



Universidade de Brasília

# É só Fazer

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1 Contest

2 Data structures

3 Matching

4 Math

Contest (1)

template.cpp26 lines

```
#include <bits/stdc++.h>

using namespace std;

#define int long long
#define endl '\n'
#define rep(i, a, b) for(int i = (a); i < (b); ++i)
#define all(x) begin(x), end(x)
#define sz(x) (int)(x).size()
#define debug(var) cout << #var << ": " << var << endl
#define pb push_back
#define eb emplace_back
typedef long long ll;
typedef pair<int, int> pii;
typedef vector<int> vi;

void solve() {
}

int32_t main() {
    ios_base::sync_with_stdio(0); cout.tie(0); cin.tie(0);
    int t = 1;
    while(t--) solve();

    return 0;
}
```

.bashrc3 lines

```
alias c='g++ -Wall -Wconversion -Wfatal-errors -g -std=c++17 \
-fsanitize=undefined,address'
xmodmap -e 'clear lock' -e 'keycode 66=less greater' #caps = ⇐
```

.vimrc4 lines

```
set cin ai is ts=4 sw=4 nu rnu
" Select a region and then type :Hash
ca Hash w !cpp -dD -P -fpreprocessed \| tr -d '[:space:]' \
\| md5sum \| cut -c-6
```

hash.sh3 lines

```
# Hashes a file, ignoring all whitespace and comments. Use for
# verifying that code was correctly typed.
cpp -dD -P -fpreprocessed | tr -d '[:space:]' | md5sum |cut -c-6
```

troubleshoot.txt52 lines

```
Pre-submit:
Write a few simple test cases if sample is not enough.
Are time limits close? If so, generate max cases.
Is the memory usage fine?
Could anything overflow?
Make sure to submit the right file.
```

```
Wrong answer:
Print your solution! Print debug output, as well.
Are you clearing all data structures between test cases?
Can your algorithm handle the whole range of input?
Read the full problem statement again.
Do you handle all corner cases correctly?
Have you understood the problem correctly?
Any uninitialized variables?
Any overflows?
Confusing N and M, i and j, etc.?
Are you sure your algorithm works?
What special cases have you not thought of?
Are you sure the STL functions you use work as you think?
Add some assertions, maybe resubmit.
Create some testcases to run your algorithm on.
Go through the algorithm for a simple case.
Go through this list again.
Explain your algorithm to a teammate.
Ask the teammate to look at your code.
Go for a small walk, e.g. to the toilet.
Is your output format correct? (including whitespace)
Rewrite your solution from the start or let a teammate do it.
```

```
Runtime error:
Have you tested all corner cases locally?
Any uninitialized variables?
Are you reading or writing outside the range of any vector?
Any assertions that might fail?
Any possible division by 0? (mod 0 for example)
Any possible infinite recursion?
Invalidated pointers or iterators?
Are you using too much memory?
Debug with resubmits (e.g. remapped signals, see Various).
```

```
Time limit exceeded:
Do you have any possible infinite loops?
What is the complexity of your algorithm?
Are you copying a lot of unnecessary data? (References)
How big is the input and output? (consider scanf)
Avoid vector, map. (use arrays/unordered_map)
What do your teammates think about your algorithm?
```

```
Memory limit exceeded:
What is the max amount of memory your algorithm should need?
Are you clearing all data structures between test cases?
```

Data structures (2)

SegTree.h731230, 37 lines

```
template<typename Spec>
struct SegTree {
    using LS = Spec;
    using S = typename LS::S;
    using K = typename LS::K;
    int n;
    vector<S> seg;

    SegTree(const vector<S> & v)
        : n(v.size()), seg(2*n) {
        rep(i, 0, n) seg[i+n] = v[i];
        for(int i = n-1; i >= 1; i--) seg[i] = LS::op(seg[i*2], seg[i*2+1]);
    }

    void update(int no, K val) {
```

```
no += n;
seg[no] = LS::update(val, seg[no]);
while (no > 1) no /= 2, seg[no] = LS::op(seg[no*2], seg[no*2+1]);
}

S query(int l, int r) { // [l, r)
    S vl = LS::id(), vr = LS::id();
    for (l += n, r += n; l < r; l /= 2, r /= 2) {
        if (l & 1) vl = LS::op(vl, seg[l++]);
        if (r & 1) vr = LS::op(seg[--r], vr);
    }
    return LS::op(vl, vr);
}
};

struct Spec {
    using S = int;
    using K = int;
    static S op(S a, S b) { return max(a, b); }
    static S update(K f, S a) { return f; }
    static S id() { return 0; }
};
```

