. In open-addressed hash tables it is fairly easy to create a poor hash function.

2. The cost of a good hash function can be significantly higher than the inner loop of the lookup algorithm for a sequential list or search tree. Hash tables are not effective when the number of entries is very small. 3

For certain string processing applications, such as spell-checking, hash tables may be less efficient than trees, finite automata, or arrays. If each key is represented by a small enough number of bits, then,

instead of a hash table, one may use the key directly as the index into an

Write short notes on garbage collection.

Searching and Sorting

AKTU 2017-18, Marks 3.5 AKTU 2014-15, Marks 05

- 1 When some memory space becomes reusable due to the deletion of a node from a list or due to deletion of entire list from a program then we want the space to be available for future use.
- 2. One method to do this is to immediately reinsert the space into the freestorage list. This is implemented in the linked list. This method may be too time consuming for the operating system of a 3.
- computer. 4. In another method, the operating system of a computer may periodically collect all the deleted space onto the free storage list. This type of
- technique is called garbage collection. Garbage collection usually takes place in two steps. First the computer 5. runs through all lists, tagging those cells which are currently in use and then the computer runs through the memory, collecting all untagged
- The garbage collection may take place when there is only some minimum amount of space or no space at all left in the free storage list or when the CPU is idle and has time to do the collection.

Que 3.11. Write the conditions when collision occurs in hashing.

Describe any collision detection algorithm in brief.

Condition when collision occurs: Refer Q. 3.8, Page 3-6A, Unit-3.

space onto the free storage list.

3-8 A (CS/IT-Sem-3)

array of values.

Que 3.10.

Answer

6.

Answer

4

Collision detection algorithm: One of the collision detection algorithms is grid based algorithm. a.

- In this algorithm, grids are space-filling. h.
- Each cell or voxel (volume pixel) has a list of objects which intersects it. C.
- The uniform grid is used to determine which objects are near to an d. object by examining object-lists of the cells the object overlaps. Intersections for a given object are found by going through the object e.
- lists for all voxels containing the object, performing intersection tests against objects on those lists.

Data Structure 3–9 A (CS/IT	
f.	A grid based collision detection algorithm then works as follows: 1. for $i = 1$ to n 2. $v_{\min} = \text{voxel (min (bbox (object (i))))}$ 3. $v_{\max} = \text{voxel (max (bbox (object (i))))}$ 4. for $x = v_{\min_x}$ to $x = v_{\max_x}$ 5. for $y = v_{\min_y}$ to $y = v_{\max_y}$ 6. for $z = v_{\min_y}$ to $z = v_{\max_z}$ 7. for $j = 1$ to $n_{\text{objects (voxel }(x, y, z))}$ 8. if (not tested (object (i), object (j)) 9. intersect (object (i), object (j))
	PART-3
	Sorting : Insertion Sort, Selection Sort, Bubble Sort.
_	
	Questions-Answers
	Long Answer Type and Medium Answer Type Questions
Q	ue 3.12. Write a short note on insertion sort.
	AKTU 2014-15, Marks 05
Δ	nswer
1. 2.	In insertion sort, we pick up a particular value and then insert it at the appropriate place in the sorted sublist, <i>i.e.</i> , during k^{th} iteration the element $a[k]$ is inserted in its proper place in the sorted sub-array $a[1]$, $a[2]$, $a[3]$, $a[k-1]$. This task is accomplished by comparing $a[k]$ with $a[k-1]$, $a[k-2]$, $a[k-3]$ and so on until the first element $a[j]$ such that $a[j] \le a[k]$ is foun
3.	Then each of the elements $a[k-1]$, $a[k-2]$, $a[j+1]$ are moved one position up at then element $a[k]$ is inserted in $[j+1]$ st position in the array. Insertion-Sort (A)
	inscrion sort (1)
	1. for $j \leftarrow 2$ to length[A] 2. do key $\leftarrow A[j]$ /*Insert A[j] into the sorted sequence A[1j-1]. 3. $i \leftarrow j-1$
	2. do key $\leftarrow A[j]$ /*Insert $A[j]$ into the sorted sequence $A[1j-1]$.
	2. do key $\leftarrow A[j]$ /*Insert $A[j]$ into the sorted sequence $A[1j-1]$. 3. $i \leftarrow j-1$ 4. while $i > 0$ and $A[i] > \text{key}$ 5. do $A[i+1] \leftarrow A[i]$

Complexity of best case is O(n)Complexity of average case is $O(n^2)$ Complexity of worst case is $O(n^2)$ Que 3.13. Write a short note on selection sort.

Answer

3-10 A (CS/IT-Sem-3)

 In selection sort we repeatedly find the next largest (or smallest) element in the array and move it to its final position in the sorted array.
 We begin by selecting the largest element and moving it to the highest

Searching and Sorting

2. We begin by selecting the largest element and moving it to the highes index position.

We can do this by swapping the element at the highest index and the

3. We can do this by swapping the element at the highest index and the largest element.

4. We then reduce the effective size of the array by one element and

4. We then reduce the effective size of the array by one element and repeat the process on the smaller sub-array.
5. The process stops when the effective size of the array becomes 1 (an

array of 1 element is already sorted). Selection-Sort (A):

1. $n \leftarrow \operatorname{length}[A]$ 2. $\operatorname{for} j \leftarrow 1 \operatorname{to} n - 1$ 3. $\operatorname{smallest} \leftarrow j$

4. for $i \leftarrow j + 1$ to n5. if A[i] < A[smallest]6. then smallest $\leftarrow i$

7. exchange(A[j], A[smallest])

Analysis of selection sort:

Complexity of best case is $O(n^2)$.

Complexity of average case is $O(n^2)$. Complexity of worst case is $O(n^2)$.

Que 3.14. Discuss bubble sort.

Discuss bubble sor

Answer

3.

- Bubble sort is the simplest sorting algorithm that works by repeatedly swapping the adjacent element if they are in wrong order.
 Bubble sort procedure is based on following idea:
 - a. Suppose if the array contains n elements, then (n-1) iterations are required to sort this array.
 b. The set of items in the array are scanned again and again and if any
 - two adjacent items are found to be out of order, they are reversed.c. At the end of the first iteration, the lowest value is placed in the first position.
 - d. At the end of the second iteration, the next lowest value is placed in the second position and so on.
 - the second position and so on. It is very efficient in large sorting jobs. For n data items, this method requires n(n-1)/2 comparisons.

Bubble-sort (A) :1. for $i \leftarrow 1$ to length [A]2. for $j \leftarrow \text{length}[A]$ down to i + 1

3-11 A (CS/IT-Sem-3)

into two halves in such a way that the elements in the left sub-array are less than and the elements in the right sub-array are greater than the partitioning element.

Repeat while $A \text{ [LOC]} \leq A \text{ [RIGHT]}$ and $\text{LOC} \neq \text{RIGHT}$

Then these two sub-arrays are sorted separately. This procedure is recursive in nature with the base criteria. Algorithm:

QUICK (A, N, BEG, END, LOC):

[Scan from RIGHT to LEFT]

Data Structure

if A[i] < A[i-1]

3.

3.

2.

ล.

b.

ii.

- [Initialize] Set LEFT := BEG, RIGHT := END and LOC := BEG 1.
 - RIGHT := RIGHT 1 [End of Loop]
 - If LOC = RIGHT, then: Return
 - If A [LOC] > A [RIGHT], then: c.

 - [Interchange A [LOC] and A [RIGHT]] i.
 - TEMP := A [LOC], A [LOC] := A [RIGHT],A [RIGHT] = TEMPSet LOC := RIGHT
 - iii. Go to step 3 [End of if structure]
- [Scan from LEFT to RIGHT] 3.
 - Repeat while A [LEFT] $\leq A$ [LOC] and LEFT \neq LOC:

	DELT:- DELT: 1		
	[End of Loop]		
b.	If LOC = LEFT, then: Return,		
c.	If A [LEFT] $> A$ [LOC], then		
	i. $[Interchange A [LEFT] and A [LOC]]$		
	TEMP := A [LOC], A [LOC] := A [LEFT],		
	A [LEFT] := TEMP		
	ii. Set $LOC := LEFT$		
	iii. Go to step 2		
	[End of if structure]		
Quick sort: This algorithm sorts an array A with N elements.			
1. [In	itialize] Top := NULL		
2. [PU	USH boundary values of A onto stack when A has 2 or more elements]		
If I	V > 1, then : TOP := TOP + 1, LOWER [1] := 1, UPPER [1] := N		
3. Re	peat steps 4 to 7 while $TOP \neq NULL$		
4. [PO	OP sublist from stacks]		
Set	t BEG := LOWER [TOP], END := UPPER [TOP],		
TO	P = TOP - 1		
5. Ca	ll Quick (A, N, BEG, END, LOC)		
6. [PU	USH left sublist onto stack when it has 2 or more elements]		
If I	BEG < LOC - 1 then:		

[PUSH right sublist onto stack when it has 2 or more elements]

Write a recursive quick sort algorithm.

Searching and Sorting

3-12 A (CS/IT-Sem-3)

LEFT := LEFT + 1

TOP := TOP + 1, LOWER [TOP] := BEG,

TOP := TOP + 1, LOWER [TOP] := LOC + 1

UPPER [TOP] = LOC - 1[End of if structure]

If LOC + 1 < END, then:

UPPER [TOP] := END [END of if structure] [END of step 3 loop]

Analysis of quick sort: Complexity of worst case is $O(n^2)$. Complexity of best case is $O(n \log n)$. Complexity of average case is $O(n \log n)$.

QUICK-SORT (A, p, r):

 $q \leftarrow \text{PARTITION}(A, p, r)$

QUICK-SORT (A, p, q - 1)QUICK-SORT (A, q + 1, r)

If p < r then

PARTITION (A, p, r):

 $x \leftarrow A[r]$

 $i \leftarrow p - 1$

7.

8.

Exit

Que 3.16.

Answer

1.

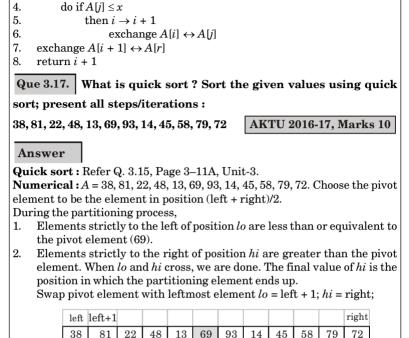
2.

3.

4.

1.

2.



3-13 A (CS/IT-Sem-3)

Move hi left and lo right as far as we can; then swap A[lo] and A[hi], and move hi and lo one more position.

Repeat above

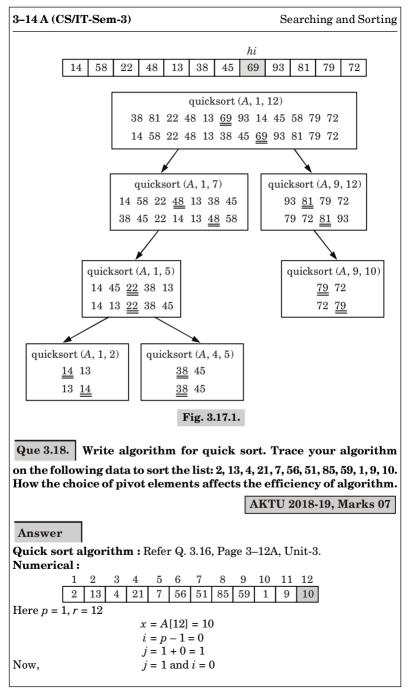
Data Structure

for $j \to p$ to r-1

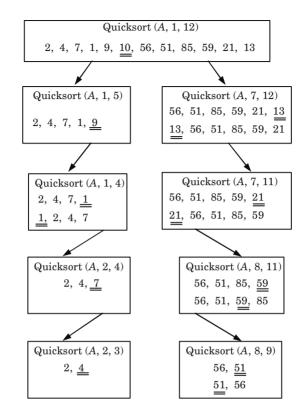
3.

Repeat above until hi and lo cross; then hi is the final position of the pivot element, so swap A[hi] and A[left].

Partitioning complete; return value of hi.



Data Structure	3-15 A (CS/IT-Sem-3)
$A[1] = 2 \le 10 (\text{True})$	
then $i = 0 + 1 = 1$ and $A[1] \leftrightarrow$	A[1]
Now, $j = 2$ and $i = 1$	
$A[2] = 13 \text{ and } 13 \nleq 10 \text{ (False)}$	
So, $j = 3$ $i = 1$	
$A[3] = 4 \text{ and } 4 \le 10 \text{ (True)}$	
then, $i = 1 + 1 = 2$ and $A[2] \leftrightarrow$	A[3]
	1 12
i.e., 2 4 13 21 7 56 51 85 59 1 9	9 10
Now, $j = 4$ and $i = 2$	
$A[4] = 21 \text{ and } 21 \nleq 10 \text{ (False)}$	9)
j = 5 and $i = 2$	
$A[5] = 7 \le 10 \text{ (True)}$	4.500
then, $i = 2 + 1 = 3 \text{ and } A[3] \leftrightarrow$	A[5]
	1 12
i.e., 2 4 7 21 13 56 51 85 59 1 9	9 10
Now, $j = 6$ and $i = 3$	
$A[6] = 56 \text{ and } 56 \nleq 10$	
So, $j = 7$ and $i = 3$	
$A[7] = 51 \text{ and } 51 \nleq 10$	
j = 8 and $i = 3$	
$A[8] = 85 \text{ and } 85 \nleq 10$	
j = 9 and $i = 3$	
$A[9] = 59 \text{ and } 59 \ 10$	
j = 10 and i = 3	
$A[10] = 1 \le 10 \text{ (True)}$	4.54.03
then, $i = 3 + 1 = 4$ and $A[4] \leftrightarrow$	· A[10]
i.e., 2 4 7 1 13 56 51 85 59 21 8	
j = 11 and $i = 4$	
$A[11] = 9 \le 10 \text{ (True)}$	
$i = 4 + 1 = 5 \text{ and } A[5] \leftrightarrow$	A[11]
1 2 3 4 5 6 7 8 9 10 1	1 12
	3 10
$A[6] \leftrightarrow A[12]$	
Partitioning complete, return value of q	· :
1 2 3 4 5 6 7 8 9	10 11 12
2 4 7 1 9 10 56 51 85	59 21 13
	· · · · · · · · · · · · · · · · · · ·
1	



Choice of pivot element affects the efficiency of algorithm:

If we choose the last or first element of an array as pivot element then it results in worst case scenario with $O(n^2)$ time complexity. If we choose the median as pivot element then it divides the array into two halves every time and results in best or average case scenario with time complexity $O(n \log n)$. Thus, the efficiency of quick sort algorithm depends on the choice of pivot element.

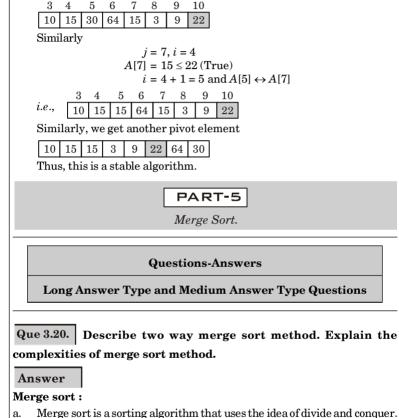
Que 3.19. Use quick sort algorithm to sort 15, 22, 30, 10, 15, 64, 1, 3, 9, 2. Is it a stable sorting algorithm? Justify.

AKTU 2017-18, Marks 07

			3							
$\operatorname{Let} A[] =$	15	22	30	10	15	64	1	3	9	2

Here p = 1, r = 10

Data Struc	eture	3–17 A (CS/IT-Sem-3)
	x = A[10] i.e., x = 2	
	i = p - 1 i.e., i = 0	
	j = 1 to 9	
Now,	j = 1 and $i = 0$	
	$A[j] = A[1] = 15$ and $15 \le 2$	
So,	j = 2 and $i = 0$	
	$A[2] = 22 \le 2 \text{ (False)}$	
Now,	j = 3 and $i = 0$	
	$A[3] = 30 \le 2 \text{ (False)}$	
	j = 4 and $i = 0$	
	$A[4] = 10 \le 2 \text{ (False)}$	
	$j = 5$ $A[5] = 15 \le 2 \text{ (False)}$	
	j = 6	
	$A[6] = 64 \le 2 \text{ (False)}$	
	j = 7	
	$A[7] = 1 \le 2 \text{ (True)}$	
	i = 0 + 1 = 1	
	$A[1] \leftrightarrow A[7]$	
	1 2 3 4 5 6 7 8 9	10
i.e.,	1 22 30 10 15 64 15 3 9	2
'		
	j = 8 and $i = 1$	
	$A[8] = 3 \le 2 \text{ (False)}$ j = 9 and i = 1	
	$A[9] = 9 \le 2 \text{ (False)}$	
then,	$A[0] = 0 \le 2 \text{ (Palse)}$ $A[1+1] \leftrightarrow A[r]$	
l uncii,	$A[2] \leftrightarrow A[10]$	
	$q \leftarrow 2$	
	•	10
i.e.,		22
1		22
QUIC	K SORT (A, 1, 1)	
	$\frac{2}{2}$	
1	2	
QUIC	K SORT (A, 3, 10)	
3 4	4 5 6 7 8 9 10	
30 1	10 15 64 15 3 9 22	
Here		
nere	p = 3, r = 10 x = A[10] = 22	
	i = 3 - 1 = 2	
	j = 3 to 9; j = 3 and i = 3	2
	$A[3] = 30 \le 22 \text{ (False)}$	=
	j = 4 and $i = 2$	
	$A[4] = 10 \le 22 (True)$	
	$i = 2 + 1 = 3$ and $A[3] \leftrightarrow$	A[4]



Searching and Sorting

10

22

 $i = 3 + 1 = 4 \text{ and } A[4] \leftrightarrow A[5]$

This algorithm divides the array into two halves, sorts them separately

This procedure is recursive, with the base criteria that the number of

j = 5 and i = 3 $A[5] = 15 \le 22 \text{ (True)}$

3-18 A (CS/IT-Sem-3)

10 30 15 64 15

i.e.,

a. h.

С.

1.

2.

3.

4.

and then merges them.

 $MERGE_SORT(a, p, r)$:

then $q \leftarrow \lfloor (p+r)/2 \rfloor$

MERGE-SORT (A, p, q)MERGE-SORT (A, q + 1, r)

if p < r

elements in the array is not more than 1.

5.

1.

5.

6. 7.

8.

3-19 A (CS/IT-Sem-3)

Extra memory

O(n)

 $n_1 = q - p + 1$ 2. $n_0 = r - q$ 3. Create arrays L [1 $n_1 + 1$] and

 $R[1....n_9 + 1]$ for i = 1 to n_1

4. do L[i] = A[p + i - 1]

MERGE (A, p, q, r)

endfor for j = 1 to n_2

R[j] = A[q+j]endfor

 $L[n_1+1]=\infty, R[n_2+1]=\infty$ i = 1, j = 1

for k = p to rdo

if $L[i] \leq R[i]$

then $A[k] \leftarrow L[i]$ i = i + 1

else

exit

endif endfor

9.

7.

Complexity of merge sort algorithm:

A[k] = R[j]i = i + 1

Let f(n) denote the number of comparisons needed to sort an 1.

n-element array *A* using the merge sort algorithm. The algorithm requires at most $\log n$ passes. 2.

3. Moreover, each pass merges a total of n elements, and by the discussion on the complexity of merging, each pass will require at most ncomparisons. Accordingly, for both the worst case and average case, 4.

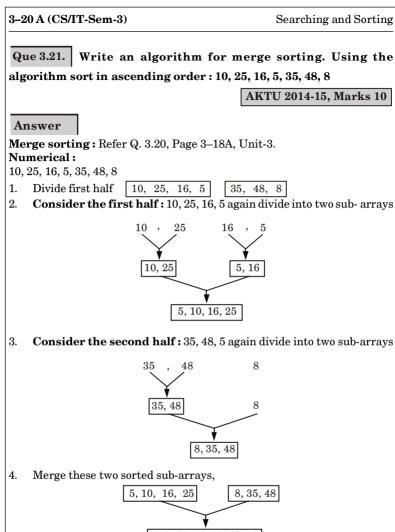
 $f(n) \le n \log n$ 5.

This algorithm has the same order as heap sort and the same average order as quick sort. The main drawback of merge sort is that it requires an auxiliary array 6. with n elements.

Each of the other sorting algorithms requires only a finite number of

extra locations, which is independent of n. The results are summarized in the following table: 8.

Worst case Algorithm Average case Merge sort $n \log n = O(n \log n)$ $n \log n = O(n \log n)$



5, 8, 10, 16, 25, 35, 45

This is the sorted array.

Que 3.22. How do you calculate the complexity of sorting algorithms? Also, write a recursive function in 'C' to implement the merge sort on given set of integers. AKTU 2015-16, Marks 10

Answer Complexity: Refer Q. 3.20, Page 3–18A, Unit-3.

```
int j = mid + 1;
   int k = low:
   while ((i \le mid) \&\& (j \le high))
   if (array [i] <= array [i])
        temp [k++] = array [i++];
    else
        temp [k++] = array [i++];
        while (i \le mid)
    temp [k++] = array [i++];
    while (j <= high)
    temp [k++] = array [i++];
    for (i = low; i \le high; i++)
    array [i] = temp [i];
   void merge_sort (int low, int high)
    int mid:
    if (low != high)
    mid = (low + high) / 2:
    merge sort (low, mid):
    merge sort (mid + 1, high);
    merge (low, mid, high);
                              PART-6
                      Heap Sort and Radix Sort.
                         Questions-Answers
     Long Answer Type and Medium Answer Type Questions
Que 3.23. Write a short note on heap sort.
```

3-21 A (CS/IT-Sem-3)

AKTU 2014-15, Marks 05

Data Structure

int temp [MAX];
int i = low;

void merge (int low, int mid, int high)

Function:

$\neq i$				
then exchange $A[i] \leftrightarrow A[largest]$				
APIFY [A, largest]				
(A):				
MAX-HEAP(A)				
ength [A] down to 2				
$xchange A[1] \leftrightarrow A[i]$				
heap-size $[A] \leftarrow$ heap-size $[A] - 1$				
MAX-HEAPIFY $(A, 1)$				
Write a short note on radix sort.				
OR				
AKTU 2017-18, Marks 3.5				
1 // (// (// XX))				

Radix sort is a small method that many people uses when alphabetizing a large list of names (here Radix is 26, 26 letters of alphabet).

Specifically, the list of name is first sorted according to the first letter of

Intuitively, one might want to sort numbers on their most significant

each name, *i.e.*, the names are arranged in 26 classes.

OR.

Heap sort finds the largest element and puts it at the end of array, then

the second largest item is found and this process is repeated for all other

Interchange the root (maximum) element with the last element.

Repeat step (a) and (b) until there are no more elements.

Use repetitive downward operation from root node to rebuild the

The general approach of heap sort is as follows:

heap of size one less than the starting.

Complexity of heap sort for all cases is $O(n \log_2 n)$.

if $r \le \text{heap-size}[A]$ and A[r] > A [largest]

if $l \le \text{heap-size } [A] \text{ and } A[l] > A[i]$

From the given array, build the initial max heap.

Searching and Sorting

AKTU 2017-18. Marks 3.5

3-22 A (CS/IT-Sem-3)

Explain heap sort.

elements

Analysis of heap sort:

MAX-HEAPIFY(A, i):

then largest $\leftarrow l$ else largest $\leftarrow i$

then largest $\leftarrow r$

 $i \leftarrow \text{left}[i]$

 $r \leftarrow \text{right } [i]$

Answer

h.

С.

d.

1

2.

1.

2.

3.

4.

5.

6.

7.

Answer

digit.

1

2.

3.

4

3-23 A (CS/IT-Sem-3)

- 5 On the first pass entire numbers sort on the least significant digit and combine in an array. 6. Then on the second pass, the entire numbers are sorted again on the
- second least-significant digits and combine in an array and so on. Following example shows how radix sort operates on seven 3-digit 7. number

Table 3.24.1.					
Input	1^{st} pass	2 nd pass	3 rd pass		
329	720	720	329		
457	355	329	355		
657	436	436	436		
839	457	839	457		
436	657	355	657		
720	329	457	720		
355	839	657	839		

- 8. In the above example, the first column is the input.
- The remaining shows the list after successive sorts on increasingly 9. significant digits position.
- The code for radix sort assumes that each element in the n-element 10. array A has d digits, where digit 1 is the lowest-order digit and d is the highest-order digit.

RADIX SORT (A. d) for $i \leftarrow 1$ to d do

use a stable sort to sort array A on digit i// counting sort will do the job

- **Analysis:** The running time depends on the table used as an intermediate sorting 1.
- algorithm. 2. When each digit is in the range 1 to k, and k is not too large,
- COUNTING SORT is the obvious choice. In case of counting sort, each pass over n d-digit numbers takes
- 3. $\Theta(n+k)$ time.
- 4. There are *d* passes, so the total time for radix sort is $\Theta(n+k)$ time. There are d passes, so the total time for radix sort is $\Theta(dn + kd)$. When d is constant and $k = \Theta(n)$, the radix sort runs in linear time.

VERY IMPORTANT QUESTIONS

Following questions are very important. These questions may be asked in your SESSIONALS as well as UNIVERSITY EXAMINATION.

- Q. 1. What is collision? Discuss collision resolution techniques.

 Ans. Refer Q. 3.8.
- Q. 2. What do you mean by hashing and collision? Discuss the advantages and disadvantages of hashing over other searching techniques.

Ans. Refer Q. 3.9.

Q.3. Write short notes on garbage collection.

Ans. Refer Q. 3.10.

Q.4. Write a short note on insertion sort.

Ans. Refer Q. 3.12.

Q. 5. What is quick sort? Sort the given values using quick sort; present all steps/iterations: 38, 81, 22, 48, 13, 69, 93, 14, 45, 58, 79, 72

Ans. Refer Q. 3.17.

Q. 6. Write algorithm for quick sort. Trace your algorithm on the following data to sort the list: 2, 13, 4, 21, 7, 56, 51, 85, 59, 1, 9, 10. How the choice of pivot elements affects the efficiency of algorithm.

Ans. Refer Q. 3.18.

Q. 7. Use quick sort algorithm to sort 15, 22, 30, 10, 15, 64, 1, 3, 9, 2. Is it a stable sorting algorithm? Justify.

Ans. Refer Q. 3.19.

Q. 8. Write an algorithm for merge sorting. Using the algorithm sort in ascending order: 10, 25, 16, 5, 35, 48, 8

Ans. Refer Q. 3.21.

Q. 9. How do you calculate the complexity of sorting algorithms? Also, write a recursive function in 'C' to implement the merge sort on given set of integers.

Ans. Refer Q. 3.22.

Q. 10. Write a short note on heap sort.

Ans. Refer Q. 3.23.

Q.11. Write a short note on radix sort.

Ans. Refer Q. 3.24.



Graphs

CONTENTS

		used with Graphs
Part-2	:	Data Structure for Graph

Part-1: Graphs: Terminology 4-2A to 4-4A

Matrices, Adjacency List, Adjacency

Part-3	:	Graph Traversal:	4-7A to	4-12A
		Depth First Search and		
		Breadth First Search,		
		0 1 0		

Connected Component

Prim's and Kruskal's Algorithm

Warshall Algorithm and Dijkstra Algorithm

PART-1

Graphs: Terminology used with Graph.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 4.1. What is a graph? Describe various types of graph. Briefly

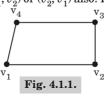
Answer

- 1. A graph is a non-linear data structure consisting of nodes and edges. A graph is a finite sets of vertices (or nodes) and set of edges which 2
- connect a pair of nodes.

explain few applications of graph.

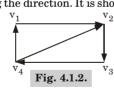
Types of graph: Undirected graph: 1.

- If the pair of vertices is unordered then graph G is called an
 - undirected graph. That means if there is an edge between v_1 and v_2 then it can be h. represented as (v_1, v_2) or (v_2, v_1) also. It is shown in Fig. 4.1.1.

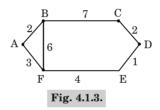


2. Directed graph:

- If the pair of vertices is ordered then graph G is called directed a. graph.
 - b. That is, a directed graph or digraph is a graph which has ordered pair of vertices (v_1, v_2) where v_1 is the tail and v_2 is the head of the edge.
 - If the graph is directed then the line segments of arcs have arrow c. heads indicating the direction. It is shown in Fig. 4.1.2.



3. Weighted graph: A graph is said to be a weighted graph if all the edges in it are labelled with some numbers. It is shown in the Fig. 4.1.3.



- 4. Simple graph : A graph or directed graph which does not have any self-loop or parallel edges is called a simple graph.
 5. Multi-graph : A graph which has either a self-loop or parallel edges or
- Multi-graph: A graph which has either a self-loop or parallel edges or both is called a multi-graph.
 Complete graph:
- a. A graph is complete graph if each vertex is adjacent to every other vertex in graph or there is an edge between any pair of nodes in the
 - graph.
 b. An undirected complete graph will contain n(n-1)/2 edges.

7. Regular graph:

- A graph is regular if every node is adjacent to the same number of nodes.
 - b. Here every node is adjacent to 3 nodes.



Fig. 4.1.4.

- 8. Planar graph: A graph is planar if it can be drawn in a plane without any two intersecting edges.
- 9. Connected graph:
 - a. In a graph G, two vertices v_1 and v_2 are said to be connected if there is path in G from v_1 to v_2 or v_2 to v_1 .
 - b. Connected graph can be of two types:
 - i. Strongly connected graph
 - ii. Weakly connected graph



(a) Connected graph



(b) Not connected graph

Fig. 4.1.5.

4-4	A (CS/IT-Sem-3) Graj	phs			
10.	Acyclic graph: If a graph (digraph) does not have any cycle then i called as acyclic graph.	t is			
12.	Cyclic graph : A graph that has cycles is called a cyclic graph. Biconnected graph : A graph with no articulation points is calle biconnected graph.	d a			
	lications of graph:	0110			
1.	Graph is a non-linear data structure and is used to present various operations and algorithms.	ous			
2.	Graphs are used for topological sorting.				
3.	Graphs are used to find shortest paths.				
4.	They are required to minimize some aspect of the graph, such as dista among all the vertices in the graph.	nce			
Qι	e 4.2. What is graph? Discuss various terminologies used	in			
gra	ph.				
Ar	swer				
Gra	ph : Refer Q. 4.1, Page 4–2A, Unit-4.				
	ious terminologies used in graphs are:				
1.	Self loop: If there is an edge whose starting and end vertices are sa	me			
2.	that is (v_2, v_2) is an edge then it is called a self loop or simply a loop. Parallel edges: A pair of edges e and e' of G are said to be parallel	iff			
	they are incident on precisely the same vertices.	. 111			
3.	Adjacent vertices: A vertex u is adjacent to (or the neighbour	of)			
	other vertex v if there is an edge from u to v .				
4.	Incidence: In an undirected graph the edge (u, v) is incident on verting u and v . In a digraph the edge (u, v) is incident from node u and incident to node v .				
5.	Degree of vertex : The degree of a vertex is the number of edges.	ges			
	incident to that vertex. In an undirected graph, the number of edconnected to a node is called the degree of that node.				
	PART-2				
	Data Structure for Graph Representations : Adjacency Matrices, Adjacency List, Adjacency.				
	Questions-Answers				
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	Long Answer Type and Medium Answer Type Questions				
Qu	e 4.3. Discuss the various types of representation of graph	1.			

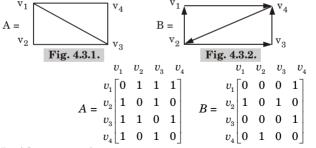
Answer

Two types of graph representation are as follows:

- Matrix representation: Matrices are commonly used to represent graphs for computer processing. Advantages of representing the graph in matrix lies on the fact that many results of matrix algebra can be readily applied to study the structural properties of graph from an algebraic point of view.
 - a. Adjacency matrix:
 - i. Representation of undirected graph: The adjacency matrix of a graph G with n vertices and no parallel edges is a $n \times n$ matrix $A = [a_{ij}]$ whose elements are given by $a_{ii} = 1$, if there is an edge between i^{th} and j^{th} vertices
 - = 0, if there is no edge between them
 ii. Representation of directed graph: The adjacency matrix of a digraph *D*, with *n* vertices is the matrix

$$A = [a_{ij}]_{n \times n}$$
 in which
 $a_{ij} = 1$ if arc (v_i, v_j) is in D
 $= 0$ otherwise

For example : Representation of following undirected and directed graph is :



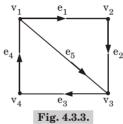
- b. Incidence matrix
 - i. Representation of undirected graph: Consider a undirected graph G = (V, E) which has n vertices and m edges all labelled. The incidence matrix $I(G) = [b_{ij}]$, is then $n \times m$ matrix, where

$$\begin{aligned} b_{ij} &= 1 & \text{ when edge } e_j \text{ is incident with } v_i \\ &= 0 & \text{ otherwise} \end{aligned}$$

ii. Representation of directed graph: The incidence matrix $I(D) = [b_{ij}]$ of digraph D with n vertices and m edges is the $n \times m$ matrix in which.

$$b_{ij} = 1$$
 if arc j is directed away from vertex v_i
= -1 if arc j is directed towards vertex v_i
= 0 otherwise.

Find the incidence matrix to represent the graph shown in Fig. 4.3.3.



The incidence matrix of the digraph of Fig. 4.3.3 is

$$I(D) = \begin{vmatrix} 1 & 0 & 0 & -1 & 1 \\ -1 & 1 & 0 & 0 & 0 \\ 0 & -1 & 1 & 0 & -1 \\ 0 & 0 & -1 & 1 & 0 \end{vmatrix}$$

2. Linked representation:

h.

- In linked representation, the two nodes structures are used:
 - For non-weighted graph: ล

INFO Adi-list For weighted graph: Weight INFO Adj-list

- where Adj-list is the adjacency list *i.e.*, the list of vertices which are adjacent for the corresponding node.
- The header nodes in each list maintain a list of all adjacent vertices ii of that node for which the header node is meant.
- iii. Suppose a directed graph

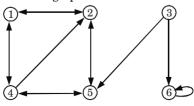
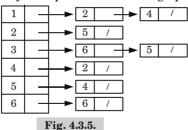


Fig. 4.3.4.

The adjacency list representation of this graph. iv.



Answer

1. Adjacency multilist representation maintains the lists as multilists, that

is, lists in which nodes are shared among several lists.
For each edge there will be exactly one node, but this node will be in two lists i.e., the adjacency lists for each of the two nodes, it is incident to.

The node structure now becomes:

Mark | vertex 1 | vertex 2 | path 1 | path 2

where mark is a one bit mark field that may be used whether or not the edge has been examined. The declarations in C are :

#define n 20
typedef struct edge {BOOLEAN mark;

int vertex1, vertex2;
NEXTEDGE path1, path2:

*NEXTEDGE;
NEXTEDGE headnode [n]:

PART-3

Graph Traversal: Depth First Search and Breadth First Search, Connected Component.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Graph is represented by its nodes and edges, so traversal of each node is

Que 4.5. Write a short note on graph traversal.

Answer

Traversing a graph:

i.

- the traversing in graph.
- ii. There are two standard ways of traversing a graph.
- iii. One way is called a breadth first search, and the other is called a depth first search.
- iv. During the execution of our algorithms, each node N of G will be in one of three states, called the status of N, as follows:
- $\begin{array}{ll} \text{Status} = 1 & \Rightarrow (\text{Ready state}). \text{ The initial state of the node } N. \\ \text{Status} = 2 & \Rightarrow (\text{Waiting state}). \text{ The node } N \text{ is on the queue or stack, waiting to be processed.} \\ \text{Status} = 3 & \Rightarrow (\text{Processed state}). \text{ The node } N \text{ has been} \end{array}$

processed.

search beginning at a starting node A is as follows: First we examine the starting node A.

to be processed, and by using a field STATUS which tells us the current status of any node.

Breadth First Search (BFS): The general idea behind a breadth first

Graphs

Algorithm: This algorithm executes a breadth first search on a graph G beginning at a starting node A. Initialize all nodes to ready state (STATUS=1). ii Put the starting node A in queue and change its status to the waiting

state (STATUS = 2) Repeat steps (iv) and (v) until queue is empty. iii

4_8 A (CS/IT-Som-3)

1.

2.

ล

Remove the front node N of queue. Process N and change the status of iv. N to the processed state (STATUS = 3). Add to the rear of queue all the neighbours of *N* that are in the ready v.

(STATUS = 2).[End of loop] vi. End

state (STATUS=1) and change their status to the waiting state

Depth First Search (DFS): The general idea behind a depth first

search beginning at a starting node A is as follows: First, we examine the starting node A. ล. Then, we examine each node N along a path P which begins at A; h.

that is, we process neighbour of A, then a neighbour of neighbour of A, and so on. This algorithm uses a stack instead of queue.

Algorithm: Initialize all nodes to ready state (STATUS = 1). i.

ii Push the starting node A onto stack and change its status to the waiting

state (STATUS = 2). Repeat steps (iv) and (v) until queue is empty. iii.

Pop the top node N of stack, process N and change its status to the iv.

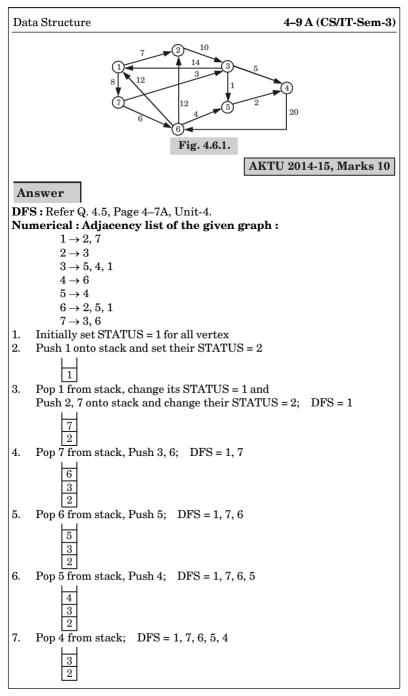
(STATUS = 2).

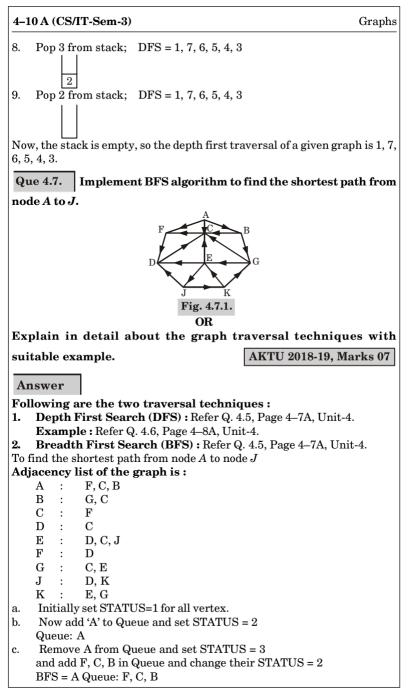
processed state (STATUS = 3). Push onto stack all the neighbours of *N* that are still in the ready state v. (STATUS = 1) and change their status to the waiting state

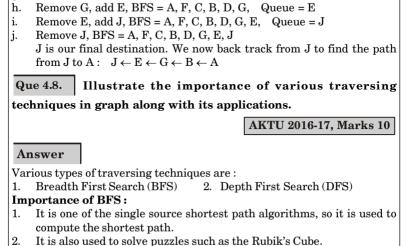
[End of loop] vi. End. Write and explain DFS graph traversal algorithm. Que 4.6.

OR

Write DFS algorithm to traverse a graph. Apply same algorithm for the graph given in Fig. 4.6.1 by considering node 1 as starting node.







BFS is not only the quickest way of solving the Rubik's Cube, but also

Finding the shortest path between two nodes u and v, with path length

measured by number of edges (an advantage over depth first search). Ford-Fulkerson method for computing the maximum flow in a flow

Application of BFS: Breadth first search can be used to solve many problems

Remove C, add F, but F is already visited. So no vertex will be added in

BFS = A, F, Queue = B. D

Remove B, add G, BFS = A, F, C, B, Queue = D, G

Remove D. BFS = A, F, C, B, D, Queue = G

4-11 A (CS/IT-Sem-3)

- Serialization/Deserialization of a binary tree vs serialization in sorted 4. order, allows the tree to be re-constructed in an efficient manner.
- 5. Construction of the failure function of the Aho-Corasick pattern matcher.
- Testing bipartiteness of a graph. **Importance of DFS:** DFS is very important algorithm as based upon DFS.

the most optimal way of solving it.

in graph theory, for example:

network.

Copying garbage collection.

Data Structure

this step

Remove F. add D in Queue BFS = A, F Queue = C, B, D,

Ы

e

f

g.

h

3.

1

2.

3.

- there are O(V + E)-time algorithms for the following problems : Testing whether graph is connected. 1.
- 2. Computing a spanning forest of G. Computing the connected components of G. 3.
- 4.
- Computing a path between two vertices of G or reporting that no such path exists. Computing a cycle in *G* or reporting that no such cycle exists. 5.

Que 4.9. Define connected component and strongly connected component. Write an algorithm to find strongly connected components.

Answer

2.

3.

Connected component: Connected component of an undirected graph is a sub-graph in which any two vertices are connected to each other by paths, and which is connected to no additional vertices in the super graph. **Strongly connected component:** A directed graph is strongly connected if there is a path between all pairs of vertices. A strong component is a

maximal subset of strongly connected vertices of subgraph. Kosaraju's algorithm is used to find strongly connected components in a graph.

For each vertex u of the graph, mark u as unvisited. Let L be empty. For each vertex u of the graph do Visit(u), where Visit(u) is the recursive

For each element u of L in order, do Assign(u, u) where Assign (u, root)

Kosaraju's algorithm :

- subroutine. If u is unvisited then:
- a. Mark u as visited.
- b. For each out-neighbour *v* of *u*, do Visit(*v*).c. Prepend *u* to *L*. Otherwise do nothing.
- is the recursive subroutine. If \boldsymbol{u} has not been assigned to a component then :
- a. Assign *u* as belonging to the component whose root is root.
- b. For each in-neighbour v of u, do Assign (v, root).

Otherwise do nothing.

PART-4

Spanning Tree, Minimum Cost Spanning Trees : Prim's and Kruskal's Algorithm.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 4.10. What do you mean by spanning tree and minimum

spanning tree?

Answer

Spanning tree:

- 1 A spanning tree of an undirected graph is a sub-graph that is a tree which contains all the vertices of graph.
- A spanning tree of a connected graph G contains all the vertices and has 2 the edges which connect all the vertices. So, the number of edges will be 1 less than the number of nodes.
- If graph is not connected, *i.e.*, a graph with *n* vertices has edges less than 3. n-1 then no spanning tree is possible.
- A connected graph may have more than one spanning trees.
- Minimum spanning tree: In a weighted graph, a minimum spanning tree is a spanning tree that has minimum weight than all other spanning trees of the same graph.
- 2. There are number of techniques for creating a minimum spanning tree for a weighted graph but the most famous methods are Prim's and Kruskal's algorithm.

Que 4.11. Write down Prim's algorithm to find out minimal spanning tree.

Answer

First it chooses a vertex and then chooses an edge with smallest weight incident on that vertex. The algorithm involves following steps:

Step 1: Choose any vertex V_1 of G.

Step 2: Choose an edge $e_1 = V_1^{\mathsf{T}} V_2$ of G such that $V_2 \neq V_1$ and e_1 has smallest weight among the edge e of G incident with V_1 .

