VIENNA UNIVERSITY OF TECHNOLOGY

105.625 PR ADVANCED ECONOMICS PROJECT

Double Sided Matching

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1 Introduction

Double sided matching is about finding a match between two sets of elements. The first algorithm which should solve this problem was described by David Gale and Lloyd S. Shapley in 1962 [1]. The focus will lie on the examination of this algorithm and the creation of a simulation model for it, which can be applied to different economic issues. The selected economic issues will be presented in the following chapters.

1.1 Motivation and Problem Description

In many daily live situations there are hidden double sided matching problems. For example students usually have the opportunity to apply to a number of schools. In this case students and schools have to be matched together. Both parties have preferences which need to be taken into consideration. In our everyday life we usually don't have the time to find an appropriate solution.

In some cases these problems even go by without solving them. In other cases however, it is crucial to solve them, e.g. if we consider medical school graduates and open positions in hospitals. Due to multiple reasons (e.g. different preferences, high number of elements in the two sets) this problem cannot be solved intuitively or in linear time.

1.2 Aim and Objectives

The aim of this paper is to develop a simulation model prototype which can solve similar problems, like the ones discussed above. With this model we could answer questions like:

- Are there "stable" solutions for this kind of problem?
- How can it be applied to all prospective students and universities in Austria?
- Is there also a solution for the current labour supply and demand in the European Union?

1.3 Structure

In the second chapter a theoretical overview is provided regarding the double sided matching problem and what stability means in this context. The focus lies on the Gale and Shapley Algorithm, basic information about the game theory and the relationship between them.

The third chapter describes the prototype of the simulation model, which implements the previously discussed theory into practice. As a simulation environment NetLogo ¹

¹Available at https://ccl.northwestern.edu/netlogo/, accessed April 28, 2016

will be used. The prototype will be firstly evaluated on a simple discotheque example. In this case it is assumed, that an equal number of men and women are in a discotheque and the objective is to form couples.

The fourth chapter deals with the examination of data from Austrian universities and their integration into the prototype. As a result, a solution for this double sided matching problem will be provided.

Chapter five deals with the labour market in the European Union, trying to match the labour demand and labour supply.

Finally the most important findings and results are summarized and compared in the last chapter. Additionally there is a short outlook into further research.

2 Theory

In this chapter the necessary theoretical background for the realization of this project is discussed.

2.1 The Double Sided Matching Problem

The double sided matching problem describes a problem, which has two sets of elements. These sets are disjoint and may be equal in size, but this is not mandatory. The purpose of the double sided matching algorithm is to find a solution, so every element of the first set has a corresponding counterpart in the other set. This can be best described in an example: Assume that the elements are men and women and that there are only heterosexuals preferences for the individuals. The two sets are now male and female. The double sided matching algorithm shall create couples, which consists of a man and woman.

The solutions of the matchings can have different properties, which might be very important (e.g. stability). The output of the algorithm of men and women is not allowed to be unstable, i.e. there are two men α and β who are assigned to women A and B although β prefers A to B and A prefers α to β . If this does not occur, the assignment is called *stable*. If there is more than one stable solution the *optimal* one can be of particular interest.

Optimality means that a solution has the best outcome for an individual or set. In this case optimality can be achieved from the perspective of the first set of elements or from the second set. There can also be a trade-off from the perspective of the both sets, it this case optimality is achieved by weighting the expected value of both sets. These properties have been described in the paper by Gale and Shapley [1].

Generally in economics this is also known as pareto efficiency [2, p. 46]. Pareto efficiency is a characteristic for a solution where any change which would improve one property on one hand, but will worsen another one on the other hand.

2.2 Gale and Shapley Algorithm

In the paper of Gale and Shapley [1] an algorithm was proposed for solving the double sided matching problem. Lets assume there are two sets of elements: one contains men and the other one women. The size of the two sets is equal, the preferences are heterosexual and there are no polygamies (i.e. one element is only allowed to be matched with one element from the other set). The aim of the algorithm is to find a stable way of marrying men and women. Each men and women has their own preference for their marriage partner.

First Iteration

In the first iteration each man proposes to the woman who he ranked first. Afterwards a woman has a list of men that proposed to her. This list might be zero, if not she rejects

every men, except her highest preferred man on this list. If a man is not rejected he and the woman create a temporary couple. All man who are not in a couple are single.

Second Iteration

In the second interaction each man who is single, proposes to his highest ranked woman, who he didn't already proposed to. Each woman now chooses the man which she ranks the highest out of her received proposals. If a man is not rejected he and the woman create a temporary couple (Note: after the second iteration some men, who have been in a couple from the first iteration might be now single).

Further Iterations

The third iteration is the same as the second one. This continues until no men is single any more. If this condition is satisfied a stable solution is found for the double sided matching problem. The stability of the solution of this algorithm has been proven by contradiction [1].