LazySeg.h3beda5, 96 lines

```
template<typename Spec>
struct LazySeg {
    using LS = Spec;
    using S = typename LS::S;
    using K = typename LS::K;
    int n;
    vector<S> seg;
    vector<K> lazy;
    vector<bool> has_lazy;
    // vector<int> lx, rx; // Additional info

    LazySeg(vector<S> & v) : n(v.size()), seg(2*n), lazy(n),
        has_lazy(n) {
        rep(no, 0, n) seg[no+n] = v[no];
        for (int no = n-1; no >= 1; no--) pull(no);

        // Additional info, n must be power of two
        /*
        lx.assign(2*n, 0); rx.assign(2*n, 0);
        lx[1] = 0; rx[1] = n;
        rep(no, 1, n) {
            int mid = (lx[no] + rx[no])/2;
            lx[no*2] = lx[no]; rx[no*2] = mid;
            lx[no*2+1] = mid; rx[no*2+1] = rx[no];
        }
        */
    }

    S query(int l, int r) { // [l, r)
        l += n;
        r += n;
        push_to(l); push_to(r-1);
        S vl = LS::id(), vr = LS::id();
        while(l < r) {
            if (l & 1) vl = LS::op(vl, seg[l++]);
            if (r & 1) vr = LS::op(seg[--r], vr);
            l >>= 1; r >>= 1;
        }
        return LS::op(vl, vr);
    }
};
```

```
void update(int l, int r, K val) {
    l += n;
    r += n;
    push_to(l); push_to(r-1);
    int lo = l, ro = r-1;
    while(l < r) {
        if (l & 1) lo = max(lo, l), apply(l++, val);
        if (r & 1) ro = max(ro, r), apply(--r, val);
        l >>= 1; r >>= 1;
    }
    pull_from(lo);
    pull_from(ro-1);
}

void apply(int no, K val) {
    seg[no] = LS::update(val, seg[no]);
    // seg[no] = LS::update(val, seg[no], lx[no], rx[no]);

    if (no < n) {
        if (has_lazy[no]) lazy[no] = LS::compose(val, lazy[no]);
        else lazy[no] = val;
        has_lazy[no] = true;
    }
}

void pull_from(int no) {
    while(no > 1) no >>= 1, pull(no);
}

void pull(int no) {
    seg[no] = LS::op(seg[no*2], seg[no*2+1]);
}

void push_to(int no) {
    int h = 0; int p2 = 1;
    while(p2 < no) p2 *= 2, h++;
    for (int i = h; i >= 1; i--) push(no >> i);
}

void push(int no) {
    if (has_lazy[no]) {
        apply(no*2, lazy[no]);
        apply(no*2+1, lazy[no]);
        has_lazy[no] = false;
    }
}

};

struct Spec {
    using S = int;
    using K = int;
    static S op(S a, S b) { return max(a, b); }
    static S update(K f, S a) { return f + a; }
    static K compose(const K f, const K g) { return f + g; }
    static S id() { return 0; }
};
```

## Matching (3)

### OnlineMatching.h

**Description:** Modified khun developed for specific question able to run  $2 * 10^6$  queries, in  $2 * 10^6 \times 10^6$  graph in 3 seconds codeforces  
**Time:**  $\mathcal{O}(confia)$

6ac539, 42 lines

```
struct OnlineMatching {
    int n = 0, m = 0;
    vector<int> vis, match, dist;
    vector<vector<int>>> g;
```

```
vector<int> last;
int t = 0;

OnlineMatching(int n_, int m_) : n(n_), m(m_),
vis(n, 0), match(m, -1), dist(n, n+1), g(n), last(n, -1)
{}

void add(int a, int b) {
    g[a].pb(b);
}

bool kuhn(int a) {
    vis[a] = t;
    for(int b: g[a]) {
        int c = match[b];
        if (c == -1) {
            match[b] = a;
            return true;
        }
        if (last[c] != t || (dist[a] + 1 < dist[c]))
            dist[c] = dist[a] + 1, last[c] = t;
    }
    for (int b: g[a]) {
        int c = match[b];
        if (dist[a] + 1 == dist[c] && vis[c] != t && kuhn(c)) {
            match[b] = a;
            return true;
        }
    }
    return false;
}

bool can_match(int a) {
    t++;
    last[a] = t;
    dist[a] = 0;
    return kuhn(a);
}
};
```

## Math (4)

### LinearDiophantineEquation.h

**Description:** Find a solution to equation  $a*x + b*y = c$

**Time:**  $\mathcal{O}(\log(a))$

538f05, 14 lines

```
array<ll, 3> exgcd(ll a, ll b) {
    if (a == 0) return {0, 1, b};
    auto [x, y, g] = exgcd(b % a, a);
    return {y - b / a * x, x, g};
}

array<ll, 4> find_any_solution(ll a, ll b, ll c) {
    assert(a != 0 || b != 0);
    auto [x, y, g] = exgcd(a, b);
    if (c % g) return {false, 0, 0, 0};
    x *= c / g;
    y *= c / g;
    return {true, x, y, g};
}
```