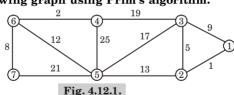
Step 3: If edges e_1, e_2, \dots, e_i have been chosen involving end points V_1, V_2, \dots

...... V_{i+1} , choose an edge $e_{i+1} = V_j V_k$ with $V_j = \{V_1, \dots, V_{i+1}\}$ and $V_k \notin \{V_1, \dots, V_{i+1}\}$ such that e_{i+1} has smallest weight among the edges of G with precisely one end in $\{V_1, \dots, V_{i+1}\}$.

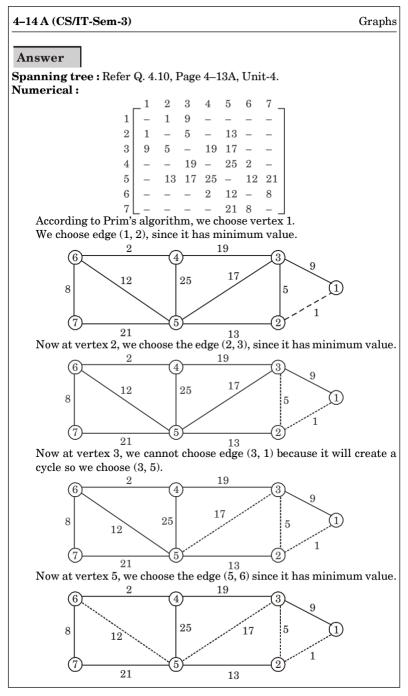
Step 4: Stop after n-1 edges have been chosen. Otherwise goto step 3.

Define spanning tree. Find the minimal spanning tree Que 4.12.

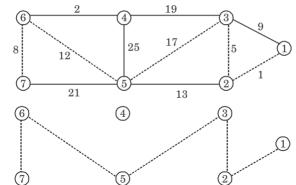
for the following graph using Prim's algorithm.



AKTU 2014-15, Marks 10



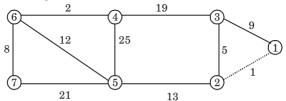
Now at vertex 6, we choose the edge (6, 7) since it has minimum value.



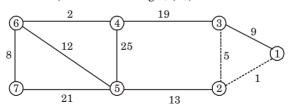
Since in spanning tree, the tree should cover all the vertices and should not make cycle.

But in the above tree, 4 is remaining so the above asked question is wrong. If we assume to remove the edge from {3, 5} then the spanning tree is:

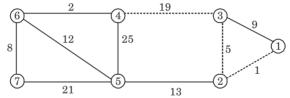
According to Prim's algorithm, let's choose vertex 1. We choose edge {1, 2}, since it has minimum value.



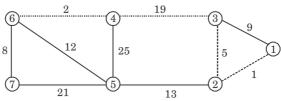
Now at vertex 2, we choose the edge (2,3), since it has minimum value.



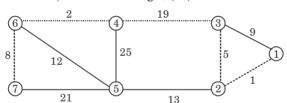
Now at vertex 3, we choose the edge (3, 4), since it has minimum value.



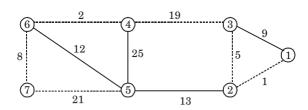
Now at vertex 4, we choose the edge (4, 6), since it has minimum value.



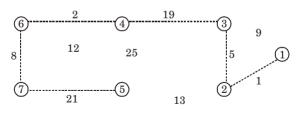
Now at vertex 6, we choose the edge (6, 7), since it has minimum value.



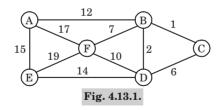
Now at vertex 7, we cannot choose the edge (7, 6), because we have already traversed this edge these we choose (7, 5).



 \therefore The spanning tree is



Que 4.13. Define spanning tree. Also construct minimum spanning tree using Prim's algorithm for the given graph.

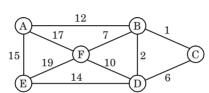


AKTU 2017-18, Marks 07

Answer

Spanning tree: Refer Q. 4.10, Page 4–13A, Unit-4.

Numerical:



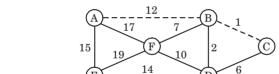
Let us take A as source node.

Now we look on weight

w(A, B) = 12, w(A, F) = 17, w(A, E) = 15

$$w(A, B)$$
 is smallest. Choose $e = (AB)$

Now we look on weight

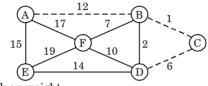


Now we look on weight w(C, D) = 6

w(C, D) is smallest condots choose e = (CD)



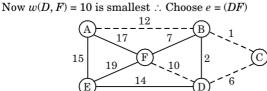
Graphs



Now we look on weight

w(D, B) = 2, w(D, F) = 10, w(D, E) = 14

w(D, B) is smallest but forms a cycle Discard it.



Now we look on weight

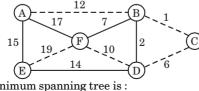
w(F, B) = 7, w(F, A) = 17, w(F, E) = 19w(F, B) is smallest but forms cycle

Discard it

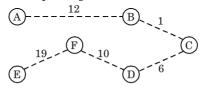
w(F, A) is smallest but forms cycle

Discard it.

choose e = (FE)



The final minimum spanning tree is:



Que 4.14. Write Kruskal's algorithm to find minimum spanning tree.

Answer

- In this algorithm, we choose an edge of G which has smallest weight i. among the edges of G which are not loops.
- ii. This algorithm gives an acyclic subgraph T of G and the theorem given below proves that T is minimal spanning tree of G. Following steps are required:

Step 1: Choose e_1 , an edge of G, such that weight of e_1 , $w(e_1)$ is as small as possible and e_1 is not a loop.

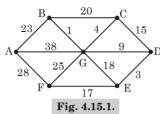
Step 2: If edges e_1, e_2, \dots, e_i have been selected then choose an edge e_{i+1} not already chosen such that

i. the induced subgraph, $G[\{e_1, ..., e_{i+1}\}]$ is acyclic and ii. $w(e_{i+1})$ is as small as possible

Step 3: If *G* has *n* vertices, stop after n-1 edges have been chosen. Otherwise repeat step 2.

If G be a weighted connected graph in which the weight of the edges are all non-negative numbers, let T be a sub-graph of G obtained by Kruskal's algorithm then, T is minimal spanning tree.

Que 4.15. Consider the following undirected graph.



a. Find the adjacency list representation of the graph.b. Find a minimum cost spanning tree by Kruskal's algorithm.

AKTU 2015-16, Marks 10

Answer

a.

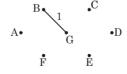
b.



Fig. 4.15.2.

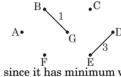
Kruskal's algorithm:

We will choose e = BG as it has minimum weight.

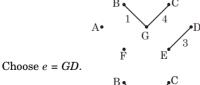


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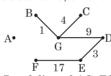
ii. Now choose e = ED.



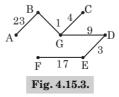
iii. Choose e = CG, since it has minimum weights.



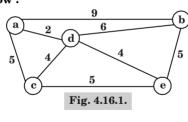
v. Choose e = EF and discard BC, CD and GE because they form cycle.



vi. Now choose e = AB and discard AG, FG and AF because they form cycle. Final minimum spanning tree is given as:



Que 4.16. What is spanning tree? Describe Kruskal's and Prim's algorithm to find the minimum cost spanning tree and explain the complexity. Determine the minimum cost spanning tree for the graph given below:



Answer

Spanning tree: Refer Q. 4.10, Page 4–13A, Unit-4. Kruskal's algorithm: Refer Q. 4.14, Page 4–18A, Unit-4.

Prim's algorithm: Refer Q. 4.11, Page 4–13A, Unit-4.

Complexity:

1

- A. Time complexity of Prim's algorithm:
 - The time complexity of Prim's algorithm depends on the data structures used for the graph and for ordering the edges by weight.
 A simple implementation of Prim's, using an adjacency matrix or an
 - adjacency list graph representation and linearly searching an array of weights to find the minimum weight edge to add, requires O(|V|2) running time.

B. Time complexity of Kruskal's algorithm:

the graph and V is the number of vertices, all with simple data structures.

2. These running times are equivalent because:

Kruskal's algorithm can be shown to run in $O(E \log E)$ time, or

equivalently, $O(E \log V)$ time, where E is the number of edges in

a. E is at most V^2 and $\log V^2 = 2 \log V$ is $O(\log V)$. b. Each isolated vertex is a separate component of the minimum

spanning forest. If we ignore isolated vertices we obtain $V \leq$

Numerical: Let us take 'a' as a source node

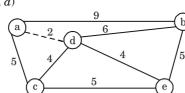
Let us take 'a' as a source node

Now look on weight

w(a, d) = 2, w(a, b) = 9 w(a, c) = 5

2E, so $\log V$ is $O(\log E)$.

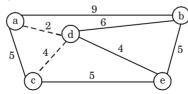
w(a, d) is smallest. choose e = (a, d)



Now look on weight

$$w(d, b) = 6, w(d, c) = 4, w(d, e) = 4$$

- w(d, c) is smallest. choose e = (d, c)
- \therefore Choose e = (d, c)



5

2

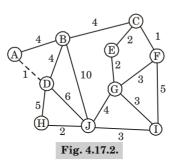
Fig. 4.17.1.

3

Answer

Prim's algorithm:

According to algorithm we choose vertex A from the set $\{A, B, C, D, E,$ F, G, H, I, J.



Now edge with smallest weight incident on A is e = (AD)2.

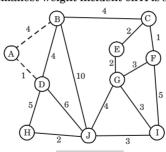


Fig. 4.17.3.

Now we look on weight

We choose e = AB since it is minimum.

w(D, B) can also be chosen because it has same value.

w(B, C) = 4, w(B, J) = 10, w(D, H) = 5, w(D, J) = 6Again,

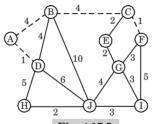


Fig. 4.17.5.

We choose e = BC since it has minimum value. Now, w(B, J) = 10, w(C, E) = 2, w(C, F) = 1We choose e = CF because w(C, F) has minimum value. Now, w(C, E) = 2, w(F, G) = 3, w(F, I) = 5

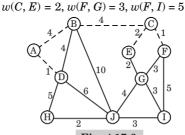


Fig. 4.17.6.

We choose e = CE, since w(C, E) has minimum value. w(E, G) = 2, w(F, G) = 3, w(F, I) = 5

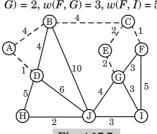
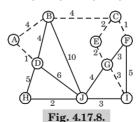
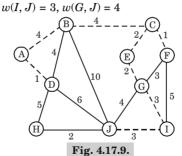


Fig. 4.17.7.

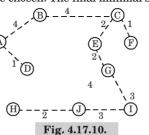
We choose e = EG, since w(E, G) has minimum value. w(G, J) = 4, w(G, I) = 3, w(F, I) = 5



We choose e = GI, since w(G, I) has minimum value.



We choose e = IJ, since w(I, J) has minimum value, w(J, H) = 2Hence, e = JH will be chosen. The final minimal spanning tree is:



r 1g

Kruskal's algorithm:

i. We will choose e = AD and CF as it has minimum weight.

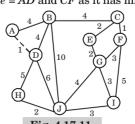
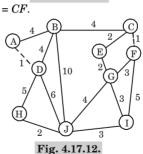
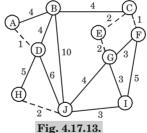


Fig. 4.17.11.

ii. Now choose e = CF.



iii. Choose CE, EG and HJ since they have same and minimum weights.



iv. Choose IJ and GI as it has minimum weight and discard GF because it forms cycle.

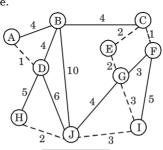
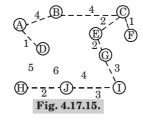


Fig. 4.17.14.

v. Choose AB and BC and discard BD, GJ, DH, DJ, BJ, FI because they form cycle.

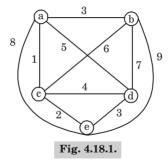
We get the final minimal spanning tree as



Que 4.18. Discuss Prim's and Kruskal's algorithm. Construct minimum spanning tree for the below given graph using Prim's

algorithm (Source node = a).

AKTU 2016-17, Marks 15



Answer

 $\textbf{Prim's algorithm:} \ \text{Refer Q. 4.11, Page 4-13A, Unit-4.}$

Kruskal's algorithm: Refer Q. 4.14, Page 4–18A, Unit-4.

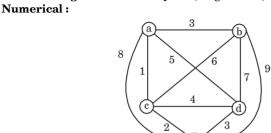


Fig. 4.18.2.

Start with source node = a

Now, edge with smallest weight incident on a is e = (a, c).

So, we choose e = (a, c).

Now we look on weights : w(c, d) = 4, w(c, e) = 2, w(c, b) = 5

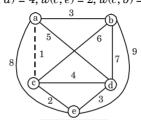


Fig. 4.18.3.

Since minimum is w(c, e) = 2. We choose e = (c, e)Again, w(e, d) = 3

$$w(e, a) = 8$$

w(e,b)=7

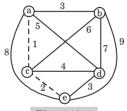


Fig. 4.18.4.

Since minimum is w(e, d) = 3, we choose e = (e, d)

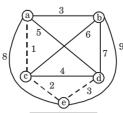


Fig. 4.18.5.

Now, w(d, b) = 7, and w(a, b) = 3Since minimum is w(a, b) = 3, we choose e = (a, b)

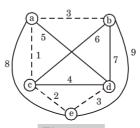
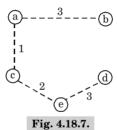


Fig. 4.18.6.

Therefore, the minimum spanning tree is :



PART-5

Transitive Closure and Shortest Path Algorithm : Warshall Algorithm and Dijkstra Algorithm.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 4.19. Explain transitive closure.

Answer

- The transitive closure of a graph G is defined to be the graph G' such that G' has the same nodes as G and there is an edge (v_i, v_j) in G' whenever there is a path from v_i to v_j in G.
 Accordingly the path matrix P of the graph G is precisely the adjacency
- matrix of its transitive closure G'.

 3. The transitive closure of a graph G is defined as G^* or $G' = (V, E^*)$. where, $E^* = \{(i, j) \text{ there is a path from vertex } i \text{ to } i$
- vertex j in G}

 4. We construct the transitive closure $G^* = (V, E^*)$ by putting edge (i, j) into E^* if and only if $t_{ij}(n) = 1$.
- 5. The recursive definition of $t_{ij}^{(k)}$ is

$$t_{ij}^{(0)} = \begin{cases} 0 \text{ if } i \neq j \text{ and } (i,j) \notin E \\ 1 \text{ if } i = j \text{ or } (i,j) \in E \end{cases}$$

and for $k \ge 1$

$$t_{ij}^{(k)} = t_{ij}^{(k-1)} \vee (t_{ik}^{(k-1)} \wedge t_{kj}^{(k-1)})$$

Que 4.20. Write down Warshall's algorithm for finding all pair shortest path.

Answer

1.

shortest paths in a weighted, directed graph.

2. A single execution of the algorithm will find the shortest path between all pairs of vertices.

Floyd Warshall algorithm is a graph analysis algorithm for finding

- 3. It does so in $\Theta(V^3)$ time, where V is the number of vertices in the graph.
- 4. Negative-weight edges may be present, but we shall assume that there are no negative-weight cycles.

 $\{v_0, v_0, ..., v_{m-1}\}.$ Let the vertices of G be $V = \{1, 2, ..., n\}$, and consider a subset 6 $\{1, 2, \dots, k\}$ of vertices for some k. 7

The algorithm considers the "intermediate" vertices of a shortest path. where an intermediate vertex of a simple path $p = (v_1, v_0, ..., v_m)$ is any vertex of p other than v_1 or v_m , that is, any vertex in the set

- For any pair of vertices $i, j \in V$, consider all paths from i to j whose intermediate vertices are all drawn from $\{1, 2, \dots, k\}$, and let p be a minimum-weight path from among them.
- 8. Let $d_{ii}^{(k)}$ be the weight of a shortest path from vertex i to vertex j with all intermediate vertices in the set $\{1, 2, ..., k\}$.

$$d_{ij}^{(k)} = egin{cases} w_{ij} & ext{if } k=0 \ \min(d_{ij}^{(k-1)}, d_{ik}^{(k-1)} + d_{kj}^{(k-1)}) & ext{if } k \geq 1 \end{cases}$$

A recursive definition is given by

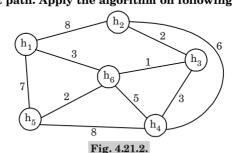
Flovd Warshall (w):

1 $n \leftarrow \text{rows}[w]$ 2 $D^{(0)} \leftarrow w$

5

- 3 for $k \leftarrow 1$ to n
- 4 do for $i \leftarrow 1$ to n
- 5. do for $i \leftarrow 1$ to n
- do $d_{ii}^{(k)} \leftarrow \min(d_{ij}^{(k-1)}, d_{ik}^{(k-1)} + d_{kj}^{(k-1)})$ 6
- 7 return $D^{(n)}$

Que 4.21. Write the Floyd Warshall algorithm to compute the all pair shortest path. Apply the algorithm on following graph:



AKTU 2018-19, Marks 07

Answer

Floyd's Warshall algorithm: Refer Q. 4.20, Page 4-29A, Unit-4. Numerical: We cannot solve this using Floyd Warshall algorithm because the given graph is undirected.

Que 4.22. Write and explain Dijkstra's algorithm for finding shortest path.

OR
Write and explain an algorithm for finding shortest path between any two nodes of a given graph.

Answer

e.

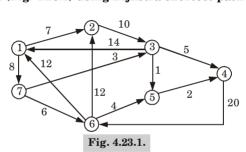
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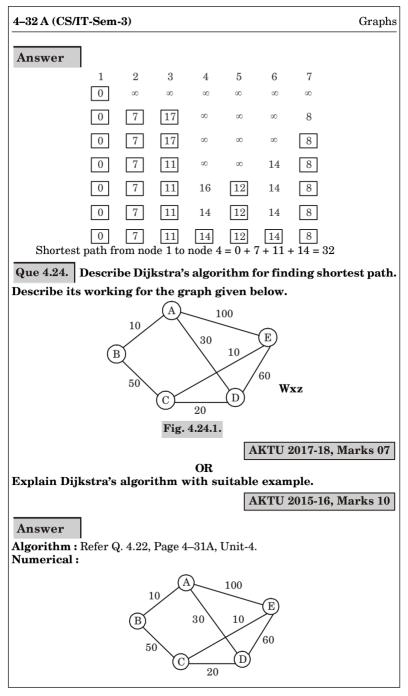
g.

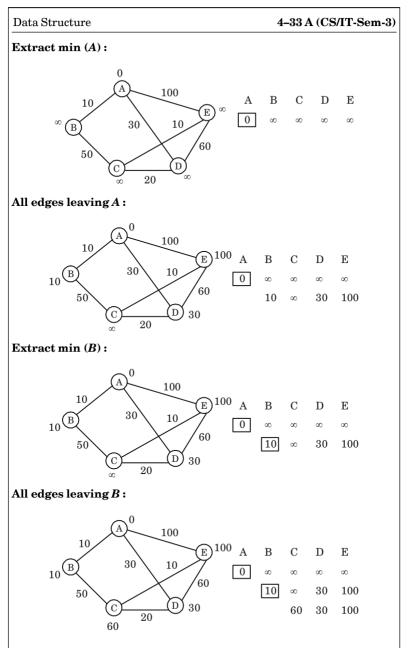
- a. Dijkstra's algorithm, is a greedy algorithm that solves the single-source shortest path problem for a directed graph G = (V, E) with non-negative edge weights, i.e., we assume that $w(u, v) \ge 0$ each edge $(u, v) \in E$.
- b. Dijkstra's algorithm maintains a set S of vertices whose final shortest-path weights from the source s have already been determined.
- c. That is, for all vertices $v \in S$, we have $d[v] = \delta(s, v)$.

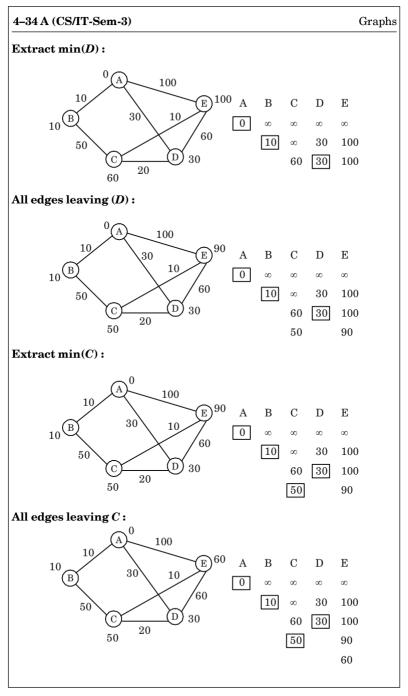
 d. The algorithm repeatedly selects the vertex $u \in V S$ with the minimum
 - shortest-path estimate, inserts u into S, and relaxes all edges leaving u. We maintain a priority queue Q that contains all the vertices in v-s, keved by their d values.
 - Graph G is represented by adjacency list. Dijkstra's always chooses the "lightest or "closest" vertex in V - S to
 - insert into set S, that it uses as a greedy strategy. DIJKSTRA (G, w, s)
 - 1. INITIALIZE-SINGLE-SOURCE (G, s)
 - 2. $S \leftarrow \phi$
 - 3. $Q \leftarrow V[G]$ 4. while $Q \neq \emptyset$
 - 5. do $u \leftarrow \text{EXTRACT-MIN}(Q)$
 - 6. $S \leftarrow S \cup \{u\}$
 - 7. for each vertex $v \in Adi[u]$
 - 8. do RELAX (u, v, w)

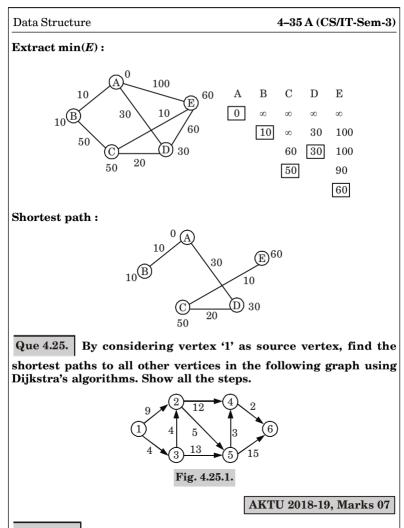
Que 4.23. Find out the shortest path from node 1 to node 4 in a given graph (Fig. 4.23.1) using Dijkstra shortest path algorithm.





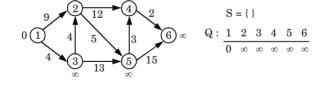


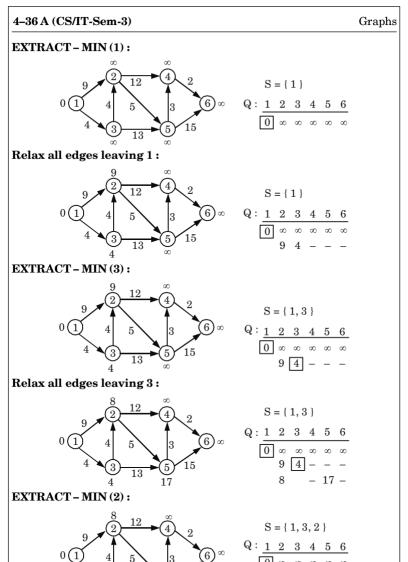




Answer

Initialize:





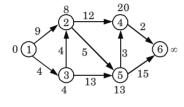
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 $0 \propto \propto \propto \propto \propto$



4-37 A (CS/IT-Sem-3)

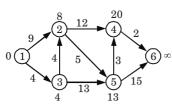
Relax all edges leaving 2:



$$Q: \underbrace{1 \ 2 \ 3 \ 4 \ 5 \ 6}_{0 \ \infty \ \infty \ \infty \ \infty \ \infty \ \infty} = \underbrace{0 \ 4 \ - \ - \ -}_{20 \ 13 \ -}$$

 $S = \{1, 3, 2\}$

EXTRACT - MIN (5):

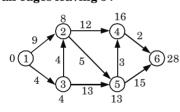


$$S = \{1, 3, 2, 5\}$$

$$Q : \underbrace{1 \ 2 \ 3 \ 4 \ 5 \ 6}_{0 \ \infty \ \infty \ \infty \ \infty \ \infty}$$

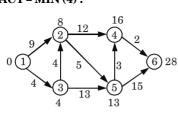
$$9 \ \underbrace{4}_{0 \ -17 \ -20}_{0 \ 13 \ -1}$$

Relax all edges leaving 5:

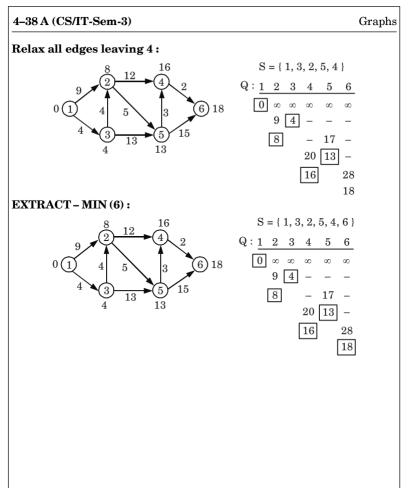


 $S = \{1, 3, 2, 5\}$

EXTRACT - MIN (4):



 $S = \{1, 3, 2, 5, 4\}$

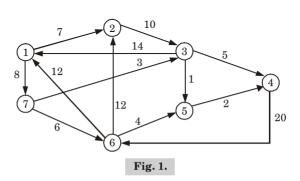


VERY IMPORTANT QUESTIONS

Following questions are very important. These questions may be asked in your SESSIONALS as well as

UNIVERSITY EXAMINATION

Q. 1. Write DFS algorithm to traverse a graph. Apply same algorithm for the graph given in Fig. 1 by considering node 1 as starting node.

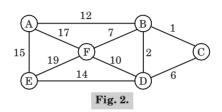


Ans. Refer Q. 4.6.

Q. 2. Illustrate the importance of various traversing techniques in graph along with its applications.

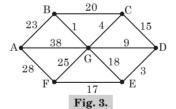
Ans. Refer Q. 4.8.

Q. 3. Define spanning tree. Also construct minimum spanning tree using Prim's algorithm for the given graph.



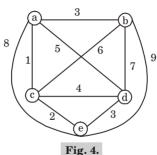
Ans. Refer Q. 4.13.

- Q.4. Consider the following undirected graph.
 - a. Find the adjacency list representation of the graph.
 b. Find a minimum cost spanning tree by Kruskal's algorithm.



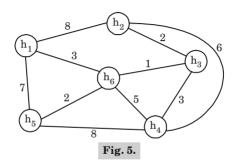
Ans. Refer Q. 4.15.

Q. 5. Discuss Prim's and Kruskal's algorithm. Construct minimum spanning tree for the below given graph using Prim's algorithm (Source node = a).



Ans. Refer Q. 4.18.

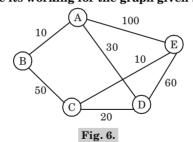
Q. 6. Write the Floyd Warshall algorithm to compute the all pair shortest path. Apply the algorithm on following graph:



Ans. Refer Q. 4.21.

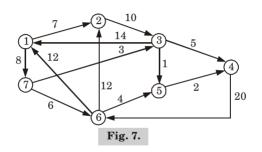
Q. 7. Describe Dijkstra's algorithm for finding shortest path.

Describe its working for the graph given below.



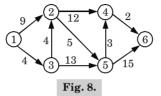
Ans. Refer Q. 4.24.

Q. 8. Find out the shortest path from node 1 to node 4 in a given graph (Fig. 7) using Dijkstra shortest path algorithm.



Ans. Refer Q. 4.23.

Q. 9. By considering vertex '1' as source vertex, find the shortest paths to all other vertices in the following graph using Dijkstra's algorithms. Show all the steps.



Ans. Refer Q. 4.25.



Trees

CONTENTS					
Part-1	:	Basic Terminology Used With			
Part-2	:	Binary Search Tree, Strictly			
Part-3	:	Tree Traversal Algorithm:			
Part-4	:	Operation of Insertion, Deletion, 5-19A to 5-22A Searching and Modification of Data in Binary Search			
Part-5	:	Threaded Binary Trees,			
Part-6	:	Concept and Basic			

PART-1

Basic Terminology used with Tree, Binary Trees, Binary Tree Representation: Array Representation and Pointer (Linked List) Representation

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 5.1. Explain the following terms:

- Vertex of Tree i. Tree ii. iii. Depth iv. Degree of an element
- Degree of Tree v. wi. Leaf

Answer

i.

- **Tree:** A tree T is a finite non-empty set of elements. One of these elements is called the root, and the remaining elements, if any is partitioned into trees is called subtree of T. A tree is a non-linear data structure.
- ii. **Vertex of tree:** Each node of a tree is known as vertex of tree.

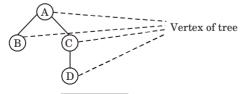
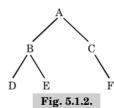


Fig. 5.1.1.

iii. Depth: The depth of binary tree is the maximum level of any leaf in the tree. This equals the length of the longest path from the root to any leaf. Depth of Fig. 5.1.2 tree is 2.



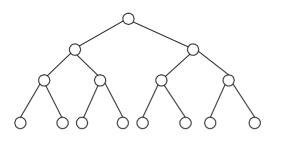
iv. **Degree of an element:** The number of children of node is known as degree of the element.

- v. Degree of tree: In a tree, node having maximum number of degree is known as degree of tree.
- vi. Leaf: A terminal node in tree is known as leaf node or a node which has no child is known as leaf node.

Que 5.2. Show that the maximum number of nodes in a binary tree of height h is $2^{h+1}-1$.

Answer

If we consider the maximum nodes in a tree then all leaves will have the same depth and all internal nodes have left child and right child both.



Node depth $0 2^0 = 1$

depth 1 $2^1 = 2$ depth 2 $2^2 = 4$

depth 3 $2^3 = 8$

Fig. 5.2.1.

- 1. The root has 2 children at depth 1, each of which has 2 children at depth 2 i.e. , 4.
- 2. Thus, the number of leaves at depth h is 2^h , so we can calculate the maximum number of nodes in a binary tree as:

$$= 1 + 2 + 4 + 8 + 16 + \dots 2^{h}$$

$$= 2^{0} + 2^{1} + 2^{2} + 2^{3} + \dots 2^{h}$$

$$= \sum_{i=1}^{h} 2^{i} = \frac{2^{h+1} - 1}{2 - 1} = 2^{h+1} - 1$$

Thus, a binary tree having height h, has $2^{h+1}-1$ maximum number of nodes.

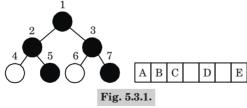
Que 5.3. Explain binary tree representation using array.

Answer

- 1. In an array representation, nodes of the tree are stored level-by-level, starting from $0^{\rm th}$ level.
- 2. Missing elements are represented by white boxes.
- 3. This representation scheme is wasteful of space when many elements are missing.
- 4. In fact, a binary tree that has n-elements may require an array of size up to 2^n (including position 0) for its representation.

5-4 A (CS/IT-Sem-3)

- This maximum size is needed when each element (except the root) of the *n*-element binary tree is the right child of its parent. 6
- Fig. 5.3.1, shows such a binary tree with four elements. Binary trees of this type are called right-skewed binary trees.



Que 5.4. Explain binary tree representation using linked list.

Answer

1

3

4.

- Consider a binary tree T which uses three parallel arrays, INFO, LEFT and RIGHT, and a pointer variable ROOT. 2
 - First of all, each node N of T will correspond to a location K such that: INFO[K] contains the data at the node N
 - LEFT[K] contains the location of the left child of node N. h RIGHT[K] contains the location of the right child of node N.
 - ROOT will contain the location of the root R of T
 - If any subtree is empty, then the corresponding pointer will contain the null value.
- If the tree *T* itself is empty, then ROOT will contain the null value. 5.
- INFO may actually be a linear array of records or a collection of parallel 6. arrays.

Que 5.5. Write a C program to implement binary tree insertion,

deletion with example.

AKTU 2016-17, Marks 10

Answer

if(!(*tree))

#include<stdlib.h> #include<stdio h> struct bin_tree { int data: struct bin tree *right, *left; typedef struct bin_tree node; void insert(node *tree, int val) node *temp = NULL;

```
Data Structure
                                                       5-5 A (CS/IT-Sem-3)
temp = (node *)malloc(sizeof(node)):
temp->left = temp->right = NULL:
temp->data = val:
*tree = temp:
return:
if(val < (*tree)->data)
insert(&(*tree)->left, val);
else if(val > (*tree)->data)
insert(&(*tree)->right, val);
void print inorder(node *tree)
if (tree)
print inorder(tree->left):
printf("%d\n",tree->data);
print inorder(tree->right):
void deltree(node *tree)
if (tree)
deltree(tree->left):
deltree(tree->right):
free(tree):
void main()
node *root;
node *tmp;
//int i:
root = NULL:
/* Inserting nodes into tree */
insert(&root, 9);
insert(&root, 4);
insert(&root, 15);
insert(&root, 6);
insert(&root, 12):
insert(&root, 17);
insert(&root, 2);
```

```
Trees
5-6 A (CS/IT-Sem-3)
/* Printing nodes of tree */
printf("After insertion inorder display\n"):
print inorder(root):
/* Deleting all nodes of tree */
deltree(root)
printf("Tree is empty");
Output of program:
After insertion inorder display
4
6
q
12
15
17
Tree is empty.
Que 5.6.
            Write the C program for various traversing techniques
                                             AKTU 2016-17, Marks 10
of binary tree with neat example.
Answer
#include<stdio h>
#include<stdlib.h>
struct node
int value:
node* left;
node* right;
struct node* root;
struct node* insert(struct node* r. int data):
void inorder(struct node* r):
void preorder(struct node* r):
void postorder(struct node* r):
int main()
root = NULL;
int n, v;
printf("How many data do you want to insert ?\n");
scanf("%d", &n);
for(int i=0; i< n; i++){
printf("Data %d: ", i+1);
scanf("%d", &v):
root = insert(root, v);
```

```
Data Structure
                                                       5-7 A (CS/IT-Sem-3)
printf("Inorder Traversal:"):
inorder(root)
printf("\n"):
printf("Preorder Traversal:"):
preorder(root):
printf("\n"):
printf("Postorder Traversal :");
postorder(root):
printf("\n"):
return 0:
struct node* insert(struct node* r. int data)
if(r==NIII.L)
r = (struct node*) malloc(sizeof(struct node)):
r->value = data:
r > left = NULL:
r->right = NULL:
else if(data < r->value){
r > left = insert(r > left, data):
else {
r->right = insert(r->right, data);
return r:
void inorder(struct node* r)
if(r!=NULL){
inorder(r->left);
printf("%d", r->value);
inorder(r->right);
void preorder(struct node* r)
if(r!=NULL){
printf("%d", r->value);
preorder(r->left);
preorder(r->right);
void postorder(struct node* r)
```

5-8	A (CS/IT-Sem-3) Trees					
post	=NULL){ order(r->left); order(r->right); tf("%d", r->value);					
) Out	put :					
Hov 5	many data do you want to insert ?					
3 2	order Traversal : 4 5 der Traversal :					
	3 4 5 order Traversal : 3 4 3					
1	PART-Z Binary Search Tree, Strictly Binary Tree, Complete Binary Tree, A Extended Binary Tree.					
	V					
	Questions-Answers					
	Long Answer Type and Medium Answer Type Questions					
Qu	e 5.7. Explain binary search tree and its operations. Make a					
	binary search tree for the following sequence of numbers, show all steps: 45, 32, 90, 34, 68, 72, 15, 24, 30, 66, 11, 50, 10.					
	AKTU 2015-16, Marks 10					
An	swer					
Bin	ary search tree:					
1. 2.	A binary search tree is a binary tree. Binary search tree can be represented by a linked data structure in which each node is an object.					
3.	In addition to a key field, each node contains fields left, right and P , which point to the nodes corresponding to its left child, its right child and its parent respectively.					
4.	A non-empty binary search tree satisfies the following properties: a. Every element has a key (or value) and no two elements have the same value.					
	b. The keys, if any, in the left subtree of root are smaller than the key in the node.					

я.

4

5

h.

c.

1 2.

3 4.

5.

6.

7.

8

9.

do $v \leftarrow x$

5-9 A (CS/IT-Sem-3)

The left and right subtrees of the root are also binary search tree. Ы Various operations of BST are :

Searching in a BST: Searching for a data in a binary search tree is much faster than in

arrays or linked lists. The TREE-SEARCH (x, k) algorithm searches the tree root at x for a node whose key value equals to k. It returns a pointer to the node if it exist otherwise NIL. TREE-SEARCH (x, k)

If x = NIL or k = kev [x]1 2. then return x3. If k < key [x]

then return TREE-SEARCH (left [x], k) else return TREE-SEARCH (right [x], k) Traversal operation on BST:

All the traversal operations are applicable in binary search trees. The in ascending (increasing) order.

inorder traversal on a binary search tree gives the sorted order of data Insertion of data into a binary search tree:

To insert a new value w into a binary search tree T, we use the procedure TREE-INSERT. The procedure passed a node *z* for which kev[z] = w. left [z] = NIL and Right [z] = NIL.

 $v \leftarrow NII$ $x \leftarrow \text{root} [T]$ while $r \neq NII$.

if kev [z] < kev [x]then $x \leftarrow \text{left } [x]$

else $x \leftarrow \text{right } [x]$

 $P[z] \leftarrow v$ if v = NIL

10. then root $|T| \leftarrow z$ else if key [z] < key [y]11 then left $[v] \leftarrow z$

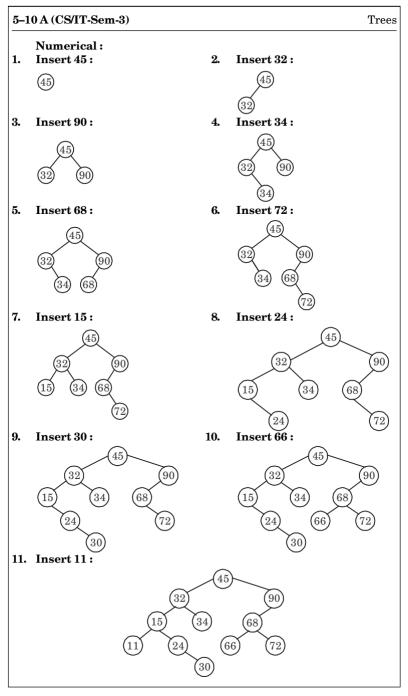
12. else right $[v] \leftarrow z$

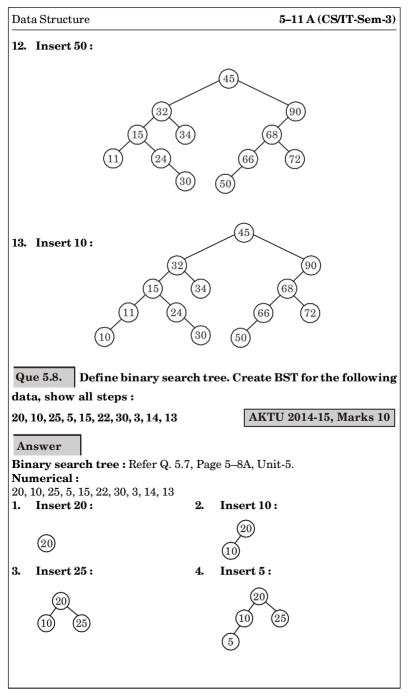
13. Delete a node: Deletion of a node from a BST depends on the number d.

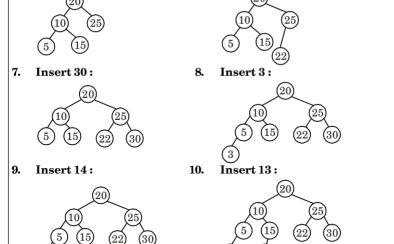
of its children. Suppose to delete a node with key = z from BST T, there are 3 cases that can occur. **Case 1:** *N* has no children. Then *N* is deleted from *T* by simply replacing the location of N in the parent node P(N) by the null pointer.

Case 2: N has exactly one child. Then N is deleted from T by simply replacing the location of N in P(N) by the location of the only child of N. **Case 3:** N has two children. Let S(N) denote the inorder successor of N.

(The reader can verify that S(N) does not have a left child). Then N is deleted from T by first deleting S(N) from T (by using Case 1 or Case 2) and then replacing node N in T by the node S(N).







6

Insert 22 ·

Trees

Que 5.9. Write a short note on strictly binary tree, complete

binary tree and extended binary tree.

Answer

Strictly binary tree: If every non-leaf node in a binary tree has non-empty left and right

5-12 A (CS/IT-Sem-3)

Insert 15

5.

- subtree, the tree is termed as strictly binary tree.
- A strictly binary tree with n leaves always contains 2n 1 nodes. h.
- If every non-leaf node in a binary tree has exactly two children, the tree c. is known as strictly binary tree. Complete binary tree: A tree is called a complete binary tree if tree

satisfies following conditions: Each node has exactly two children except leaf node. ล.

- b. All leaf nodes are at same level.
- If a binary tree contains m nodes at level l, it contains at most 2m nodes c.

at level l+1.

Extended binary tree:

- A binary tree *T* is said to be 2-tree or extended binary tree if each node a. has either 0 or 2 children.
- Nodes with 2 children are called internal nodes and nodes with 0 children b. are called external nodes.

PART-3

Tree Traversal Algorithm: Inorder, Preorder and Postorder, Constructing Binary Tree From Given Tree Traversal.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 5.10. Define tree, binary tree, complete binary tree and full

binary tree. Write algorithm or function to obtain traversals of a binary tree in preorder, postorder and inorder.

AKTU 2017-18, Marks 07

Answer

Tree: Refer Q. 5.1, Page 5–2A, Unit-5.

Binary tree:

- 1. A binary tree T is defined as a finite set of elements called nodes, such that:
 - a. *T* is empty (called the null tree).
 - b. T contains a distinguished node R, called the root of T, and the remaining nodes of T form an ordered pair of disjoint binary trees T_1 and T_2 .
- 2. If T does contain a root R, then the two trees T_1 and T_2 are called, respectively, the left and right subtrees of R.
- 3. If T_1 is non-empty, then its root is called the left successor of R similarly, if T_2 is non-empty, then its root is called the right successor of R.

Complete binary tree: Refer Q. 5.10, Page 5–14A, Unit-5.

Full binary tree:

- 1. A full binary tree is formed when each missing child in the binary tree is replaced with a node having no children.
- 2. These leaf nodes are drawn as squares in the Fig. 5.10.1.

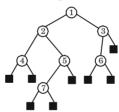
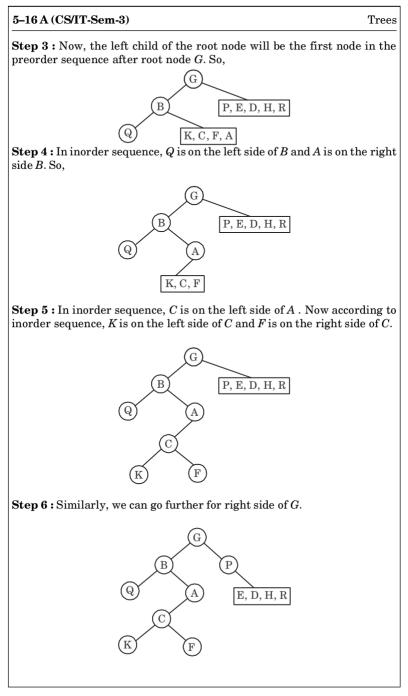


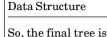
Fig. 5.10.1. Full binary tree.