2.3 Relevance to Game Theory

2.3.1 General

"Game theory is about what happens when people - or genes, or nations - interact" [3, p. 1]. An important aspect for participating parties is to anticipate how the opposite party will react on certain actions. Mathematics shall help to analyse, understand and estimate outcomes of such games. Depending on the information participants have, they decide how to act basing on rules contained in their strategy. Game theory is widely applied in economics. Companies use game theory to estimate e.g. reactions of competitors or behaviour of employees. The major advantages of game theory are its precision and its universal applicability to all kind of games. [3, pp. 1-3]

In addition there are some assumptions which are made during preparation and execution by every individual who is interacting with another one:

- Well-specified choices
- Well-defined end-state
- Specified pay-off
- · Perfect knowledge
- · Rationality

However, these perfect preconditions will never be met in real scenarios. In the context of double sided matching, it is important to have well-specified choices defined. Nevertheless, there might be chances to get into a nearly worst-case scenario instead. But

furthermore, as a consequence of these listed assumptions above, there are two different kind of games:

- · Static ones
- · Dynamic ones

The two items can be combined with the following kind of knowledge

- Incomplete
- Complete (there is no private information)

Depending on the nature of the game, whether it is static or dynamic and the knowledge is complete or incomplete four different combinations can be made. For a better understanding, following examples only consist of two players (every combination can be used for a higher amount of players too):

• Static and (in)complete information

As of complete information, the players action set can be presented in an N \times M matrix. Therefore all information (also private) is known to every player and each player is able to easily eliminate the pay-offs of the other players. The pay-off is the outcome of a chosen action of a player which depends on the state or previous actions of the game. The pay-off can change dynamically while the game is in progress. As of incomplete information players are forced to be uncertain about the other player's actions and pay-offs. Besides that, there are two basic steps

- 1. Player 1 and 2 are choosing actions out of a set, which were predefined by them before.
- 2. After their actions, they receive their pay-offs.
- Dynamic and complete information

When basic assumptions are made on complete information, players will create a strategy to ensure to get the highest return of each action. Although the strategy might be changed during the game after each turn. Incomplete information leads to communication of uninformed parties (i.e. closed private information) which might end up to under- or overestimate the others pay-offs. In general there will be a Nash Equilibrium between those parties. This equilibrium is created by players because they choose a strategy which do not depend on the other players. There are three basic steps:

- 1. Player 1 chooses an action out of his/her predefined set.
- 2. Player 2 observes player 1's action and chooses an action based on his/her observation.
- 3. After their actions, they receive their pay-offs.

The previously described theory is based on information of the paper "An introduction to applicable game theory" [4].

2.3.2 Example for the Application of Game Theory

Game theory is also very popular in the field of economics. Many companies primarily apply game theory to estimate the reactions of their competitors. In the last auction for broadband internet frequencies in Germany, all major providers hired game theorists out of two reasons. Firstly, they wanted to win the auction for the desired frequency and secondly, they also did not want to overpay for the frequency. The bidding behaviour of a provider indicated the interest rate for a frequency. As a consequence, other providers retained their bids for parts of this frequency so the interested provider did not need to overpay for it. The positive result for the providers was, that the 700-MHz frequency parts were sold for the minimum bidding price. [5]

2.3.3 Double Sided Matching Problem and Game Theory

Like described in chapter 2, the goal of the three main problems, which will be simulated in the course of this project, is to bring different parties together. In the original marriage problem discussed by Shapley, the goal was to match men and women so the overall situation is stable. This idea can also be applied to other areas like the labour market or university applications. In each of these three problems the parties need to have a strategy how to react to moves of the counterpart. If, for example, a university offers a place to a student and this is not the student's favourite one, he/she has to decide whether to accept the place (to be on the safe side) or still hope to get accepted from the favourite university (and as a consequence accept to be on the waiting list there). Not only the student needs to have a strategy how to deal with these situations but also universities have to incorporate different reactions of students into their application process (e.g. how many students to invite) [1].

The double sided matching problem is a dynamic game. The players of the two sets have incomplete information. The algorithm uses the information of both sets, therefore it has complete information.

An important aspect of the game or matching is that the rules have to be clear, which was mentioned by Roth and Sotomayor. The way agents are matched to each other influences the analysis of the problem. A possible rule might be that individuals like a student and university are only brought together if both parties agree to the matching. Other norms of a game might contain the way an individual proposes to another one or whether there exists a moderating individual [6, p. 492].

2.3.4 Double Sided Matching Problem and Optimal Stopping

The double sided matching problem also relates to the optimal stopping problem. The optimal stopping problem concerns itself with choosing the optimal time to stop an undertaken action and at the same time to minimize the expected costs and maximize the profit. A concrete example in this case is if a men is trying to find a women to spend the rest of his life with, when should he stop looking?

A few algorithms as a possible solution for the optimal stopping problem have been presented by Christian & Griffiths 2016 [7]. For the previously mentioned example of partner looking, one algorithm proposes to invest 37% of the time in looking and immediately after to stop looking and take the next best offer. 37% is the provably optimal solution [7, p. 2]. This algorithm is recommended in the case of *no-information games* (e.g. in the case of partner searching, it is hard to quantify the information, because it is hard to compare people to each other. There is no concrete criteria, one can only assume that one person is better or more suitable than another person, but not by how much) [7, p. 18].

Another possible solution for the previously mentioned problem is to set a threshold from the beginning and to take the first option that exceeds it. Christian & Griffiths 2016 [7] recommended this approach in the case of *full-information games*. A suitable example for this case is that of a house selling: the value of the house is known and there is also information about the state of the market, which allows to predict a range of offers. In this case a threshold is set and the first offer that exceeds this threshold can be accepted. This example does not include waiting costs. In the case of waiting costs, they also have to be taken into account and it is recommended to decline an offer if the chance of a better offer multiplied by how much better it is compensate the waiting costs.