# Techniques (A)

|  |           |
|--|-----------|
| techniques.txt                                     | 159 lines |
| Recursion  |           |
| Divide and conquer                                 |           |
| Finding interesting points in N log N              |           |
| Algorithm analysis                                 |           |
| Master theorem                                     |           |
| Amortized time complexity                          |           |
| Greedy algorithm                                   |           |
| Scheduling   |           |
| Max contiguous subvector sum                       |           |
| Invariants   |           |
| Huffman encoding                                   |           |
| Graph theory                                       |           |
| Dynamic graphs (extra book-keeping)                |           |
| Breadth first search                               |           |
| Depth first search                                 |           |
| * Normal trees / DFS trees                         |           |
| Dijkstra's algorithm                               |           |
| MST: Prim's algorithm                              |           |
| Bellman-Ford                                       |           |
| Konig's theorem and vertex cover                   |           |
| Min-cost max flow                                  |           |
| Lovasz toggle                                      |           |
| Matrix tree theorem                                |           |
| Maximal matching, general graphs                   |           |
| Hopcroft-Karp                                      |           |
| Hall's marriage theorem                            |           |
| Graphical sequences                                |           |
| Floyd-Warshall                                     |           |
| Euler cycles                                       |           |
| Flow networks                                      |           |
| * Augmenting paths                                 |           |
| * Edmonds-Karp                                     |           |
| Bipartite matching                                 |           |
| Min. path cover                                    |           |
| Topological sorting                                |           |
| Strongly connected components                      |           |
| 2-SAT  |           |
| Cut vertices, cut-edges and biconnected components |           |
| Edge coloring                                      |           |
| * Trees  |           |
| Vertex coloring                                    |           |
| * Bipartite graphs (=> trees)                      |           |
| * 3^n (special case of set cover)                  |           |
| Diameter and centroid                              |           |
| K'th shortest path                                 |           |
| Shortest cycle                                     |           |
| Dynamic programming                                |           |
| Knapsack   |           |
| Coin change  |           |
| Longest common subsequence                         |           |
| Longest increasing subsequence                     |           |
| Number of paths in a dag                           |           |
| Shortest path in a dag                             |           |
| Dynprog over intervals                             |           |
| Dynprog over subsets                               |           |
| Dynprog over probabilities                         |           |
| Dynprog over trees                                 |           |
| 3^n set cover                                      |           |
| Divide and conquer                                 |           |
| Knuth optimization                                 |           |
| Convex hull optimizations                          |           |
| RMQ (sparse table a.k.a 2^k-jumps)                 |           |
| Bitonic cycle                                      |           |
| Log partitioning (loop over most restricted)       |           |
| Combinatorics                                      |           |

|  |
|--|
| Computation of binomial coefficients         |
| Pigeon-hole principle                        |
| Inclusion/exclusion                          |
| Catalan number                               |
| Pick's theorem                               |
| Number theory                                |
| Integer parts                                |
| Divisibility                                 |
| Euclidean algorithm                          |
| Modular arithmetic                           |
| * Modular multiplication                     |
| * Modular inverses                           |
| * Modular exponentiation by squaring         |
| Chinese remainder theorem                    |
| Fermat's little theorem                      |
| Euler's theorem                              |
| Phi function                                 |
| Frobenius number                             |
| Quadratic reciprocity                        |
| Pollard-Rho                                  |
| Miller-Rabin                                 |
| Hensel lifting                               |
| Vieta root jumping                           |
| Game theory                                  |
| Combinatorial games                          |
| Game trees                                   |
| Mini-max                                     |
| Nim  |
| Games on graphs                              |
| Games on graphs with loops                   |
| Grundy numbers                               |
| Bipartite games without repetition           |
| General games without repetition             |
| Alpha-beta pruning                           |
| Probability theory                           |
| Optimization                                 |
| Binary search                                |
| Ternary search                               |
| Unimodality and convex functions             |
| Binary search on derivative                  |
| Numerical methods                            |
| Numeric integration                          |
| Newton's method                              |
| Root-finding with binary/ternary search      |
| Golden section search                        |
| Matrices                                     |
| Gaussian elimination                         |
| Exponentiation by squaring                   |
| Sorting                                      |
| Radix sort                                   |
| Geometry                                     |
| Coordinates and vectors                      |
| * Cross product                              |
| * Scalar product                             |
| Convex hull                                  |
| Polygon cut                                  |
| Closest pair                                 |
| Coordinate-compression                       |
| Quadtrees                                    |
| KD-trees                                     |
| All segment-segment intersection             |
| Sweeping                                     |
| Discretization (convert to events and sweep) |
| Angle sweeping                               |
| Line sweeping                                |
| Discrete second derivatives                  |
| Strings                                      |
| Longest common substring                     |
| Palindrome subsequences                      |

|   |
|---|
| Knuth-Morris-Pratt                                    |
| Tries   |
| Rolling polynomial hashes                             |
| Suffix array  |
| Suffix tree   |
| Aho-Corasick  |
| Manacher's algorithm                                  |
| Letter position lists                                 |
| Combinatorial search                                  |
| Meet in the middle                                    |
| Brute-force with pruning                              |
| Best-first (A*)                                       |
| Bidirectional search                                  |
| Iterative deepening DFS / A*                          |
| Data structures                                       |
| LCA (2^k-jumps in trees in general)                   |
| Pull/push-technique on trees                          |
| Heavy-light decomposition                             |
| Centroid decomposition                                |
| Lazy propagation                                      |
| Self-balancing trees                                  |
| Convex hull trick (wcipeg.com/wiki/Convex_hull_trick) |
| Monotone queues / monotone stacks / sliding queues    |
| Sliding queue using 2 stacks                          |
| Persistent segment tree                               |