5–14 A (CS/IT-Sem-3)				
 3.	Each node is either a leaf or has degree exactly 2.			
υ.	Algorithm for preorder traversal:			
	Preorder (INFO, LEFT, RIGHT, ROOT)			
1.	[Initially push NULL onto STACK, and initialize PTR]			
Τ.	Set TOP = 1, STACK [1] = NULL and PTR = ROOT			
2.	Repeat steps 3 to 5 while $PTR \neq NULL$			
2. 3.	Apply process to INFO [PTR]			
ა. 4.	1101			
4.	[Right child?]			
	If RIGHT [PTR] ≠ NULL			
	Then			
	[Push on STACK]			
	Set TOP = TOP + 1 and			
	STACK [TOP] = RIGHT [PTR]			
_	Endif			
5.	[Left child?]			
	If LEFT $[PTR] \neq NULL$ then			
	set PTR = LEFT[PTR]			
	Else			
	[Pop from STACK]			
	set $PTR = STACK[TOP]$ and $TOP = TOP - 1$			
	Endif			
	End of step 2			
6.	Exit			
	Algorithm for inorder traversal:			
	Inorder (INFO, LEFT, RIGHT, ROOT)			
1.	[Push NULL onto STACK and initialize PTR]			
	Set $TOP = 1$, $STACK[1] = NULL$ and $PTR = ROOT$			
2.	Repeat while PTR≠NULL			
	[Push leftmost path onto STACK]			
a.	Set $TOP = TOP + 1$ and			
	STACK [TOP] = PTR			
b.	Set PTR = LEFT [PTR]			
	End loop			
3.	Set $PTR = STACK[TOP]$ and $TOP = TOP - 1$			
4.	Repeat steps 5 to 7 while PTR ≠ NULL			
5.	Apply process to INFO[PTR]			
6.	[Right Child?] If RIGHT [PTR] ≠ NULL			
	Then			
a.	Set PTR = RIGHT [PTR]			
b.	goto step 2			
	Endif			
7.	Set PTR = STACK[TOP] and TOP = TOP – 1			
1.	End of Step 4 Loop			
8.	Exit			
o.	PAIL			

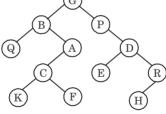
5-15 A (CS/IT-Sem-3)

Data Structure





G



Postorder of tree: Q, K, F, A, B, E, H, R, D, P, G

Que 5.12. Draw a binary tree with following traversal:

Inorder: DBHEAIFJCG

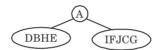
Preorder: ABDEHCFLJG

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5-17 A (CS/IT-Sem-3)

Answer

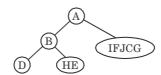
Answer \mid From preorder traversal, we get root node to be A.



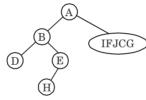
Now considering left subtree.

Observing both the traversal we can get B as root node and D as left child and

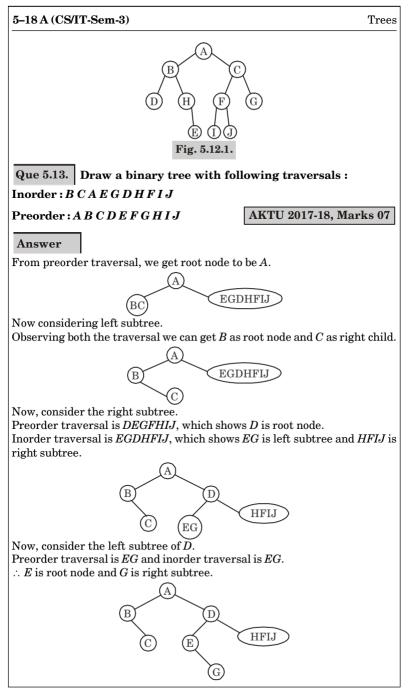
HE as a right subtree.

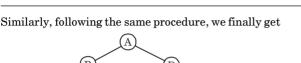


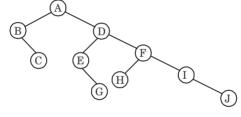
Now observing the preorder traversal we get E as a root node and H as a left child.



Repeating the above process with the right subtree of root node A, we finally obtain the required tree in given Fig. 5.12.1.







5-19 A (CS/IT-Sem-3)

PART-4

Operation of Insertion, Deletion, Searching and Modification of Data in Binary Search.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 5.14. Write a procedure to insert a new element in a binary search tree.

Answer

1. 2

4.

Data Structure

INSBST(INFO, LEFT, RIGHT, ROOT, AVAIL, ITEM, LOC)

- A binary search tree T is in memory and an ITEM of information is given. This algorithm finds the location LOC of ITEM in T or adds ITEM as a new node in T at location LOC.
 - Call FIND(INFO, LEFT, RIGHT, ROOT, ITEM, LOC, PAR).
 - If LOC \neq NULL, then Exit.
- [Copy ITEM into new node in AVAIL list.]
 a. If AVAIL = NULL, then write OVERFLOW, and Exit.
 - Set NEW := AVAIL, AVAIL := LEFT[AVAIL] and
 - INFO[NEW] := ITEM.
 - Set LOC := NEW, LEFT[NEW] := NULL and
 - RIGHT[NEW] := NULL.
 [Add ITEM to tree.]
 - If PAR = NULL, then: Set ROOT := NEW.

Else if ITEM < INFO[PAR], then:

Else if ITEM < INFO[PAR], then Set LEFT[PAR] := NEW.

Else:

h

c.

Set RIGHT[PAR] := NEW

End of If structure

Trees

Else: Call CASEA(INFO, LEFT, RIGHT, ROOT, LOC, PAR) [End of If structure] [Return deleted node to the AVAIL list] Set LEFT[LOC] := AVAIL and AVAIL := LOC

If RIGHT[LOC] ≠ NULL and LEFT[LOC] ≠ NULL, then: Call CASEB(INFO, LEFT, RIGHT, ROOT, LOC, PAR)

Que 5.16. Write a procedure to delete an element from binary search tree where node does not have two children.

CASEA(INFO, LEFT, RIGHT, ROOT, LOC, PAR)

This procedure deletes the node N at location LOC, where N does not have two children. The pointer PAR gives the location of the parent of N, or else PAR = NULL indicates that N is the root node. The pointer CHILD gives the location of the only child of N, or else CHILD = NULL indicates N has no children.

If LEFT[LOC] = NULL and RIGHT[LOC] = NULL, then:

Set CHILD := NULL. Else if LEFT(LOC) ≠ NULL, then:

[Delete node containing ITEM]

Set CHILD := LEFT[LOC].

Set CHILD := RIGHT[LOC].[End of If structure.]

[Initializes CHILD]

5-20 A (CS/IT-Sem-3)

3

5

1.

2.

Exit

Answer

If $PAR \neq NULL$, then:

If LOC = LEFT[PAR], then:

Set LEFT[PAR] := CHILD.

Else:

Else

Set RIGHT[PAR] := CHILD.

Que 5.18. Write a procedure to search an element in the binary

A binary search tree T is the memory and an ITEM of information is given. This procedure finds the location LOC of ITEM in T and also the location

Que 5.17. Write procedure to delete an element from binary search

This procedure will delete the node N at location LOC, where N has two children. The pointer PAR gives the location of the parent of N, or else PAR = NULL indicates that N is the root node. The pointer SUC gives the location of the inorder successor of N, and PARSUC gives the location of

5-21 A (CS/IT-Sem-3)

Data Structure

Else ·

Return

Answer

Else ·

Else ·

Return.

Answer

h.

4.

3

[End of If structure]

[End of If structure.]

Set ROOT := CHILD

tree where node has two children.

the parent of the inorder successor.

1. [Find SUC and PARSUC]

Set RIGHT[PAR] := SUC

Set LEFT[SUC] := LEFT[LOC] and

FIND(INFO, LEFT, RIGHT, ROOT, ITEM, LOC, PAR)

PAR of the parent of ITEM. There are three special cases:

RIGHT[SUC] := RIGHT[LOC].

[End of If structure.]

Set ROOT := SUC. [End of If structure.]

CASEB(INFO, LEFT, RIGHT, ROOT, LOC, PAR)

5-2	5–22 A (CS/IT-Sem-3) Trees				
i. ii. iii.	LOC = NULL and PAR = NULL will indicate that the tree is empty. LOC = NULL and PAR = NULL will indicate that ITEM is the root of T. LOC = NULL and PAR = NULL will indicate that ITEM is not in T and can be added to T as a child of the node N with location PAR.				
1.	[Tree empty?] If ROOT = NULL, then: Set LOC := NULL and PAR := NULL, and Return.				
2.	[ITEM at root?] If ITEM = INFO[ROOT], then: Set LOC := ROOT and PAR := NULL, and Return.				
3.	[Initialize pointers PTR and SAVE.] If ITEM < INFO[ROOT], then: Set PTR := LEFT[ROOT] and SAVE := ROOT. Else:				
	Set PTR := RIGHT[ROOT] and SAVE := ROOT. [End of If structure.]				
4. 5.	Repeart steps 5 and 6 while PTR \neq NULL: [ITEM found ?] If ITEM = INFO[PTR], then: Set LOC := PTR and PAR := SAVE, and				
6.	Return. If ITEM < INFO[PTR], then: Set SAVE := PTR and PTR := LEFT[PTR]. Else: Set SAVE := PTR and PTR := RIGHT[PTR]. [End of If structure]				
7. 8.	[End of step 4 loop.] [Search unsuccessful.] Set LOC := NULL and PAR := SAVE. Exit.				
PART-5 Threaded Binary Trees, Traversing Threaded Binary Trees, Huffman Coding using Binary Tree.					
Questions-Answers					
Long Answer Type and Medium Answer Type Questions					
Que 5.19. What is a threaded binary tree? Explain the advantages					
OI 1	of using a threaded binary tree. AKTU 2017-18, Marks 07				

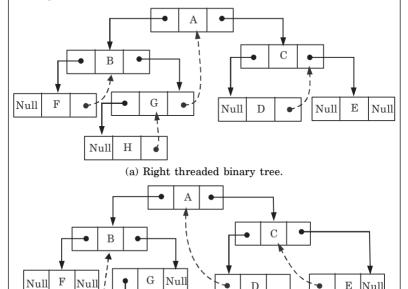
5-23 A (CS/IT-Sem-3)

Null

Null

Data Structure

Threaded binary tree is a binary tree in which all left child pointers that are NULL points to its inorder predecessor and all right child pointers that are NULL points to its inorder successor.



(b) Left threaded binary tree

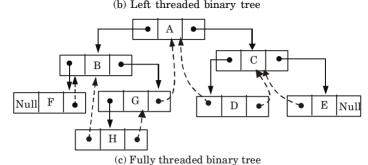


Fig. 5.19.1.

Advantages of using threaded binary tree:

Н Null

1. In threaded binary tree the traversal operations are very fast.

- 2 In threaded binary tree, we do not require stack to determine the predecessor and successor node. In a threaded binary tree, one can move in any direction i.e., upward or 3
- downward because nodes are circularly linked. Insertion into and deletions from a threaded tree are all although time 1 consuming operations but these are very easy to implement.

Que 5.20. Write algorithm/function for inorder traversal of threaded binary tree.

Answer

h

Answer

2

Algorithm for inorder traversal in threaded binary tree:

- Initialize current as root While current is not NIII.I.
- If current does not have left child ล Print current's data
 - Go to the right, *i.e.*, current = current->right
 - Else Make current as right child of the rightmost node in current's ล
 - left subtree h Go to this left child, *i.e.*, current = current->left

Que 5.21. What is Huffman tree? Create a Huffman tree with

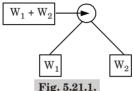
following numbers:

24, 55, 13, 67, 88, 36, 17, 61, 24, 76

AKTU 2014-15, Marks 10

Huffman tree is a binary tree in which each node in the tree represents a

- symbol and each leaf represent a symbol of original alphabet. **Huffman algorithm:**
- Suppose, there are n weights $W_1, W_2,, W_n$. 1
- 2. Take two minimum weights among the n given weights. Suppose W_1 and W_2 are first two minimum weights then subtree will be:



- Now the remaining weights will be $W_1 + W_2$, W_3 , W_4 ,, W_n . 3.
- Create all subtree at the last weight. 4.

Numerical:

 $\begin{bmatrix} 24 \\ A \end{bmatrix}, \begin{bmatrix} 55 \\ B \end{bmatrix}, \begin{bmatrix} 13 \\ C \end{bmatrix}, \begin{bmatrix} 67 \\ D \end{bmatrix}, \begin{bmatrix} 88 \\ E \end{bmatrix}, \begin{bmatrix} 36 \\ F \end{bmatrix}, \begin{bmatrix} 17 \\ G \end{bmatrix}, \begin{bmatrix} 61 \\ H \end{bmatrix}, \begin{bmatrix} 24 \\ I \end{bmatrix}, \begin{bmatrix} 76 \\ J \end{bmatrix}$

Arrange all the numbers in ascending order:

13, 17, 24, 24, 36, 55, 61, 67, 76, 88 C , G , A , I , F , B , H , D , J , E

30 , 36 , 48 , 55 , 61 , 67 , 76 , 88 13 17 24 24 A I

48 , 55 B , 61 66, 67 D , 76 J E 30 36 F G G G

61, 66, 67, 76, 88, 103 H, 66, 67, 76, 88, 103 30 36 F 48 55 B 13 17 C G A I

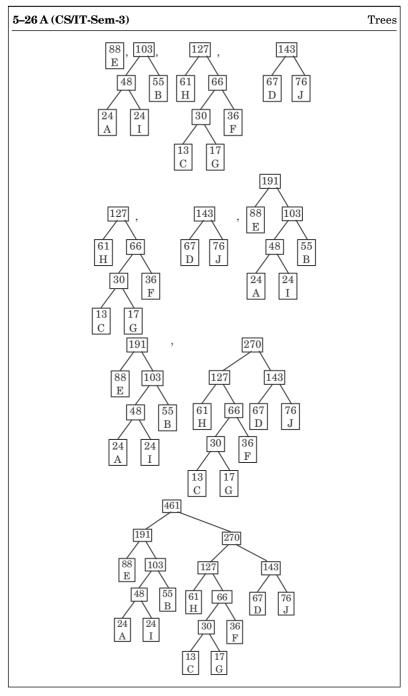
67, 76, 88, 103, 127 D 48 55 61 66 B H 30 36 A I F

13

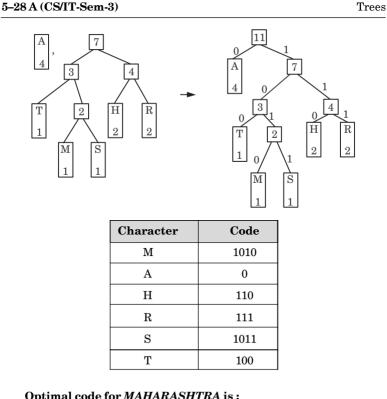
C

17

G



3



Optimal code for MAHARASHTRA is:

1010011001110101111101001110

PART-6

Concept and Basic Operation for AVL Tree, B tree and Binary Heaps.

Questions-Answers

Long Answer Type and Medium Answer Type Questions

Que 5.23. Define AVL trees. Explain its rotation operations with example. Construct an AVL tree with the values 10 to 1 numbers **AKTU 2016-17, Marks 15** into an initially empty tree.

Answer

- i An AVL (or height balanced) tree is a balanced binary search tree.
- ii In an AVL tree, balance factor of every node is either -1, 0 or +1.
- iii Balance factor of a node is the difference between the heights of left and right subtrees of that node.

Balance factor = height of left subtree - height of right subtree

- In order to balance a tree, there are four cases of rotations: i37
- Left Left rotation (LL rotation): In LL rotation every node moves 1. one position to left from the current position.

Insert 1, 2 and 3





After LL rotation

tree is balanced

Tree is unhalanced To make tree balance we use LL rotation which moves nodes one position to left

Fig. 5.23.1.

2. Right Right rotation (RR rotation): In RR rotation every node moves one position to right from the current position.

Insert 3, 2 and 1







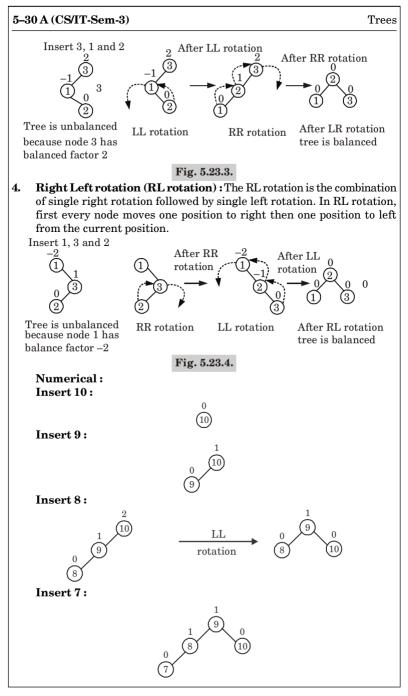
Tree is unbalanced because node 3 has balance factor 2

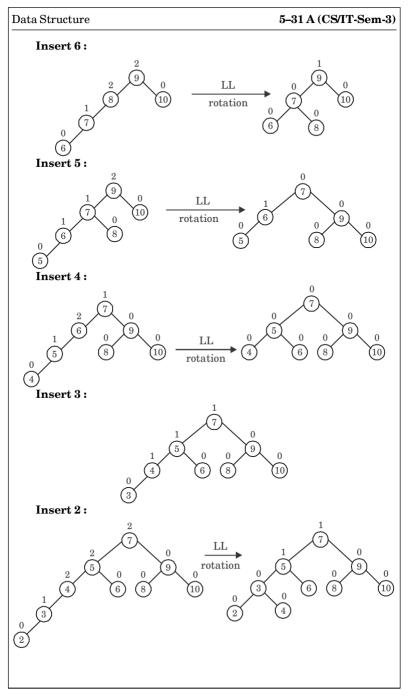
To make tree balance we use RR rotation which moves nodes one position to right

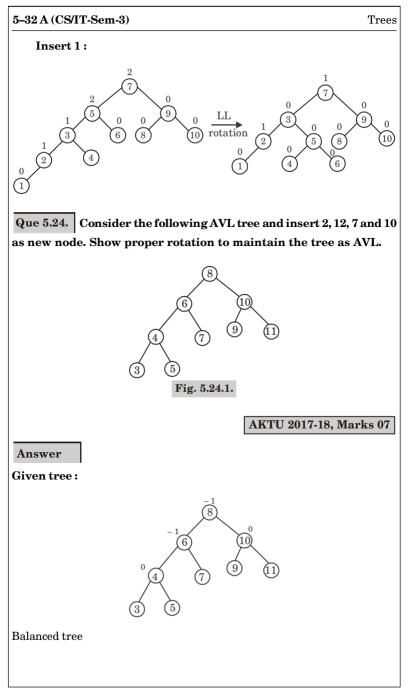
After RR Rotation tree is balanced

Fig. 5.23.2.

3. Left Right rotation (LR rotation): The LR Rotation is combination of single left rotation followed by single right rotation. In LR rotation, first every node moves one position to left then one position to right from the current position.

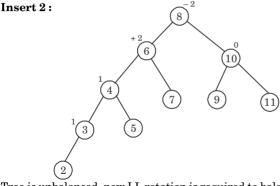




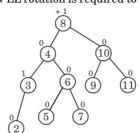




5-33 A (CS/IT-Sem-3)

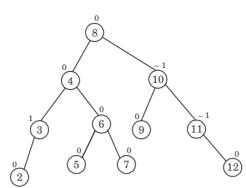


Tree is unbalanced, now LL rotation is required to balance it.



Now the tree is balanced

Insert 12:



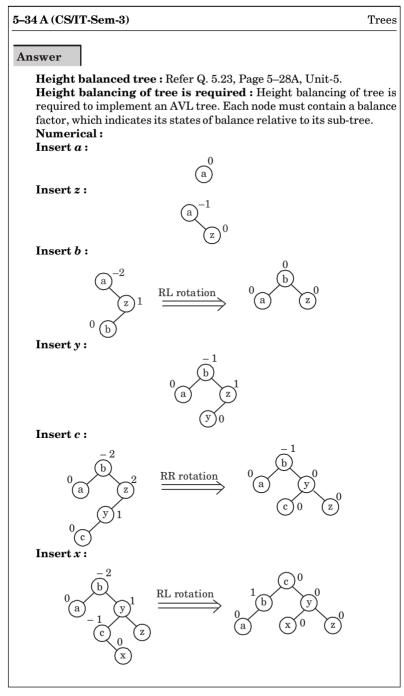
Tree is balanced, so there is no need to balance the tree.

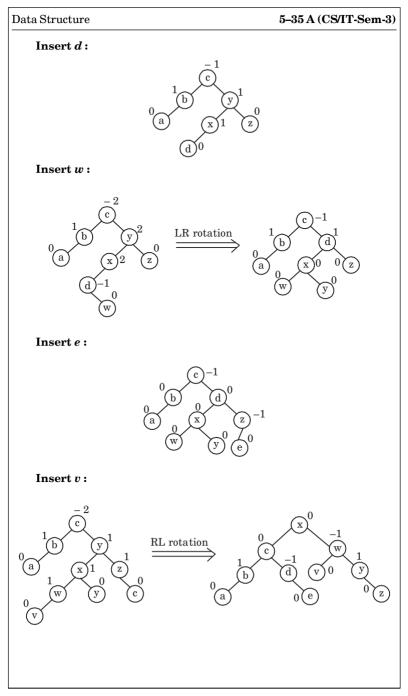
Insert 7: 7 is already in the tree hence it cannot be inserted in the AVL tree. **Insert 10:** 10 is also in the tree hence it cannot be inserted in the AVL tree.

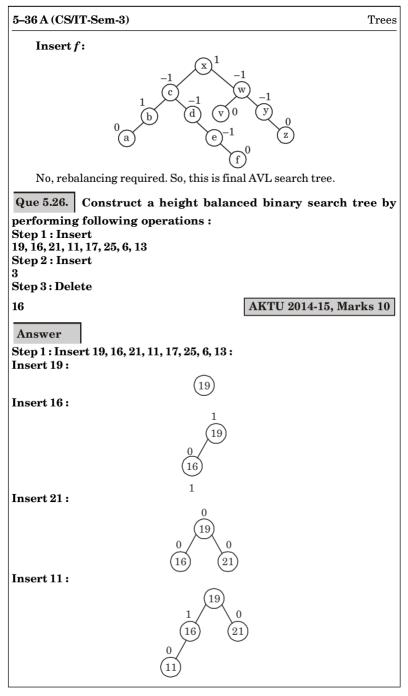
Que 5.25. What is height balanced tree? Why height balancing of tree is required? Create an AVL tree for the following elements: a,

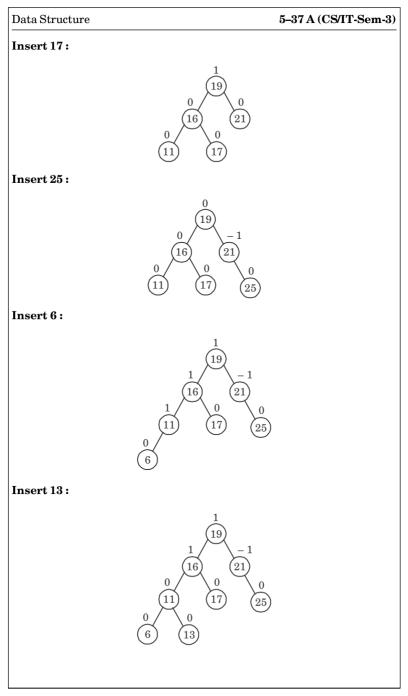
z, b, y, c, x, d, w, e, v, f.

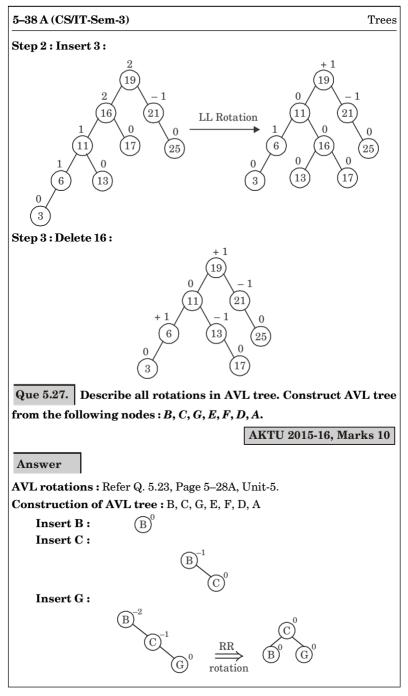
AKTU 2018-19, Marks 07

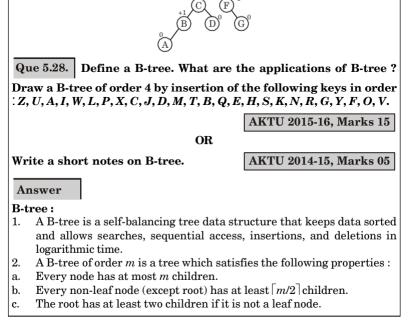












5-39 A (CS/IT-Sem-3)

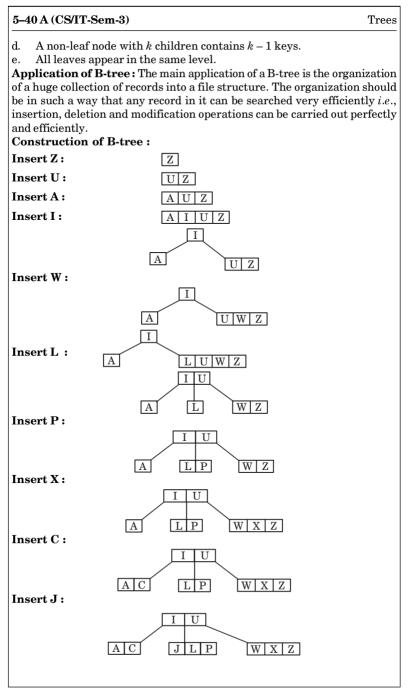
Data Structure

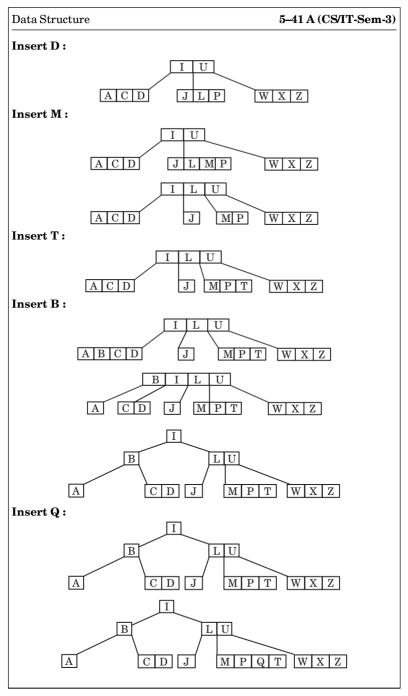
Insert E

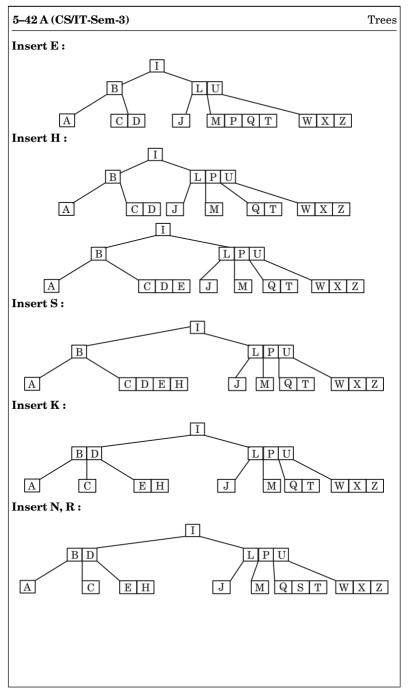
Insert F:

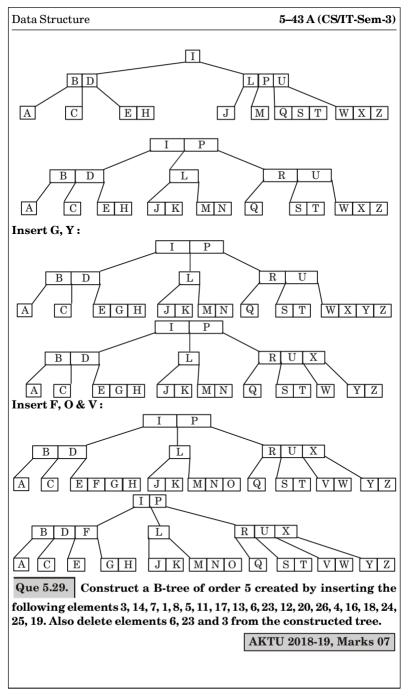
Insert D :

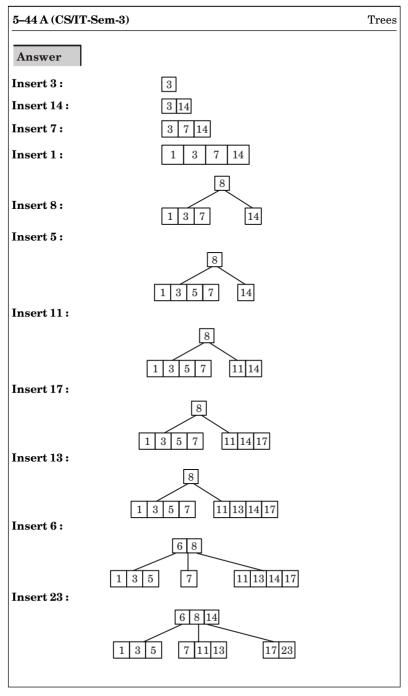
Insert A:

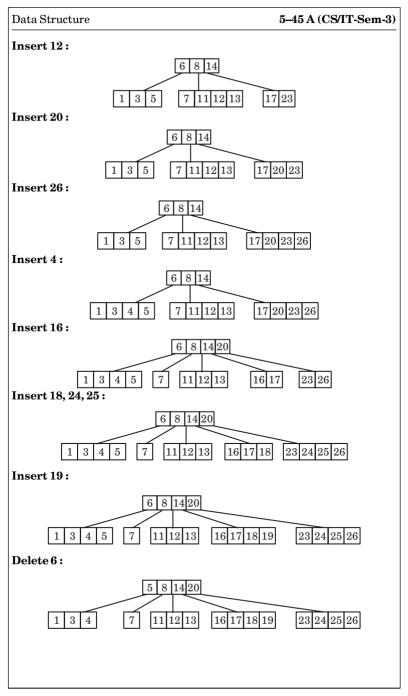


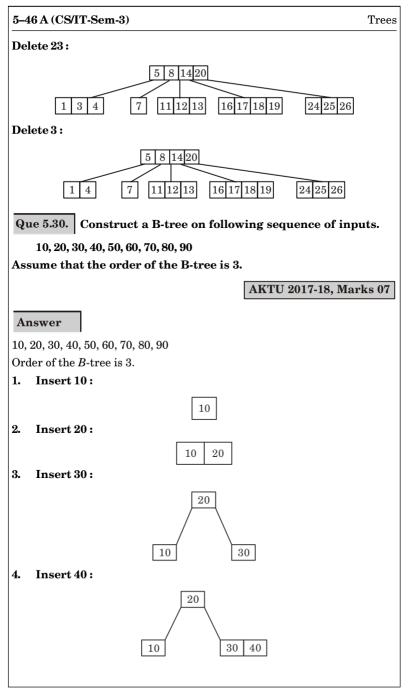


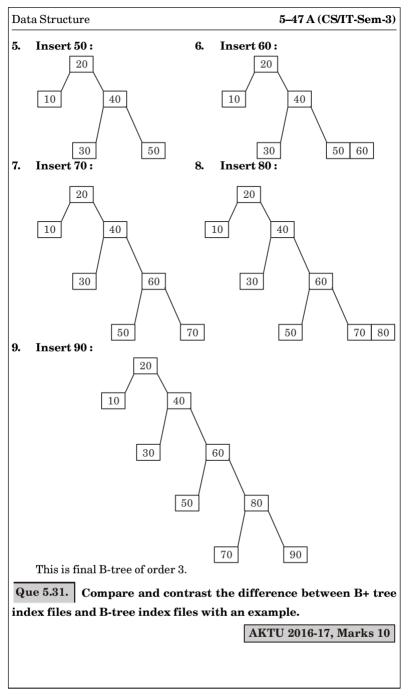






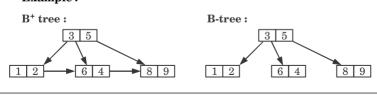






Answer

S. No.	Basis	B ⁺ tree	B-tree		
1.	Definition	B ⁺ tree is an <i>n</i> -array tree with a variable but often large number of children per node. A B ⁺ tree consists of a root, internal nodes and leaves. The root may be either a leaf or a node with two or more children.	A B-tree is an organizational structure for information storage and retrieval in the form of a tree in which all terminal nodes are at the same distance from the base, and all non-terminal nodes have between n and $2n$ sub-trees or pointers (where n is an integer).		
2.	Space complexity	O(n)	O(n)		
3.	Storage	In a B ⁺ tree, data is stored only in leaf nodes.	In a B-tree, search keys and data are stored in internal or leaf nodes.		
4.	Data	The leaf nodes of the tree store the actual record rather than pointers to records.	The leaf nodes of the tree store pointers to records rather than actual records.		
5.	Space	These trees do not waste space.	These trees waste space.		
6.	Function of leaf nodes	In B ⁺ tree, leaf node data are ordered in a sequential linked list.	In B-tree, the leaf node cannot store using linked list.		
7.	Searching	In B ⁺ tree, searching of any data is very easy because all data is found in leaf nodes.	In B-tree, searching becomes difficult as data cannot be found in the leaf node.		
8.	Search accessibility	In B ⁺ tree, the searching becomes easy.	In B-tree, the search is not that easy as compared to a B+ tree.		
9.	Redundant key	They store redundant search key.	They do not store redundant search key.		
Example:					



5-49 A (CS/IT-Sem-3)

2. The array is completely filled on all levels except possibly lowest. 3 We represent heaps in level order, going from left to right. 4

If an array A contains key values of nodes in a heap, length [A] is the 5

total number of elements Heap-size [A] = Length [A] = Number of elements. The root of the tree A[1] and given index i of a node the indices of its 6 parent, left child and right child can be computed:

LEFT(i) return 2i RIGHT (i) return 2i + 1

PARENT (i) return floor (i/2)

deletion with example.

Data Structure

1

VERY IMPORTANT QUESTIONS

Following questions are very important. These questions may be asked in your SESSIONALS as well as

UNIVERSITY EXAMINATION.

Q.1. Write a C program to implement binary tree insertion.

Ans. Refer Q. 5.5. Q. 2. Write the C program for various traversing techniques of

binary tree with neat example. Ans. Refer Q. 5.6.

Q. 3. Explain binary search tree and its operations. Make a binary search tree for the following sequence of numbers, show all steps: 45, 32, 90, 34, 68, 72, 15, 24, 30, 66, 11, 50, 10. Ans. Refer Q. 5.7.

Q.4. Define binary search tree. Create BST for the following data, show all steps: 20, 10, 25, 5, 15, 22, 30, 3, 14, 13 Ans. Refer Q. 5.8.

Trees

Q. 10. What is Huffman tree? Create a Huffman tree with following numbers: 24, 55, 13, 67, 88, 36, 17, 61, 24, 76

Ans. Refer Q. 5.21.

Q.11. Explain Huffman algorithm. Construct Huffman tree for

using a threaded binary tree.

MAHARASHTRA with its optimal code.

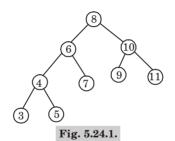
Ans. Refer Q. 5.22.

Ans. Refer Q. 5.19.

5-50 A (CS/IT-Sem-3)

Q. 12. Define AVL trees. Explain its rotation operations with example. Construct an AVL tree with the values 10 to 1 numbers into an initially empty tree.
 Ans. Refer Q. 5.23.

Q. 13. Consider the following AVL tree and insert 2, 12, 7 and 10 as new node. Show proper rotation to maintain the tree as AVL.



Ans. Refer Q. 5.24.

Q.14. Construct a height balanced binary search tree by performing following operations:

Step 1 : Insert 19, 16, 21, 11, 17, 25, 6, 13

Step 2: Insert 3

Step 3 : Delete

Ans. Refer Q. 5.26.

Q. 15. What is height balanced tree? Why height balancing of tree is required? Create an AVL tree for the following elements: a, z, b, y, c, x, d, w, e, v, f.

Ans. Refer Q. 5.25.

Q. 16. Describe all rotations in AVL tree. Construct AVL tree from the following nodes: B, C, G, E, F, D, A.

Ans. Refer Q. 5.27.

Q. 17. Define a B-tree. What are the applications of B-tree? Draw a B-tree of order 4 by insertion of the following keys in order: Z, U, A, I, W, L, P, X, C, J, D, M, T, B, Q, E, H, S, K, N, R, G, Y, F, O, V.

Ans. Refer Q. 5.28.

Q. 18. Construct a B-tree of order 5 created by inserting the following elements 3, 14, 7, 1, 8, 5, 11, 17, 13, 6, 23, 12, 20, 26, 4, 16, 18, 24, 25, 19. Also delete elements 6, 23 and 3 from the constructed tree.

Ans. Refer Q. 5.29.

Q. 19. Construct a B-tree on following sequence of inputs. 10, 20, 30, 40, 50, 60, 70, 80, 90

Assume that the order of the B-tree is 3.

Ans. Refer Q. 5.30.



Array and Linked List (2 Marks Questions)

AKTU 2017-18, Marks 02

1.1. Define the term data structure. List some linear and nonlinear data structures stating the application area where

Ans. It is a particular way of storing and organizing data in a computer so that it can be used efficiently.

It can be classified into two types:

i. Linear data structures :

they will be used.

- 1. Array
- Stacks
 Queue
- 3. Queue 4 Linked list
- ii. Non-linear data structures :
 - 1. Tree
 - 2. Graph
- 1.2. Name few terminologies used in data structure.

Ans. Few terminologies used in data structure are:

- Data
 Entity
- 2. Entit
- 4 Record
- 5. File
- 1.3. What are the data types used in C?
- Ans. Data type used in C are:
 - 1. Primitive data types
 - 2. Non-primitive data types
 - 1.4. Name some primitive data types.
- Ans. Primitive data types are:
 - 1. Integer data type
 - 2. Floating point data type
 - 3. Character data type
 - 4. Void data type
 - 1.5. Define an algorithm.

- 1.6. Give the criteria that an algorithm must satisfy.
- Ans. Every algorithm must satisfy the following criteria:
- 1. Input
- 2. Output 3 Definiteness
- 4 Effectiveness 5 Finiteness
- 1.7. What are the characteristics of an algorithm?
- Ans. Characteristics of an algorithm are:
 - 1. It should be free from ambiguity.
 - 2 It should be concise 3 It should be efficient.
- 1.8. What are the different ways of analyzing an algorithm?
- Ans. Different ways of analyzing an algorithm: 1. Worst case running time
 - 2. Average case running time
 - 3. Best case running time
 - 1.9. Define complexity.
- **Ans.** The complexity of an algorithm M is the function f(n) which gives the running time and/or storage space requirement of the algorithm in terms of the size n of the input data.
- 1.10. Define time complexity and space complexity of an AKTU 2016-17, Marks 02 algorithm.
- **Ans. Time complexity:** Time complexity is the amount of time it needs to run to completion. **Space complexity:** Space complexity is the amount of memory it needs to run to completion.
- 1.11. What are the various asymptotic notations? Explain the AKTU 2015-16, Marks 02 Big-Oh notation.

Ans. Various asymptotic notations are:

- 1. Theta notation $(\theta notation)$
- 2. Big-Oh (O notation)
- 3. Omega notation (Ω notation)
- **Big-Oh notation**: It is used when there is only an asymptotic upper bound. For a given function g(n), O(g(n)) is denoted by a set of functions.

SQ-3 A (CS/IT-Sem-3)

AKTU 2016-17, Marks 02

Non-linear data structure

Examples of non-linear data

structures are trees and graphs.

1.13. Write down the properties of Abstract Data Type (ADT).

Ans. Properties of Abstract Data Type (ADT): i. It is used to simplify the description of abstract algorithm to classify

1.12. Define time-space tradeoff.

- and evaluate data structure ii. It is an important conceptual tool in OOPs and design by contract
- methodologies for software development.

1.14. Differentiate linear and non-linear data structures.

Ans

S. No.

3

Data Structure

		It is a data structure whose elements do not form a sequence.
2.	Every element in the	There is no unique predecessor or

1.15. What do you mean by an array?

predecessor and unique

Examples of linear data

structure are arrays, linked

lists, stacks and queues.

integer, real or strings.

Linear data structure

Ans. An array is a list of finite number of elements of same data type *i.e.*,

1.16. What are the merits and demerits of array data AKTU 2016-17, Marks 02 structures?

Ans. Merits of array:

SIICCESSOT

- 1. Array is a collection of elements of similar data type.
- 2. Hence, multiple applications that require multiple data of same data type are represented by a single name. Demerits of array:
- 1. Linear arrays are static structures, *i.e.*, memory used by them cannot be reduced or extended.
- 2. Previous knowledge of number of elements in the array is necessary.

SQ-4A (CS/IT-Sem-3)

AKTU 2018-19, Marks 02

START = NULL and there is a

Ans. Pointers are variable which can hold the address of another variable

Some of the examples of pointer declarations are: int * ptr1:

float * ptr2:

a linked list.

unsigned int * ptr3:

1.18. Differentiate between array and pointer.

Ans

S. No.	Array	Pointer			
1.	Array can be initialized at definition.	Pointer cannot be initialized at definition.			
2.	Static in nature.	Dynamic in nature.			
3.	It cannot be resized.	It can be resized.			

1.19. Differentiate between overflow and underflow condition in

2.

Ans. S. No. Overflow Underflow Overflow condition occurs in Underflow condition occurs when 1. linked list when data are we delete data from empty linked inserted into a list but there list. is no available space.

In linked list overflow occurs | In linked list underflow occurs when

there is an insertion deletion operation. operation.

when AVAIL = NIII L and

1.20. Write a function to reverse the list.

Ans. node * reverse (node * p){

node *q, *r; q = (node*) NULL; while (p != NULL) r = q; q = p; $p = p \rightarrow \text{next};$ $p \to \text{next} = r$;

return(q);

1.21. Given a 2D array A [-100:100, -5:50]. Find the address of element A [99, 49] considering the base address 10 and each element requires 4 bytes for storage. Follow row major order.

AKTU 2015-16, Marks 02

Ans. LOC(A[i][j]) =Base (A) + w [n (i – lower bound for row index) + (j – lower bound for column index)) LOC (A[99][49]) = 10 + 4 [50 (99 – (–100) + 49 – (–5)]

= 10 + 4 [50 (199) + 54] = 40026

1.22. Explain the application of sparse matrices.

AKTU 2015-16, Marks 02

Ans. There are two applications of sparse matrix which are:

- There are two applications of sparse matrix which are:
 Triangular matrix: In this, all entries above the main diagonal are zero or, equivalently, where non-zero entries can only occur on or below the main diagonal.
- Tridiagonal matrix: In this, all non-zero entries can occur only on the diagonal or on elements immediately above or below the diagonal.





Stacks and Queues (2 Marks Questions)

2.1. What are the applications of stack?

Ans. Applications of stack are:

- i. Infix to postfix conversion.
- ii. Implementing function calls.
- iii. Page-visited history in a web browser.
- iv. Undo sequence in a text editor.
- 2.2. Mention the limitations of stack using array.