Finally Christian & Griffiths 2016 [7, pp. 28-30] recommend to always stop looking at a certain point.

3 Prototype

A prototype for solving the double sided matching problem was developed in NetLogo². In this chapter the prototype is evaluated on a discotheque example. In this case, it is assumed that an equal number of men and women are in a discotheque and the objective is to form couples based on the individual preferences. Afterwards the prototype will be evaluated on more complex problems (e.g., matching students and universities and matching labour supply and labour demand). In the following, the data model, the data generation script, the graphical user interface (GUI) and code from NetLogo will be described.

3.1 Data Model

According to the problem description we defined a generic data model for every individual. This data model is valid for the discotheque example, the university and labour market example, and contains the following attributes:

- id: unique object identifier
- name: object name (e.g. male1 or female1)
- maxMatchesInt: integer value representing the maximum number of matchings for this individual (e.g. in the disco example each person is maximally matched with one other person)
- sideInt: integer helper variable assigning an individual to one of the two participant groups
- partnerList: list of identifiers of the partners, ordered according to the preference of an individual
- rankList: list of ranks (values between 1 to 0) for the partners from the partnerList; the list is ordered from highest to lowest preferences. If the value is equal to 1 this partner is a perfect match.
- hasProposedToList: list of identifiers representing the individuals to which an individual has proposed
- gotProposedByList: list of identifiers representing the individuals from which an individual received proposals. The gotProposedByList is only valid for one iteration.
- tmpMatchList: list containing the identifiers of individuals to whom a temporary match was established
- activeFlag: boolean value stating if an individual is matched or not respectively if the individual gave up (they already proposed to all individuals from the partnerList but only received rejections)

²Available at https://ccl.northwestern.edu/netlogo/, accessed April 28, 2016

3.2 Data Generation

In order to generate random data, which represents the individuals and their preferences the statistical computing language R³ has been used. The generated data is exported as a CSV list, which is then read from NetLogo. The R script accepts the following parameters:

- seed: integer value, which is used as a seed by the number generator. The default value is 123.
- numberOfMen: integer value representing the number of men which should be created. The default value is 10.
- numberOfWomen: integer value representing the number of women which should be generated. The default value is 10.
- pickyLower: float value between 0 and 1 representing the lower bound which will be used in order to generate a number that represents how picky a person is. The value 0 means accepts every possible match, the value 1 excepts none.
- pickyUpper: float value between 0 and 1 representing the upper bound which will be used in order to generate a number that represents how picky a person is. The value 0 means excepts every possible match, the value 1 excepts none.

The script can be called as follows from the command line:

```
Rscript initDisco.R 123 10 10 0 0
```

The script generates a CSV which looks as follows:

³Available at https://www.r-project.org/, accessed April 28, 2016

3.3 **GUI**

One of the main goals in the design phase was to keep the GUI simple and clear. The GUI was structured in two main parts - the control and the information section.

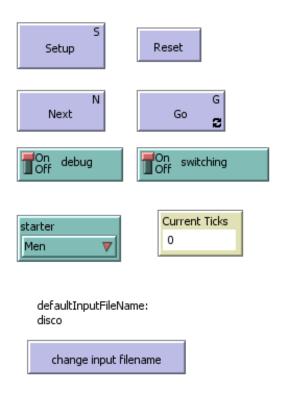


Figure 3.1: The control section for the disco example

Figure 3.1 shows the control section in the GUI. With the buttons **Setup** and **Reset** the simulation model can be initialized or reset after a simulation run. The button Next advises the program to perform one simulation step, if Go is activated the simulation continues until a termination criterion is met. In the disco example the main termination criterion is if every proposing person is already matched to another person. Another criterion for termination is if the proposing person already proposed to every person in his partnerList but got rejected every time. The debug switch enables or disables debug messages which are printed during the setup phase and simulation run. The speed of a simulation run can be increased if the **debug** switch is set to Off. The second switch, switching, controls, if the two parties propose to each other alternatively (On) or if only one party proposes to the other one (Off). With the drop-down list **starter** the user can determine which party starts proposing. The reporting box Current Ticks shows the current number of simulation steps. The button change input file name raises a dialogue box where the user can enter the filename of an input file which shall be used in the simulation. Together with the number of ticks the file name will also be used as the name for the CSV export file.

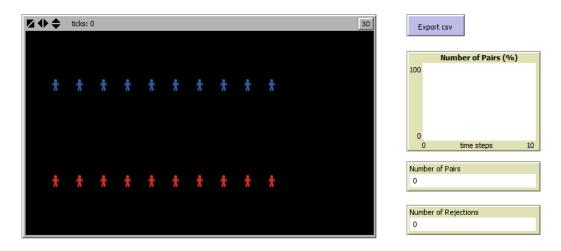


Figure 3.2: The information section for the disco example

Figure 3.2 shows the information section of the disco example GUI. All created humans are shown in the world area. Men are coloured blue and women are red. On setup of the simulation the proposing site is shown in the top row. As soon as two people are matched their colour changes to green and a link between the two is established. If a couple is divorced the link is removed and the colour changes back to the original one. The plot named **Number of Pairs** (%) illustrates at each point in time how many of the possible couples exist. If the simulation contains 10 men and 10 women and currently 4 couples exist, the plot shows that 40% are matched. The reporting box **Number of Pairs** shows the absolute number of couples. The other reporting box, **Number of Rejections**, indicates how many couples were divorced over time. With the button **Export CSV** the current properties of all humans are exported to a CSV file. The file name is a combination of the input file name, the starting side, if the switching is activated and the current number of ticks.

3.4 NetLogo Code

At the beginning of the NetLogo code the extensions, the data model and the needed global variables are defined. The rest of the code is based on procedures (i.e. a sequence of NetLogo commands which begins with *to* and ends with *end*). The most important procedures are the following:

- *setup* and *reset*: both clear all results and reset the whole model to an initial empty state.
- *open-file*: procedure used to open a CSV list which represents the individuals and their preferences.
- *setup-globals*: procedure used to set up all global variables (e.g., current number of pairs, shape of the humans, etc.)
- *step*: procedure which represents going one step in the double sided matching algorithm. The proposing site proposes and the proposals are also processed.
- go: calls step until a termination criterion is met.
- *calc-stats*: calculate some statistical information (e.g., number of pairs, number of rejections).
- *clear-before-match*: empties the list of the proposals as a preparation for the next matching round.
- propose-to[sender receiver]: sends the proposals.
- process-proposals [tmpId]: processes the proposals.
- reject-proposals [tmpId rejectList]: rejects the proposals.
- create-tmpCouples [tmpId acceptList]: creates temporary couples.

3.5 Simulation Runs

The discotheque problem was simulated three times: once with a simple and small dataset of 20 persons (10 men and 10 women) and twice with a dataset of 200 persons (100 men and 100 women).

3.5.1 Simulation Run 1: Small Dataset

In the first simulation a dataset which represents 20 individuals (10 males and 10 females) was used. This dataset was generated using the previously described R script. After the first simulation step there were already 6 couples (see figure 3.3).

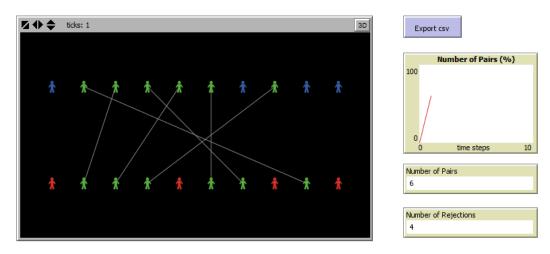


Figure 3.3: Simulation 1, step 1

In the next few steps the number of couples continued to increase by 1 at each step. After the third step 8 couples were formed (see figure 3.4).

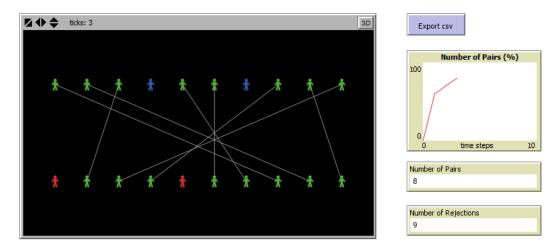


Figure 3.4: Simulation 1, step 3

Afterwards the number of couples continued to increase slowly and some of them changed according to the individuals preferences. As we can see in the figure 3.5 the male number 10 (upper right corner) was in a couple with female number 3, however male number 10 is now single, because female number 3 is now in a couple with male number 6 which is better according to their preferences.

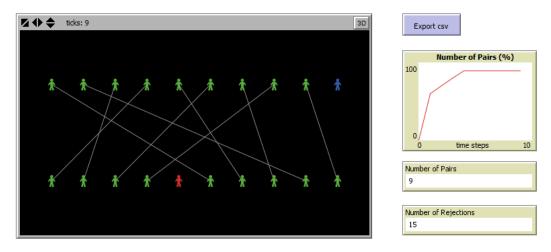


Figure 3.5: Simulation 1, step 9

In the further steps, the couples continued to change according to the individuals preferences and finally after 27 steps the double sided matching problem was solved and 10 couples have been created (see figure 3.6).

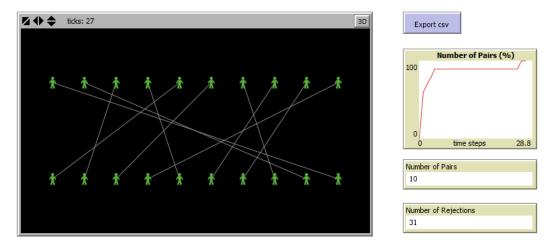


Figure 3.6: Simulation 1, step 27

3.5.2 Simulation Run 2: Large Dataset

The second simulation consisted of a dataset representing 100 men and 100 women. In the first step of the simulation 49 couples were formed (see figure 3.7).

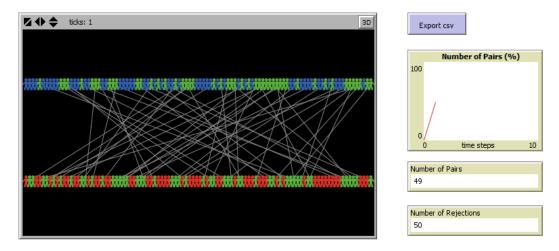


Figure 3.7: Simulation 2, step 1

As observed in the previous simulation, in the next few steps the number of formed couples continued to increase (see figure 3.8).