- Ans. Limitations of stacks using array: i. The maximum size of the stack once defined cannot be changed.
 - ii. Trying to push a new element into a full stack causes an overflow condition.
- 2.3. What are the notations used in evaluation of arithmetic expressions using prefix and postfix forms?

AKTU 2015-16, Marks 02

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- Ans. Notations used in evaluation of arithmetic expressions are: i. Infix notation: In this notation, the operator symbol is placed between its two operands. For example: To add A to B we can write as, A + B or B + A
 - ii. Polish (Prefix) notation: Here the operator symbol is placed before its two operands.
 - For example: To add A to B we can write as, + AB or + BA iii. Reverse polish (Postfix) notation: In this notation, the operator
 - symbol is placed after its two operands. For example: To add A and B we can write as: AB+ or BA+
 - 2.4. If the Tower of Hanoi is operated on n = 10 disks, calculate

the total number of moves.

OR. Calculate total number of moves for Tower of Hanoi for

AKTU 2017-18, Marks 02 n = 10 disks.

For *n* number of disks, total number of moves Ans. For 10 disks, *i.e.*, n = 10, total number of moves $= 2^{10} - 1$

= 1024 - 1= 1023

Therefore, if the Tower of Hanoi is operated on n = 10 disks, then total number of moves are 1023.

2.5. Give the infix, postfix and prefix notation of (A + B) + C.

Ans.

the element 2.7 Differentiate between iteration and recursion.

Postfix notation: (AB) + C = AB + C +Prefix notation: +AB+C=++ABC

Data Structure

Ans. Infix notation : (A + B) + C

Ans. S No Iteration Recursion It is a technique of defining i It is a process of executing statement until some anything in terms of itself. specified condition is satisfied ii Iterative counterpart of a It is a worse option to go for simple problem is more efficient problems. term of memory utilization and execution

2.8. Discuss the steps for converting an infix expression to

Ans. Steps for converting an infix expression to postfix

i. Parenthesize the expression starting from left to right. ii. During parenthesizing the expression, the operands associated with operator having higher precedence are first parenthesized.

iii. Once the expression is converted to postfix then remove the

2.9. Write some applications of queue.

postfix expression.

expression:

parenthesis.

speed.

Ans. Application of queues are:

i. Operating systems schedule jobs in the order of arrival.

ii. Simulation of real world queues such as lines at a ticket counter. iii. Multiprogramming.

iv. Waiting times for customers at call center.

2.10. Translate infix expression into its equivalent postfix

SQ-7 A (CS/IT-Sem-3)

expression: A * (B + D)/E - F * (G + H/K). AKTU 2015-16, Marks 02

Ans. Infix expression : A * (B + D)/E - F * (G + H/K)

A * (BD +)/E - F * (G + HK/)

ABC /DE ABC / DE*

ABC / DE*F

ABC / DE*F ++ -

(ABD + * E/) - (FGHK/+*)ABD + * E/FGHK / + * -Equivalent postfix expression is: ABD + * E/FGHK / + * -

Е

F

Expression : A - B/C + D*E + F

A (BD +)*/E - F* (GHK/+)

2.11. Convert the following arithmetic infix expression into its equivalent postfix expression. AKTU 2017-18, Marks 02

 $(\Delta B/C + D*F + F)$ Anc

Character	Stack	Postfix
((
A	(A
_	(-	A
В	(-	AB
/	(-/	AB
C	(-/	ABC
+	(– +	ABC /
D	(– +	ABC / D
*	(-+*	ABC / D

2.12. Write the difference between stack and queue.

A == C

Ans.		
S. No.	Stack	Queue
i.	A stack is logically a LIFO type of list.	A queue is logically a FIFO type of list.
ii.	No element other than the top of stack element is visible.	No element other than front and rear element are visible.

(- ++

(- ++

2.13. What are the advantages of queue over stack?

Ans. Advantages of queue over stack are: i. An element that is inserted first in the queue will be the first

element to be removed. ii. Insertion and deletion, both are possible only on one end in stack. While in queue elements are inserted at one end and elements are deleted at other end

2.14. Write down the limitations of circular queue.

- Ans. Limitations of circular queue are:
 - i. We cannot distinguish between full and empty queue.
 - Front and rear indices are in exactly the same relative positions for an empty and for a full queue.
- 2.15. What is the significance of priority queue?

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Ans. Priority queue is a data structure in which elements can be stored as per their priorities. And therefore one can remove the elements from such queue according to their priorities. Such type of queue is useful to operating system in job scheduling algorithms.

- $\ensuremath{\textbf{2.16.}} \ensuremath{\textbf{Name the types of recursion.}}$
- Ans. Types of recursion are:
 - i. Direct recursion
 - ii. Indirect recursion
 - iii. Tail recursion
- iv. Linear and tree recursion
- 2.17. Write the syntax to check whether a given circular queue is full or empty.

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OR

Explain circular queue. What is the condition if circular queue is full?

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Ans. Circular queue: A circular queue is one in which the insertion of a new element is done at the very first location of the queue if the last location at the queue is full.

Syntax to check circular queue is full:

If $((front == MAX - 1) \mid | (front == 0 \&\& rear == MAX - 1))$

Syntax to check circular queue is empty:

If (front == 0 && rear == -1)

2.18. What is recursion? Give disadvantages of recursion.

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Ans. Recursion: Recursion is the process of expressing a function that calls itself to perform specific operation.

Disadvantages of recursion:

- Recursive solution is always logical and it is very difficult to trace, debug and understand.
- 2. Recursion takes a lot of stack space, usually not considerable when the program is small and running on a PC.
- 3. Recursion uses more processor time.





Searching and Sorting (2 Marks Questions)

- 3.1. What do you mean by searching?
- Ans. Searching is a process of finding the location of given elements in the linear arrays. The search is said to be successful if the given element is found.
 - 3.2. Name two searching techniques.
- Ans. Two searching techniques are:
 - Linear (sequential) search
 Binary search
 - 3.3. Define sequential search.
- Ans. In sequential search, each element of an array is read one-by-one sequentially and it is compared with the desired element.
 - 3.4. Define index sequential search.
- Ans. In index sequential search, an index file is created, that contains some specific group or division of required record when the index is obtained, then the partial indexing takes place as it is loaded in a specific group.
 - 3.5. What do you mean by hashing?
- Ans. Hashing is a searching technique that is used to uniquely identify a specific object from a group of similar objects.
 - 3.6. Classify the hashing functions based on the various methods by which the key value is found.

AKTU 2015-16, Marks 02

- Ans. Hashing functions on various methods by which the key value is founded are:
 - i. Division method ii. Multiplication method
 - iii. Mid square method iv. Folding method
 - 3.7. What is collision?
- Ans. Collision is a situation which occur when we want to add a new record R with key K to our file F, but the memory location address H(k) is already occupied.
 - 3.8. Discuss various collision resolution strategies for hash table.

SQ-11A (CS/IT-Sem-3)

- Ans. Collision resolution strategies for hash table are: i. Chaining method: It hold the address of a table element by using
 - h(K) = key% table slots ii. Open addressing method: In this, all the elements of the dynamic
 - sets are stored in hash table itself
 - 3.9. What is sorting? How is sorting essential for database

AKTU 2016-17, Marks 02 applications?

Ans. Sorting: It is an operation which is used to put the elements of list in a certain order, i.e., either in decreasing or increasing order. Sorting essential for database applications: Sorting is easier and faster to locate items in a sorted list than unsorted. Sorting algorithms can be used in a program to sort an array for later searching or writing out to an ordered file or report. Sorted arrays/

3.10. What do you understand by stable and in-place sorting?

lists make it easier to find things more quickly.

AKTU 2018-19, Marks 02

Stable sorting: Stable sorting is an algorithm where two objects Ans. with equal keys appear in the same order in sorted output as they appear in the input unsorted array. **In-place sorting:** An in-place sorting is an algorithm that does not need an extra space and produces an output in the same memory that contains the data by transforming the input 'in-place'. However,

a small constant extra space used for variables is allowed.

3.11. Differentiate between internal and external sorting.

Ans.

S. No.	Internal sorting	ting External sorting	
i.	The internal sorting resides in main memory.	External sorting resides in secondary memory.	
ii.	It is independent of time	It is dependent on time.	

3.12. Give the worst case and best case time complexity of binary search. AKTU 2016-17, Marks 02

Ans. Worst case: In each comparison, the size of the search area is reduced by half. So, the efficiency of the binary search method at the worst case is $\log_2 n + 1$, *i.e.*, $O(\log_2 n + 1)$ where n is the total number of items that will be used for the binary search.

Best case: The best case of binary search occurs when the element we are searching for is the middle element of the list/array because in that case we will get the desired result in a single go. In this case, the time complexity of the algorithm will be O(1).





Graphs (2 Marks Questions)

- 4.1. What are the applications of graphs?
- Ans. Applications of graph are:
 - i. Representing relationship between components in electronic
 - ii. Transportation network in highway network, flight network.
 - iii. Computer network in local area network.
 - 4.2. Write down the applications of DFS.
- Ans. Applications of DFS:
 - i. Topological sorting.
 - ii. Finding connected components.
 - iii. Finding strongly connected components.
 - iv. Solving puzzles such as mazes.
 - 4.3. Write down the applications of BFS.
- Ans. Applications of BFS:
 - i. Finding all nodes within one connected component.
 - ii. Finding the shortest path between two nodes.

4.4. Define connected and strongly connected graph.

Ans. Connected graph: A graph G is said to be connected if there is at

least one path between every pair of vertices in G. **Strongly connected graph:** A graph G is said to be strongly connected if there is at least one directed path from every vertex to every other vertex.

- 4.5. What are the advantages of DFS over BFS?
- Ans. Advantages of DFS over BFS:
 - i. DFS has much lower memory requirement than BFS.
 - ii. DFS is better than BFS if the solution is at maximum depth.
 - 4.6. How the graph can be represented in memory? Explain

with suitable example. AKTU 2018-19, Marks 02

OR

List the different types of representation of graphs.

AKTU 2017-18, Marks 02

Ans. Graph can be represented in memory using:

- 1. Matrix representation
- 2. Linked representation

For example: Consider the following directed graph:



Fig. 1.

Matrix representation:

$$\begin{bmatrix} v_1 & v_2 & v_3 & v_4 \\ v_1 & 0 & 0 & 0 & 1 \\ v_2 & 1 & 0 & 1 & 0 \\ v_3 & 0 & 0 & 0 & 1 \\ v_4 & 0 & 1 & 0 & 0 \end{bmatrix}$$

Linked representation:

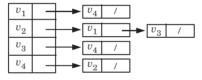


Fig. 2.

4.7. Discuss the disadvantages of Dijkstra's algorithm.

Ans. Disadvantages of Dijkstra's algorithm are:

- It does a blind search thereby consuming a lot of time and wasting necessarily resource.
- ii. It cannot handle negative edges. This leads to acyclic graphs.

4.8. How many ways are there to implement Kruskal's algorithm?

Ans. Ways to implement Kruskal's algorithm:

- i. By using disjoint sets : Using UNION and FIND operation.
- ii. By using priority queue : Maintains weights in priority queue. \\

4.9. How Prim's algorithm is similar to Dijkstra's algorithm?

Ans.

- Similar to Dijkstra algorithm, in Prim's algorithm we also keep distance values and paths in distance table.
- ii. The implementation of Prim's algorithm is identical to that of Dijkstra's algorithm so the running time is $O(\,|\,V\,|^{\,2})$ without heaps and $O(E\,\log V)$ using binary heaps.

4.10. Prove that the number of odd degree vertices in a connected graph should be even. AKTU 2016-17, Marks 02

Ans. Let V_1 and V_2 be the set of vertices of even and odd degrees respectively. Thus, $V_1 \cap V_2 = \emptyset$ and $V_1 \cup V_2 = V$.

By Handshaking theorem,

$$2|E| = \sum_{v \in V} \deg(v) = \sum_{v \in V} \deg(v) + \sum_{v \in V_0} \deg(v)$$

As both 2|E| and $\sum_{v \in V} \deg(v)$ are even. So, $\sum_{v \in V} \deg(v)$ must be

even.

Putting

Ans

Since, $\deg(v)$ is odd for all $v \in V_2$. So, the number of odd degree vertices in a connected graph must be even.

4.11. Number of nodes in a complete tree is 100000. Find its depth.

AKTU 2018-19, Marks 02

We know that, $n = 2^{h+1} - 1$ $(n+1) = 2^{h+1}$ $\log_2(n+1) = h+1$

 $\log_2(n+1) - 1 = h$ n = 100000

Number of nodes in a complete tree = 100000

 $h = \log_2(100000 + 1) - 1$ h = 15 (approx)





Trees (2 Marks Questions)

5.1. Define tree.

Ans. A tree T is a finite non-empty set of elements. One of these elements is called the root, and the remaining elements, if any is partitioned into trees is called subtree of T. A tree is a non-linear data structure.

5.2. Define the depth of a node.

Ans. The depth of a node is the length of the path from the root to the node. A (rooted) tree with only one node (the root) has a depth of zero.

5.3. Describe the properties of binary tree.

Ans. Properties of binary tree are:

- i. The number of nodes n in a full binary tree is $2^{n+1}-1$.
- The number of leaf nodes in a full binary tree is 2^h where h is the height.
- iii. The number of NULL links in a complete binary tree of n nodes is n + 1.

5.4. Define complete binary tree. Give example.

AKTU 2016-17, Marks 02

Ans. A tree is called complete binary tree if tree satisfies following conditions:

- 1. Each node has exactly two children except leaf node.
- 2. All leaf nodes are at same level.
- 3. If a binary tree contains m nodes at level l, it contains at most 2m nodes at level l+1.

Example:

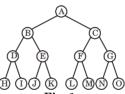


Fig. 1.

5.5. For tree construction which is the suitable and efficient

data structure and why?

AKTU 2015-16, Marks 02

- it is easily accessible due to the concept of pointer used in it. 5.6. Discuss the concept of "successor" and "predecessor" in AKTU 2017-18, Marks 02 binary search tree.
 - Ans. In binary search tree, if a node X has two children, then its predecessor is the maximum value in its left subtree and its successor. is the minimum value in its right subtree.
 - 5.7. Explain height balanced tree. List general cases to maintain AKTU 2017-18, Marks 02 the height.

- Ans
 - i. An AVL (or height balanced) tree is a balanced binary search tree. ii. In an AVL tree, balance factor of every node is either -1, 0 or +1. iii. Balance factor of a node is the difference between the heights of left and right subtrees of that node.

Balance factor = height of left subtree - height of right subtree. General cases to maintain the height are:

- a. Left Left rotation (LL rotation)
- b. Right Right rotation (RR rotation)
- c. Left Right rotation (LR rotation) d. Right Left rotation (RL rotation)
- 5.8. Draw a binary tree for the expression: A * B (C + D) * (P/Q)

AKTU 2018-19, Marks 02

Ans.

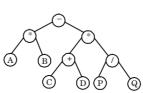


Fig. 2.

5.9. What is the maximum height of any AVL tree with 7 nodes? AKTU 2015-16, Marks 02

Ans. Maximum height of any AVL tree with 7 nodes is 3.

5.10. When does a graph become tree?

AKTU 2016-17, Marks 02

Ans. A graph becomes a tree when there is exactly one path between

- 5.11. How can we traverse a binary tree?
- **Ans.** We can traverse a binary tree using:

every pair of its vertices.

2. Preorder traversing 3. Postorder traversing Inorder traversing $\Theta\Theta\Theta$

(SEM. III) ODD SEMESTER THEORY **EXAMINATION, 2014-15**

DATA STRUCTURES USING C

Time: 3 Hours

printf("%d", i);

Max. Marks: 100 $(5 \times 4 = 20)$

SP-1 A (CS/IT-Sem-3)

- 1. Attempt any four parts of the following: a. Define data structure. Describe about its need and types. Why do we need a data type?
 - b. Write difference between array and linked list.
 - c. What do you understand by complexity of an algorithm? Compute the worst case complexity for the following C code: main() int s = 0, i, j, n; for (j = 0; j < (3 * n); j++)for (i = 0; i < n; i++)s = s + i;
 - d. Write the difference between malloc() and calloc() functions. Why do we use dynamic memory allocation?
 - e. Write an algorithm or C code to insert a node in doubly link list in beginning.
 - f. What is row-major order? Explain with an example.
 - **2.** Attempt any **four** parts of the following: $(5 \times 4 = 20)$ a. What is Tower of Hanoi problem? Write the recursive code
 - in C language for the problem. b. What is circular queue? Write a C code to insert an element
 - in circular queue. Write all the condition for overflow.

- c. What is stack? Implement stack with singly linked list.
- d. Write the procedures for insertion, deletion and traversal of a queue.
- e. Write a function in C language to reverse a string using stack.
- f. Convert following infix expression into postfix expression A + (B * C + D)/E.
- 3. Attempt any two parts of the following: $(10 \times 2 = 20)$
- a. Construct a height balanced binary search tree by performing following operations:

Step 1: Insert

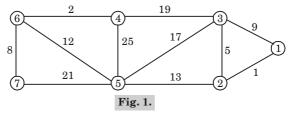
19, 16, 21, 11, 17, 25, 6, 13

Step 2: Insert

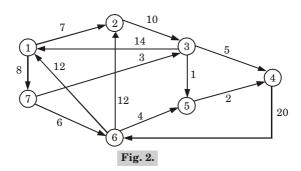
Step 3: Delete

16

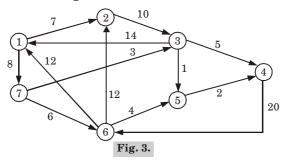
- b. What is Huffman tree? Create a Huffman tree with following numbers:
 - 24, 55, 13, 67, 88, 36, 17, 61, 24, 76
- c. Define binary search tree. Create BST for the following data, show all steps: 20, 10, 25, 5, 15, 22, 30, 3, 14, 13
- 4. Attempt any two parts of the following: $(10 \times 2 = 20)$
- a. Define spanning tree. Find the minimal spanning tree for the following graph using Prim's algorithm.



b. Find out the shortest path from node 1 to node 4 in a given graph (Fig. 4) using Dijkstra shortest path algorithm.



c. Write DFS algorithm to traverse a graph. Apply same algorithm for the graph given in Fig. 5 by considering node 1 as starting node.



- **5.** Attempt any **two** parts of the following: $(10 \times 2 = 20)$
- a. What do you mean by hashing and collision? Discuss the advantages and disadvantages of hashing over other searching techniques.
- b. Write an algorithm for merge sorting using the algorithm sort in ascending order.

10, 25, 16, 5, 35, 48, 8

- c. Write short notes on any three of the following:
- i. B-tree
- ii. Insertion sort
- iii. Heap sort
- iv. Garbage collection

SOLUTION OF PAPER (2014-15)

- 1. Attempt any **four** parts of the following: $(5 \times 4 = 20)$
- a. Define data structure. Describe about its need and types. Why do we need a data type?

Ans. Data structure:

- 1. A data structure is a way of organizing all data items that considers not only the elements stored but also their relationship to each other.
- 2. Data structure is the representation of the logical relationship existing between individual elements of data.
- 3. Data structure is define as a mathematical or logical model of particular organization of data items. Data structure is needed because:
- 1. It helps to understand the relationship of one element with the other.
- 2. It helps in the organization of all data items within the memory. The data structures are divided into following categories:
- 1. Linear data structure: a. A linear data structure is a data structure whose elements form a
- sequence, and every element in the structure has a unique predecessor and unique successor.
- b. Examples of linear data structure are arrays, linked lists, stacks and queues.
 - 2. Non-linear data structure:
 - a. A non-linear data structure it is a data structure whose elements do not form a sequence. There is no unique predecessor or unique successor.
 - b. Examples of non-linear data structures are trees and graphs. **Need of data type:** The data type is needed because it determines what type of information can be stored in the field and how the data can be formatted.

b. Write difference between array and linked list.

Ans.

S. No.	Array	Linked list
1.	An array is a list of finite number of elements of same data type <i>i.e.</i> , integer, real or string etc.	A linked list is a linear collection of data elements called nodes which are connected by links.
2.	Elements can be accessed randomly.	Elements cannot be accessed randomly. It can be accessed only sequentially.

or circular linked list.

element or node.

is a complex process.

Location or address of element is

stored in the link part of previous

The nodes in the linked list can be

In linked list, modifying the node

Pointers are used in linked list.

added and deleted from the list.

3.

4.

5.

6.

7.

Ans.

a. 1-D array

b. 2-D array c. n-D array

location.

declared.

modified

array.

Each array element is

independent and does not

have a connection with

previous element or with its

Array elements cannot be added, deleted once it is

In array, elements can be

easily identifying the index value. Pointer cannot be used in

in terms of the size n of the input data.

count. This calculation is as follows:

Worst case complexity: $\Omega(n) + \Omega(3n) = \Omega(n)$

the data size n.

compute the worst case complexity for the following c	
code:	
main()	
mam()	
{	
int s = 0, i, j, n;	
for $(j = 0; j < (3 * n); j++)$	
{	
for $(i = 0; i < n; i++)$	
{	
s = s + i;	
}	
printf("%d", i);	
<u>}</u> }	

The complexity of an algorithm M is the function f(n) which gives the running time and/or storage space requirement of the algorithm

2. The storage space required by an algorithm is simply a multiple of

The time complexity can be calculated by computing the frequency

c. What do you understand by complexity of an algorithm? Compute the worst case complexity for the following C

Code		Frequency count
for $(j = 0; j < (3*)$	(n); j ++)	(3*n) + 1

for $(i = 0; i < n; i ++)$	((3*n)*n) + 1		
s = s + i;	((3*n)*n)		
$\operatorname{printf}(\text{``%d"}, i)$	3n		
Total	$6n^2 + 6n + 2$		
By considering only the order of magnitude, we can express the worst case time complexity $\mathrm{O}(n^2)$.			
d Write the difference between malles() and calles()			

Solved Paper (2014-15)

((0))) ...

functions. Why do we use dynamic memory allocation?

Ans.

SP-6A (CS/IT-Sem-3)

S. No.	malloc()	calloc()
1.	It takes single argument.	It takes two argument.
2.	Does not initialize the allocated memory.	Initialize the allocated memory to zero.
3.	Syntax of malloc(): Void *malloc(size_t n);	Syntax of calloc(): Void * calloc (size = t n, size_t size);

Uses of dynamic memory allocation:

- i. In dynamic memory allocation, data structure can grow and shrink during the execution time. ii. They have efficient memory utilization because memory is not
- iii. Insertion and deletion can be done very easily at the desired position. e. Write an algorithm or C code to insert a node in doubly

preallocated.

link list in beginning.

Ans. Insertion at beginning: 1. IF PTR = NULL then Write OVERFLOW

- Go to Step 9
- [END OF IF]
- 2. SET NEW NODE = PTR 3. SET PTR = PTR -> NEXT
- 4. SET NEW NODE -> DATA = VAL
- 5. SET NEW NODE -> PREV = NULL
- 6. SET NEW NODE -> NEXT = START 7. SET HEAD -> PREV = NEW NODE
 - 8. SET HEAD = NEW NODE
 - 9. EXIT

f. What is row-major order? Explain with an example.

Ans.

- 1. In row major order, the element of an array is stored in computer memory as row-by-row.
- 2. Under row major representation, the first row of the array occupies the first set of memory locations reserved for the array, the second row occupies the next set, and so forth.
- 3. In row major order, elements of a two-dimensional array are ordered as:

 $\begin{array}{l} A_{11}, A_{12}, A_{13}, A_{14}, A_{15}, A_{16}, A_{21}, A_{22}, A_{23}, A_{24}, A_{25}, A_{26}, A_{31},, A_{46}, A_{51}, \\ A_{52},, A_{56} \end{array}$

Example:

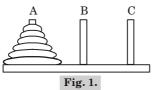
Let us consider the following two-dimensional array:

$$\begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \end{bmatrix}$$

- a. Move the elements of the second row starting from the first element to the memory location adjacent to the last element of the first row.
- b. When this step is applied to all the rows except for the first row, we have a single row of elements. This is the row major representation.
- c. By application of above mentioned process, we get $\{a,b,c,d,e,f,g,h,i,j,k,l\}$
- **2.** Attempt any **four** parts of the following: $(5 \times 4 = 20)$
- a. What is Tower of Hanoi problem? Write the recursive code in C language for the problem.

Ans. Tower of Hanoi problem:

- 1. Suppose three pegs, labelled A, B and C is given, and suppose on peg A, there are finite number of *n* disks with decreasing size.
- 2. The object of the game is to move the disks from peg \bar{A} to peg C using peg B as an auxiliary.
- 3. The rule of game is follows:
- a. Only one disk may be moved at a time. Specifically only the top disk on any peg may be moved to any other peg.
- b. At no time, can a larger disk be placed on a smaller disk.

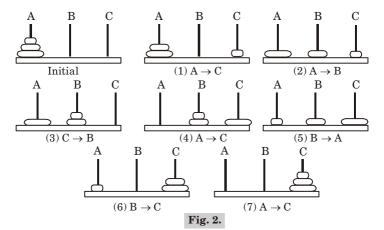


The solution to the Tower of Hanoi problem for n = 3.

Total number of steps to solve Tower of Hanoi problem of n disk

$$= 2^n - 1 = 2^3 - 1 = 7$$





Recursive code for Tower of Hanoi:

#include<stdio.h>

```
#include<conio.h>
void main()
clrscr();
int n;
char A = 'A', B = 'B', C = 'C';
void hanoi (int, char, char, char);
printf("Enter number of disks:");
scanf("%d", &n);
printf("\n\n Tower of Hanoi problem with %d disks\n", n);
printf("Sequence is : \n");
hanoi (n, A, B, C);
      printf("\n");
           getch();
void hanoi (int n, char A, char B, char C)
If(n! = 0)
hanoi (n-1, A, C, B);
printf("Move disk %d from %c to %c\n, n, A, C,");
hanoi (n-1, B, A, C);
```

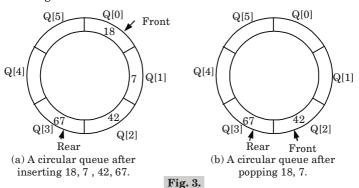
b. What is circular queue? Write a C code to insert an element in circular queue. Write all the condition for overflow.

Ans.

- 1. A circular queue is one in which the insertion of a new element is done at the very first location of the queue if the last location at the queue is full.
- 2. In circular queue, the elements Q[0], Q[1], Q[2] ... Q[n 1] is represented in a circular fashion.

For example: Suppose Q is a queue array of six elements.

3. PUSH and POP operation can be performed on circular queue. Fig. 3 will illustrate the same.



C code to insert an element in circular queue : void insert ()

```
int item:
if((front == 0 \&\& rear == Max - 1) | | ((front == rear + 1))
printf("Queue is overflow\n");
return;
if(front == -1) / *If queue is empty*/
front = 0;
rear = 0;
}
else
if(rear == Max - 1) /*rear is at last position of queue*/
rear = 0:
else
rear = rear + 1:
printf("Input the element for insertion:");
scanf("%d", &item);
cqueue [rear] = item;
```

SP-10 A (CS/IT-Sem-3)

1. (front = 0) and (rear = Max - 1) 2. front = rear + 1If any of these two conditions is satisfied, it means that overflow occurs.

Solved Paper (2014-15)

c. What is stack? Implement stack with singly linked list. Ans. Stack:

- 1. A stack is one of the most commonly used data structure. 2. A stack, also called Last In First Out (LIFO) system, is a linear list
- in which insertion and deletion can take place only at one end,
- called top.
- 3. This structure operates in much the same way as stack of trays. 4. If we want to remove a tray from stack of trays it can only be
- removed from the top only.

5. The insertion and deletion operation in stack terminology are known as PUSH and POP operations.

```
Implementation using singly linked list:
typedef struct stack
    int *data:
    struct stack *next;
    }stack:
void push(stack **top, int *data)
```

newn = (stack *)malloc(sizeof(stack));

newn->next = (stack *)NULL;

stack *newn:

newn->data = data:

if(*top == NULL)

newn->next = (*top);*top = newn;

int *pop(stack **top)

int *rval = (int *)NULL;

tmp = *top;*top = (*top)->next;rval = tmp->data; free(tmp);

*top = newn;return:

stack *tmp; if(*top!= NULL) }

```
return(rval);
}
```

d. Write the procedures for insertion, deletion and traversal of a queue. Ans.

1. Insertion:

Insert in Q (Queue, Max, Front, Rear, Element)

Let Queue is an array, Max is the maximum index of array, Front

and Rear to hold the index of first and last element of Queue respectively and Element is value to be inserted.

Step 1: If Front = 1 and Rear = Max or if Front = Rear + 1 Display "Overflow" and Return

Step 2: If Front = NULL [Queue is empty] Set Front = 1 and Rear = 1

else if Rear = N, then Set Rear = 1

else

Set Rear = Rear + 1

[End of if Structure] **Step 3:** Set Queue [Rear] = Element [This is new element]

Step 4: End

2. Deletion: Delete from Q (Queue, Max, Front, Rear, Item)

Step 1: If Front = NULL [Queue is empty] display "Underflow" and Return

Step 2: Set Item = Queue [Front]

Step 3: If Front = Rear [Only one element] Set Front = Rear and Rear = NULL

Else if

Set Front = 1Else Set Front = Front + 1

Front = N, then

[End if structure]

Step 4: End

3. Traversal of a queue: Here queue has Front End FE and Rear End RE. This algorithm traverse queue applying an operation

PROCESS to each element of queue:

Step 1: [Initialize counter] Set K = FE

Step 2: Repeat step 3 and 4 while $K \le RE$ Step 3: [Visit element] Apply PROCESS to queue [K]

Step 4: [Increase counter] Set K = K + 1 [End of step 2 loop]

Step 5: Exit

```
Ans. #include<stdio.h>
#include<conio.h>
#include<string.h>
#define MAX 20
int top = -1;
char stack [MAX];
```

e. Write a function in C language to reverse a string using

Solved Paper (2014-15)

SP-12 A (CS/IT-Sem-3)

stack.

```
for(i = 0; i < strlen(str); i++)
    push (str [i]);
    for(i = 0; i < strlen(str); i++)
    str[i] = pop();
    printf("Reversed string is :");
    puts (str);
    getch();
    }

push (char item)
    {
        if(top == MAX - 1)
        printf("Stack overflow\n");
        else
        stack[++top] = item;
    }
    char pop()
    {
        if(top == - 1)</pre>
```

printf("Stack underflow \n");
else
 return stack [top - -];
}

f. Convert following infix expression into postfix expression
 A + (B * C + D)/E.

Ans. (A + (B * C + D)/E)

Character	Stack	Postfix
((
A	(A
+	(+	A
((+(A
В	(+(AB
*	(+(*	AB
C	(+(*	ABC
+	(+(+	ABC*
D	(+(+	ABC*D
)	(+	ABC*D+
/	(+/	ABC*D+
E	(+/	ABC*D+E
)	(ABC*D+E/+

Resultant postfix expression : ABC * D + E/+

3. Attempt any **two** parts of the following: $(10 \times 2 = 20)$

a. Construct a height balanced binary search tree by performing following operations:

19, 16, 21, 11, 17, 25, 6, 13 Step 2: Insert

Step 3: Delete

Step 1: Insert

16

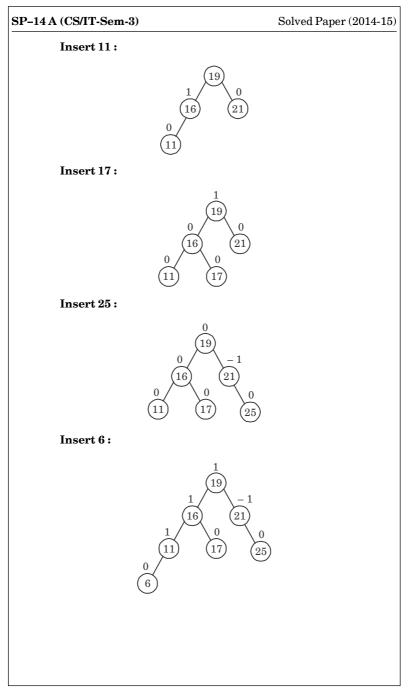
Step 1: Insert 19, 16, 21, 11, 17, 25, 6, 13:

Insert 19:

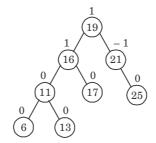
Ans.

Insert 16:

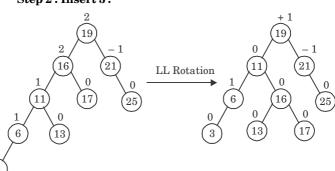
Insert 21:



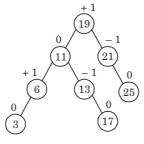
Insert 13:



Step 2: Insert 3:



Step 3: Delete 16:



b. What is Huffman tree? Create a Huffman tree with following numbers:

24, 55, 13, 67, 88, 36, 17, 61, 24, 76

Ans. Huffman tree is a binary tree in which each node in the tree represents a symbol and each leaf represent a symbol of original alphabet.

Numerical:

67,

Arrange all the numbers in ascending order:

24,

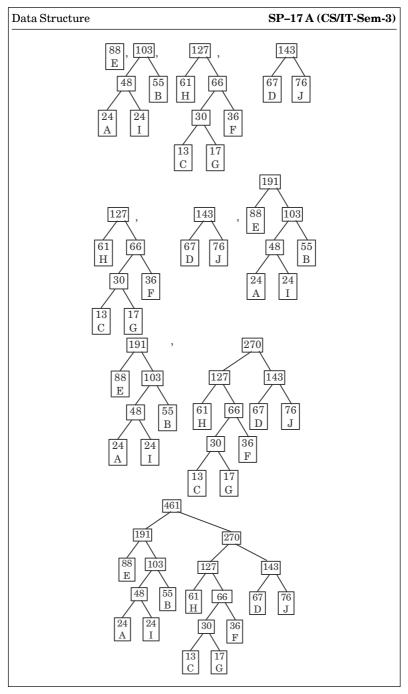
C G \mathbf{F}

F G

> Η Ε F В

Е Η В F

С



- c. Define binary search tree. Create BST for the following data, show all steps:
 - 20, 10, 25, 5, 15, 22, 30, 3, 14, 13
 - Ans. Binary search tree:
 - 1. A binary search tree is a binary tree. 2. Binary search tree can be represented by a linked data structure in
 - which each node is an object.
 - 3. In addition to a key field, each node contains fields left, right and *P*, which point to the nodes corresponding to its left child, its right child and its parent respectively.

6.

8.

Numerical:

20, 10, 25, 5, 15, 22, 30, 3, 14, 13

1. Insert 20: 2. Insert 10:

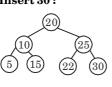
Insert 25:

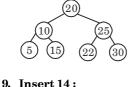
Insert 5:

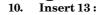
5. Insert 15:

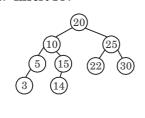
Insert 22: Insert 3:

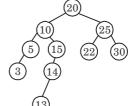
7. Insert 30:





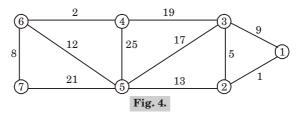






20

- **4.** Attempt any **two** parts of the following: $(10 \times 2 = 20)$
- a. Define spanning tree. Find the minimal spanning tree for the following graph using Prim's algorithm.



Ans. Spanning tree:

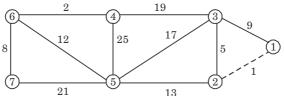
1. A spanning tree of a graph is a sub-graph which is a tree and contains all the vertices of graph.

Numerical:

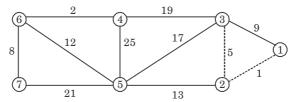
$$\begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ - & 1 & 9 & - & - & - & - \\ 2 & 1 & - & 5 & - & 13 & - & - \\ 3 & 9 & 5 & - & 19 & 17 & - & - \\ 4 & - & - & 19 & - & 25 & 2 & - \\ 5 & - & 13 & 17 & 25 & - & 12 & 21 \\ 6 & - & - & 2 & 12 & - & 8 \\ 7 & - & - & - & 21 & 8 & - \end{bmatrix}$$

According to Prim's algorithm, we choose vertex ${\bf 1}.$

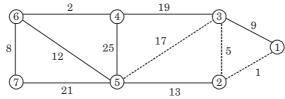
We choose edge (1, 2), since it has minimum value.



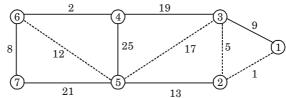
Now at vertex 2, we choose the edge (2, 3), since it has minimum value.



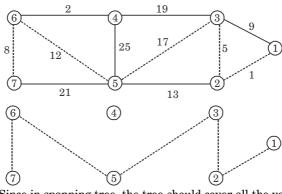
Now at vertex 3, we cannot choose edge $(3,\,1)$ because it will create a cycle so we choose $(3,\,5).$



Now at vertex 5, we choose the edge (5, 6) since it has minimum value.



Now at vertex 6, we choose the edge (6, 7) since it has minimum value.

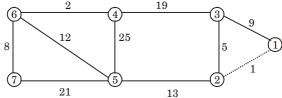


Since in spanning tree, the tree should cover all the vertices and should not make cycle.

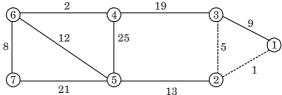
But in the above tree, 4 is remaining so the above asked question is wrong. If we assume to remove the edge from $\{3, 5\}$ then the spanning tree is:

According to Prim's algorithm, let's choose vertex 1.

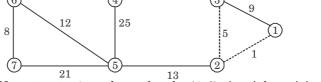
We choose edge {1, 2}, since it has minimum value.



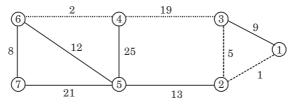
Now at vertex 2, we choose the edge (2, 3), since it has minimum value.



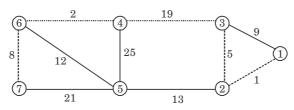
Now at vertex 3, we choose the edge (3, 4), since it has minimum value.



Now at vertex 4, we choose the edge (4, 6), since it has minimum value.



Now at vertex 6, we choose the edge (6, 7), since it has minimum value.



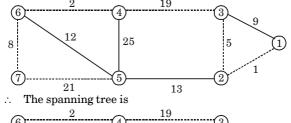


8

9

5

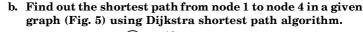
Now at vertex 7, we cannot choose the edge (7, 6), because we have already traversed this edge these we choose (7, 5).

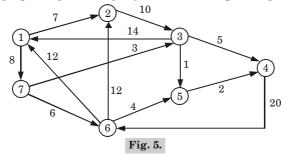


25

12

(7)———(5) (2)———1



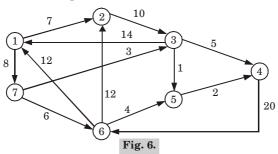


Ans.

1	2	3	4	5	6	7
0	∞	∞	∞	∞	∞	∞
0	7	17	∞	∞	∞	8
0	7	17	∞	∞	∞	8
0	7	11	∞	∞	14	8
0	7	11	16	12	14	8
0	7	11	14	12	14	8
0	7	11	14	12	14	8

Shortest path from node 1 to node 4 = 0 + 7 + 11 + 14 = 32

c. Write DFS algorithm to traverse a graph. Apply same algorithm for the graph given in Fig. 6 by considering node 1 as starting node.



Ans. Depth First Search (DFS): The general idea behind a depth first search beginning at a starting node *A* is as follows:

- a. First, we examine the starting node A.
- b. Then, we examine each node N along a path P which begins at A; that is, we process neighbour of A, then a neighbour of neighbour of A, and so on.
- c. This algorithm uses a stack instead of queue.

Algorithm:

- i. Initialize all nodes to ready state (STATUS = 1).
- ii. Push the starting node A onto stack and change its status to the waiting state (STATUS = 2).
- iii. Repeat steps (iv) and (v) until queue is empty.
- iv. Pop the top node N of stack, process N and change its status to the processed state (STATUS = 3).
- v. Push onto stack all the neighbours of N that are still in the ready state (STATUS = 1) and change their status to the waiting state (STATUS = 2).

[End of loop]

vi. End.

Numerical: Adjacency list of the given graph:

 $1 \rightarrow 2, 7$

 $2 \rightarrow 3$

 $3 \to 5, 4, 1$

 $4 \rightarrow 6$

 $5 \rightarrow 4$

 $6 \to 2, 5, 1$

 $0 \rightarrow 2, 0,$

 $7 \rightarrow 3, 6$

1. Initially set STATUS = 1 for all vertex

- 2. Push 1 onto stack and set their STATUS = 2
- 3. Pop 1 from stack, change its STATUS = 1 and

1 usii 2, 7 onto stack and change then STATOS = 2, DFS = 1	
7	
2	
4. Pop 7 from stack, Push 3, 6: DFS = 1, 7	

5. Pop 6 from stack, Push 5; DFS = 1, 7, 6

6. Pop 5 from stack, Push 4; DFS = 1, 7, 6, 5

7. Pop 4 from stack; DFS = 1, 7, 6, 5, 4

nto stock and change their STATUS - 2.

Solved Paper (2014-15)

SP-24 A (CS/IT-Sem-3)

8. Pop 3 from stack; DFS = 1, 7, 6, 5, 4, 39. Pop 2 from stack; DFS = 1, 7, 6, 5, 4, 3

Now, the stack is empty, so the depth first traversal of a given

graph is 1, 7, 6, 5, 4, 3. **5.** Attempt any **two** parts of the following: $(10 \times 2 = 20)$ a. What do you mean by hashing and collision? Discuss the advantages and disadvantages of hashing over other searching techniques.

Ans. Hashing: 1. Hashing is a technique that is used to uniquely identify a specific object from a group of similar objects. 2. Hashing is the transformation of a string of characters into a usually shorter fixed-length value or key that represents the original string.

- Collision: 1. Collision is a situation which occur when we want to add a new record R
- with key k to our file F, but the memory location address H(k) is already occupied. 2. A collision occurs when more than one keys map to same hash

value in the hash table.

Advantages of hashing over other search techniques:

- 1. The main advantage of hash tables over other table data structures is speed. This advantage is more apparent when the number of entries is large (thousands or more).
- 2. Hash tables are particularly efficient when the maximum number of entries can be predicted in advance, so that the bucket array can be allocated once with the optimum size and never resized.
- 3. If the set of key-value pairs is fixed and known ahead of time (so insertions and deletions are not allowed), one may reduce the average lookup cost by a careful choice of the hash function, bucket table size, and internal data structures.

Disadvantages of hashing over other search techniques:

- Hash tables can be more difficult to implement than self-balancing binary search trees. Choosing an effective hash function for a
- hash tables it is fairly easy to create a poor hash function.