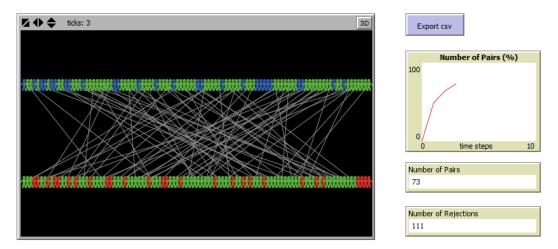


Figure 3.8: Simulation 2, step 3

As the number of steps continued to increase the number of couples increased slowly and a change in the partners was observed (see figure 3.9).

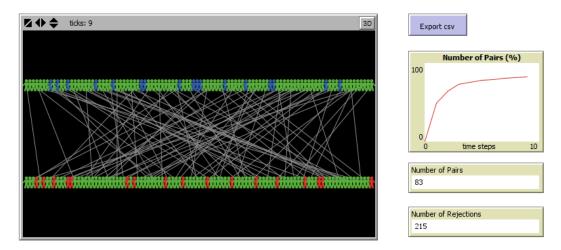


Figure 3.9: Simulation 2, step 9

As the simulation went on, the model started to reach a stable point, where the couples increased only slowly and the number of rejections increased much faster. Finally after 127 steps the model has reached a final state where 94 couples were formed. The final state of the model is illustrated in figure 3.10.

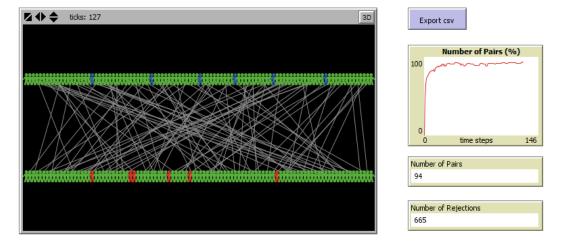


Figure 3.10: Simulation 2, step 127

3.5.3 Simulation Run 3: Large Dataset and Lower Preferences

The second simulation was repeated with a similar dataset, but where the individuals did not have too many preferences (i.e., they were not so picky) regarding their partner. During this simulation the couples were formed faster. After the first step (see figure 3.11) there were 59 couples formed (compared to 49 from the previous simulation - see figure 3.7).

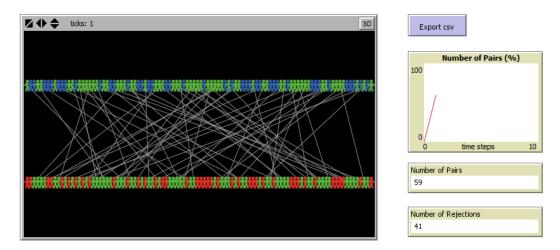


Figure 3.11: Simulation 3, step 1

After the third step there were 79 (compared to 73 from the previous simulation) and after the ninth step there were 90 (compared to 83) couples. Finally the model reached a stable state after 118 steps, where 100 couples were formed. Another observation that was made with the new dataset is that the number of rejections was much lower than in the previous simulation. In the end there were 465 rejections (see figure 3.12) compared to 665 from the previous run (see figure 3.10).

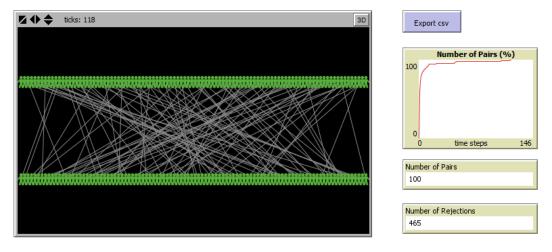


Figure 3.12: Simulation 3, step 118

4 Prototype Evaluation: College Applications in Austria

4.1 Subsection

Text...

5 Prototype Evaluation: Labour Market in the European Union

5.1 Subsection

Text...

6 Summary

6.1 Subsection

Text...