 2. The cost of a good hash function can be significantly higher than the inner loop of the lookup algorithm for a sequential list or search tree.

specific application is more an art than a science. In open-addressed

- Hash tables are not effective when the number of entries is very small. For certain string processing applications, such as spellchecking, hash tables may be less efficient than trees, finite automata, or arrays.
- 4. If each key is represented by a small enough number of bits, then, instead of a hash table, one may use the key directly as the index into an array of values.
- b. Write an algorithm for merge sorting using the algorithm sort in ascending order. 10, 25, 16, 5, 35, 48, 8
- Ans. Merge sort :
 - a. Merge sort is a sorting algorithm that uses the idea of divide and conquer.
 - b. This algorithm divides the array into two halves, sorts them separately and then merges them.
 - separately and then merges them.
 c. This procedure is recursive, with the base criteria that the number
 - of elements in the array is not more than 1. **MERGE_SORT** (a, p, r):
 - MERGE_SORT (a, p, r): 1. if p < r
 - 2. then $q \leftarrow \lfloor (p+r)/2 \rfloor$
 - 3. MERGE-SORT (A, p, q)
 - 4. MERGE-SORT (A, q + 1, r)
 - 5. MERGE (A, p, q, r)
 - MERGE (A, p, q, r):
 - $1. n_1 = q p + 1$
 - $2. n_2 = r q$

do

Solved Paper (2014-15)

3. Create arrays L [1 $n_1 + 1$] and $R[1....n_2+1]$ 4. for $i = 1 \text{ to } n_1$

> L[i] = A[p+i-1]endfor

5. for j = 1 to n_2 do R[j] = A[q+j]endfor

6. $L[n_1 + 1] = \infty$, $R[n_2 + 1] = \infty$ i = 1, j = 1

k = p to rdo

8. for if $L[i] \leq R[j]$ then $A[k] \leftarrow L[i]$

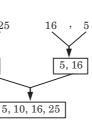
i = i + 1else A[k] = R[j]

j = j + 1endif endfor 9. exit Numerical:

10, 25, 16, 5, 35, 48, 8 1. Divide first half 10, 25, 16, 5 2. Consider the first half: 10, 25, 16, 5 again divide into two subarrays 10 25

10, 25

35, 48

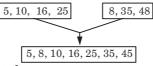


35, 48, 8

3. **Consider the second half:** 35, 48, 5 again divide into two subarrays 35 48 8

8, 35, 48

4. Merge these two sorted sub-arrays,



This is the sorted array.

c. Write short notes on any three of the following:

i. B-tree

Ans. B-tree: 1. A B-tree is a self-balancing tree data structure that keeps data

- sorted and allows searches, sequential access, insertions, and deletions in logarithmic time.
- 2. A B-tree of order m is a tree which satisfies the following properties:
- a. Every node has at most m children.
- b. Every non-leaf node (except root) has at least $\lceil m/2 \rceil$ children.
- c. The root has at least two children if it is not a leaf node.
- d. A non-leaf node with k children contains k-1 keys. e. All leaves appear in the same level.

ii. Insertion sort

Ans.

- 1. In insertion sort, we pick up a particular value and then insert it at the appropriate place in the sorted sublist, i.e., during k^{th} iteration the element a[k] is inserted in its proper place in the sorted sub-array $a[1], a[2], a[3] \dots a[k-1].$
- 2. This task is accomplished by comparing a[k] with a[k-1], a[k-2], a[k-3] and so on until the first element a[i] such that $a[i] \le a[k]$ is found.
- 3. Then each of the elements a[k-1], a[k-2], a[j+1] are moved one position up and then element a[k] is inserted in [j+1]st position in the array.

Insertion-Sort (A)

- 1. for $j \leftarrow 2$ to length[A]
- 2. do key $\leftarrow A[j]$ /*Insert A[j] into the sorted sequence A[1...j-1].*/
- 3. $i \leftarrow j 1$ 4. while i > 0 and A[i] > key
- 5. do $A[i+1] \leftarrow A[i]$
- 6. $i \leftarrow i 1$
- 7. $A[i+1] \leftarrow \text{kev}$

Analysis of insertion sort:

Complexity of best case is O(n)

Complexity of average case is $O(n^2)$

Complexity of worst case is $O(n^2)$

iii. Heap sort

for all other elements.

1. Heap sort finds the largest element and puts it at the end of array,

b. Interchange the root (maximum) element with the last element. c. Use repetitive downward operation from root node to rebuild the heap of size one less than the starting.

then the second largest item is found and this process is repeated

- d. Repeat step (a) and (b) until there are no more elements.
- MAX-HEAPIFY (A, i):

2. The general approach of heap sort is as follows: a. From the given array, build the initial max heap.

- 1. $i \leftarrow \text{left}[i]$
- 2. $r \leftarrow \text{right } [i]$
- 3. if $l \le \text{heap-size } [A] \text{ and } A[l] > A[i]$
- 4. then largest $\leftarrow l$
- 5. else largest $\leftarrow i$ 6. if $r \le \text{heap-size } [A] \text{ and } A[r] > A \text{ [largest]}$
- 7. then largest $\leftarrow r$
- 8. if largest $\neq i$ 9. then exchange $A[i] \leftrightarrow A[largest]$
- 10. MAX-HEAPIFY [A, largest]
- HEAP-SORT(A): 1. BUILD-MAX-HEAP (A)
- 2. for $i \leftarrow \text{length } [A] \text{ down to } 2$
- 3. do exchange $A[1] \leftrightarrow A[i]$ heap-size $[A] \leftarrow$ heap-size [A] - 14.
- MAX-HEAPIFY(A, 1)5.

iv. Garbage collection

Ans. 1. When some memory space becomes reusable due to the deletion of

- then we want the space to be available for future use. 2. One method to do this is to immediately reinsert the space into the
- free-storage list. This is implemented in the linked list.
- 3. This method may be too time consuming for the operating system of a computer.

a node from a list or due to deletion of entire list from a program

- 4. In another method, the operating system of a computer may periodically collect all the deleted space onto the free storage list. This type of technique is called garbage collection.
- 5. Garbage collection usually takes place in two steps. First the computer runs through all lists, tagging those cells which are currently in use and then the computer runs through the memory, collecting all untagged space onto the free storage list. 6. The garbage collection may take place when there is only some
 - minimum amount of space or no space at all left in the free storage list or when the CPU is idle and has time to do the collection.



SP-1 A (CS/IT-Sem-3)

B.Tech.

(SEM. III) ODD SEMESTER THEORY EXAMINATION, 2015-16

DATA STRUCTURES USING C

Time: 3 Hours Max. Marks: 100

Section-A

1. Attempt all parts. All parts carry equal marks. Write answer of each part in short. $(2 \times 10 = 20)$ a. Given a 2D array A [- 100 : 100, -5 : 50]. Find the address of

element A [99, 49] considering the base address 10 and each

- element requires 4 bytes for storage. Follow row-major order.
 - Big-oh notation.

 c. What are the notations used in evaluation of arithmetic

b. What are the various asymptotic notations? Explain the

- d. Classify the hashing functions based on the various methods by which the key value is found.
- e. What is the maximum height of any AVL tree with 7 nodes ?

f. If the Tower of Hanoi is operated on n = 10 disks, calculate

the total number of moves.

expressions using prefix and postfix forms?

- g. Define connected and strongly connected graph.
- i. For tree construction which is the suitable and efficient data structure and why?

h. Translate infix expression into its equivalent postfix

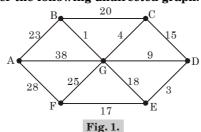
j. Explain the application of sparse matrices.

expression: A * (B + D)/E - F* (G + H/K).

Section-B

Note: Attempt any **five** questions from this section. $(10 \times 5 = 50)$

- 2. Consider the linear arrays AAA [5:50], BBB [-5:10] and CCC [1:8].
- a. Find the number of elements in each array.
 - b. Suppose base (AAA) = 300 and w = 4 words per memory cell for AAA. Find the address of AAA [15], AAA [35] and AAA [55].
 - 3. Describe all rotations in AVL tree. Construct AVL tree from the following nodes: B, C, G, E, F, D, A.
 - 4. Explain binary search tree and its operations. Make a binary search tree for the following sequence of numbers, show all steps: 45, 32, 90, 34, 68, 72, 15, 24, 30, 66, 11, 50, 10.
 - 5. Explain Dijkstra's algorithm with suitable example.
 - 6. Write a C function for linked list implementation of stack. Write all the primitive operations.
 - 7. Draw a binary tree with following traversal: Inorder: DBHEAIFJCG Preorder: ABDEHCFLJG
 - 8. Consider the following undirected graph.



- a. Find the adjacency list representation of the graph.
- b. Find a minimum cost spanning tree by Kruskal's algorithm.
- 9. How do you calculate the complexity of sorting algorithms? Also, write a recursive function in 'C' to implement the merge sort on given set of integers.

Ans.

Section-C

Note: Attempt any **two** questions from this section. $(15 \times 2 = 30)$

10. What are doubly linked lists? Write C program to create doubly linked list.

OR

How do you find the complexity of an algorithm? What is the relation between the time and space complexities of an algorithm? Justify your answer with an example.

- 11. Write an algorithm for finding solution to the Tower of Hanoi problem. Explain the working of your algorithm (with 4 disks) with diagrams.
- 12. Define a B-tree. What are the applications of B-tree? Draw a B-tree of order 4 by insertion of the following keys in order: Z, U, A, I, W, L, P, X, C, J, D, M, T, B, Q, E, H, S, K, N, R, G, Y, F, O, V.



SOLUTION OF PAPER (2015-16)

Section-A

- 1. Attempt all parts. All parts carry equal marks. Write answer of each part in short. $(2 \times 10 = 20)$ a. Given a 2D array A = 100 : 100 = 5 : 50. Find the address of
- element A [99, 49] considering the base address 10 and each element requires 4 bytes for storage. Follow row-major order.
- Ans. LOC(A[i][j]) = Base (A) + w [n (i lower bound for row index) + (j lower bound for column index)) LOC (A[99][49]) = 10 + 4 [50 (99 – (–100) + 49 – (–5)]

= 10 + 4 [50 (199) + 54] = 40026

- b. What are the various asymptotic notations? Explain the Big-oh notation.
- Ans. Various asymptotic notations are:
 - 1. Theta notation $(\theta$ notation)
 - 2. Big-Oh (O notation)
 - Omega notation (Ω notation)
 Big-Oh notation: It is used when there is only an asymptotic
 - of functions.

 c. What are the notations used in evaluation of arithmetic

upper bound. For a given function g(n), O(g(n)) is denoted by a set

- expressions using prefix and postfix forms?

 Ans. Notations used in evaluation of arithmetic expressions are:
 - i. Infix notation: In this notation, the operator symbol is placed between its two operands.
 - For example: To add A to B we can write as, A + B or B + A
 - ii. Polish (Prefix) notation: Here the operator symbol is placed before its two operands.

For example: To add A to B we can write as, + AB or + BA

- iii. Reverse polish (Postfix) notation: In this notation, the operator symbol is placed after its two operands.For example: To add A and B we can write as: AB+ or BA+
- d. Classify the hashing functions based on the various methods by which the key value is found.
- Ans. Hashing functions on various methods by which the key value is founded are:
 - i. Division method ii. Multiplication method
 - iii. Mid square method iv. Folding method
 - e. What is the maximum height of any AVL tree with 7 nodes?

Ans. Maximum height of any AVL tree with 7 nodes is 3.

f. If the Tower of Hanoi is operated on n = 10 disks, calculate

the total number of moves.

Ans. For n number of disks, total number of moves = $2^n - 1$ For 10 disks, *i.e.*, n = 10, total number of moves = $2^{10} - 1$ = 1024 - 1= 1023

Therefore, if the Tower of Hanoi is operated on n=10 disks, then total number of moves are 1023.

g. Define connected and strongly connected graph.

Ans. Connected graph: A graph G is said to be connected if there is at least one path between every pair of vertices in G.
 Strongly connected graph: A graph G is said to be strongly connected if there is at least one directed path from every vertex to

h. Translate infix expression into its equivalent postfix expression: A*(B+D)/E - F*(G+H/K).

expression : A * (B + D)/E - F * (G + H/K).

Ans. Infix expression : A * (B + D)/E - F * (G + H/K) A * (BD +)/E - F * (G + HK/)

A (BD +)*/E - F* (GHK/+) (ABD + * E/) - (FGHK/+*) ABD + * E/FGHK / + * -

every other vertex.

Equivalent postfix expression is: ABD + * E/FGHK / + * -

 i. For tree construction which is the suitable and efficient data structure and why?
 Ans. Linked list is the most suitable and efficient data structure because

it is easily accessible due to the concept of pointer used in it.

j. Explain the application of sparse matrices.

Ans. There are two applications of sparse matrix which are:

There are two applications of sparse matrix which are:
 The sparse matrices are useful for computing large scale operations that dense matrices can not handle.

2. It is used in solving partial differential equations.

Section-B

Note: Attempt any **five** questions from this section. $(10 \times 5 = 50)$

2. Consider the linear arrays AAA [5:50], BBB [-5:10] and CCC [1:8].

a. Find the number of elements in each array. b. Suppose base (AAA) = 300 and w = 4 words per memory cell

b. Suppose base (AAA) = 300 and w = 4 words per memory cell for AAA. Find the address of AAA [15], AAA [35] and AAA [55].

Ans.

a. The number of elements is equal to the length; hence use the formula:

Length = UB - LB + 1

Length (AAA) = 50 - 5 + 1 = 46

Length (BBB) = 10 - (-5) + 1 = 16

Length (CCC) = 8 - 1 + 1 = 8

b. Use the formula

LOC(AAA[i]) = Base(AAA) + w(i - LB)

LOC(AAA[15]) = 300 + 4(15 - 5) = 340

LOC(AAA[35]) = 300 + 4(35 - 5) = 420

AAA [55] is not an element of AAA, since 55 exceeds UB = 50.

3. Describe all rotations in AVL tree. Construct AVL tree from the following nodes: B, C, G, E, F, D, A.

Ans. AVL rotations:

- i. An AVL (or height balanced) tree is a balanced binary search tree.
- ii. In an AVL tree, balance factor of every node is either -1, 0 or +1.
- iii. Balance factor of a node is the difference between the heights of left and right subtrees of that node.

Balance factor = height of left subtree – height of right subtree

- iv. In order to balance a tree, there are four cases of rotations :
- Left Left rotation (LL rotation): In LL rotation every node moves one position to left from the current position.

Insert 1, 2 and 3



 $0 \\ 0 \\ 0 \\ 0 \\ 3$

Tree is unbalanced

To make tree balance we use LL rotation which moves nodes one position to left.

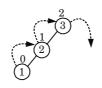
After LL rotation tree is balanced

Fig. 1.

2. Right Right rotation (RR rotation): In RR rotation every node moves one position to right from the current position.

Insert 3, 2 and 1







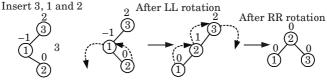
Tree is unbalanced balance factor 2

To make tree balance we use because node 3 has RR rotation which moves

After RR Rotation tree is balanced

nodes one position to right Fig. 2.

3. Left Right rotation (LR rotation): The LR Rotation is combination of single left rotation followed by single right rotation. In LR rotation, first every node moves one position to left then one position to right from the current position.



Tree is unbalanced because node 3 has balanced factor 2

LL rotation

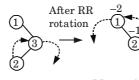
RR rotation

After LR rotation tree is balanced

Fig. 3.

4. Right Left rotation (RL rotation): The RL rotation is the combination of single right rotation followed by single left rotation. In RL rotation, first every node moves one position to right then one position to left from the current position.





After LL

Tree is unbalanced because node 1 has balance factor -2

RR rotation LL rotation After RL rotation tree is balanced

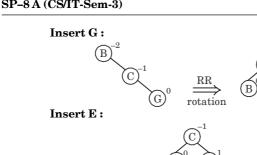
Fig. 4.

Construction of AVL tree: B, C, G, E, F, D, A

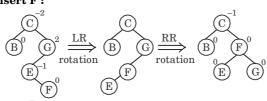
Insert B:

Insert C:

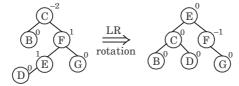




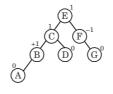
Insert F:



Insert D:



Insert A:



4. Explain binary search tree and its operations. Make a binary search tree for the following sequence of numbers, show all steps: 45, 32, 90, 34, 68, 72, 15, 24, 30, 66, 11, 50, 10.

Ans. Binary search tree:

- 1. A binary search tree is a binary tree.
- 2. Binary search tree can be represented by a linked data structure in which each node is an object.
- 3. In addition to a key field, each node contains fields left, right and *P*, which point to the nodes corresponding to its left child, its right child and its parent respectively.
- 4. A non-empty binary search tree satisfies the following properties:

h.

c.

d.

the same value.

key in the node.

a. Searching in a BST:

1. If x = NIL or k = kev[x]

the keys in the node.

Various operations of BST are:

The keys, if any, in the left subtree of root are smaller than the

The keys, if any in the right subtree of the root are larger than

The left and right subtrees of the root are also binary search

SP-9A (CS/IT-Sem-3)

arrays or linked lists. The TREE-SEARCH (x, k) algorithm searches the tree root at x for a node whose key value equals to k. It returns a pointer to the node if it exist otherwise NIL. TREE-SEARCH (x, k)

Searching for a data in a binary search tree is much faster than in

- 2. then return x3. If k < kev [x]4. then return TREE-SEARCH (left [x], k)
- 5. else return TREE-SEARCH (right [x], k) b. Traversal operation on BST:
 - All the traversal operations are applicable in binary search trees. The inorder traversal on a binary search tree gives the sorted order
 - of data in ascending (increasing) order.
- c. Insertion of data into a binary search tree:

 - To insert a new value w into a binary search tree T, we use the
 - procedure TREE-INSERT. The procedure passed a node z for which
- key[z] = w, left [z] = NIL and Right [z] = NIL.
- 2. $x \leftarrow \text{root} [T]$ 3. while $x \neq NIL$

1. $\nu \leftarrow \text{NIL}$

- 4. do $y \leftarrow x$
- 5. if key [z] < key [x]6. then $x \leftarrow \text{left } [x]$
- 7. else $x \leftarrow \text{right } [x]$
- 8. $P[z] \leftarrow y$
- 9. if y = NIL10. then root $|T| \leftarrow z$
- 11. else if key |z| < key |y|
- 12. then left $[v] \leftarrow z$
- 13. else right $[y] \leftarrow z$

pointer.

- **d. Delete a node:** Deletion of a node from a BST depends on the number of its children. Suppose to delete a node with key = z from
- BST *T*, there are 3 cases that can occur. **Case 1**: N has no children. Then N is deleted from T by simply replacing the location of N in the parent node P(N) by the null

Case 2: N has exactly one child. Then N is deleted from T by simply replacing the location of N in P(N) by the location of the only child of N.

Case 3: N has two children. Let S(N) denote the inorder successor of N. (The reader can verify that S(N) does not have a left child). Then N is deleted from T by first deleting S(N) from T (by using Case 1 or Case 2) and then replacing node N in T by the node S(N).

Numerical:

1. Insert 45:

2. Insert 32 :

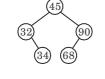
3. Insert 90 :

(45)

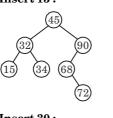
4. Insert 34:

5. Insert 68 :

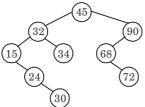
6. Insert 72:

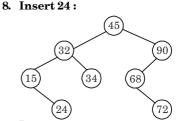


7. Insert 15:

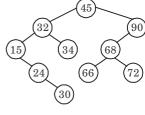


9. Insert 30:

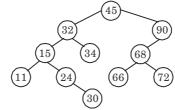




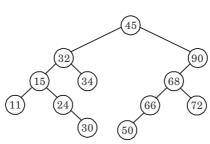
10. Insert 66:

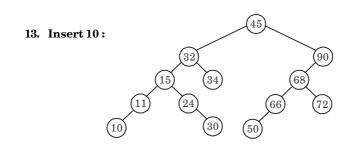


11. Insert 11:



12. Insert 50:





5. Explain Dijkstra's algorithm with suitable example.

Ans. Algorithm:

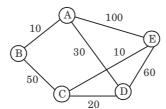
- a. Dijkstra's algorithm, is a greedy algorithm that solves the single-source shortest path problem for a directed graph G=(V,E) with non-negative edge weights, *i.e.*, we assume that $w(u,v) \geq 0$ each edge $(u,v) \in E$.
- b. Dijkstra's algorithm maintains a set S of vertices whose final shortest-path weights from the source s have already been determined.
- c. That is, for all vertices $v \in S$, we have $d[v] = \delta(s, v)$.
- d. The algorithm repeatedly selects the vertex $u \in V S$ with the minimum shortest-path estimate, inserts u into S, and relaxes all edges leaving u.

- e. We maintain a priority queue Q that contains all the vertices in v-s, keyed by their d values.
 - f. Graph G is represented by adjacency list.
 - g. Dijkstra's always chooses the "lightest or "closest" vertex in V-S to insert into set S, that it uses as a greedy strategy.

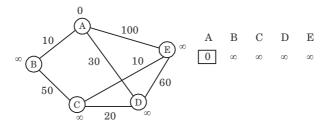
 $\begin{array}{ll} \text{DIJKSTRA} \ (G, \, w, \, s) \\ \text{1.} \ \ \text{INITIALIZE-SINGLE-SOURCE} \ (G, \, s) \end{array}$

- 2. $S \leftarrow \phi$
- 3. $Q \leftarrow V[G]$
- 4. while $Q \neq \emptyset$
- 5. do $u \leftarrow \text{EXTRACT-MIN}(Q)$
- 6. $S \leftarrow S \cup \{u\}$
- 7. for each vertex $v \in Adj[u]$
- 8. do RELAX (u, v, w)

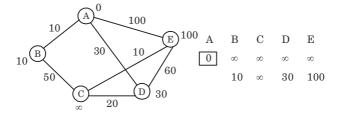
Example: Working of Dijkstra's algorithm for following graph:



Extract min (A):



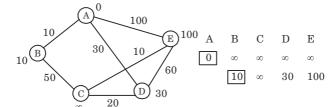
All edges leaving A:



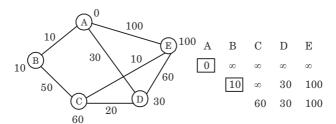


SP-13 A (CS/IT-Sem-3)

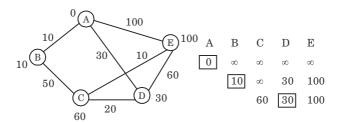
Extract min (B):



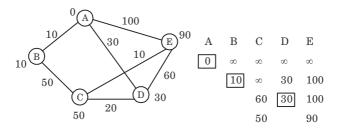
All edges leaving B:



Extract min(D):



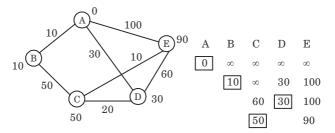
All edges leaving (D):

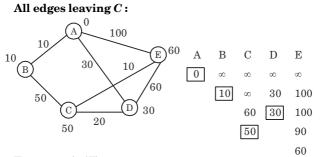




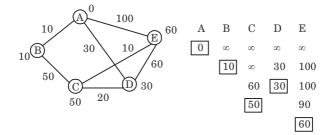
Solved Paper (2015-16)

Extract min(C):

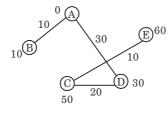




Extract min(E):



Shortest path:



Write all the primitive operations.

```
6. Write a C function for linked list implementation of stack.
Ans. #include<stdio.h>
      #include<conio.h>
      #include<alloc.h>
           struct node
           int info:
           struct node *link;
           };
                struct node *top;
                void main()
                void create(), traverse(), push(), pop();
                create():
                printf("\n stack is:\n");
                traverse():
                pop();
                printf("After push the element in the stack is : \n");
                traverse():
                pop();
                printf("After pop the element in the stack is : \n")
                traverse():
                getch();
                void create()
                struct node *ptr, *cpt;
                char ch:
                ptr = (struct node *) malloc (sizeof (struct node));
                printf("Input first info");
                scanf("%d", &ptr -> info);
                ptr -> link = NULL:
           do
                cpt = (struct node *) malloc (sizeof (struct node));
                printf("Input next information");
                scanf("%d", &cpt -> info);
                cpt \rightarrow link = ptr;
                ptr = cpt;
                printf("Press < Y/N > for more information");
                ch = getch();
```

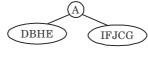
while (ch == 'Y')top = ptr;

```
void traverse()
     struct node *ptr;
    printf("Traversing of stack: \n");
     ptr = top;
     while (ptr != NULL)
     printf ("%d\n", ptr -> info);
     ptr = ptr -> link;
void push()
     struct node *ptr;
     ptr = (struct node *) malloc (sizeof (struct node));
     if(ptr == NULL)
     printf("Overflow\n");
     return;
     printf("Input New node information");
    scanf("%d", &ptr -> info);
     ptr -> link = top;
     top = ptr;
void pop()
     struct node *ptr;
     if(top == NULL)
     printf("Underflow \n");
     return;
     ptr = top:
     top = ptr -> link;
     free (ptr);
```

7. Draw a binary tree with following traversal: Inorder: DBHEAIFJCG

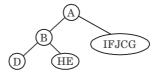
Preorder: ABDEHCFIJG

Ans. From preorder traversal, we get root node to be A.

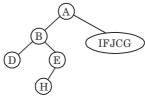


Now considering left subtree.

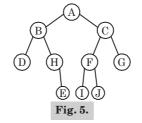
Observing both the traversal we can get B as root node and D as left child and HE as a right subtree.



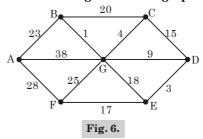
Now observing the preorder traversal we get E as a root node and H as a left child.



Repeating the above process with the right subtree of root node A, we finally obtain the required tree in given Fig. 5.



8. Consider the following undirected graph.



- ${\bf a.} \ \ {\bf Find} \ the \ adjacency \ list \ {\bf representation} \ of \ the \ graph.$
- b. Find a minimum cost spanning tree by Kruskal's algorithm.

Ans.

a.

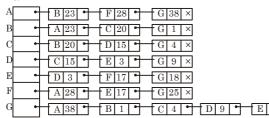
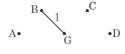


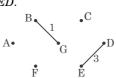
Fig. 7.

b. Kruskal's algorithm:

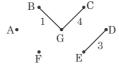
i. We will choose e = BG as it has minimum weight.



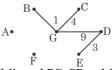
ii. Now choose e = ED.



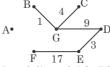
iii. Choose e = CG, since it has minimum weights.



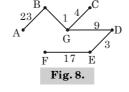
iv. Choose e = GD.



v. Choose e = EF and discard BC, $C\overline{D}$ and GE because they form cycle.



vi. Now choose e=AB and discard AG, FG and AF because they form cycle. Final minimum spanning tree is given as :



9. How do you calculate the complexity of sorting algorithms? Also, write a recursive function in 'C' to implement the merge sort on given set of integers.

Ans. Complexity of sorting algorithms:

- 1. The complexity of a sorting algorithm measures the running time as a function of the number *n* of items to be sorted.
 - 2. We know that each sorting algorithm S is made up of the following operations, where $A_1, A_2, ..., A_n$ contain the items to be sorted and B is an auxiliary location:
 - B is an auxiliary location:

 a. Comparisons, which test whether $A_i < A_j$ or test whether $A_i < B$ b. Interchanges, which switch the contents of A_i and A_j or of
 - A_i and B c. Assignments, which set $B:=A_i$ and then set $A_j:=B$ or $A_j:=A_i$
 - 3. The complexity function measures only the number of comparisons.
 4. There are two main cases whose complexity we calculate *i.e.*, the worst case and the average case.
 Function:

```
void merge (int low, int mid, int high)
{
int temp [MAX];
```

int i = low; int j = mid + 1; int k = low;

while ((i <= mid) && (j <= high))
{
 if (array [i] <= array [j])
 temp [k++] = array [i++];</pre>

else $\operatorname{temp}\left[k++\right] = \operatorname{array}\left[j++\right];$

while (i <= mid) {
temp [k++] = array [i++];
while (j <= high)
temp [k++] = array [j++];

for $(i = low; i \le high; i++)$

array [i] = temp [i];
}
void merge_sort (int low, int high)

```
SP-20 A (CS/IT-Sem-3)
```

Solved Paper (2015-16)

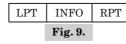
```
int mid:
if (low != high)
mid = (low + high) / 2;
merge sort (low, mid);
merge sort (mid + 1, high);
merge (low, mid, high):
```

Section-C

Note: Attempt any **two** questions from this section. $(15 \times 2 = 30)$ 10. What are doubly linked lists? Write C program to create doubly linked list.

Ans. Doubly linked list: 1. The doubly or two-way linked list uses double set of pointers, one

- pointing to the next node and the other pointing to the preceding node. 2. In doubly linked list, all nodes are linked together by multiple links which help in accessing both the successor and predecessor node
- for any arbitrary node within the list. 3. Every node in the doubly linked list has three fields:

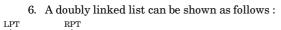


4. LPT will point to the node in the left side (or previous node) i.e., LPT will hold the address of the previous node, RPT will point to the

INFO

INFO NULL

- node in the right side (or next node) i.e., RPT will hold the address of the next node. 5. INFO field store the information of the node.



INFO

Fig. 10. Doubly linked list.

7. The structure defined for doubly linked list is: struct node

```
int info:
        struct node *rpt;
        struct node *lpt:
        node:
Program:
```

include<stdio.h>

SP-21 A (CS/IT-Sem-3)

```
struct node *first;
void main()
```

create(); getch();

include<conio.h> #include<alloc.h> struct node

> int info: struct node *lpt; struct node *rpt;

void create()

struct node *ptr, *cpt; char ch; ptr = (struct node *) malloc (size of (struct node));

printf("Input first node information");

scanf ("%d", & ptr \rightarrow info); $ptr \rightarrow lpt = NULL$; first = ptr: do

cpt = (struct node *) malloc (size of (struct node)); printf("Input next node information");

scanf ("%d", & cpt \rightarrow info); $ptr \rightarrow rpt = cpt$; $cpt \rightarrow lpt = ptr$;

ptr = cpt;

while $(ch == \Upsilon)$: $ptr \rightarrow rpt = NULL$;

ch = getch();

OR. How do you find the complexity of an algorithm? What is

printf ("Press <Y/N> for more node");

the relation between the time and space complexities of an algorithm? Justify your answer with an example. Ans. Complexity of an algorithm:

The complexity of an algorithm M is the function f(n) which gives the running time and/or storage space requirement of the algorithm in terms of the size n of the input data. 2. The storage space required by an algorithm is simply a multiple of

the data size n. 3. Following are various cases in complexity theory: **Average case:** The expected value of f(n) for any possible

Best case: The minimum possible value of f(n) for any possible

amount of space which does not depend on the input. For every size of the input the algorithm will take the same

Worst case: The maximum value of f(n) for any possible a.

b.

c.

input.

input.

input. Types of complexity:

Relation between the time and space complexities of an algorithm: 1. The time and space complexities are not related to each other. 2. They are used to describe how much space/time our algorithm takes based on the input. 3. For example, when the algorithm has space complexity of: O(1) i.e., constant then the algorithm uses a fixed (small)

1. **Space complexity:** The space complexity of an algorithm is the

2. Time complexity: The time complexity of an algorithm is the

amount of memory it needs to run to completion.

amount of time it needs to run to completion.

(constant) amount of space. O(n), $O(n^2)$, $O(\log(n))$ - these indicate that we create additional b. objects based on the length of our input. 4. In contrast, the time complexity describes how much time our

algorithm consumes based on the length of the input.

- 5. For example, when the algorithm has time complexity of: O(1) *i.e.*, constant then no matter how big is the input it always
 - takes a constant time. O(n), $O(n^2)$, $O(\log(n))$ - again it is based on the length of the h. input.

function(list *l*) {

For example: function(list 1) {

```
for (node in l) {
                            print("I got a list"); }
    print(node):
In this example, both take O(1) space as we do not create additional
objects which shows that time and space complexity might be
```

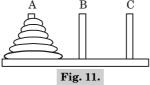
11. Write an algorithm for finding solution to the Tower of Hanoi problem. Explain the working of your algorithm (with 4 disks) with diagrams.

Ans. Tower of Hanoi problem:

different.

- 1. Suppose three pegs, labelled A, B and C is given, and suppose on peg A, there are finite number of n disks with decreasing size. 2. The object of the game is to move the disks from peg A to peg C
 - using peg B as an auxiliary. 3. The rule of game is follows:

- a. Only one disk may be moved at a time. Specifically only the top disk on any peg may be moved to any other peg.
- b. At no time, can a larger disk be placed on a smaller disk.



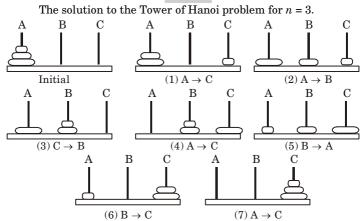


Fig. 12.

Total number of steps to solve Tower of Hanoi problem of n disk = $2^n - 1 = 2^3 - 1 = 7$

Algorithm:

TOWER (N, BEG, AUX, END)

This procedure gives a recursive solution to the Tower of Hanoi problem for N disks.

- 1. If N = 1, then:
 - a. Write: $\text{BEG} \to \text{END}$
 - b. Return [End of If structure]

2. [Move N – 1 disk from peg BEG to peg AUX]

- Call TOWER (N 1, BEG, END, AUX) 3. Write: BEG \rightarrow END
- 4. [Move N 1 disk from peg AUX to peg END]
 Call TOWER (N 1, AUX, BEG, END)
- 5. Return

Time complexity:

Let the time required for n disks is T(n).

There are 2 recursive calls for n-1 disks and one constant time operation to move a disk from 'from' peg to 'to' peg. Let it be k_l . Therefore,

TOWER (2, A, B, C)——A \rightarrow CA \rightarrow C

Fig. 13. Recursive solution to Tower of Hanoi problem for n = 4.

 \overrightarrow{TOWER} (1, B, A, C) B \rightarrow C

following 15 moves:

Observe that the recursive solution for n = 4 disks consist of the

12. Define a B-tree. What are the applications of B-tree? Draw a B-tree of order 4 by insertion of the following keys in order: Z, U, A, I, W, L, P, X, C, J, D, M, T, B, Q, E, H, S, K, N, RG, Y, F, O, V.

Ans. B-tree:

- 1. A B-tree is a self-balancing tree data structure that keeps data sorted and allows searches, sequential access, insertions, and deletions in logarithmic time.
 - 2. A B-tree of order *m* is a tree which satisfies the following properties:
 - Every node has at most *m* children.
 - Every non-leaf node (except root) has at least $\lceil m/2 \rceil$ children. b.
 - The root has at least two children if it is not a leaf node. c.
 - d. A non-leaf node with k children contains k-1 keys.
 - All leaves appear in the same level.

Application of B-tree: The main application of a B-tree is the organization of a huge collection of records into a file structure. The organization should be in such a way that any record in it can be searched very efficiently i.e., insertion, deletion and modification operations can be carried out perfectly and efficiently.

Construction of B-tree:

Insert Z: \overline{z} Insert U: UZ

Insert A: Z Insert I:

T Α U Z

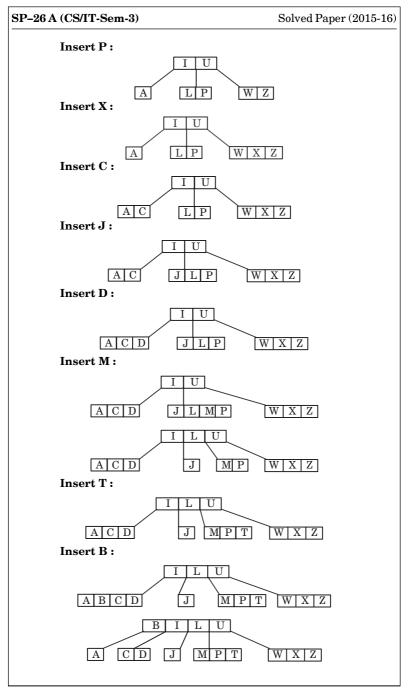
Insert W:

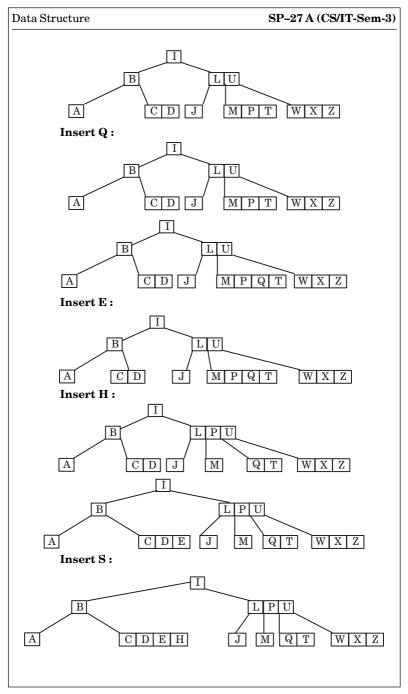
Α $\mathbf{U} \mathbf{W} \mathbf{Z}$ T Insert L: Α LUWZ U

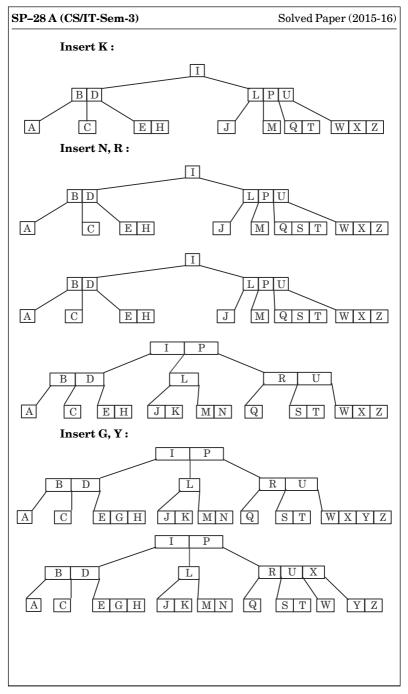
L

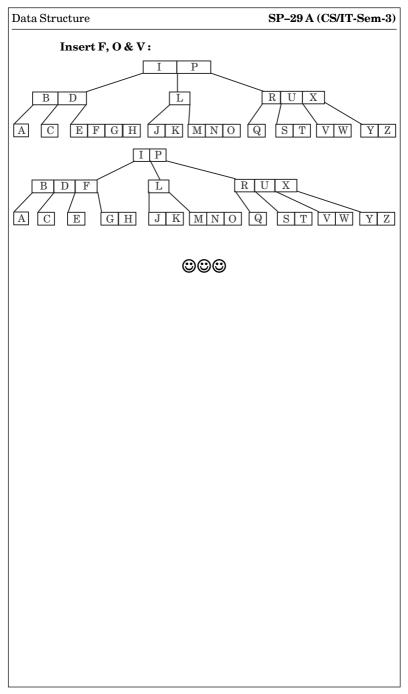
 $W \mid Z$

Α









(SEM. III) ODD SEMESTER THEORY EXAMINATION, 2016-17 DATA STRUCTURES USING 'C'

Section-A

SP-1 A (CS/IT-Sem-3)

Max. Marks: 100

1. Attempt all parts. All parts carry equal marks. Write answer of

Data Structure

Time: 3 Hours

algorithm.

each part in short. $(2 \times 10 = 20)$ a. Define time complexity and space complexity of an

b. What are the merits and demerits of array data structures?

d. Differentiate linear and non-linear data structures.

c. How do you push elements in a linked stack?

e. What is the significance of priority queue?

f. Define complete binary tree. Give example.

g. When does a graph become tree?

3. Solve the following:

graph should be even.

i. What is sorting? How is sorting essential for database applications?

h. Prove that the number of odd degree vertices in a connected

j. Give the worst case and best case time complexity of binary search.

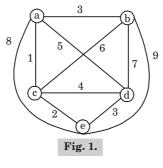
Section-B

Note: Attempt any five questions from this section. (10 × 5 = 50)
2. What is recursion? Write a recursive program to find sum of digits of the given number. Also, calculate the time complexity.

- a. ((A-(B+C)*D)/(E+F)) [Infix to postfix]
- b. $(A+B)+*C-(D-E) ^F$ [Infix to prefix]
- c. 752 + *415 /- [Evaluate the given postfix expression]
 - 4. Write a C program to implement the array representation of circular queue.
- 5. Write a C program to implement binary tree insertion, deletion with example.
- 6. Write the C program for various traversing techniques of binary tree with neat example.7. What is quick sort? Sort the given values using quick sort;
- present all steps/iterations:
 38, 81, 22, 48, 13, 69, 93, 14, 45, 58, 79, 72

 8. Illustrate the importance of various traversing techniques
- in graph along with its applications.9. Compare and contrast the difference between B+ tree index
- 9. Compare and contrast the difference between B+ tree indefiles and B-tree index files with an example.
- Note: Attempt any two questions from this section. $(15 \times 2 = 30)$
 - What is meant by circular linked list? Write the functions to perform the following operations in a doubly linked list.
 Creation of list of nodes.
 - b. Insertion after a specified node.c. Delete the node at a given position.
 - d. Sort the list according to descending order.
 - e. Display from the beginning to end.
 - 11. Define AVL trees. Explain its rotation operations with example. Construct an AVL tree with the values 10 to 1 numbers into an initially empty tree.

12. Discuss Prim's and Kruskal's algorithm. Construct minimum spanning tree for the below given graph using Prim's algorithm (Source node = a).





SOLUTION OF PAPER (2016-17)

Section-A

- 1. Attempt all parts. All parts carry equal marks. Write answer of each part in short. $(2 \times 10 = 20)$
- a. Define time complexity and space complexity of an algorithm.
 Ans. Time complexity: Time complexity is the amount of time it needs
- to run to completion.

 Space complexity: Space complexity is the amount of memory it needs to run to completion.
- b. What are the merits and demerits of array data structures?
- Ans. Merits of array:
 1. Array is a collection of elements of similar data type.
 - 2. Hence, multiple applications that require multiple data of same data type are represented by a single name.
 - Demerits of array:1. Linear arrays are static structures, *i.e.*, memory used by them cannot be reduced or extended.
 - 2. Previous knowledge of number of elements in the array is necessary.

Ans. To insert an element onto stack is known as PUSH operation. Before inserting first we increase the top pointer and then insert

the element.

c. How do you push elements in a linked stack?

d. Differentiate linear and non-linear data structures.

Ans.

S. No.	Linear data structure	Non-linear data

5. No.	Linear data structure	Non-linear data structure
1.	It is a data structure whose elements form a sequence.	It is a data structure whose elements do not form a sequence.
2.	Every element in the structure has a unique predecessor and unique successor.	There is no unique predecessor or unique successor.
3.	Examples of linear data	Examples of non-linear data

structure are arrays, linked | structures are trees and graphs.

e. What is the significance of priority queue?

lists, stacks and queues.

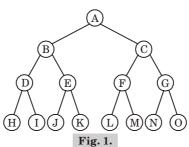
Ans. Priority queue is a data structure in which elements can be stored as per their priorities. And therefore one can remove the elements from such queue according to their priorities. Such type of queue is useful to operating system in job scheduling algorithms.

f. Define complete binary tree. Give example.

Ans. A tree is called complete binary tree if tree satisfies following conditions:

- 1. Each node has exactly two children except leaf node.
- 2. All leaf nodes are at same level.
- 3. If a binary tree contains m nodes at level l, it contains at most 2m nodes at level l+1.

Example:



g. When does a graph become tree?

Ans. A graph becomes a tree when there is exactly one path between every pair of its vertices.

h. Prove that the number of odd degree vertices in a connected graph should be even.

Ans. Let V_1 and V_2 be the set of vertices of even and odd degrees respectively. Thus, $V_1 \cap V_2 = \emptyset$ and $V_1 \cup V_2 = V$.

By Handshaking theorem,

$$2 \, | \, E \, | \ = \ \sum_{v \, \in V} \deg(v) \ = \ \sum_{v \, \in V_1} \deg(v) \ + \ \sum_{v \, \in V_2} \deg(v)$$

As both $2 \, |E|$ and $\sum_{v \, \in V_1} \deg(v)$ are even. So, $\sum_{v \, \in V_2} \deg(v)$ must be

even.