7 Appendix

7.1 Discoteque code

```
extensions [array]
 2 extensions [string]
 3 breed [humans human]
 5; used for drawing a line between the couples
   undirected-link-breed [ pairs pair ]
   ; humans are turtles (common breed)
8
 9
10 ; NetLogo is case-insensitive
11
12 humans-own [
13
     id
14
     name
15
     maxMatchesInt
     sideInt
16
17
      partnerList
18
      rankList
19
     has Proposed To List\\
20
      gotProposedByList
     tmpMatchList
21
22
      activeFlag
23 ]
24
  ;; global variables
25
26
   globals [
27
     csv fileList; fileList named csv
28
      startSideInt; set in setup-globals from GUI-slider
29
      switchingFlag; set in setup-globals from GUI-switch
      debugFlag; set in setup-globals from GUI-switch
30
31
      user-input-filename;
32
      input-filename; set default in setup-globals or from GUI-button
      current_nr_of_pairs
33
      current_nr_of_pairs_percent
34
35
      current_nr_of_rejects
36 ]
37
38 ;; method which is called from the setup button
39 to setup
40
     clear-all
      if debugFlag = true [
41
42
       show "after clear-all"
        show "clear-all"
43
```

```
44
       show count humans]
45
      setup-globals
      if debugFlag = true [show "after open-file"
46
         show "count humans after open-file"
47
48
         show count humans]
49
      reset-ticks
50
   end
51
52 to reset
53
      clear-ticks
      clear-turtles
54
55
      clear-patches
      clear-drawing
56
57
      clear-all-plots
      clear-output
58
      if debugFlag = true [show "after clear-all"
59
         show "clear-all"
60
61
         show count humans]
62
      setup-globals
63
      if debugFlag = true [show "after open-file"
64
         show "count humans after open-file"
65
         show count humans]
      reset-ticks
66
67
   end
68
69
70
   ;; stackoverflow.com/questions/27096948/how-to-read-a-csv-filve-with
       -netlogo
71
   to open-file
72
      file -open (word input-filename ".csv")
73
      set fileList []
74
     while [not file-at-end?] [
75
76
        set csv file-read-line
77
        set csv word csv ";" ; add comma for loop termination
78
        let mylist [] ; list of values
79
        let i 0
80
        while [not empty? csv]
81
82
          let $x position ";" csv
83
84
          if i > 0
85
            let $item substring csv 0 $x ; extract item
            carefully [set $item read-from-string $item][]; convert if
86
               number
87
            set mylist lput $item mylist ; append to list
88
          1
```

```
set csv substring csv ($x + 1) length csv ; remove item and
89
              comma
90
          set i i + 1
91
         if debugFlag = true [show mylist]
92
93
         if item 0 mylist != "id"[
94
          create-humans 1 [
95
             set id item 0 mylist
96
             set name item 1 mylist
97
             set maxMatchesInt item 2 mylist
             set sideInt item 3 mylist
98
             let tmpPartnerListString string:split-string item 4 mylist
99
100
             set partnerList read-from-string (word tmpPartnerListString)
101
                   set partnerList string:split-int item 4 mylist "#"
             let tmpRankListString string:split-string item 5 mylist "#"
102
             set rankList read-from-string (word tmpRankListString)
103
                   set rankList string:split-int item 5 mylist "#"
104
             set hasProposedToList []
105
             set gotProposedByList []
106
107
             set tmpMatchList []
108
             set activeFlag true
109
          1
110
        set fileList lput mylist fileList
111
         if debugFlag = true [show "count humans at end of open-file"
112
113
         show count humans
114
         show "fileList at end of open-file"
115
         show fileList]
116
      file-close
117
   end
118
119
120 to setup-globals
121
      ifelse starter = "Men" [set startSideInt 1] [set startSideInt 2]
      set debugFlag debug
122
      set switchingFlag switching
123
124
      ifelse user-input-filename = 0 [set input-filename "
          disco100NotPicky"] [set input-filename user-input-filename]
      set current_nr_of_rejects 0
125
126
      set current_nr_of_pairs 0
127
      set current nr of pairs percent 0
      let current_world_width world-width
128
129
130
      open-file; and read initialisation data from csv file
131
      ; define starting position and start color
132
      let number_women count humans with [sideInt = 2]
```

```
133
      let xposHumansStart current_world_width / 2; starting position
          for humans
134
      let i 1
135
      foreach sort humans with [sideInt = startSideInt] [
136
        ask?
137
          let number_starting count humans with [sideInt = startSideInt]
138
           set shape "person"
139
          set size 1
140
          set heading 0
141
           ; positioning and color
142
          set ycor 4
          ifelse sideInt = 1 [set color blue] [set color red]
143
          let xposHumans i / (number starting + 1) * current world width
144
               xposHumansStart
145
          set xcor xposHumans
146
          set i i + 1
147
        ]
148
      1
149
      set i 1
      foreach sort humans with [sideInt != startSideInt] [
150
151
        ask?
152
          let number_notstarting count humans with [sideInt !=
              startSideInt]
153
          set shape "person"
          set size 1
154
155
          set heading 0
156
           ; positioning and color
157
          set ycor -4
158
          ifelse sideInt = 1 [set color blue] [set color red]
159
           let xposHumans i / (number_notstarting + 1) *
              current_world_width - xposHumansStart
160
          set xcor xposHumans
161
          set i i + 1
162
        ]
163
      1
164 end
165
166 to go
      if count humans with [activeFlag = true and (sideInt =
167
          startSideInt or switchingFlag = true)] = 0 [stop]
168
      step
169
   end
170
171
172
173
    to step
                                      ---- begin of step
174
      if debugFlag = true [show "----
```

```
175
         show "count humans at begin of step"
176
         show count humans]
177
      clear-before-match
178