Since, $\deg(v)$ is odd for all $v \in V_2$. So, the number of odd degree vertices in a connected graph must be even.

i. What is sorting? How is sorting essential for database applications?

Ans. Sorting: It is an operation which is used to put the elements of list in a certain order. *i.e.*, either in decreasing or increasing order. Sorting essential for database applications: It is easier and faster to locate items in a sorted list than unsorted. Sorting algorithms can be used in a program to sort an array for later searching or writing out to an ordered file or report. Sorted arrays/

j. Give the worst case and best case time complexity of binary search.

lists make it easier to find things more quickly.

Ans. Worst case: In each comparison, the size of the search area is reduced by half. So, the efficiency of the binary search method at the worst case is $\log_2 n + 1$, *i.e.*, $O(\log_2 n + 1)$ where n is the total number of items that will be used for the binary search. **Best case:** The best case of binary search occurs when the element we are searching for is the middle element of the list/array because

in that case we will get the desired result in a single go. In this case.

Section-B

the time complexity of the algorithm will be O(1).

Note: Attempt any five questions from this section. (10 × 5 = 50)
2. What is recursion? Write a recursive program to find sum of digits of the given number. Also, calculate the time complexity.

Ans. Recursion:
1. Recursion is a process of expressing a function that calls itself to

#include<conio.h>
int sum(int n)

- perform specific operation.

 2. Indirect recursion occurs when one function calls another function that then calls the first function.
- 2. Indirect recursion occurs when one function calls another function that then calls the first function.Program:#include<stdio.h>

```
{
    if(n < 10)
    return(n);
    else
    return(n % 10 + sum (n / 10));
}
main()</pre>
```

int s,n; printf("\nEnter any number:"); scanf("%d",&n); s = sum(n); printf("\nSum of digits = %d", s);

SP-7A (CS/IT-Sem-3)

getch();

return 0;

as the problem is reduced by a factor of 10 each time the program recurse.

Time complexity:

ii. So, we can conclude that time taken by program is linear in terms of the length of the digit of the input number n.

i. Assume that *n* is a 10 digit number. The function is called 10 times

- iii. So, time complexity is,
- T(n) = O(length of digit of (n)) where n is the number whose sum of individual digit is to be found.
- 3. Solve the following: a. ((A-(B+C)*D)/(E+F)) [Infix to postfix]

b. $(A + B) + *C - (D - E) ^F$ [Infix to prefix] c. 752 + *415 - /- [Evaluate the given postfix expression]

```
Ans.
```

a.

```
((A - (B + C)*D)/(E + F))
```

$$((A - (B + C)*D)/(EF +))$$

 $((A - (B + C)*D)/X)$

$$((A - (BC +)*D)/X)$$

$$((A - (Y * D)) / X)$$

 $((A - (YD *)) / X)$

$$((\mathbf{A} - (\mathbf{Y}\mathbf{D}^{+})) / \mathbf{X})$$

$$((\mathbf{A} - \mathbf{Z})) / \mathbf{X})$$

$$((AZ -)/X)$$

$$(T/X)$$

ABC + D * - EF + /
This is the required postfix form.
b.
$$(A + B) + *C - (D - E) \wedge F$$

$$(+ AB) + *C - (D - E) \wedge F$$

$$X + C - (D - E) \wedge F$$

$$X + *C - (-DE) \wedge F$$

$$X + *C - (Y \wedge F)$$

Solved Paper (2016-17)

/occurred

 $X + *C - (\underbrace{Y \wedge F}_{Z})$ X + *(C - Z)X + * (-CZ)

X + *T

* + XT

* + + AB - CZ $* + + AB - C \wedge YF$

* + + $AB - C \land - DEF$

Now put the values,

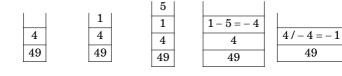
This is the required prefix form.

c. 752 + *415 - / - :

First thi

Symbol scanned	Stack
7	7
5	7, 5
2	7, 5, 2
+	7,5+2
*	7*(5+2)
4	7*(5+2), 4
1	7*(5+2), 4, 1
5	7*(5+2), 4, 1, 5
_	7*(5+2), 4, 1-5
/	7*(5+2), 4/(1-5)
_	(7*(5+2)) - (4/(1-5))

5 7	5 + 2 = 7	7*7=49
7, 5, 2 inserted	+ occurred	* occurred



4 inserted 1 inserted 5 inserted - occurred

49 - (-1) = 50- occurred

Hence, the value is 50

```
Data Structure

4. Write a C program to implement the array representation of circular queue.

Ans.

#include<stdio.h>
#include<conio.h>
#include<process.h>
#define MAX 10

typedef struct {
    int front, rear;
    int elements [MAX];
    } queue;
    void createqueue (queue *aq) {
        aq -> front = aq -> rear = -1
```

int isempty (queue *aq)

int isfull (queue *aq) {

else

else

else

else

void main()

int delete (queue *aq) {
 int temp;

return temp;

int ch, elmt;

 $if(aq \rightarrow front = = -1)$ return 1:

return 0:

return 1;

return 0;

 $aq \rightarrow front = aq \rightarrow rear = 0;$

temp = aq -> element [aq -> front]; if(aq -> front = aq -> rear) aq -> front = aq -> rear = -1;

 $aq \rightarrow front = (aq \rightarrow front + 1) \% MAX;$

aq -> rear = (aq -> rear + 1) % MAX; aq -> element [aq -> rear] = value;

void insert (queue *aq, int value) {
 if(aq -> front = = -1)

if(((aq -> front = = 0) && (aq -> rear = = MAX - 1))

| (aq - front == aq - rear + 1)|

```
SP-10 A (CS/IT-Sem-3)
```

int data;

struct bin_tree *right, *left;

Solved Paper (2016-17)

```
queue q;
                  create queue (&q);
                  while (1) {
                  printf("1. Insertion \n");
                  printf("2. Deletion \n");
                  printf("3. Exit \n");
                  printf("Enter your choice");
                  scanf("%d",&ch);.
                        switch (ch)
                                 case 1:
                                 if(isfull (&q))
                                 printf("queue is full");
                                 getch();
                                 else
                                 printf("Enter value");
                                 scanf("%d", &elmt);
                                 insert (&q, elmt);
                                 break;
                                 case 2: if (isempty (&q))
                                 printf("queue empty");
                                 getch();
                                 else
                                 printf("Value deleted is % d", delete (&q));
                                 getch();
                                 break:
                                 case 3:
                                 exit(1);
      } }
   5. Write a C program to implement binary tree insertion,
      deletion with example.
Ans. #include<stdlib.h>
      #include<stdio.h>
      struct bin_tree {
```

```
Data Structure
                                                    SP-11 A (CS/IT-Sem-3)
         };
         typedef struct bin_tree node;
         void insert(node *tree, int val)
         node *temp = NULL;
         if(!(*tree))
         temp = (node *)malloc(sizeof(node));
         temp->left = temp->right = NULL;
         temp->data = val;
         *tree = temp;
         return;
         if(val < (*tree)->data)
         insert(&(*tree)->left, val);
         else if(val > (*tree)->data)
         insert(&(*tree)->right, val);
         void print_inorder(node *tree)
         if (tree)
         print inorder(tree->left);
         printf("%d\n",tree->data);
         print_inorder(tree->right);
         void deltree(node *tree)
         if (tree)
         deltree(tree->left);
         deltree(tree->right);
         free(tree);
         void main()
         node *root:
         node *tmp;
         //int i;
         root = NULL;
         /* Inserting nodes into tree */
```

```
SP-12 A (CS/IT-Sem-3)
                                                     Solved Paper (2016-17)
         insert(&root, 9);
         insert(&root, 4);
         insert(&root, 15):
         insert(&root, 6);
         insert(&root, 12):
         insert(&root, 17);
         insert(&root, 2);
         /* Printing nodes of tree */
         printf("After insertion inorder display\n");
         print_inorder(root);
         /* Deleting all nodes of tree */
         deltree(root):
         printf("Tree is empty");
         Output of program:
         After insertion inorder display
         2
         4
         6
         9
         12
         15
         17
         Tree is empty.
```

6. Write the C program for various traversing techniques of

binary tree with neat example.

struct node* insert(struct node* r, int data);

printf("How many data do you want to insert ?\n");

Ans. #include<stdio.h>
#include<stdlib.h>
struct node

int value;
node* left;
node* right;

int main()

root = NULL; int n, v;

scanf("%d", &n); for(int i=0; i<n; i++){

struct node* root;

void inorder(struct node* r);
void preorder(struct node* r);
void postorder(struct node* r);

printf("Data %d: ", i+1);

r->value = data: r->left = NULL; r->right = NULL;

else {

return r:

if(r!=NULL){ inorder(r->left); printf("%d", r->value); inorder(r->right);

if(r!=NULL){

else if(data < r->value){ r->left = insert(r->left, data);

r->right = insert(r->right, data);

void inorder(struct node* r)

void preorder(struct node* r)

printf("%d", r->value): preorder(r->left); preorder(r->right);

SP-13 A (CS/IT-Sem-3)

scanf("%d", &v); root = insert(root, v); printf("Inorder Traversal:"); inorder(root); printf("\n"); printf("Preorder Traversal:"): preorder(root); printf("\n"); printf("Postorder Traversal:"); postorder(root); printf("\n"); return 0; struct node* insert(struct node* r, int data) if(r==NULL)

r = (struct node*) malloc(sizeof(struct node)):

```
SP-14 A (CS/IT-Sem-3)
```

and conquer.

Solved Paper (2016-17)

```
if(r!=NULL){
      postorder(r->left):
     postorder(r->right);
      printf("%d", r->value);
      Output:
      How many data do you want to insert?
      Preorder Traversal:
      32145
      Inorder Traversal:
      12345
     Postorder Traversal:
      12543
  7. What is quick sort? Sort the given values using quick sort;
      present all steps/iterations:
     38, 81, 22, 48, 13, 69, 93, 14, 45, 58, 79, 72
Ans. Quick sort:
```

void postorder(struct node* r)

2. This algorithm finds the elements, called pivot, that partitions the array into two halves in such a way that the elements in the left sub-array are less than and the elements in the right sub-array are

1. Quick sort is a sorting algorithm that also uses the idea of divide

greater than the partitioning element.

3. Then these two sub-arrays are sorted separately. This procedure is

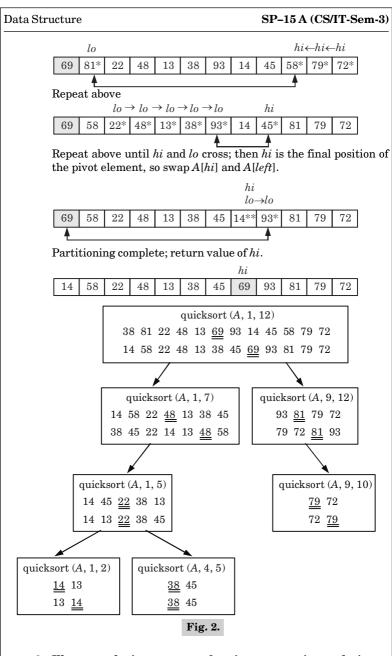
recursive in nature with the base criteria. **Numerical**: A = 38, 81, 22, 48, 13, 69, 93, 14, 45, 58, 79, 72. Choose the pivot element to be the element in position (left + right)/2.

- During the partitioning process,

 1. Elements strictly to the left of position *lo* are less than or equivalent to the pivot element (69).
- 2. Elements strictly to the right of position hi are greater than the pivot element. When lo and hi cross, we are done. The final value of hi is the position in which the partitioning element ends up. Swap pivot element with leftmost element lo = left + 1; hi = right;

•	-										
left	left+1										right
38	81	22	48	13	69	93	14	45	58	79	72
					•						

Move hi left and lo right as far as we can; then swap A[lo] and A[hi], and move hi and lo one more position.



8. Illustrate the importance of various traversing techniques in graph along with its applications.

Ans. Various types of traversing techniques are:

- 1. Breadth First Search (BFS)
- 2. Depth First Search (DFS)
- Importance of BFS:
- 1. It is one of the single source shortest path algorithms, so it is used to compute the shortest path.
- $2. \;\;$ It is also used to solve puzzles such as the Rubik's Cube.
- 3. BFS is not only the quickest way of solving the Rubik's Cube, but also the most optimal way of solving it.

Application of BFS: Breadth first search can be used to solve many problems in graph theory, for example:

- 1. Copying garbage collection.
- 2. Finding the shortest path between two nodes *u* and *v*, with path length measured by number of edges (an advantage over depth first search).
- 3. Ford-Fulkerson method for computing the maximum flow in a flow network.
- 4. Serialization/Deserialization of a binary tree vs serialization in sorted order, allows the tree to be re-constructed in an efficient manner.
- 5. Construction of the failure function of the Aho-Corasick pattern matcher.
- 6. Testing bipartiteness of a graph.

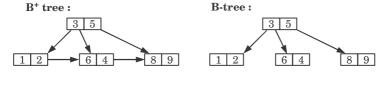
Importance of DFS : DFS is very important algorithm as based upon DFS, there are $\mathrm{O}(V+E)$ -time algorithms for the following problems :

- 1. Testing whether graph is connected.
- 2. Computing a spanning forest of G.
- 3. Computing the connected components of G.
- 4. Computing a path between two vertices of ${\it G}$ or reporting that no such path exists.
- 5. Computing a cycle in G or reporting that no such cycle exists.

 Application of DES: Algorithms that use doubt first search
- **Application of DFS:** Algorithms that use depth first search as a building block include:
- 1. Finding connected components.
- 2. Topological sorting.
- Finding 2-(edge or vertex)-connected components.
- 4. Finding 3-(edge or vertex)-connected components.
- 5. Finding the bridges of a graph.
- 6. Generating words in order to plot the limit set of a group.
- $7. \ \ Finding strongly connected components.$
- 9. Compare and contrast the difference between B+ tree index files and B-tree index files with an example.

•	72	~
	ш	ĸ

S. No. Basis		B+ tree	B-tree		
1.	Definition	B ⁺ tree is an <i>n</i> -array tree with a variable but often large number of children per node. A B ⁺ tree consists of a root, internal nodes and leaves. The root may be either a leaf or a node with two or more children.	A B-tree is an organizational structure for information storage and retrieval in the form of a tree in which all terminal nodes are at the same distance from the base, and all non-terminal nodes have between n and $2n$ sub-trees or pointers (where n is an integer).		
2.	Space complexity	O(n) $O(n)$			
3.	only in leaf nodes. and data are stored		In a B-tree, search keys and data are stored in internal or leaf nodes.		
4.	Data	The leaf nodes of the tree store the actual record rather than pointers to records. The leaf nodes of the tree store pointers to rather than actual records.			
5.	Space	These trees do not waste space.	These trees waste space.		
6.	Function of leaf nodes	In B ⁺ tree, leaf node data are ordered in a sequential linked list.	In B-tree, the leaf node cannot store using linked list.		
7.	Searching	In B ⁺ tree, searching of any data is very easy because all data is found in leaf nodes.	In B-tree, searching becomes difficult as data cannot be found in the leaf node.		
8.	Search accessibility	In B ⁺ tree, the searching becomes easy.	In B-tree, the search is not that easy as compared to a B+ tree.		
9.	Redundant key	They store redundant search key.	They do not store redundant search key.		
	Example:				



Note: Attempt any **two** questions from this section.

10. What is meant by circular linked list? Write the functions to perform the following operations in a doubly linked list.

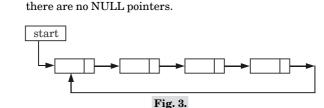
a. Creation of list of nodes. b. Insertion after a specified node.

that the last element points to the first element, Fig. 3 shows a circular linked list with 4 nodes for non-empty circular linked list,

d. Sort the list according to descending order.

c. Delete the node at a given position.

e. Display from the beginning to end. Ans. Circular linked list: A circular list is a linear linked list, except



Functions:

```
a. To create a list:
   void create()
```

```
struct node *ptr, *cpt;
char ch:
```

ptr = (struct node *) malloc (size of (struct node)); printf("Input first node information");

```
scanf ("%d", & ptr \rightarrow info);
ptr \rightarrow lpt = NULL;
```

first = ptr;do

cpt = (struct node *) malloc (size of (struct node)); printf("Input next node information"); scanf ("%d", & cpt \rightarrow info);

 $cpt \rightarrow lpt = ptr$; ptr = cpt: printf ("Press <Y/N> for more node");

 $ptr \rightarrow rpt = cpt$;

ch = getch(); while (ch == 'Y');

 $ptr \rightarrow rpt = NULL$;

b. To insert after a specific node:

void insert given node ()

SP-19 A (CS/IT-Sem-3)

```
struct node *ptr, *cpt, *tpt, *rpt, *lpt;
   int m:
   ptr = (struct node *) malloc (size of (struct node));
   if(ptr == NULL)
   printf("OVERFLOW");
   return:
   printf ("input new node information");
   scanf("%d", & ptr -> info);
   printf ("input node information after which insertion");
   scanf ("%d", & m);
   cpt = first:
   while (cpt -> info != m)
   cpt = cpt -> rpt;
   tpt = cpt -> rpt;
   cpt \rightarrow rpt = ptr;
   ptr \rightarrow lpt = cpt;
   ptr \rightarrow rpt = tpt:
   tpt -> lpt = ptr:
   printf ("Insertion is done \n");
c. To delete the node at a given position:
   void deleteNode(int data) {
   struct dllNode *nPtr, *tmp = head;
   if(head == NULL) {
   printf("Data unavailable \n"):
   return;
   else if (tmp->data == data) {
   nPtr = tmp - next:
   tmp->next = NULL;
   free(tmp):
   head = nPtr:
   totNodes--:
   } else {
   while (tmp->next != NULL && tmp->data != data) {
   nPtr = tmp:
   tmp = tmp - next;
   if(tmp->next == NULL \&\& tmp->data != data) {
   printf("Given data unavailable in list\n"):
   return:
   } else if (tmp->next != NULL && tmp->data == data) {
   nPtr->next = tmp->next;
   tmp->next->previous = tmp->previous:
```

```
tmp->next = NULL;
   tmp->previous = NULL;
   free(tmp);
   printf("Data deleted successfully\n");
   totNodes --:
   } else if (tmp->next == NULL && tmp->data == data) {
   nPtr->next = NULL;
   tmp->next = tmp->previous = NULL:
   free(tmp);
   printf("Data deleted successfully\n");
   totNodes--:
d. To sort the list according to descending order:
   void insertionSort() {
   struct dllNode *nPtr1. *nPtr2:
   int i, j, tmp;
   nPtr1 = nPtr2 = head;
   for (i = 0; i < totNodes; i++) {
   tmp = nPtr1->data:
   for (j = 0; j < i; j++)
   nPtr2 = nPtr2 - next:
   for (j = i; j > 0 \&\& nPtr2 -> previous -> data < tmp; j--) {
   nPtr2->data = nPtr2->previous->data;
   nPtr2 = nPtr2 -> previous;
   nPtr2->data = tmp:
   nPtr2 = head:
   nPtr1 = nPtr1 -> next:
e. To display from the beginning to end:
   void display()
   if(head == NULL)
   printf("\nList is Empty!!!");
   else
   struct Node *temp = head;
   printf("\nList elements are: \n");
   printf("NULL <---");</pre>
   while(temp -> next != NULL)
   printf("\%d <===>",temp -> data);
```

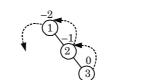
```
printf("%d ---> NULL", temp -> data);
```

11. Define AVL trees. Explain its rotation operations with example. Construct an AVL tree with the values 10 to 1 numbers into an initially empty tree.

Ans.

- i. An AVL (or height balanced) tree is a balanced binary search tree.
- ii. In an AVL tree, balance factor of every node is either -1, 0 or +1.
- iii. Balance factor of a node is the difference between the heights of left and right subtrees of that node.
 - Balance factor = height of left subtree height of right subtree
- iv. In order to balance a tree, there are four cases of rotations: 1. Left Left rotation (LL rotation): In LL rotation every node moves one position to left from the current position.

Insert 1, 2 and 3



Tree is unbalanced

To make tree balance we use LL rotation which moves nodes one position to left

After LL rotation tree is balanced

Fig. 4.

2. Right Right rotation (RR rotation): In RR rotation every node moves one position to right from the current position.

Insert 3, 2 and 1



Tree is unbalanced because node 3 has balance factor 2



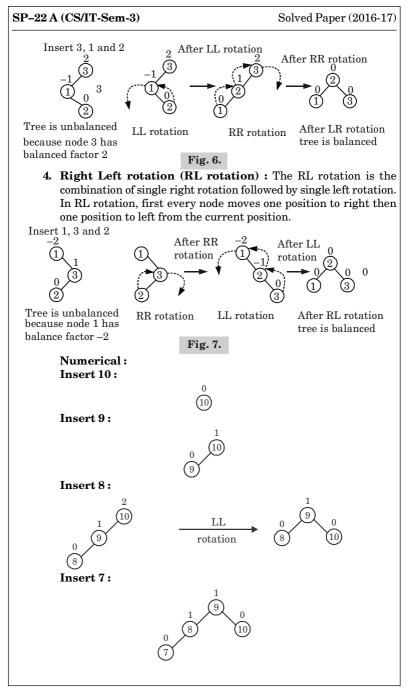
To make tree balance we use RR rotation which moves nodes one position

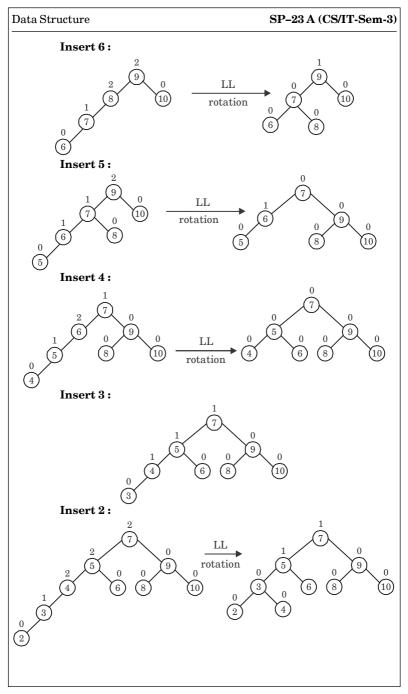


After RR Rotation tree is balanced

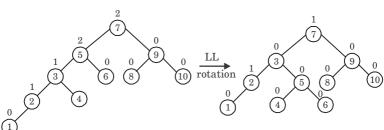
to right Fig. 5.

3. Left Right rotation (LR rotation): The LR Rotation is combination of single left rotation followed by single right rotation. In LR rotation, first every node moves one position to left then one position to right from the current position.

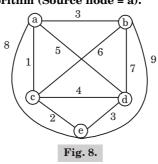




Insert 1:



12. Discuss Prim's and Kruskal's algorithm. Construct minimum spanning tree for the below given graph using Prim's algorithm (Source node = a).



Ans. Prim's algorithm:

First it chooses a vertex and then chooses an edge with smallest weight incident on that vertex. The algorithm involves following steps:

Step 1 : Choose any vertex V_1 of G.

Step 2: Choose an edge $e_1 = V_1 V_2$ of G such that $V_2 \neq V_1$ and e_1 has smallest weight among the edge e of G incident with V_1 .

Step 3: If edges e_1 , e_2 ,, e_i have been chosen involving end points V_1 , V_2 ,, V_{i+1} , choose an edge $e_{i+1} = V_j V_k$ with $V_j = \{V_1$ $V_{i+1}\}$ and $V_k \notin \{V_1$ $V_{i+1}\}$ such that e_{i+1} has smallest weight among the edges of G with precisely one end in $\{V_1$ $V_{i+1}\}$.

Step 4: Stop after n-1 edges have been chosen. Otherwise goto step 3.

Kruskal's algorithm:

- i. In this algorithm, we choose an edge of G which has smallest weight among the edges of G which are not loops.
- ii. This algorithm gives an acyclic subgraph T of G and the theorem given below proves that T is minimal spanning tree of G. Following steps are required:

Step 1 : Choose e_1 , an edge of G, such that weight of e_1 , $w(e_1)$ is as small as possible and e_1 is not a loop.

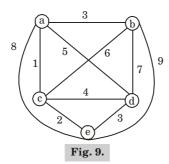
Step 2: If edges $e_1, e_2,, e_i$ have been selected then choose an edge e_{i+1} not already chosen such that

- i. the induced subgraph, $G[\{e_1, \dots, e_{i+1}\}]$ is acyclic and
- ii. $w(e_{i+1})$ is as small as possible

Step 3: If G has n vertices, stop after n-1 edges have been chosen. Otherwise repeat step 2.

If G be a weighted connected graph in which the weight of the edges are all non-negative numbers, let T be a sub-graph of G obtained by Kruskal's algorithm then, T is minimal spanning tree.

Numerical:



Start with source node = a

Now, edge with smallest weight incident on a is e = (a, c).

So, we choose e = (a, c).

Now we look on weights:

$$w(c, d) = 4, w(c, e) = 2, w(c, b) = 5$$

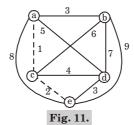
8 1 4 0 7

Fig. 10.

Since minimum is w(c, e) = 2. We choose e = (c, e)

Again,
$$w(e, d) = 3$$

 $w(e, a) = 8$
 $w(e, b) = 7$



Since minimum is w(e, d) = 3, we choose e = (e, d)

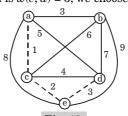
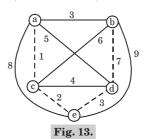
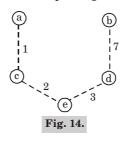


Fig. 12.

Now, w(d, b) = 7, we choose w(d, b)



Therefore, the minimum spanning tree is:



 $\Theta\Theta\Theta$

B.Tech.

(SEM. III) ODD SEMESTER THEORY EXAMINATION, 2017-18 DATA STRUCTURES

Time: 3 Hours

Max. Marks: 70

 $(2 \times 7 = 14)$

SP-1 A (CS/IT-Sem-3)

Note: Attempt all sections. Assume missing data, if any.

Section - A

- 1. Attempt all questions in brief.
- a. Define the term data structure. List some linear and nonlinear data structures stating the application area where they will be used.
- b. Discuss the concept of "successor" and "predecessor" in binary search tree.c. Convert the following arithmetic infix expression into its
 - equivalent postfix expression. Expression : A - B/C + D*E + F
- d. Explain circular queue. What is the condition if circular queue is full?

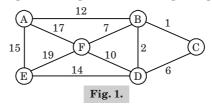
e. Calculate total number of moves for Tower of Hanoi for

- n = 10 disks.
- f. List the different types of representation of graphs.
- g. Explain height balanced tree. List general cases to maintain the height.

Section-B

- **2.** Attempt any **three** of the following: $(7 \times 3 = 21)$
- a. What do you understand by time space tradeoff? Explain best, worst and average case analysis in this respect with an example.
- b. Use quick sort algorithm to sort 15, 22, 30, 10, 15, 64, 1, 3, 9, 2. Is it a stable sorting algorithm? Justify.

c. Define spanning tree. Also construct minimum spanning tree using Prim's algorithm for the given graph.



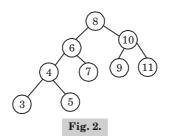
- d. Define tree, binary tree, complete binary tree and full binary tree. Write algorithm or function to obtain traversals of a binary tree in preorder, postorder and inorder.
- e. Construct a B-tree on following sequence of inputs. 10, 20, 30, 40, 50, 60, 70, 80, 90
 Assume that the order of the B-tree is 3.

Section-C

- **3.** Attempt any **one** part of the following: $(7 \times 1 = 7)$
- a. What are the various asymptotic notations? Explain Big O notation.
- Write an algorithm to insert a node at the end in a circular linked list.
- **4.** Attempt any **one** part of the following: $(7 \times 1 = 7)$
- a. What is a stack? Write a C program to reverse a string using stack.
- b. Define the recursion. Write a recursive and non-recursive program to calculate the factorial of the given number.
- **5.** Attempt any **one** part of the following: $(7 \times 1 = 7)$
- a. Draw a binary tree with following traversals:
 Inorder: BCAEGDHFIJ

 $\mathbf{Preorder}: A\ B\ C\ D\ E\ F\ G\ H\ I\ J$

b. Consider the following AVL tree and insert 2, 12, 7 and 10 as new node. Show proper rotation to maintain the tree as AVL.

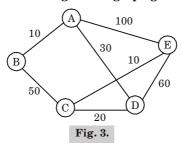


6. Attempt any **one** part of the following:

 $(7 \times 1 = 7)$

- a. What is a threaded binary tree? Explain the advantages of using a threaded binary tree.
- b. Describe Dijkstra's algorithm for finding shortest path.

 Describe its working for the graph given below.



- **7.** Attempt any **one** part of the following: $(7 \times 1 = 7)$
- a. Write short notes on:
- i. Hashing technique
- ii. Garbage collection
- b. Explain the following: $(7 \times 1 = 7)$
- i. Heap sort
- ii. Radix sort



SOLUTION OF PAPER (2017-18)

Note: Attempt all sections. Assume missing data, if any.

Section - A

1. Attempt all questions in brief.

 $(2 \times 7 = 14)$

a. Define the term data structure. List some linear and nonlinear data structures stating the application area where they will be used.

Ans. It is a particular way of storing and organizing data in a computer so that it can be used efficiently.

It can be classified into two types:

- i. Linear data structures:1. Array2. Stacks
 - 3. Queue 4. Linked list
- ii. Non-linear data structures:
 - 1. Tree
 - 2. Graph
- b. Discuss the concept of "successor" and "predecessor" in binary search tree.

Ans. In binary search tree, if a node *X* has two children, then its predecessor is the maximum value in its left subtree and its successor is the minimum value in its right subtree.

c. Convert the following arithmetic infix expression into its equivalent postfix expression.

Expression : A - B/C + D*E + F

Ans. (A - B/C + D*E + F)

Character	Stack	Postfix
((
A	(A
_	(-	A
В	(-	AB
/	(-/	AB
\mathbf{C}	(-/	ABC
+	(-+	ABC /
D	(-+	ABC / D
*	(-+*	ABC / D
\mathbf{E}	(-+*	ABC /DE
+	(- ++	ABC / DE*
\mathbf{F}	(- ++	ABC / DE*F
)	(ABC / DE*F ++ -

SP-5A (CS/IT-Sem-3)

 $(7 \times 3 = 21)$

d. Explain circular queue. What is the condition if circular queue is full?

Ans. Circular queue: A circular queue is one in which the insertion of a new element is done at the very first location of the queue if the last location at the queue is full.

Syntax to check circular queue is full:

If $((front == MAX - 1) \mid | (front == 0 \&\& rear == MAX - 1))$

e. Calculate total number of moves for Tower of Hanoi for n = 10 disks.

Ans. For *n* number of disks, total number of moves For 10 disks, *i.e.*, n = 10, total number of moves $= 2^{10} - 1$ = 1024 - 1

= 1023Therefore, if the Tower of Hanoi is operated on n = 10 disks, then total number of moves are 1023.

f. List the different types of representation of graphs.

- Ans. Different types of representation of graphs: 1. Matrix representation
 - 2. Linked representation
 - g. Explain height balanced tree. List general cases to maintain the height.

Ans.

- i. An AVL (or height balanced) tree is a balanced binary search tree. ii. In an AVL tree, balance factor of every node is either -1, 0 or +1. iii. Balance factor of a node is the difference between the heights of
- left and right subtrees of that node. Balance factor = height of left subtree - height of right subtree.

General cases to maintain the height are:

- a. Left Left rotation (LL rotation)
- b. Right Right rotation (RR rotation)
- c. Left Right rotation (LR rotation)
- d. Right Left rotation (RL rotation)

Section-B

- **2.** Attempt any **three** of the following:
- a. What do you understand by time space tradeoff? Explain best, worst and average case analysis in this respect with an example.
- Ans. Time-space trade-off:
 - 1. The time-space trade-off refers to a choice between algorithmic solutions of data processing problems that allows to decrease the

running time of an algorithmic solution by increasing the space to store data and vice-versa.

2. Time-space trade-off is basically a situation where either space efficiency (memory utilization) can be achieved at the cost of time or time efficiency (performance efficiency) can be achieved at the cost of memory.

Best, worst and average case analysis: Suppose we are implementing an algorithm that helps us to search for a record amongst a list of records. We can have the following three cases which relate to the relative success our algorithm can achieve with respect to time:

1. Best case:

a. The record we are trying to search is the first record of the list.

b. If f(n) is the function which gives the running time and f(n) storage space requirement of the algorithm in terms of the size f(n) of the input data, this particular case of the algorithm will produce a complexity f(n) = 1 for our algorithm f(n) as the algorithm will run only 1 time until it finds the desired record.

2. Worst case:

a. The record we are trying to search is the last record of the list.

b. If f(n) is the function which gives the running time and / or storage space requirement of the algorithm in terms of the size n of the input data, this particular case of the algorithm will produce a complexity C(n) = n for our algorithm f(n), as the algorithm will run n times until it finds the desired record.

3. Average case:

a. The record we are trying to search can be any record in the list.

b. In this case, we do not know at which position it might be.

C. Hence we take an average of all the possible times our algorit

c. Hence, we take an average of all the possible times our algorithm may run.

d. Hence assuming for n data, we have a probability of finding any one of them is 1/n.

e. Multiplying each of these with the number of times our algorithm might run for finding each of them and then taking a sum of all those multiples, we can obtain the complexity C(n) for our algorithm f(n) in case of an average case as following:

$$C(n) = 1 \cdot \frac{1}{2} + 2 \cdot \frac{1}{2} + \dots + n \cdot \frac{1}{2}$$

$$C(n) = (1 + 2 + \dots + n) \cdot \frac{1}{2}$$

$$C(n) = \frac{n(n+1)}{2} \cdot \frac{1}{n} = \frac{n+1}{2}$$

Hence in this way, we can find the complexity of an algorithm for average case as

$$C(n) = O((n+1)/2)$$

SP-7A (CS/IT-Sem-3)

Now, i = 1 and i = 0A[j] = A[1] = 15 and $15 \le 2$ So, i = 2 and i = 0 $A[2] = 22 \le 2$ (False) Now, j = 3 and i = 0 $A[3] = 30 \le 2$ (False)

Data Structure

j = 4 and i = 0 $A[4] = 10 \le 2 \text{ (False)}$ i = 5 $A[5] = 15 \le 2$ (False) j = 6

i = p - 1 i.e., i = 0j = 1 to 9

 $A[6] = 64 \le 2 \text{ (False)}$ j = 7 $A[7] = 1 \le 2 \text{ (True)}$ i = 0 + 1 = 1 $A[1] \leftrightarrow A[7]$ 5 1 2 3 4 6 7 8 9 10 i.e.,

22 30 10 15 15 3 64 j = 8 and i = 1 $A[8] = 3 \le 2$ (False) i = 9 and i = 1 $A[9] = 9 \le 2 \text{ (False)}$

then, $A[1+1] \leftrightarrow A[r]$ $A[2] \leftrightarrow A[10]$ $q \leftarrow 2$ 1 3 4 5 10 i.e., 30 10 15 64 15 3 22

QUICK SORT (A, 1, 1) 2 1 2 1

QUICK SORT (A, 3, 10)3 4 5 6

30 10 15 64

Here

7 8 9 10 15 3

x = A[10] = 22

22 p = 3, r = 10

$$i = 3 - 1 = 2$$

 $j = 3$ to 9; $j = 3$ and $i = 2$
 $A[3] = 30 \le 22$ (False)
 $j = 4$ and $i = 2$
 $A[4] = 10 \le 22$ (True)
 $i = 2 + 1 = 3$ and $A[3] \leftrightarrow A[4]$

i.e.,
$$\begin{bmatrix} 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ \hline 10 & 30 & 15 & 64 & 15 & 3 & 9 & 22 \\ \hline j = 5 \text{ and } i = 3 \end{bmatrix}$$

$$A[5] = 15 \le 22 \text{ (True)}$$

 $i = 3 + 1 = 4 \text{ and } A[4] \leftrightarrow A[5]$

Similarly

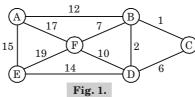
$$j = 7, i = 4$$

 $A[7] = 15 \le 22 \text{ (True)}$
 $i = 4 + 1 = 5 \text{ and } A[5] \leftrightarrow A[7]$

Similarly, we get another pivot element

Thus, this is a stable algorithm.

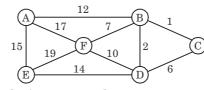
c. Define spanning tree. Also construct minimum spanning tree using Prim's algorithm for the given graph.



Ans. Spanning tree:

 A spanning tree of graph is a sub-graph which is a tree and contains all the vertices of graph.

Numerical:

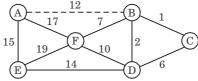


Let us take A as source node.

Now we look on weight

$$w(A, B) = 12, w(A, F) = 17, w(A, E) = 15$$

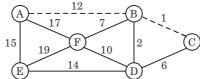
w(A, B) is smallest. Choose e = (AB)



Now we look on weight

$$w(B,\,F)=7,\,w(B,\,D)=2,\,w(B,\,C)=1$$

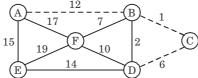
w(B, C) is smallest choose e = (BC)



Now we look on weight

$$w(C, D) = 6$$

w(C, D) is smallest choose e = (CD)

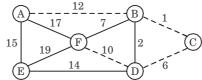


Now we look on weight

$$w(D, B) = 2, w(D, F) = 10, w(D, E) = 14$$

- w(D, B) is smallest but forms a cycle
- ∴ Discard it.

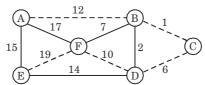
Now w(D, F) = 10 is smallest :: Choose e = (DF)



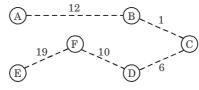
Now we look on weight

$$w(F,B) = 7, w(F,A) = 17, w(F,E) = 19$$

- :: w(F, B) is smallest but forms cycle
- : Discard it
- w(F, A) is smallest but forms cycle
- .. Discard it
- \therefore choose e = (FE)



The final minimum spanning tree is:



d. Define tree, binary tree, complete binary tree and full binary tree. Write algorithm or function to obtain traversals of a binary tree in preorder, postorder and inorder.

Tree : A tree T is a finite non-empty set of elements. One of these Ans. elements is called the root, and the remaining elements, if any is partitioned into trees is called subtree of T. A tree is a non-linear data structure.

- Binary tree: 1. A binary tree T is defined as a finite set of elements called nodes.
 - such that: *T* is empty (called the null tree).

 - T contains a distinguished node R, called the root of T, and the remaining nodes of T form an ordered pair of disjoint binary trees T_1 and T_2 .

Complete binary tree: A tree is called a complete binary tree if tree satisfies following conditions:

- a. Each node has exactly two children except leaf node.
- b. All leaf nodes are at same level.
- c. If a binary tree contains m nodes at level l, it contains at m at mnodes at level l+1.

Full binary tree:

A full binary tree is formed when each missing child in the binary tree is replaced with a node having no children.

Algorithm for preorder traversal:

Preorder (INFO, LEFT, RIGHT, ROOT)

- 1. [Initially push NULL onto STACK, and initialize PTR] Set TOP = 1, STACK [1] = NULL and PTR = ROOT
- 2. Repeat steps 3 to 5 while PTR \neq NULL
- 3. Apply process to INFO [PTR]
- 4. [Right child?] If RIGHT (PTR) ≠ NULL

Then

- [Push on STACK] Set TOP = TOP + 1 and STACK [TOP] = RIGHT [PTR] Endif 5. [Left child?]
 - If LEFT [PTR] ≠ NULL then set PTR = LEFT[PTR]Else
 - [Pop from STACK] set PTR = STACK[TOP] and TOP = TOP - 1Endif End of step 2
 - 6. Exit Algorithm for inorder traversal: Inorder (INFO, LEFT, RIGHT, ROOT)
 - 1. [Push NULL onto STACK and initialize PTR] Set TOP = 1, STACK[1] = NULL and PTR = ROOT
 - 2. Repeat while PTR≠NULL [Push leftmost path onto STACK]
 - STACK[TOP] = PTRb. Set PTR = LEFT [PTR]
 - End loop 3. Set PTR = STACK[TOP] and TOP = TOP - 1
 - 4. Repeat steps 5 to 7 while PTR ≠ NULL
 - 5. Apply process to INFO[PTR] 6. [Right Child?] If RIGHT [PTR] ≠ NULL
 - Then a. Set PTR = RIGHT [PTR]

a. Set TOP = TOP + 1 and

- b. goto step 2
- Endif 7. Set PTR = STACK[TOP] and TOP = TOP - 1
 - End of Step 4 Loop
 - 8. Exit Algorithm for postorder traversal:
 - Postorder (INFO, LEFT, RIGHT, ROOT)
 - 1. [Push NULL onto STACK and initialize PTR]
 - Set TOP = 1, STACK[1] = NULL and PTR = ROOT
 - 2. [Push leftmost path onto STACK] Repeat steps 3 to 5 while PTR ≠ NULL
 - 3. Set TOP = TOP + 1 and STACK[TOP] = PTR
 - [Pushes PTR on STACK] 4. If RIGHT [PTR] ≠ NULL
- Then

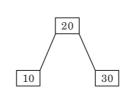
Set TOP = TOP + 1 and STACK [TOP] = RIGHT [PTR] Endif

- 5. Set PTR = LEFT [PTR] End of step 2 loop
- 6. Set PTR = STACK [TOP] and TOP = TOP 1
 [Pops node from STACK]
- [Pops node from STACK]
 7. Repeat while PTR > 0
- a. Apply process to INFO [PTR]
- b. Set PTR = STACK [TOP] and TOP = TOP 1End loop
- 8. If PTR < 0 Then
 a. Set PTR = PTR
- b. goto step 2 Endif
- 9. Exit
- e. Construct a B-tree on following sequence of inputs. 10, 20, 30, 40, 50, 60, 70, 80, 90
 Assume that the order of the B-tree is 3.

10

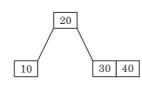
Ans. 10, 20, 30, 40, 50, 60, 70, 80, 90 Order of the *B*-tree is 3.

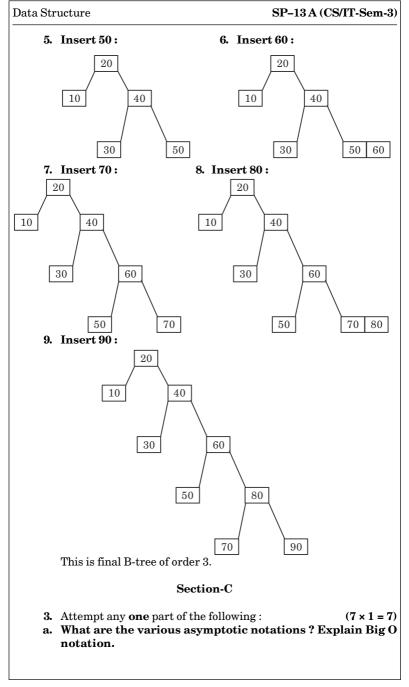
- 1. Insert 10:
- 2. Insert 20:
- 3. Insert 30:



10 | 20

4. Insert 40:



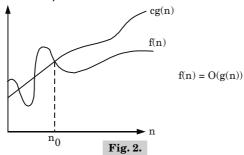


Ans. Various asymptotic notations:

- 1. θ-Notation (Same order) 2. Oh-Notation (Upper bound)
- Ω-Notation (Lower bound) 4. Little - Oh notation (o)
- 5. Little omega notation (ω) **Big Oh-Notation:**
 - 1. Big-Oh is formal method of expressing the upper bound of an algorithm's running time.
 - 2. It is the measure of the longest amount of time it could possibly take for the algorithm to complete.
 - 3. More formally, for non-negative functions, f(n) and g(n), if there exists an integer n_0 and a constant c > 0 such that for all integers $n > n_0$.

$$f(n) \le cg(n)$$

4. Then, f(n) is Big-Oh of g(n). This is denoted as : $f(n) \in O(g(n))$ *i.e.*, the set of functions which, as n gets large, grow faster than a constant time f(n).



b. Write an algorithm to insert a node at the end in a circular linked list.