      foreach sort humans with [activeFlag = true and sideInt =
          startSideInt] [ ; start of proposing
179
180
           if debugFlag = true [show "count humans at begin of ask humans
               with activeFlag=true and sideInt=startSideInt"
181
             show count humans with [activeFlag = true and sideInt =
                startSideInt]
             show "myId"
182
183
             show id
             show "myName"
184
185
             show name
             show "partnerList"
186
187
             show partnerList
188
             show "hasProposedToList"
189
             show hasProposedToList]
           let tmpPotentialPartnersList list-difference partnerList
190
              hasProposedToList; set-difference of partnerList \
              hasProposedToList
191
           if length tmpPotentialPartnersList = 0 [
192
             set activeFlag false; this human has no potential partners
                to propose to
193
             stop; break
194
195
           if length tmpMatchList >= maxMatchesInt [
196
             set activeFlag false; this human has enough current matches
197
             stop
198
           1
           let myPreferredPartner item 0 tmpPotentialPartnersList; most
199
              preferred partner from tmp...List
200
          propose-to id myPreferredPartner
201
202
      ]; end of proposing
      if debugFlag = true [show "end of proposing"]
203
      foreach sort humans with [length gotProposedByList > 0 and sideInt
204
           != startSideInt] [
205
        ask? [
206
           process-proposals id
207
        ]
208
209
       if switchingFlag = true [set startSideInt ((startSideInt + 1) mod
210
      if startSideInt = 0 [set startSideInt 2]
       if debugFlag = true [show "switchingFlag"
211
212
         show switchingFlag
         show "startSideInt"
213
```

```
214
         show startSideInt]
215
      calc-stats
216
      tick
217
      if debugFlag = true [show "############ end of step
          #########"]
218 end
219
220 to calc-stats
221
      set current_nr_of_pairs 0
222
      ask humans with [sideInt = startSideInt] [
         if length tmpMatchList = maxMatchesInt [
223
224
            set current_nr_of_pairs current_nr_of_pairs + 1
225
        1
226
      1
227
     let countedHumans count humans with [sideInt = startSideInt]
228
      ifelse countedHumans = 0 [
229
        set current_nr_of_pairs_percent 0
230
      ] [
231
         set current_nr_of_pairs_percent current_nr_of_pairs /
            countedHumans
232
         set current_nr_of_pairs_percent current_nr_of_pairs_percent *
233
         if current_nr_of_pairs = 0 [set current_nr_of_pairs_percent 0]
234
235
      if debugFlag = true [ show "Current Nr of Pairs"
236
       show current_nr_of_pairs
237
       show "Current Nr of Pairs Percent"
238
       show current_nr_of_pairs_percent
239
     1
240
    end
241
242 to clear-before-match
243
      ask humans [
         set gotProposedByList []; delete gotProposedbyList (in
244
            preparation for next matching-round)
245
246
   end
247
    to propose-to [sender receiver]
248
      if debugFlag = true [show "---
                                       ----- begin of propose-to
249
250
      ask humans with [id = sender] [
251
         set hasProposedToList lput receiver hasProposedToList
252
         if debugFlag = true [show "hasProposedToList"
253
           show hasProposedToList
254
           show "receiver"
255
           show receiver]
         ask humans with [id = receiver] [
256
```

```
257
           set gotProposedByList lput sender gotProposedByList
           if debugFlag = true [show "female side"
258
259
             show "gotProposedByList"
260
             show gotProposedByList]
261
        1
262
      1
263
      if debugFlag = true [show "########### end of propose-to
          ###########"]
264
    end
265
266
    to process-proposals [tmpId]
      if debugFlag = true [show "----
                                       ----- begin of process-
267
          proposals ----"
268
         show "count humans at begin of process-proposals"
269
         show count humans]
270
      ask humans with [id = tmpId] [
271
         if debugFlag = true [show "gotProposedByList"
272
           show gotProposedByList
           show "sideInt"
273
274
           show sideInt
275
           show "maxMatchesInt"
276
           show maxMatchesInt]
        let tmpPotentialCoupleList []
277
278
        ifelse length tmpMatchList = 0 [
279
           set tmpPotentialCoupleList gotProposedByList
280
281
        set tmpPotentialCoupleList list-union-set tmpMatchList
            gotProposedByList
282
283
         if debugFlag = true [show "tmpPotentialCoupleList"
284
           show tmpPotentialCoupleList]
285
        let tmpRejectList []
286
        let tmpCoupleList []
        ifelse length tmpPotentialCoupleList > maxMatchesInt [
287
288
           set tmpCoupleList list-order tmpPotentialCoupleList rankList
              partnerList maxMatchesInt
           if debugFlag = true [show "has more proposals than willing to
289
              accept"
             show "tmpCoupleList"
290
             show tmpCoupleList]
291
           set tmpRejectList list-difference tmpPotentialCoupleList
292
              tmpCoupleList
293
        ] [
        set tmpCoupleList tmpPotentialCoupleList
294
295
296
        if length tmpRejectList > 0 [
297
           reject-proposals id tmpRejectList
298
        ]
```

```
299
        if length tmpCoupleList > 0 [
300
          create-tmpCouples id tmpCoupleList
301
        ]
302
      1
303
      if debugFlag = true [show "########### end of process-
          proposals ###########"]
304
   end
305
306
    to reject-proposals [tmpId rejectList]
      if debugFlag = true [show "----- begin of reject-
307
          proposals ----"
308
      let rejecter 0
309
      ask humans with [id = tmpId] [
310
        set rejecter self
        set tmpMatchList list-difference tmpMatchList rejectList
311
312
        if debugFlag = true [show "tmpMatchList"
313
           show tmpMatchList]
314
        foreach rejectList [
315
          ask humans with [id = ?] [
            set tmpMatchList list-difference tmpMatchList lput tmpId []