Ans.

- 1. If PTR = NULL
- 2. Write OVERFLOW
- 3. Go to Step 1
- [END OF IF]
- 4. SET NEW_NODE = PTR
- 5. SET PTR = PTR -> NEXT
- 6. SET NEW_NODE -> DATA = VAL
- 7. SET NEW_NODE -> NEXT = HEAD
- 8. SET TEMP = HEAD
- 9. Repeat Step 10 while TEMP -> NEXT != HEAD
- 10. SET TEMP = TEMP -> NEXT
- IEND OF LOOPI
- 11. SET TEMP -> NEXT = NEW_NODE
- 12. EXIT

SP-15 A (CS/IT-Sem-3)

4. Attempt any **one** part of the following: a. What is a stack? Write a C program to reverse a string using stack. Ans.

- 1. A stack is one of the most commonly used data structure. 2. A stack, also called Last In First Out (LIFO) system, is a linear list
 - in which insertion and deletion can take place only at one end, called top.
 - 3. This structure operates in much the same way as stack of trays.
 - 4. If we want to remove a tray from stack of trays it can only be removed from the top only. 5. The insertion and deletion operation in stack terminology are
 - known as PUSH and POP operations. Program to reverse a string using stack:
 - #include<stdio.h>
 - #include<conio.h> #include<string.h>
 - #define MAX 20
 - int top = -1; char stack [MAX]:
 - char pop(); push(char); main()
 - clrscr(); char str [20]: int i:
 - printf("Enter the string:"); gets(str); for(i = 0; i < strlen(str); i++)push (str [i]); for(i = 0; i < strlen(str); i++)
 - str[i] = pop();printf("Reversed string is :"); puts (str); getch();
 - push (char item) if(top == MAX - 1)printf("Stack overflow\n"); else
 - stack[++top] = item;

Solved Paper (2017-18)

```
char pop()
              if(top == -1)
              printf("Stack underflow \n");
              return stack [top - -];
  b. Define the recursion. Write a recursive and non-recursive
      program to calculate the factorial of the given number.
Ans. Recursion:
   1. Recursion is a process of expressing a function that calls itself to
      perform specific operation.
  2. Indirect recursion occurs when one function calls another function
      that then calls the first function.
      Program:
      #include<stdio.h>
      #include<conio.h>
      void main()
      int n, a, b;
      clrscr();
      printf("Enter any number \n");
      scanf("%d", &n):
      a = recfactorial(n);
      printf("The factorial of a given number using recursion is %d
      \n", a);
      b = nonrecfactorial(n);
      printf("The factorial of a given number using nonrecursion is
      %d", b);
      getch();
      int recfactorial(int x)
      int f;
      if(x == 0)
      return(1);
      else
      f = x * recfactorial(x - 1);
      return(f);
```

int nonrecfactorial(int x)

SP-17A (CS/IT-Sem-3)

 $(7 \times 1 = 7)$

```
int i, f = 1;
for(i = 1; i <= x; i++)
{
  f = f * i;
}
return(f);
}</pre>
```

a. Draw a binary tree with following traversals:
Inorder: B C A E G D H F I J

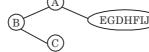
5. Attempt any **one** part of the following:

Preorder: ABCDEFGHIJ

Ans. From preorder traversal, we get root node to be A.

right child.

Now considering left subtree. Observing both the traversal we can get B as root node and C as



Now, consider the right subtree.

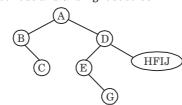
Preorder traversal is DEGFHIJ, which shows D is root node. In order traversal is EGDHFIJ, which shows EG is left subtree and

HFIJ is right subtree.

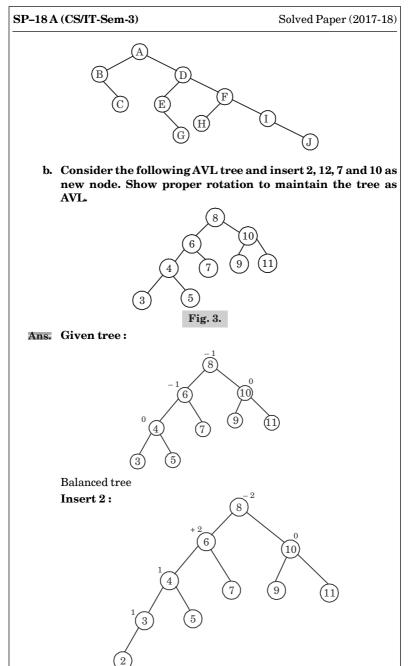
Now, consider the left subtree of D.

Preorder traversal is ${\it EG}$ and in order traversal is ${\it EG}$.

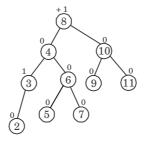
 \therefore *E* is root node and *G* is right subtree.



Similarly, following the same procedure, we finally get

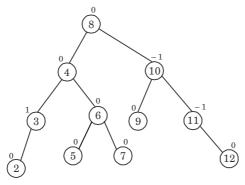


Tree is unbalanced, now LL rotation is required to balance it.



Now the tree is balanced.

Insert 12:



Tree is balanced, so there is no need to balance the tree.

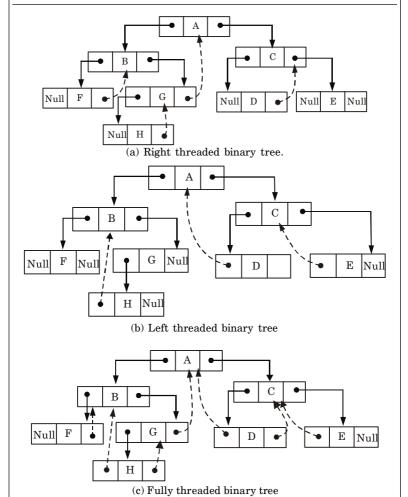
Insert 7: 7 is already in the tree hence it cannot be inserted in the AVL tree.

Insert 10: 10 is also in the tree hence it cannot be inserted in the AVL tree.

- **6.** Attempt any **one** part of the following: $(7 \times 1 = 7)$
- a. What is a threaded binary tree? Explain the advantages of using a threaded binary tree.

Ans.

- 1. To make traversal of nodes more efficient we can utilize space occupied by the NULL pointers in the leaf nodes and internal nodes having only one child node.
- 2. These pointers can be modifies to point to their corresponding inorder successor, in-order predecessor or both.
- 3. These modified pointers are known as threads and binary trees having such type of pointers are known as threaded binary tree.



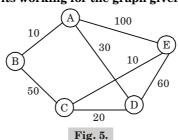
Advantages of using threaded binary tree:

 $1. \ \ In threaded binary tree the traversal operations are very fast.$

Fig. 4.

- 2. In threaded binary tree, we do not require stack to determine the predecessor and successor node.
- 3. In a threaded binary tree, one can move in any direction *i.e.*, upward or downward because nodes are circularly linked.
- 4. Insertion into and deletions from a threaded tree are all although time consuming operations but these are very easy to implement.

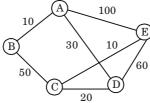
b. Describe Dijkstra's algorithm for finding shortest path.
 Describe its working for the graph given below.



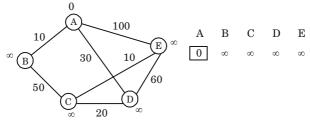
Ans. Algorithm:

- a. Dijkstra's algorithm, is a greedy algorithm that solves the single-source shortest path problem for a directed graph G=(V,E) with non-negative edge weights, *i.e.*, we assume that $w(u,v)\geq 0$ each
- edge $(u,v)\in E$. b. Dijkstra's algorithm maintains a set S of vertices whose final shortest-path weights from the source s have already been determined.
- c. That is, for all vertices $v \in S$, we have $d[v] = \delta(s, v)$.
- d. The algorithm repeatedly selects the vertex u ∈ V − S with the minimum shortest-path estimate, inserts u into S, and relaxes all edges leaving u.
 e. We maintain a priority queue Q that contains all the vertices in
- e. We maintain a priority queue Q that contains an the vertices in v-s, keyed by their d values.
- f. Graph G is represented by adjacency list.
- g. Dijkstra's always chooses the "lightest or "closest" vertex in V-S to insert into set S, that it uses as a greedy strategy.

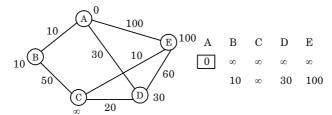
Numerical:



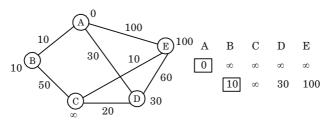
Extract min (A):



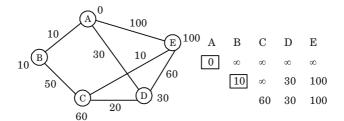
All edges leaving A:



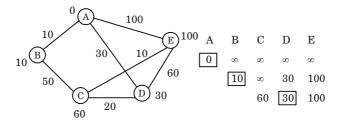
Extract min (B):



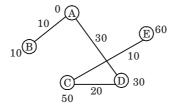
All edges leaving B:



Extract min(D):



Shortest path:



- 7. Attempt any **one** part of the following: $(7 \times 1 = 7)$
- a. Write short notes on :i. Hashing technique
- ii. Garbage collection

Ans.

- i. Hashing technique :
- Hashing technique is one of the complex searching techniques. In this technique, we consider a class of search techniques whose search time is dependent on the number of entries available in the table.
- 2. Here, we fix the position of the key (element) into the table or the file, which is determined by the hash function.
- 3. The function in which we use this key is known as the hashing function.
- 4. For example, if we want to search a number from the ten numbers of a file, then we must find the number throughout this range from the first number to the tenth number. When we use the key for fixing its position in a table, then the number can be searched very easily.

ii. Garbage collection:

- When some memory space becomes reusable due to the deletion of a node from a list or due to deletion of entire list from a program then we want the space to be available for future use.
 One method to do this is to immediately reinsert the space into the
- free-storage list. This is implemented in the linked list.

 This method may be too time enguming for the operating system.
- 3. This method may be too time consuming for the operating system of a computer.
- 4. In another method, the operating system of a computer may periodically collect all the deleted space onto the free storage list. This type of technique is called garbage collection.
- 5. Garbage collection usually takes place in two steps. First the computer runs through all lists, tagging those cells which are currently in use and then the computer runs through the memory, collecting all untagged space onto the free storage list.
- 6. The garbage collection may take place when there is only some minimum amount of space or no space at all left in the free storage list or when the CPU is idle and has time to do the collection.

 $(7 \times 1 = 7)$

- b. Explain the following:
 - i. Heap sort
- ii. Radix sort

Ans.

- i. Heap sort:
 - Heap sort finds the largest element and puts it at the end of array, then the second largest item is found and this process is repeated for all other elements.
 - 2. The general approach of heap sort is as follows:
 - a. From the given array, build the initial max heap.
 - o. Interchange the root (maximum) element with the last element.
 - c. Use repetitive downward operation from root node to rebuild the heap of size one less than the starting.
 - d. Repeat step (a) and (b) until there are no more elements.

ii. Radix sort:

- 1. Radix sort is a small method that many people uses when alphabetizing a large list of names (here Radix is 26, 26 letters of alphabet).
- 2. Specifically, the list of name is first sorted according to the first letter of each name, *i.e.*, the names are arranged in 26 classes.

 2. Intuitively, and might want to got numbers on their most
- 3. Intuitively, one might want to sort numbers on their most significant digit.
- 4. But radix sort do counter-intuitively by sorting on the least significant digits first.
- 5. On the first pass entire numbers sort on the least significant digit and combine in an array.
- 6. Then on the second pass, the entire numbers are sorted again on the second least-significant digits and combine in an array and so on.



B.Tech.

(SEM. III) ODD SEMESTER THEORY EXAMINATION, 2018-19 DATA STRUCTURES

Time: 3 Hours

Max. Marks: 70

 $(2 \times 7 = 14)$

SP-1 A (CS/IT-Sem-3)

Note: Attempt all sections. Assume missing data, if any.

Section - A

- 1. Attempt all questions in brief.
- with suitable example.

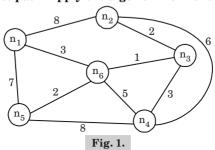
a. How the graph can be represented in memory? Explain

- b. Write the syntax to check whether a given circular queue is full or empty?
- c. Draw a binary tree for the expression: A*B-(C+D)*(P/Q)
 d. Differentiate between overflow and underflow condition in a linked list.
- e. What do you understand by stable and in-place sorting?
- f. Number of nodes in a complete tree is 100000. Find its depth.
- g. What is recursion? Give disadvantages of recursion.

Section-B

- 0 44 4 41 611 611 6 (7 0 01
- 2. Attempt any three of the following: $(7 \times 3 = 21)$ a. What do you understand by time and space tradeoff? Define the various asymptotic notations. Derive the O-notation for linear search.
 - b. Consider the following infix expression and convert into reverse polish notation using stack. $A + (B * C (D/E ^ F) * H)$
 - c. Explain Huffman algorithm. Construct Huffman tree for $\it MAHARASHTRA$ with its optimal code.

- d. What is height balanced tree? Why height balancing of tree is required? Create an AVL tree for the following elements: a, z, b, y, c, x, d, w, e, v, f.
 - Ans. Refer Q. 5.25, Page 5-33A, Unit-5.
 - e. Write the Floyd Warshall algorithm to compute the all pair shortest path. Apply the algorithm on following graph:



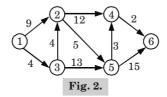
Section-C

- Attempt any one part of the following: (7 x 1 = 7)
 Write a program in C to delete a specific element in single linked list. Double linked list takes more space than single linked list for sorting one extra address. Under what condition, could a double linked list more beneficial than
- b. Suppose multidimensional arrays P and Q are declared as P(-2;2,2;22) and Q(1;8,-5;5,-10;5) stored in column major order
- i. Find the length of each dimension of P and Q
- ii. The number of elements in P and Q

single linked list.

- iii. Assuming base address (Q) = 400, W = 4, find the effective indices E_1, E_2, E_3 and address of the element Q[3, 3, 3].
 - **4.** Attempt any **one** part of the following: $(7 \times 1 = 7)$
- a. Explain Tower of Hanoi problem and write a recursive algorithm to solve it.
- b. Explain how a circular queue can be implemented using arrays. Write all functions for circular queue operations.
- 5. Attempt any **one** part of the following: $(7 \times 1 = 7)$
- a. Write the algorithm for deletion of an element in binary search tree.

- b. Construct a binary tree for the following: Inorder: Q, B, K, C, F, A, G, P, E, D, H, RPreorder: G, B, Q, A, C, K, F, P, D, E, R, HFind the postorder of the tree.
 - **6.** Attempt any **one** part of the following: $(7 \times 1 = 7)$
 - a. By considering vertex '1' as source vertex, find the shortest paths to all other vertices in the following graph using Dijkstra's algorithms. Show all the steps.



- Explain in detail about the graph traversal techniques with suitable examples.
- 7. Attempt any **one** part of the following: $(7 \times 1 = 7)$
- a. Write algorithm for quick sort. Trace your algorithm on the following data to sort the list: 2, 13, 4, 21, 7, 56, 51, 85, 59, 1, 9, 10. How the choice of pivot elements effects the efficiency of algorithm?
- b. Construct a B-tree of order 5 created by inserting the following elements 3, 14, 7, 1, 8, 5, 11, 17, 13, 6, 23, 12, 20, 26, 4, 16, 18, 24, 25, 19. Also delete elements 6, 23 and 3 from the constructed tree.



SOLUTION OF PAPER (2018-19)

Note: Attempt all sections. Assume missing data, if any.

Section - A

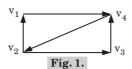
1. Attempt all questions in brief.

- $(2\times 7=14)$
- a. How the graph can be represented in memory? Explain with suitable example.

Ans. Graph can be represented in memory:

- 1. Matrix representation
- 2. Linked representation

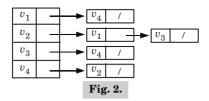
For example: Consider the following directed graph:



Matrix representation:

$$\begin{array}{c|ccccc} v_1 & v_2 & v_3 & v_4 \\ v_1 & 0 & 0 & 0 & 1 \\ v_2 & 1 & 0 & 1 & 0 \\ v_3 & 0 & 0 & 0 & 1 \\ v_4 & 0 & 1 & 0 & 0 \\ \end{array}$$

Linked representation:



b. Write the syntax to check whether a given circular queue is full or empty?

Ans. Syntax to check circular queue is full:

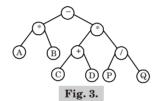
If ((front == MAX - 1) || (front == 0 && rear == MAX - 1))

Syntax to check circular queue is empty:

If (front == 0 && rear == -1)

c. Draw a binary tree for the expression : A * B - (C + D) * (P/Q)

Ans



d. Differentiate between overflow and underflow condition in a linkad list

Ans.			
S. No.	Overflow	Underflow	
1.		Underflow condition occurs when we delete data from empty linked list.	
2.	In linked list overflow occurs when AVAIL = NULL and there is an insertion operation.	In linked list underflow occurs when START = NULL and there is a deletion operation.	

e. What do you understand by stable and in-place sorting?

Ans. Stable sorting: Stable sorting is an algorithm where two objects with equal keys appear in the same order in sorted output as they appear in the input unsorted array.

In-place sorting: An in-place sorting is an algorithm that does not need an extra space and produces an output in the same memory that contains the data by transforming the input 'in-place'. However, a small constant extra space used for variables is allowed.

f. Number of nodes in a complete tree is 100000. Find its depth.

Ans. Number of nodes in a complete tree = 100000 $n = 2^{h+1} - 1$

$$(n + 1) = 2^{h+1}$$

 $\log_{2}(n + 1) = h + 1$

$$\log_2(n+1) = h + 1$$
$$\log_2(n+1) - 1 = h$$

Putting n = 100000

We know that.

 $h = \log_2(100000 + 1) - 1$ h = 15 (approx)

g. What is recursion? Give disadvantages of recursion.

Ans. Recursion: Recursion is the process of expressing a function that calls itself to perform specific operation.

Solved Paper (2018-19)

1. Recursive solution is always logical and it is very difficult to trace. debug and understand

Disadvantages of recursion:

- 2. Recursion takes a lot of stack space, usually not considerable when the program is small and running on a PC. 3 Recursion uses more processor time

Section-B

2. Attempt any three of the following: $(7 \times 3 = 21)$ a. What do you understand by time and space tradeoff? Define the various asymptotic notations. Derive the O-notation

for linear search

store data and vice-versa

- Ans Time-space trade-off: 1. The time-space trade-off refers to a choice between algorithmic solutions of data processing problems that allows to decrease the running time of an algorithmic solution by increasing the space to
 - 2. Time-space trade-off is basically a situation where either space efficiency (memory utilization) can be achieved at the cost of time or time efficiency (performance efficiency) can be achieved at the cost of memory. For Example: Suppose, in a file, if data stored is not compressed. it takes more space but access takes less time. Now if the data

stored is compressed the access takes more time because it takes time to run decompression algorithm. Various asymptotic notation : 1. θ-Notation (Same order): This notation bounds a function to

- within constant factors **2. Oh-Notation (Upper bound) :** It is the measure of the longest amount of time it could possibly take for the algorithm to complete.
- **3. Ω-Notation** (**Lower bound**) : This notation gives a lower bound for a function to within a constant factor. **4.** Little - Oh notation (o): It is used to denote an upper bound that
- is asymptotically tight because upper bound provided by O-notation is not tight. 5. Little omega notation (\omega): It is used to denote lower bound that

is asymptotically tight. **Derivation:** Best case: In the best case, the desired element is present in the

first position of the array, i.e., only one comparison is made. T(n) = O(1). Average case: Here we assume that ITEM does appear, and that

is equally likely to occur at any position in the array. Accordingly the number of comparisons can be any of the number $1, 2, 3, \ldots, n$ and each number occurs with the probability p = 1/n. Then

 $T(n) = 1 \cdot (1/n) + 2 \cdot (1/n) + 3 \cdot (1/n) \cdot \dots + n \cdot (1/n)$

SP-7 A (CS/IT-Sem-3)

$$= (1 + 2 + 3 + \dots + n) \cdot (1/n)$$

$$= n \cdot (n+1)/2 \cdot (1/n) = (n+1)/2$$

$$= O((n+1)/2) \simeq O(n)$$

Worst case: Worst case occurs when ITEM is the last element in the array or is not there at all. In this situation n comparison is made

So. $T(n) = O(n+1) \sim O(n)$

b. Consider the following infix expression and convert into reverse polish notation using stack. $A + (B * C - (D/E ^F) *$ H)

Ans. A

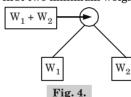
$+(B*C-(D/E \land F)*H)$									
Character	Stack	Postfix							
A	(A							
+	(+	A							
((+(A							
В	(+(AB							
*	(+ (*	AB							
C	(+ (*	ABC							
_	(+ (- (ABC*							
((+(-(ABC*							
D	(+ (- (ABC*D							
/	(+ (- (/	ABC*D							
E	(+ (- (/	ABC*DE							
^	(+ (- (/^	ABC*DE							
F	(+ (- (/^	ABC*DEF							
)	(+ (- (/^	ABC*DEF							
*	(+ (- *	ABC*DEF ^/							
н	(+(-*	ABC*DEF ^/ H							

Resultant reverse polish expression : ABC * DEF ^ / H

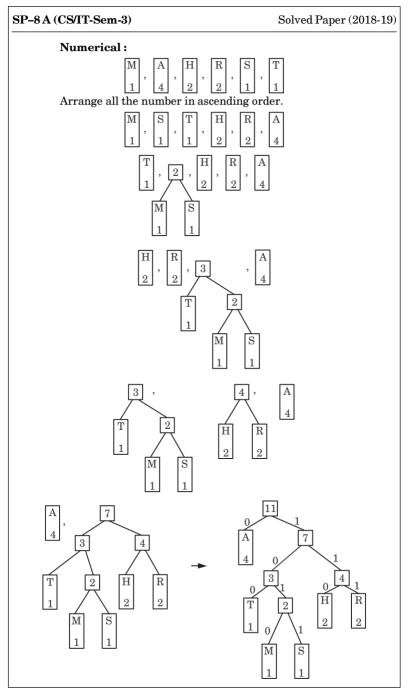
c. Explain Huffman algorithm. Construct Huffman tree for MAHARASHTRA with its optimal code.

Ans. Huffman algorithm:

- 1. Suppose, there are n weights W_1, W_2, \dots, W_n .
- Take two minimum weights among the *n* given weights. Suppose W_1 and W_2 are first two minimum weights then subtree will be:



- 3. Now the remaining weights will be $W_1 + W_2$, W_3 , W_4 ,, W_n .
- 4. Create all subtree at the last weight.



Character	Code
M	1010
A	0
Н	110
R	111
S	1011
Т	100

Optimal code for *MAHARASHTRA* **is :** 1010011001110101111110101110

101001100111010111101001110

d. What is height balanced tree? Why height balancing of tree is required? Create an AVL tree for the following elements: a, z, b, y, c, x, d, w, e, v, f.

Ans. Height balanced tree:

- i. An AVL (or height balanced) tree is a balanced binary search tree.
- ii. In an AVL tree, balance factor of every node is either -1, 0 or +1.
- iii. Balance factor of a node is the difference between the heights of left and right subtrees of that node.

Balance factor = height of left subtree - height of right subtree **Height balancing of tree** is required: Height balancing of tree is required to implement an AVL tree. Each node must contain a balance factor, which indicates its states of balance relative to its

sub-tree. **Numerical:**

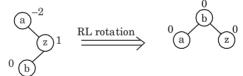
Insert a:

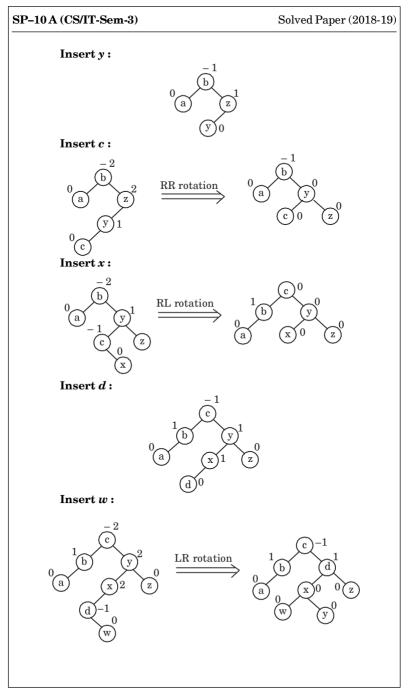
 $\begin{pmatrix} 0 \\ a \end{pmatrix}$

Insert z :

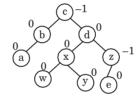


Insert b:

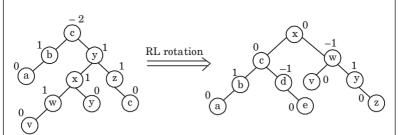




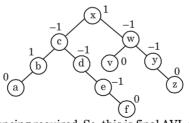
Insert e:



Insert v:

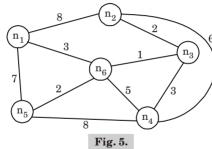


Insert f:



No, rebalancing required. So, this is final AVL search tree.

e. Write the Floyd Warshall algorithm to compute the all pair shortest path. Apply the algorithm on following graph:



```
SP-12 A (CS/IT-Sem-3)
  Ans. Floyd's Warshall algorithm:
       Flovd Warshall (w):
```

Solved Paper (2018-19)

1. $n \leftarrow \text{rows } [w]$ 2 $D^{(0)} \leftarrow w$ 3 for $b \leftarrow 1$ to n4 do for $i \leftarrow 1$ to n

5 do for $i \leftarrow 1$ to n 6. do $d_{ii}^{(k)} \leftarrow \min(d_{ii}^{(k-1)}, d_{ik}^{(k-1)} + d_{ki}^{(k-1)})$

7. return $D^{(n)}$ Numerical: We cannot solve this using Floyd Warshall algorithm

// If linked list is empty if (*head ref == NULL)

// Store head node

return:

Section-C

because the given graph is undirected.

 $(7 \times 1 = 7)$ **3.** Attempt any **one** part of the following: a. Write a program in C to delete a specific element in single linked list. Double linked list takes more space than single linked list for sorting one extra address. Under what

```
condition, could a double linked list more beneficial than
      single linked list.
Ans
     #include <stdlib.h>
```

```
// A linked list node
struct Node
int data:
struct Node *next:
/* Given a reference (pointer to pointer) to the head of a list
and an int, inserts a new node on the front of the list. */
void push(struct Node** head ref, int new data)
struct Node* new node = (struct Node*) malloc(sizeof(struct
Node)):
new node->data = new data:
new node->next = (*head ref);
(*head ref) = new node;
```

/* Given a reference (pointer to pointer) to the head of a list and a position, deletes the node at the given position */ void deleteNode(struct Node **head ref. int position)

struct Node* temp = *head_ref;
// If head needs to be removed

SP-13 A (CS/IT-Sem-3)

```
return 0;
```

Pouble linked list is more beneficial than single linked list

- 1. A double linked list can be traversed in both forward and backward direction.
- The delete operation in double linked list is more efficient if pointer to the node to be deleted is given.
- 3. In double linked list, we can quickly insert a new node before a given node.
- 4. In double linked list, we can get the previous node using previous pointer but in singly liked list we traverse the list to get the previous node.
- b. Suppose multidimensional arrays P and Q are declared as P(-2:2,2:22) and Q(1:8,-5:5,-10:5) stored in column major order
- i. Find the length of each dimension of P and Q
- ii. The number of elements in P and Q iii. Assuming base address (Q) = 400, W = 4, find the effective indices E_1, E_2, E_3 and address of the element Q[3, 3, 3].

Ans.

 The length of a dimension is obtained by Length = Upper Bound – Lower Bound + 1

Hence, the lengths of the dimension of P are,

 $L_1 = 2 - (-2) + 1 = 5$; $L_2 = 22 - 2 + 1 = 21$ The lengths of the dimension of Q are,

The lengths of the dimension of Q are, $L_1 = 8 - 1 + 1 = 8$; $L_2 = 5 - (-5) + 1 = 11$; $L_3 = 5 - (-10) + 1 = 16$

ii. Number of elements in $P = 21 \times 5 = 105$ elements

Number of elements in $Q = 8 \times 11 \times 16 = 1408$ elements

iii. The effective index E_i is obtained from $E_i = k_i - LB$, where k_i is the given index and LB, is the Lower Bound. Hence,

 $E_1 = 3 - 1 = 2$; $E_2 = 3 - (-5) = 8$; $E_3 = 3 - (-10) = 13$

The address depends on whether the programming language stores Q in row major order or column major order. Assuming Q is stored in column major order. $E_2L_2=13\times 11=143$

 $E_3^3 L_2^2 + E_2 = 143 + 8 = 151$

 $(\tilde{E}_3\tilde{L}_2)L_1 = 151 * 8 = 1208$

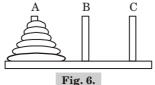
 $(E_2L_2+E_2)L_1+E_1=1208+2=1210$

Therefore, LOC(Q[3,3,3]) = 400 + 4(1210) = 400 + 4840 = 5240

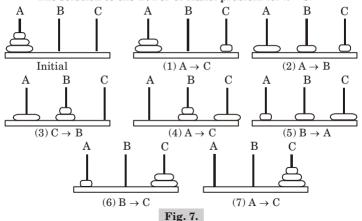
- **4.** Attempt any **one** part of the following: $(7 \times 1 = 7)$
- a. Explain Tower of Hanoi problem and write a recursive algorithm to solve it.

Ans. Tower of Hanoi problem:

- 1. Suppose three pegs, labelled A, B and C is given, and suppose on peg A, there are finite number of *n* disks with decreasing size.
- 2. The object of the game is to move the disks from peg A to peg C using peg B as an auxiliary.
- 3. The rule of game is follows:
- a. Only one disk may be moved at a time. Specifically only the top disk on any peg may be moved to any other peg.
- b. At no time, can a larger disk be placed on a smaller disk.



The solution to the Tower of Hanoi problem for n = 3.



Total number of steps to solve Tower of Hanoi problem of n disk = $2^n - 1 = 2^3 - 1 = 7$

Algorithm:

 $TOWER\,(N,\,BEG,\,AUX,\,END)$

This procedure gives a recursive solution to the Tower of Hanoi problem for N disks.

- 1. If N = 1, then:
 - a. Write: $BEG \rightarrow END$
 - b. Return

[End of If structure]

2. [Move N - 1 disk from peg BEG to peg AUX]

Call TOWER (N – 1, AUX, BEG, END)
5. Return

SP-16 A (CS/IT-Sem-3)

b. Explain how a circular queue can be implemented using arrays. Write all functions for circular queue operations.

Implementation of circular queue using array:

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Ans. Implementation of circular queue using array:
#include<stdio.h>
#include<conio.h>
#include<process.h>
#define MAX 10

typedef struct {

typedef struct {
 int front, rear;
 int elements [MAX];
 } queue;
void createqueue (queue *aq) {
 aq -> front = aq -> rear = -1

aq -> front = aq -> rear = - 1
}
int isempty (queue *aq)
{
 if(aq -> front = = - 1)
 return 1:

return 1;
else
return 0;
}
int isfull (queue *aq) {

void insert (queue *aq, int value) {
 if(aq -> front = = -1)
 aq -> front = aq -> rear = 0;
 else
 aq -> rear = (aq -> rear + 1) % MAX;
 aq -> element [aq -> rear] = value;
}

int delete (queue *aq) {
 int temp;
 temp = aq -> element [aq -> front];
 if(aq -> front = = aq -> rear)
 aq -> front = aq -> rear = -1;
 else

```
aq -> front = (aq -> front + 1) % MAX;
return temp;
}
void main()
```

SP-17 A (CS/IT-Sem-3)

Data Structure

```
int ch. elmt:
queue q:
create queue (&q):
while (1) {
printf("1. Insertion \n"):
printf("2. Deletion \n"):
printf("3. Exit \n"):
printf("Enter your choice"):
scanf("%d".&ch):.
switch (ch)
                 case 1:
                 if(isfull (&q))
                 printf("queue is full");
                 getch();
                 else
                 printf("Enter value"):
                 scanf("%d", &elmt):
                 insert (&q, elmt);
                 break;
                 case 2: if (isempty (&q))
                 printf("queue empty");
                 getch():
```

else

Function to create circular queue: void Queue :: enQueue(int value)

```
Solved Paper (2018-19)
SP-18 A (CS/IT-Sem-3)
         if((front == 0 \&\& rear == size - 1) || (rear == (front - 1)\%(size - 1)))
         printf("\nQueue is Full"):
         return:
         else if (front == -1)/* Insert First Element */
         front = rear = 0:
         arr[rear] = value:
         else if (rear == size-1 \&\& front != 0)
         rear = 0:
         arr[rear] = value:
         else
         rear++;
         arr[rear] = value:
         Function to delete element from circular queue:
         int Queue :: deQueue()
         if (front == -1)
         printf("\nQueue is Empty");
         return INT MIN;
         int data = arr[front];
         arr[front] = -1;
         if (front == rear)
         front = -1;
         rear = -1;
         else if (front == size -1)
         front = 0;
         else
         front++:
         return data:
      5. Attempt any one part of the following:
                                                                   (7 \times 1 = 7)
```

a. Write the algorithm for deletion of an element in binary

search tree.

Ans. DEL(INFO, LEFT, RIGHT, ROOT, AVAIL, ITEM) A binary search tree T is in memory, and an ITEM of information is given. This algorithm deletes ITEM from the tree.

- 1. [Find the locations of ITEM and its parent]
 Call FIND(INFO, LEFT, RIGHT, ROOT, ITEM, LOC. PAR)
- 2. ITEM in tree?
- If LOC = NULL, then write ITEM not in tree, and Exit.
- 3. [Delete node containing ITEM]
 If RIGHT|LOC| ≠ NULL and LEFT|LOC| ≠ NULL, then:

 $Call\,CASEB(INFO,LEFT,RIGHT,ROOT,LOC,PAR)$

CINE

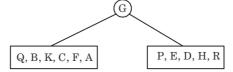
Call CASEA(INFO, LEFT, RIGHT, ROOT, LOC, PAR)
[End of If structure]

- 4. [Return deleted node to the AVAIL list]
- Set LEFT[LOC] := AVAIL and AVAIL := LOC
- 5. Exit.
- b. Construct a binary tree for the following: Inorder: Q, B, K, C, F, A, G, P, E, D, H, RPreorder: G, B, Q, A, C, K, F, P, D, E, R, HFind the postorder of the tree.

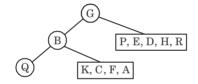
Ans. Step 1: In preorder traversal root is the first node. So, G is the root node of the binary tree. So,

 \bigcirc root

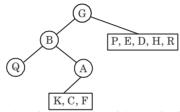
Step 2 : We can find the node of left sub-tree and right sub-tree with inorder sequence. So,



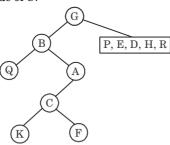
Step 3: Now, the left child of the root node will be the first node in the preorder sequence after root node G. So,



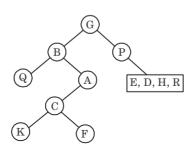
Step 4: In inorder sequence, Q is on the left side of B and A is on the right side B. So,



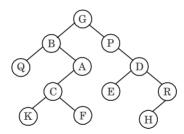
Step 5: In inorder sequence, C is on the left side of A. Now according to inorder sequence, K is on the left side of C and F is on the right side of C.



Step 6: Similarly, we can go further for right side of G.



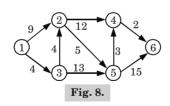
So, the final tree is



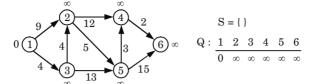
 $\textbf{Postorder of tree:}\ Q,K,F,A,B,E,H,R,D,P,G$

6. Attempt any **one** part of the following :

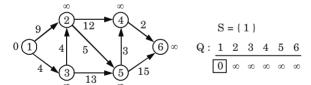
- $(7 \times 1 = 7)$
- a. By considering vertex '1' as source vertex, find the shortest paths to all other vertices in the following graph using Dijkstra's algorithms. Show all the steps.



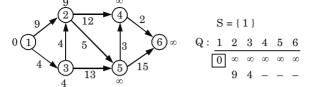
Ans. Initialize:



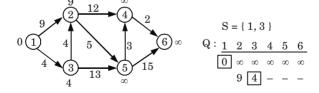
EXTRACT - MIN(1):



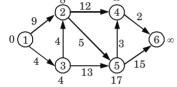
Relax all edges leaving 1:



EXTRACT - MIN (3):



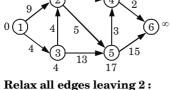
Relax all edges leaving 3:



$Q: 1 \ 2$ 3 0 ∞ 00 00 00 9 4 8 17 -

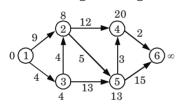
 $S = \{1, 3\}$

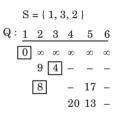
EXTRACT - MIN(2):



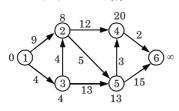
$$S = \{ 1, 3, 2 \}$$

$$Q : \underbrace{1 \ 2 \ 3 \ 4 \ 5 \ 6}_{\begin{subarray}{c|cccc} \hline 0 \ \infty & \infty & \infty & \infty & \infty \\ \hline \end{subarray}}_{\begin{subarray}{c|cccc} \hline 9 \ 4 \ - \ - & - \\ \hline \end{subarray}}$$





EXTRACT - MIN (5):

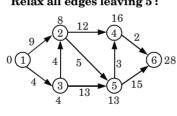


$$Q: \underbrace{1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6}_{0 \quad \infty \quad \infty \quad \infty \quad \infty \quad \infty \quad \infty}_{9 \quad 4 \quad - \quad - \quad -}$$

20 13

 $S = \{1, 3, 2, 5\}$

Relax all edges leaving 5:



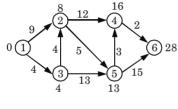
$$S = \{1, 3, 2, 5\}$$

$$Q : \underbrace{1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6}_{0 \quad \infty \quad \infty \quad \infty \quad \infty \quad \infty}_{9 \quad 4 \quad - \quad - \quad -}_{20 \quad 13 \quad -}$$

16

28

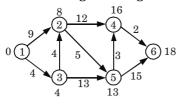
EXTRACT - MIN (4):



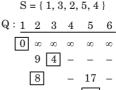
$S = \{1, 3, 2, 5, 4\}$

20 13 -16 28

Relax all edges leaving 4:



_

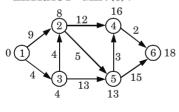


20 13 – 16 28

18

18

EXTRACT - MIN (6):



$S = \{1, 3, 2, 5, 4, 6\}$

$$Q: \underbrace{1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6}_{\begin{subarray}{ccccc} 0 & \infty & \infty & \infty & \infty & \infty \\ \hline 0 & \infty & \infty & \infty & \infty & \infty \\ \hline 9 & 4 & - & - & - \\ \hline 8 & - & 17 & - \\ \hline \end{subarray}}$$

20 13 -16 28

suitable examples. Ans. Following are the two traversal techniques:

Ans. Following are the two trav 1. Depth First Search (DFS):

The general idea behind a depth first search beginning at a starting node A is as follows:

b. Explain in detail about the graph traversal techniques with

- a. First, we examine the starting node A.
- b. Then, we examine each node N along a path P which begins at A; that is, we process neighbour of A, then a neighbour of neighbour of A, and so on.
- c. This algorithm uses a stack instead of queue.

Algorithm:

- i. Initialize all nodes to ready state (STATUS = 1).
- ii. Push the starting node A onto stack and change its status to the waiting state (STATUS = 2).

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- iii. Repeat steps (iv) and (v) until queue is empty. iv. Pop the top node N of stack, process N and change its status to the
- processed state (STATUS = 3).

 v. Push onto stack all the neighbours of *N* that are still in the ready state (STATUS = 1) and change their status to the waiting state
 - (STATUS = 2).
 [End of loop]
 vi. End.

For example : Consider the following graph

Fig. 9.

Adjacency list of the given graph:

$$1 \rightarrow 2, 3$$

$$2 \rightarrow 4$$

$$3 \rightarrow 2$$

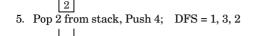
 $4 \rightarrow 3$, 1

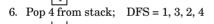
- 1. Initially set STATUS = 1 for all vertex
- 2. Push 1 onto stack and set their STATUS = 2

3. Pop 1 from stack, change its STATUS = 1 and
Push 2. 3 onto stack and change their STATUS = 2: DFS = 1

h 2,	, 3	onto	stack	and	change	e their	STAT
3	+						

4. Pop 3 from stack, Push 2, but it is already in the stack; DFS = 1, 3





Now, the stack is empty, so the depth first traversal of a given graph is 1, 3, 2, 4.

2. Breadth First Search (BFS):

The general idea behind a breadth first search beginning at a starting node A is as follows:

- a. First we examine the starting node A.
- b. Then, we examine all the neighbours of A, and so on.
- c. We need to keep track of the neighbours of a node, and that no node is processed more than once.
- d. This is accomplished by using a queue to hold nodes that are waiting to be processed, and by using a field STATUS which tells us the current status of any node.
 - **Algorithm:** This algorithm executes a breadth first search on a graph G beginning at a starting node A.
 - i. Initialize all nodes to ready state (STATUS=1).
- ii. Put the starting node A in queue and change its status to the waiting state (STATUS = 2).
 iii. Repeat steps (iv) and (v) until queue is empty.
- iii. Repeat steps (iv) and (v) until queue is empty.iv. Remove the front node N of queue. Process N and change the status of N to the processed state (STATUS = 3).
 - v. Add to the rear of queue all the neighbours of N that are in the ready state (STATUS=1) and change their status to the waiting state (STATUS = 2).

[End of loop]vi. End.For example: Consider the same graph in Fig. 11.

Adjacency list of the graph is:

- 2 : 4
- 3 : 2 4 : 1.3
- a. Initially set STATUS=1 for all vertex.

To find the shortest path from node 1 to node 4.

- b. Now add '1' to Queue and set STATUS = 2 Queue : 1
- c. Remove 1 from Queue and set STATUS = 3
 and add 2, 3 in Queue and change their STATUS = 2
- BFS = 1 Queue : 2, 3 d. Remove 2, add 4 in Queue
- d. Remove 2, add 4 in Queu BFS = 1, 2 Queue = 3, 4
- BFS = 1, 2 Queue = 3, 4 e. Remove 3, add 2, but 2 is already visited. So no vertex will be added

in this step

BFS = 1, 2, 3, Queue = 4 f. Remove 4, BFS = 1, 2, 3, 4

- Now, the Queue is empty, so breadth first search of a given graph is 1, 2, 3, 4.
- is 1, 2, 3, 4.

 7. Attempt any **one** part of the following: $(7 \times 1 = 7)$
- a. Write algorithm for quick sort. Trace your algorithm on the following data to sort the list: 2, 13, 4, 21, 7, 56, 51, 85, 59,

1. 9. 10. How the choice of pivot elements effects the efficiency of algorithm? Quick sort algorithm: Ans. QUICK-SORT (A, p, r): 1. If p < r then 2. $q \leftarrow \text{PARTITION}(A, p, r)$ 3. QUICK-SORT (A, p, q - 1)4. QUICK-SORT (A, a + 1, r)PARTITION (A, p, r): 1. $x \leftarrow A[r]$ $2. i \leftarrow p-1$ 3. for $i \rightarrow p$ to r-1do if $A[i] \leq x$ 4 5 then $i \rightarrow i + 1$ 6 exchange $A[i] \leftrightarrow A[i]$ 7. exchange $A[i+1] \leftrightarrow A[r]$ 8. return i+1Numerical: 1 2 4 7 9 10 5 6 8 11 12 9 13 4 21 56 51 85 59 1 10 Here p = 1, r = 12x = A[12] = 10i = p - 1 = 0

i = 1 + 0 = 1i = 1 and i = 0

A[1] = 2 < 10 (True)

i = 2 and i = 1 $A[2] = 13 \text{ and } 13 \nleq 10 \text{ (False)}$

i = 1 $A[3] = 4 \text{ and } 4 \le 10 \text{ (True)}$

i = 3

4 5 6 7 8 9 10 11 12

j = 4 and i = 2

21 13

i = 6 and i = 3 $A[6] = 56 \text{ and } 56 \ 10$

i = 7 and i = 3 $A[7] = 51 \text{ and } 51 \nleq 10$

3

13 21

3 4 5 6 7 8 9 10 11 12

7

i = 0 + 1 = 1 and $A[1] \leftrightarrow A[1]$

i = 1 + 1 = 2 and $A[2] \leftrightarrow A[3]$

 $i = 2 + 1 = 3 \text{ and } A[3] \leftrightarrow A[5]$

56 51 85 59 10

10

56 51 85 59 1

 $A[4] = 21 \text{ and } 21 \neq 10 \text{ (False)}$ i = 5 and i = 2 $A[5] = 7 \le 10 \text{ (True)}$

Now.

then

Now.

So.

then.

i.e.,

Now.

then,

i.e.,

So.

Now.

1 2

2

1

2

4

Choice of pivot element affects the efficiency of algorithm: If we choose the last or first element of an array as pivot element

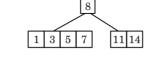
then it results in worst case scenario with $O(n^2)$ time complexity. If we choose the median as pivot element then it divides the array into two halves every time and results in best or average case scenario with time complexity $O(n \log n)$. Thus, the efficiency of quick sort algorithm depends on the choice of pivot element.

b. Construct a B-tree of order 5 created by inserting the following elements 3, 14, 7, 1, 8, 5, 11, 17, 13, 6, 23, 12, 20, 26, 4, 16, 18, 24, 25, 19, Also delete elements 6, 23 and 3 from the constructed tree

Ans.

$\mathbf{Insert}\ 3:$	3
Insert 14:	3 14
Insert 7:	3 7 14
Insert 1:	1 3 7 14
	8
Insert 8:	1 3 7 14
Insert 5:	
	8

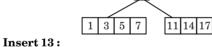
Insert 11:



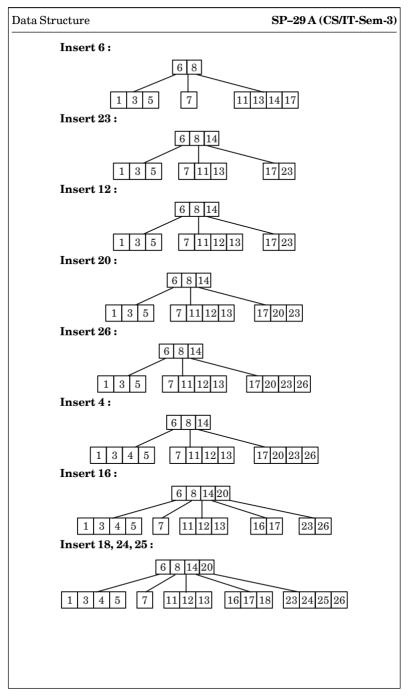
8

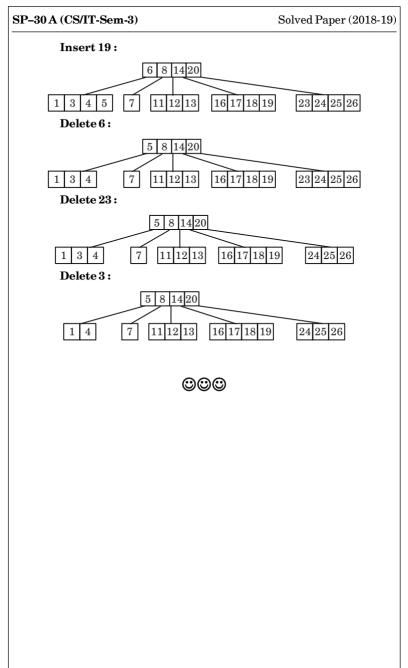
3 5

Insert 17:









Section-A

e. Define priority queue. Given one application of priority

g. What is minimum cost spanning tree? Give its

SP-1 C (CS-Sem-3)

 $(2 \times 10 = 20)$

Time: 3 Hours Max. Marks: 100 Note: 1. Attempt all Section.

b. List the various operations on linked list.

Data Structures

1. Answer **all** questions in brief. a. How can you represent a sparse matrix in memory?

c. Give some applications of stack.

d. Explain tail recursion.

queue.

applications.

f. How does bubble sort work? Explain.

h. Compare adjacency matrix and adjacency list representations of graph.

i. Define extended binary tree, full binary tree, strictly binary tree and complete binary tree.

j. Explain threaded binary tree.

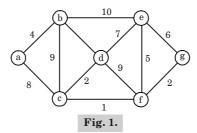
Section-B

2. Answer any **three** of the following: $(3 \times 10 = 30)$ a. What are the merits and demerits of array? Given two arrays of integers in ascending order, develop an algorithm to merge these arrays to form a third array sorted in ascending order.

b. Write algorithm for push and pop operations in stack. Transform the following expression into its equivalent postfix expression using stack: $A + (B * C - (D/E \uparrow F) * G) * H$

 $(1 \times 10 = 10)$

- c. How binary search is different from linear search? Apply binary search to find item 40 in the sorted array: 11, 22, 30, 33, 40, 44, 55, 60, 66, 77, 80, 88, 99. Also discuss the complexity of binary search.
- d. Find the minimum spanning tree in the following graph using Kruskal's algorithm :



- e. What is the difference between a binary search tree (BST) and heap? For a given sequence of numbers, construct a heap and a BST.
 - 34, 23, 67, 45, 12, 54, 87, 43, 98, 75, 84, 93, 31

Section-C

- **3.** Answer any **one** part of the following :
- a. What is doubly linked list? What are its applications? Explain how an element can be deleted from doubly linked list using C program.
- b. Define the following terms in brief:
- i. Time complexity ii. Asymptotic notation
- iii. Space complexity iv. Big O notation
 - **4.** Answer any **one** part of the following: $(1 \times 10 = 10)$
- a. i. Differentiate between iteration and recursion.
 - ii. Write the recursive solution for Tower of Hanoi problem.
 - b. Discuss array and linked representation of queue data structure. What is dequeue?
 - **5.** Answer any **one** part of the following: $(10 \times 1 = 10)$
 - a. Why is quick sort named as quick? Show the steps of quick sort on the following set of elements: 25, 57, 48, 37, 12, 92, 86, 33

 Assume the first element of the list to be the pivot element.

- b. What is hashing? Give the characteristics of hash function.
 Explain collision resolution technique in hashing.
- **6.** Answer any **one** part of the following: $(1 \times 10 = 10)$
- ${\bf a.} \ \ Explain \ Warshall's \ algorithm \ with \ the \ help \ of \ an \ example.$
- b. Describe the Dijkstra algorithm to find the shortest path. Find the shortest path in the following graph with vertex 'S' as source vertex.

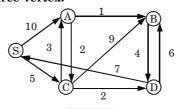


Fig. 2.

- **7.** Answer any **one** part of the following: $(7 \times 1 = 7)$
- a. Can you find a unique tree when any two traversals are given? Using the following traversals construct the corresponding binary tree:

 INORDER: HKDBILEAFCMJG

PREORDER: ABDHKEILCFGJM

Also find the post order traversal of obtained tree.

b. What is a B-Tree? Generate a B-Tree of order 4 with the alphabets (letters) arrive in the sequence as follows:
 a g f b k d h i n j e s i r x c l n t u p.



SOLUTION OF PAPER (2019-20)

Note: 1. Attempt all Section.

Section-A

1. Answer **all** questions in brief.

- $(2 \times 10 = 20)$
- a. How can you represent a sparse matrix in memory?
- Ans. There are two ways of representing sparse matrix in memory:
 - 1. Array representation 2. Linked representation
 - b. List the various operations on linked list.
- Ans. Various operations on linked list are:
- - 1. Insertion at beginning
 - 2. Insertion at end
 - 3. Deletion at beginning
 - 4. Deletion at end 5. Deletion of an element at specified location
 - 6. Insertion of an element at specified location
 - c. Give some applications of stack.
- Ans. Applications of stack are:

 - i. Infix to postfix conversion.
 - ii. Implementing function calls.
 - iii. Page-visited history in a web browser.
 - iv. Undo sequence in a text editor.
 - d. Explain tail recursion.

Ans.

Tail recursion (or tail-end recursion) is a special case of recursion in which the last operation of the function, the tail call is a recursive call. Such recursions can be easily transformed to iterations.

- e. Define priority queue. Given one application of priority queue.
- Ans. A priority queue is a data structure in which each element has been assigned a value called the priority of the element and an element can be inserted or deleted not only at the ends but at any position on the queue.

Applications of priority queue: In network communication, to manage limited bandwidth for transmission, the priority queue is used.

f. How does bubble sort work? Explain.

- Ans. Bubble sort procedure is based on following idea:
- a. Suppose if the array contains n elements, then (n-1) iterations are required to sort this array.
 - b. The set of items in the array are scanned again and again and if any two adjacent items are found to be out of order, they are reversed.
 - c. At the end of the first iteration, the lowest value is placed in the first position.
 - d. At the end of the second iteration, the next lowest value is placed in the second position and so on. $\,$

g. What is minimum cost spanning tree? Give its applications.

Ans. Minimum cost spanning tree: In a weighted graph, a minimum spanning tree is a spanning tree that has minimum weight than all other spanning trees of the same graph.

- Application of minimum cost spanning tree:

 1. Used for network designs.
- 2. Used to find approximate solutions for complex mathematical problems.
- 3. Cluster analysis.

h. Compare adjacency matrix and adjacency list representations of graph.

Ans.

S. No.	Adjacency matrix	Adjacency list	
1.	An adjacency matrix is a square matrix used to represent a finite graph.		
2.	The elements of the matrix indicate whether pairs of vertices are adjacent or not in the graph.	Each list describes the set of adjacent vertices in the graph.	
3.	Space complexity in the worst case is $O(V ^2)$.	Space complexity in the worst case is $O(V + E)$.	

- i. Define extended binary tree, full binary tree, strictly binary tree and complete binary tree.
- Ans. Extended binary tree: A binary tree *T* is said to be 2-tree or extended binary tree if each node has either 0 or 2 children.

 Full binary tree: A full binary tree is formed when each missing child in the binary tree is replaced with a node having no children.

binary tree.

Solved Paper (2019-20)

Complete binary tree: A tree is called a complete binary tree if tree satisfies following conditions: a. Each node has exactly two children except leaf node.

- All leaf nodes are at same level.
- c. If a binary tree contains m nodes at level l, it contains at m at mnodes at level l + 1.

j. Explain threaded binary tree. Ans.

- 1. To make traversal of nodes more efficient we can utilize space occupied by the NULL pointers in the leaf nodes and internal nodes having only one child node.
- 2. These pointers can be modifies to point to their corresponding inorder successor, in-order predecessor or both.
- 3. These modified pointers are known as threads and binary trees having such type of pointers are known as threaded binary tree.

Section-B

- **2.** Answer any **three** of the following:
 - $(3 \times 10 = 30)$ a. What are the merits and demerits of array? Given two arrays of integers in ascending order, develop an

algorithm to merge these arrays to form a third array

- sorted in ascending order. Ans. Merits of array:
 - 1. Array is a collection of elements of similar data type. 2. Hence, multiple applications that require multiple data of same

data type are represented by a single name.

- **Demerits of array:** 1. Linear arrays are static structures, i.e., memory used by them
- cannot be reduced or extended. 2. Previous knowledge of number of elements in the array is
- necessary. **Algorithm :** Algorithm receives as input indexes i, m, and j and an array a, where $a[i], \dots, a[m]$ and $a[m+1], \dots, a[i]$ are two sorted in

asecnding order. These two sorted arrays are merged into a single

ascending array. merge (a, i, m, j) { // index in $a[i] \dots a[m]$ p = iq = m + 1// index in $a [m+1] \dots a [j]$

// index of array C r = iwhile $(p \le m L q \le j)$ { if $(a [p] \le a [q])$ {

c[r] = a[p];p = p + 1;

SP-7 C (CS-Sem-3)

```
else { c[r] = a[q]; \\ q = q + 1; \\ \} \\ r = r + 1; \\ \} \\ \text{while } (p \le m) \{ \\ c[r] = a[p] \\ p = p + 1; \\ r = r + 1; \\ \} \\ \text{while } (q \le j) \\ c[r] = a[q] \\ q = q + 1; \\ r = r + 1; \\ \} \\ \text{for } (r = i \text{ to } j) \\ a[r] = c[r]
```

b. Write algorithm for push and pop operations in stack. Transform the following expression into its equivalent postfix expression using stack: $A + (B * C - (D/E \uparrow F) * G) * H$

Digit (CMA CIX MOD MAX DAMA)

- PUSH (STACK, TOP, MAX, DATA)

 1. If TOP = MAX 1 then write "STACK OVERFLOW and STOP"
- 3. $TOP \leftarrow TOP + 1$

2. READ DATA

- 4. STACK [TOP] ← DATA
- 5. STOP

Algorithm for POP operation:
POP (STACK, TOP, ITEM)

- 1. If TOP < 0 then write "STACK UNDERFLOW and STOP"
- 1. If for a fine write of
- 2. STACK [TOP] \leftarrow NULL
- 3. TOP ← TOP 1
- 4. STOP Numerical: $A + (B*C (D/E \uparrow F)*G) * H$

Character

Postfix

	A			
	A			
	A			
,	AB			
	AB AB			
	ABC			
,	ABC*			
1 ' '				
, ,	ABC*			
1 ' '	ABC*D			
	ABC*D			
1 1 1	ABC*DE			
1	ABC*DE			
1 1 1	ABC*DEF			
+ (− (/↑	ABC*DEF			
+ (- *	ABC*DEF ↑/			
+ (- *	ABC*DEF ↑/ G			
+	$ABC*DEF^{\uparrow}/G* -$			
+ *	ABC*DEF↑/G* –			
+*	ABC*DEF↑/G* – H			
Resultant postfix expression : ABC*DEF $^/G^* - H^* +$ How binary search is different from linear search? Apply binary search to find item 40 in the sorted array: 11, 22, 30, 33, 40, 44, 55, 60, 66, 77, 80, 88, 99. Also discuss the complexity of binary search.				
	+ (-* + +* +* xpression : ABC*DEI ch is different from find item 40 in the 6, 77, 80, 88, 99. Also			

Stack

Ans. Difference:

c.

S. No.	Binary search	Sequential (linear) search	
1.	Elementary condition <i>i.e.</i> , array should be sorted.	No elementary condition <i>i.e.</i> , array can be sorted or unsorted.	
2.	It takes less time to search an element.	It takes long time to search an element.	
3.	Complexity is $O(\log 2 n)$.	Complexity is $O(n)$.	
4.	It is based on divide and conquer method.	It searches data linearly.	
	Numerical : Given sorted array :		

6

55 | 60

7 8

66

9

70

10

80

11 12

88

99

u array 3 1

5

44

	0	1	2	3	4	
A	11	22	30	33	40	
To search element 40						

SP-9 C (CS-Sem-3)

40 < a[6]end = 6 - 1 = 5Now, beg = 0 end = 5

 $mid = (0 + 5)/2 = \lfloor 2.5 \rfloor = 2$

beg = 0, end = 12mid = (0 + 12)/2 = 6

 $a[mid] = a[2] = 30 \neq 40 (False)$ 40 > a[2]

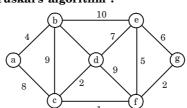
 $a[mid] = a[6] = 55 \neq 40 \text{ (False)}$

beg = 2 + 1 = 3Now, beg = 3, end = 5mid = (3 + 5)/2 = 4

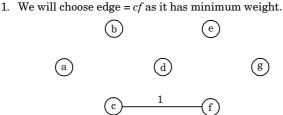
a[mid] = a[4] = 40 (True)loc = 4So, element 40 is present at location 4.

Complexity of binary search: The complexity of binary search is $O(\log_2 n)$.

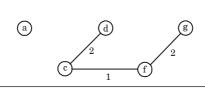
d. Find the minimum spanning tree in the following graph using Kruskal's algorithm:



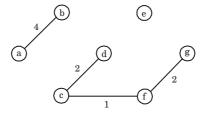
Ans.



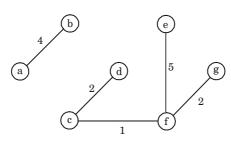
2. Now choose edge = cd and fg as it has minimum weight.



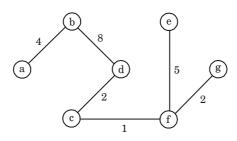
3. Now choose edge = ab



4. Now choose edge = eg



5. Now choose edge = bd and discard be, eg, de, df, bc and ac because they form cycle and we get the final minimal spanning tree as



e. What is the difference between a binary search tree (BST) and heap? For a given sequence of numbers, construct a heap and a BST. 34, 23, 67, 45, 12, 54, 87, 43, 98, 75, 84, 93, 31

Ans.

Heap

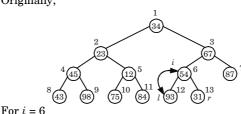
SP-11 C (CS-Sem-3)

Difference: S. No. | Binary search tree (BST)

	•		
1.	In binary search tree, for every node except the leaf node, the left child has a less key value and right child has a greater key value.	than the root, the key value of the parent node is greater or	
2.	It guarantees the order (from left to right).	It guarantees that the element at higher level is smaller or greater than element at lower level.	
3.	Time complexity to find min/ max element is $O(\log n)$.	Time complexity to find min/max is $O(1)$.	

Numerical:

Construction of heap:



MAX-HEAPIFY (A, 6)

l = 12 r = 13

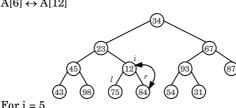
12 < 13 and A[12] = 93 A[6] = 34

A[12] > A[6] $largest \leftarrow 12$

13 = 13 A[13] = 31 A[12] = 93

A[13] > A[12]

Exchange $A[i] \leftrightarrow A[l]$ $A[6] \leftrightarrow A[12]$

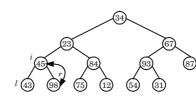


Solved Paper (2019-20)

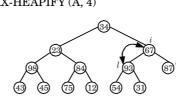
l = 10 r = 1110 < 13 and A[10] > A[5] $largest \leftarrow 10$ 11 < 13 and A[11] > A[10] $largest \leftarrow 11$

MAX-HEAPIFY (A, 5)

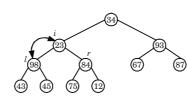
Exchange $A[5] \leftrightarrow A[11]$



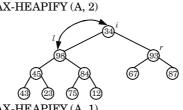
After MAX-HEAPIFY (A, 4)



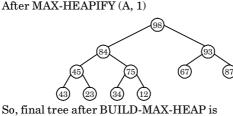
After MAX-HEAPIFY (A, 3)

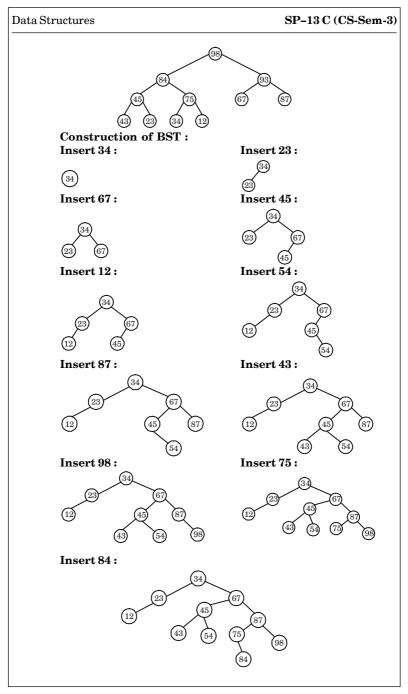


After MAX-HEAPIFY (A, 2)

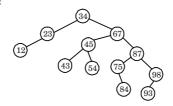


After MAX-HEAPIFY (A, 1)

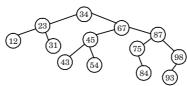




Insert 93:



Insert 31:



Section-C

- **3.** Answer any **one** part of the following : $(1 \times 10 = 10)$ a. What is doubly linked list? What are its applications?
 - Explain how an element can be deleted from doubly linked

list using C program. Ans. Doubly linked list:

- 1. The doubly or two-way linked list uses double set of pointers, one pointing to the next node and the other pointing to the preceding node.
- 2. In doubly linked list, all nodes are linked together by multiple links which help in accessing both the successor and predecessor node for any arbitrary node within the list. Applications of doubly linked list are:

- 1. Doubly linked list can be used in navigation systems where both front and back navigation is required. 2. It is used by browsers to implement backward and forward
- navigation of visited web pages.
- 3. It is used by various applications to implement undo and redo functionality.
- 4. It can be used to represent deck of cards in games.
- 5. It is used to represent various states of a game.

Deletion from doubly linked list using C program: #include<stdio.h>

#include<conio.h> typedef struct n{

int data: struct n *prev;

struct n *next;

}node:

```
getch();
      return;
     if(head == tail) {
      free(h);
     head = tail = (node *)NULL;
      return;
      if(h>next==t) {
      tail->prev = NULL;
      head = tail:
     else {
     head = head->next:
     head->prev = NULL;
      free(h);
  b. Define the following terms in brief:
                                    ii. Asymptotic notation
   i. Time complexity
 iii. Space complexity
                                    iv. Big O notation
Ans.
   i. Time complexity
  1. The complexity of an algorithm M is the function f(n) which gives
     the running time and/or storage space requirement of the
     algorithm in terms of the size n of the input data.
  2. The storage space required by an algorithm is simply a multiple of
     the data size n.
  3. Following are various cases in complexity theory:
```

node *head = NULL, *tail = NULL; Function to delete element: void delete beg(node *h. node *t) { if(head == (node*)NULL) { printf("\nList is empty.");

ii. Asymptotic notation: 1. Asymptotic notation is a shorthand way to describe running times

input.

- for an algorithm. 2. It is a line that stays within bounds.
- 3. These are also referred to as 'best case' and 'worst case' scenarios respectively.

a. Worst case: The maximum value of f(n) for any possible input. **b.** Average case: The expected value of f(n) for any possible input. **c.** Best case: The minimum possible value of f(n) for any possible

 $(1 \times 10 = 10)$

iii. Space complexity:

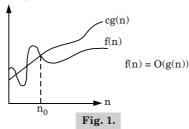
- 1. The space complexity of an algorithm is the amount of memory it needs to run to completion.
- $2. \ \ \,$ It is expressed using only Big Oh notation.
- $3. \ \ Algorithm/program should have the less space complexity.$
- 4. Lesser space used by algorithm/program, the faster it executes.

iv. Big 'Oh' notation:

- 1. Big-Oh is formal method of expressing the upper bound of an algorithm's running time.
- 2. It is the measure of the longest amount of time it could possibly take for the algorithm to complete.
- 3. More formally, for non-negative functions, f(n) and g(n), if there exists an integer n_0 and a constant c>0 such that for all integers $n>n_0$.

$$f(n) \le cg(n)$$

4. Then, f(n) is Big-Oh of g(n). This is denoted as: $f(n) \in O(g(n))$ i.e., the set of functions which, as n gets large, grow faster than a constant time f(n).



- **4.** Answer any **one** part of the following :
- a. i. Differentiate between iteration and recursion.

Ans.

S. No.	Iteration	Recursion
1.	Allows the set of instructions to be repeatedly executed.	The statement in a body of function calls the function itself.
2.	Iteration includes initialization, condition, execution of statement within loop and update the control variable.	In recursive function, only termination condition (base case) is specified.

Data Structures		SP-17 C (CS-Sem-3)		
3.	The iteration statement is repeatedly executed until a certain condition is reached.	A conditional statement is included in the body of the function to force the function to return without recursion call being executed.		
4.	Infinite loop uses CPU cycles repeatedly.	Infinite recursion can crash the system.		
5.	Iteration is applied to iteration statements or loops.	Recursion is always applied to functions.		
6.	Stack is not used.	Stack is used.		
7.	Fast in execution	Slow in execution.		
Ans.	for TOWER (4, A, B, C) (4 disks	TOWER $(1, A, C, B) \dots A \rightarrow B$		
	TOWER (2, A, B, 0	$C)$ $A \rightarrow C$ $A \rightarrow C$		
		TOWER $(1, B, A, C) \dots B \rightarrow C$		
7	$\text{TOWER } (3, A, C, B) A \rightarrow B.$	$A \rightarrow B$		
$/$ TOWER (2, C, A, B) \longrightarrow C \rightarrow B				
TOWED	/ (4 A B C) A . C	TOWER $(1, A, C, B) \dots A \rightarrow B$		
TOWER	\ (4, A, B, C) ——— A → C	TOWER (1, B, A, C) B \rightarrow C		
	TOWER (2, B, C, A	$A \longrightarrow B \rightarrow A$ $B \rightarrow A$		
		$\stackrel{\frown}{\text{TOWER}} (1, C, B, A) \dots C \rightarrow A$		
TOWER (3, B, A, C) \longrightarrow B \rightarrow C \longrightarrow TOWER (1, A, C, B) \longrightarrow A				
TOWER (2, A, B, C) \longrightarrow A \rightarrow C A \rightarrow 6				
Fig	following 15 moves:	ation for $n = 4$ disks consist of the \rightarrow A C \rightarrow B A \rightarrow B A \rightarrow C B \rightarrow C		

b. Discuss array and linked representation of queue data structure. What is dequeue?

Ans. Array representation of queue:

Algorithm to insert any element in a queue:

Step 1: If REAR = MAX - 1

Write Overflow

Go to step 4. [End of if] **Step 2:** If FRONT = -1 and REAR = -1

Set FRONT = REAR = 0

else

Set REAR = REAR + 1 [End of if]Step 3: Set QUEUE[REAR] = NUM

Step 4: Exit Linked representation of queue:

Algorithm to insert an element in queue:

Step 1: Allocate the space for the new node PTR. Step 2 : Set PTR \rightarrow DATA = VAL

Step 3: If FRONT = NULL

Set FRONT = REAR = PTRSet FRONT \rightarrow NEXT = REAR \rightarrow NEXT = NULL

else

 $Set REAR \rightarrow NEXT = PTR$

Set REAR = PTR

Set REAR → NEXT = NULL [End of if]

Step 4: Exit Algorithm for deletion of an element from queue:

Step 1: If FRONT = NULL

Write Underflow

Go to Step 5 [End of if] Step 2: Set PTR = FRONT

Step 3: Set FRONT = FRONT \rightarrow NEXT

Step 4: Free PTR

Step 5: End

Dequeue:

1. In a dequeue, both insertion and deletion operations are performed at either end of the queues. That is, we can insert an element from the rear end or the front end. Also deletion is possible from either end.



Fig. 2. Structure of a dequeue.

- 2. This dequeue can be used both as a stack and as a queue.
- 3. There are various ways by which this dequeue can be represented. The most common ways of representing this type of dequeue are:

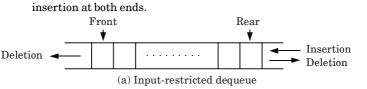
a. Using a doubly linked list

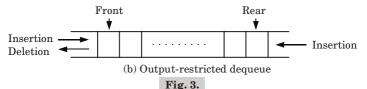
SP-19 C (CS-Sem-3)

Types of dequeue: can be added at only one end but we can delete the element from

b. Using a circular array

both ends. 2. Output-restricted dequeue: An output-restricted dequeue is a dequeue where deletions take place at only one end but allows





- **5.** Answer any **one** part of the following: $(10 \times 1 = 10)$ a. Why is quick sort named as quick? Show the steps of quick sort on the following set of elements: 25, 57, 48, 37, 12, 92, 86, 33
- Assume the first element of the list to be the pivot element. Ans. Quick sort named as Quick because: 1. It works very fast in most practical cases with time complexity of
 - $O(n \log n)$ in average case. 2. It does not need much extra memory i.e., can be implemented inplace without time overheads.

Numerical: 25 57 48 37 12 92 86 33

Here
$$p = 1$$
, $r = 8$
 $x = A[1] = 25$, $i = p - 1 = 0$, $j = 1$ to 7
Now, $j = 1$ and $i = 0$

Now,
$$j=1$$
 and $i=0$
 $A[1]=25$
then $i=0+1=1$ and $A[1]\leftrightarrow A[1]$
Now, $j=2$ and $i=1$

$$j = 2 \text{ and } i = 1$$

 $A[2] = 57 \nleq 25 \text{ (False)}$
 $j = 3 \quad i = 1$

$$A[3] = 48 \nleq 25 \text{ (False)}$$

 $j = 4 \quad i = 1$

$$j = 4$$
 $i = 1$
 $A[4] = 37 \nleq 25 \text{ (False)}$

j = 5 i = 1A[5] = 12 < 25 (True)

```
i = 1 + 1 = 2
Exchange A[2] \leftrightarrow A[5]
         1
             2
                  3
                      4
                            5
                                6
i.e.,
        25
             12
                 48
                      37
                           57
                                92
                                    86
                                         33
                  j = 6 and i = 2
Now,
              A[6] = 92 \stackrel{4}{=} 25
                  j = 7 and i = 2
              A[7] = 86 < 25
Exchange, A[2] \leftrightarrow A[1]
                            5
i.e.,
        12 | 25
                 48 37
                          57
                               92
                                    86
                                         33
                 q = 2
                    Quicksort (A, 1, 8)
            12, 25, 48, 37, 57, 92, 86, 33
    Quicksort (A, 1, 1)
                                      Quicksort (A, 3, 8)
                                   48, 37, 57, 92, 86, 33
             12
                                   33, 37, 57, 92, 86, 48
                                      Quicksort (A, 4, 8)
                                   37, 57, 92, 86, 48
                                       Quicksort (A, 5, 8)
                                        57, 92, 86, <u>48</u>
                                         48, 92, 86, 57
                                       Quicksort (A, 6, 8)
                                           92, 86, <u>57</u>
                                           57, 86, 92
                                       Quicksort (A, 7, 8)
                                             86, 92
                                       Quicksort (A, 8, 8)
                                               92
```

Sorted array using quick sort

SP-21 C (CS-Sem-3)

b. What is hashing? Give the characteristics of hash function.
 Explain collision resolution technique in hashing.

Ans. Hashing:

- Hashing is a technique that is used to uniquely identify a specific object from a group of similar objects.
- Hashing is the transformation of a string of characters into a usually shorter fixed-length value or key that represents the original string.
 In hashing, large keys are converted into small keys by using
- hash functions.
- 4. The values are then stored in a data structure called hash table.
- 5. The task of hashing is to distribute entries (key/value pairs)
- uniformly across an array.

 6. Each element is assigned a key (converted key). By using that key
- we can access the element in O(1) time.7. Using the key, the algorithm (hash function) computes an index that suggests where an entry can be found or inserted.
- 8. Hashing is used to index and retrieve items in a database because it is faster to find the item using the shorter hashed key than to find it using the original value.
- 9. The element is stored in the hash table where it can be quickly retrieved using hashed key which is defined by

 Hash Key = Key Value % Number of Slots in the Table

Characteristics of hash function:

- 1. The hash value is fully determined by the data being hashed.
- 2. The hash function uses all the input data.
- 3. The hash function "uniformly" distributes the data across the entire set of possible hash values.
- 4. The hash function generates very different hash values for similar strings.

Collision resolution technique:

Collision:

- 1. Collision is a situation which occur when we want to add a new record R with key k to our file F, but the memory location address H(k) is already occupied.
- 2. A collision occurs when more than one keys map to same hash value in the hash table.

Collision resolution technique:

Hashing with open addressing:

- 1. In open addressing, all elements are stored in the hash table itself.
- 2. While searching for an element, we systematically examine table slots until the desired element is found or it is clear that the element is not in the table.
- 3. Thus, in open addressing, the load factor λ can never exceed 1.

- 1		
- 1		
- 1		
	4	The process of examining the locations in the hash table is called

Solved Paper (2019-20)

- 5. Following are techniques of collision resolution by open addressing: a. Linear probing b. Quadratic probing c. Double hashing
 - Hashing with separate chaining: 1. This method maintains the chain of elements which have same

Ans. Floyd's Warshall algorithm:

SP-22 C (CS-Sem-3)

probing.

- hash address. 2. We can take the hash table as an array of pointers.
- 3. Size of hash table can be number of records.
- 4. Here each pointer will point to one linked list and the elements which have same hash address will be maintained in the linked list. 5. We can maintain the linked list in sorted order and each elements
- of linked list will contain the whole record with key. 6. For inserting one element, first we have to get the hash value through hash function which will map in the hash table, then that
- element will be inserted in the linked list. 7. Searching a key is also same, first we will get the hash key value in hash table through hash function, then we will search the element
- in corresponding linked list. 8. Deletion of a key contains first search operation then same as delete operation of linked list.
- **6.** Answer any **one** part of the following: $(1 \times 10 = 10)$ a. Explain Warshall's algorithm with the help of an example.
- 1. Floyd Warshall algorithm is a graph analysis algorithm for finding shortest paths in a weighted, directed graph. 2. A single execution of the algorithm will find the shortest path
- between all pairs of vertices. 3. It does so in $\Theta(V^3)$ time, where V is the number of vertices in the
- graph. 4. Negative-weight edges may be present, but we shall assume that there are no negative-weight cycles.
- 5. The algorithm considers the "intermediate" vertices of a shortest path, where an intermediate vertex of a simple path $p = (v_1, v_2, ..., v_n, ..., v_n)$
- v_m) is any vertex of p other than v_1 or v_m , that is, any vertex in the $set \{v_2, v_3, ..., v_{m-1}\}.$
- 6. Let the vertices of G be $V = \{1, 2, ..., n\}$, and consider a subset $\{1, 2, ..., k\}$ of vertices for some k.
- 7. For any pair of vertices $i, j \in V$, consider all paths from i to j whose intermediate vertices are all drawn from $\{1, 2, ..., k\}$, and let p be a minimum-weight path from among them. 8. Let $d_{ii}^{(k)}$ be the weight of a shortest path from vertex i to vertex j

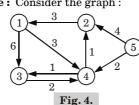
with all intermediate vertices in the set $\{1, 2, ..., k\}$.

A recursive definition is given by

$$d_{ij}^{(k)} = egin{cases} w_{ij} & ext{if } k = 0 \ \min(d_{ij}^{(k-1)}, d_{ik}^{(k-1)} + d_{kj}^{(k-1)}) & ext{if } k \geq 1 \end{cases}$$

Floyd Warshall (w):

- 1. $n \leftarrow \text{rows } [w]$
- $2. \ D^{(0)} \leftarrow w$
- 3. for $k \leftarrow 1$ to n
- 4. do for $i \leftarrow 1$ to n
- 5. do for $j \leftarrow 1$ to n
- 6. do $d_{ij}^{(k)} \leftarrow \min(d_{ij}^{(k-1)}, d_{ik}^{(k-1)} + d_{kj}^{(k-1)})$
- 7. return $D^{(n)}$ For example: Consider the graph:



$$d_{ij}^{(k)} = \min[d_{ij}^{(k-1)}, d_{ik}^{(k-1)} + d_{kj}^{(k-1)}]$$

$$\pi_{ij}^{(k)} = \begin{cases} \pi_{ij}^{(k-1)} \text{ if } d_{ij}^{(k-1)} \leq d_{ik}^{(k-1)} + d_{kj}^{(k-1)} \\ \pi_{kj}^{(k-1)} \text{ if } d_{ij}^{(k-1)} > d_{ik}^{(k-1)} + d_{kj}^{(k-1)} \end{cases}$$

$$D^{(0)} = \begin{bmatrix} 1 & 0 & \infty & 6 & 3 & \infty \\ 2 & 3 & 0 & \infty & \infty & \infty \\ \infty & \infty & 0 & 2 & \infty \\ 4 & \infty & 1 & 1 & 0 & \infty \\ 5 & 0 & 4 & \infty & 2 & 0 \\ 1 & 2 & 3 & 4 & 5 \\ 1 & 0 & 4 & 6 & 3 & \infty \\ 2 & 3 & 0 & 9 & 6 & \infty \\ 2 & 3 & 0 & 9 & 6 & \infty \\ 4 & 1 & 1 & 0 & \infty \end{bmatrix}$$

7 4

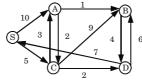
3 2 0

5

		1	2	3	4	5
	1	0	4	6	3	∞
	2	3	0	7	6	∞
$D^{(2)} =$	3	6	3	0	2	∞
$D^{(2)} =$	4	4	1	1	0	∞
	5	6	3	3	2	0_

Now, if we find $D^{(3)}$, $D^{(4)}$ and $D^{(5)}$ there will be no change in the entries.

b. Describe the Dijkstra algorithm to find the shortest path. Find the shortest path in the following graph with vertex 'S' as source vertex.

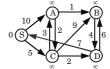


Ans. Dijkstra algorithm:

- a. Dijkstra's algorithm, is a greedy algorithm that solves the single-source shortest path problem for a directed graph G=(V,E) with non-negative edge weights, *i.e.*, we assume that $w(u,v) \geq 0$ each edge $(u,v) \in E$.
- b. Dijkstra's algorithm maintains a set S of vertices whose final shortest-path weights from the source s have already been determined.
- c. That is, for all vertices $v \in S$, we have $d[v] = \delta(s, v)$.
- d. The algorithm repeatedly selects the vertex $u \in V-S$ with the minimum shortest-path estimate, inserts u into S, and relaxes all edges leaving u.
- e. We maintain a priority queue Q that contains all the vertices in v-s, keyed by their d values.
- f. Graph G is represented by adjacency list.
- g. Dijkstra's always chooses the "lightest or "closest" vertex in V-S to insert into set S, that it uses as a greedy strategy.

Numerical:

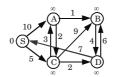
Initialize:



$$S = \{ \}$$

$$Q : \frac{S \ A \ B \ C \ D}{0 \ \infty \ \infty \ \infty \ \infty}$$

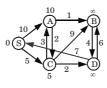
EXTRACT - MIN (S):



$$S = \{ S \}$$

$$Q : \underbrace{S A B C D}_{\boxed{0} \infty \infty \infty \infty}$$

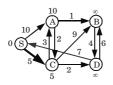
Relax all edges leaving (S):



$$S = \{ S \}$$

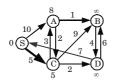
$$Q : \underbrace{S \ A \ C \ B \ D}_{0 \ \infty \ \infty \ \infty \ \infty}$$

EXTRACT - MIN (C):



$$\begin{aligned} S &= \{\,S,\,C\,\,\} \\ Q &: \underbrace{S\ A\ C\ B\ D}_{\begin{subarray}{cccc} 0 & \infty & \infty & \infty \\ \hline 0 & \infty & \infty & \infty & \infty \\ \hline 10 & \hline 5 & - & - \\ \end{subarray}} \quad \end{aligned}$$

Relax all edges leaving C:



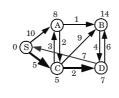
$$S = \{ S, C \}$$

$$Q : \underbrace{S \ A \ C \ B}_{0 \ \infty \ \infty \ \infty \ \infty} D$$

$$10 \ \overline{5} \ - \ -$$

$$8 \ 14 \ 7$$

EXTRACT - MIN (D):



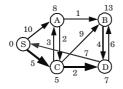
$$S = \{ S, C, D \}$$

$$Q : \underbrace{S \ A \ C \ B \ D}_{0 \ \infty \ \infty \ \infty \ \infty}$$

$$10 \ \overline{5} \ - \ -$$

14 7

Relax all edges leaving D:

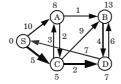


$$S = \{S, C, D\}$$

$$Q: \underbrace{S \ A \ C \ B}_{\boxed{0} \ \infty \ \infty \ \infty}$$

13

EXTRACT - MIN(A):



$$S = \{ S, C, D, A \}$$

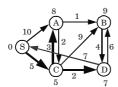
$$Q: S A C B D$$

$$0 \infty \infty \infty \infty$$

$$10 5 - -$$

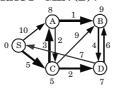
$$8 14 7$$

Relax all edges leaving A:



$S = \{ S, C, D, A \}$ $Q : \underbrace{S \ A \quad C \quad B \quad D}_{0 \ \infty \quad \infty \quad \infty \quad \infty}$ $10 \ \underbrace{5 \quad - \quad -}_{8}$ $14 \ \underbrace{7}_{9}$

EXTRACT - MIN (B):





- 7. Answer any **one** part of the following: $(7 \times 1 = 7)$
- a. Can you find a unique tree when any two traversals are given? Using the following traversals construct the corresponding binary tree:

INORDER: HKDBILEAFCMJG

PREORDER: ABDHKEILCFGJM

Also find the post order traversal of obtained tree.

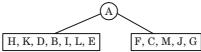
Ans. No, we cannot find unique tree when any two traversals are given. If preorder and postorder are given then we cannot find unique tree. We can find unique tree if one of the given traversal is inorder.

Numerical:

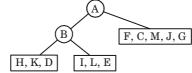
Step 1: In preorder traversal root is the first node. So, *A* is the root node of the binary tree. So,

noot

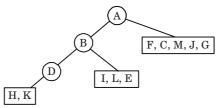
Step 2: We can find the node of left sub-tree and right sub-tree with inorder sequence. So,



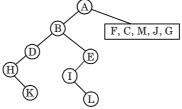
Step 3: Now, the left child of the root node will be the first node in the preorder sequence after root node *A i.e. B* So,



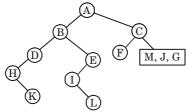
Step 4: Now the root node is D. In inorder sequence, H, K is on the left side of D. So



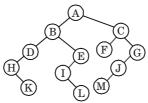
Step 5: Now the root is H. In inorder sequence, K is on the right side of H.



Step 6: Similarly, we can go further for right side of A.



So, the final tree is



Postorder of tree: K, H, D, L, I, E, B, F, M, J, G, C, A

b. What is a B-Tree? Generate a B-Tree of order 4 with the alphabets (letters) arrive in the sequence as follows: a g f b k d h i n j e s i r x c l n t u p.

Ans. B-tree:

- A B-tree is a self-balancing tree data structure that keeps data sorted and allows searches, sequential access, insertions, and deletions in logarithmic time.
- 2. A B-tree of order m is a tree which satisfies the following properties :
- a. Every node has at most m children.
- b. Every non-leaf node (except root) has at least $\lceil m/2 \rceil$ children.
- c. The root has at least two children if it is not a leaf node.
- d. A non-leaf node with k children contains k-1 keys.
- e. All leaves appear in the same level.