316
317
            set activeFlag true
318
            ifelse sideInt = 1 [set color blue] [set color red]
            set current_nr_of_rejects current_nr_of_rejects + 1
319
320
            remove-link self rejecter
321
          1
          ifelse sideInt = 1 [set color blue] [set color red]
322
323
        ]
324
      1
325
      if debugFlag = true [show "############ end of reject-proposals
           ########"]
326 end
327
328
    to create-tmpCouples [tmpId acceptList]
      if debugFlag = true [show "------tmpCouples -----"]
                                            ---- begin of create-
329
      ask humans with [id = tmpId] [
330
        set tmpMatchList acceptList
331
        if debugFlag = true [show "tmpMatchList"
332
333
           show tmpMatchList]
        foreach acceptList [
334
335
          ask humans with [id = ?] [
            set tmpMatchList list -union-set tmpMatchList lput tmpId []
336
337
            set color green
            create-link-with myself
338
339
          ]
340
          set color green
341
        ]
342
      1
```

```
if debugFlag = true [show "############ end of create-
343
          tmpCouples ###########"]
    end
344
345
346
347
    to-report list-order [listToOrder ranking partners maxMatches]
      if debugFlag = true [show "----- begin of list-order
348
      set listToOrder list-overlap listToOrder partners
349
350
      if debugFlag = true [show "listToOrder"
         show listToOrder]
351
352
      if length listToOrder > maxMatches [
        let tmpRanking get-rating-of-list partnerList listToOrder
353
            ranking
354
        let tmpList listToOrder
355
        if debugFlag = true [show "tmpRanking"
356
           show tmpRanking
357
           show "tmpList"
           show tmpList]
358
        set listToOrder []
359
360
        let i 0
361
        loop [
           if i >= maxMatches [report listToOrder]
362
363
           let j position (max tmpRanking) tmpRanking
           if debugFlag = true [show "j"
364
365
             show j
             show "item j tmpList"
366
367
             show item j tmpList
368
             show "tmpList"
369
             show tmpList]
370
           set listToOrder lput item j tmpList listToOrder
371
           set tmpRanking remove-item j tmpRanking
372
           set tmpList remove-item j tmpList
           if debugFlag = true [show "listToOrder"
373
374
             show listToOrder
375
             show "tmpList"
             show tmpList]
376
          set i i + 1
377
378
        ]
379
380
381
      report listToOrder
382
      if debugFlag = true [show "########### end of list-order
          #########"]
383 end
384
385
    ;; symmetrical difference: fullList \ toRemoveList
    to-report list-difference [fullList toRemoveList]
```

```
387
      report filter [not member? ? toRemoveList] fullList
388 end
389
390 ;; intersection of listA and listB
    to-report list-overlap [listA listB]
391
      if debugFlag = true [show "########### begin of list-overlap
392
         ##########"
393
         show listA
394
         show listB
         show filter [member? ? listB] listA]
395
396
      if debugFlag = true [show "########### end of list-overlap
         ############"]
      report filter [member? ? listB] listA
397
398 end
399
400 ;; union of listA and listB
401 to-report list-union-set [listA listB]
      let tmpList list-difference listB listA
402
403
      foreach tmpList [ set listA lput ? listA]
404
      report listA
405 end
406
407
408
   ;; gets ranking associated with fullList for partialList
    to-report get-rating-of-list [fullList partialList ranking]
      let tmpList []
410
411
      foreach partialList [
412
        set tmpList lput item (position ? fullList) ranking tmpList
413
414
      report tmpList
415 end
416
417
418
419
    420 ;;; Input filename
421
    422
423 to change-input
424
      set user-input-filename user-input "Type input filename (without
         extension)."
425
      if debugFlag = true [show "user-input-filename"
426
         show user-input-filename]
427 end
428
429
430
431
```

```
432
    433 ;;; Output matches
434
    435
436
437
   ;; write-to-file taken from
    ;; Wilensky, U. (1999). NetLogo. http://ccl.northwestern.edu/netlogo
438
        1.
439 ;; Center for Connected Learning and Computer-Based Modeling,
       Northwestern University, Evanston, IL
    ;; code from File/Models Library/Code Examples/File Output Example
440
441
442 to export-to-csv
443
      let output-filename (word input-filename "_Starter_" starter "
          _Switch_" switching "_Ticks_" ticks ".csv")
      foreach sort humans [
444
445
        ask? [
          let delimPartnerList list-concat-with-delim partnerList "#"
446
          let delimRankList list-concat-with-delim rankList "#"
447
          let delimHasProposedToList list-concat-with-delim
448
              hasProposedToList "#"
449
          let delimGotProposedByList list-concat-with-delim
              gotProposedByList "#"
450
          let delimTmpMatchList list-concat-with-delim tmpMatchList "#"
          write-csv output-filename (list (id) (name) (maxMatchesInt) (
451
              sideInt) (delimPartnerList) (delimRankList) (
              delimHasProposedToList) (delimGotProposedByList) (
              delimTmpMatchList) (activeFlag))
452
        1
453
454
    end
455
456
    ;; http://stackoverflow.com/questions/22462168/netlogo-export-
457
       tableau-issues
   to write-csv [ #filename #items ]
458
      ;; #items is a list of the data (or headers!) to write.
459
      if is-list? #items and not empty? #items
460
461
      [ file -open #filename
        ;; quote non-numeric items
462
463
        set #items map quote #items
464
        ;; print the items
465
        ;; if only one item, print it.
        ifelse length #items = 1 [ file-print first #items ]
466
467
        [file-print reduce [ (word ?1 ";" ?2) ] #items]
        ;; close-up
468
469
        file-close
470
      1
```

```
471 end
472
473 to remove—link [human1 human2]
      ask links with [(end1 = human1 and end2 = human2) or (end1 =
474
          human2 and end2 = human1) ] [
475
        die]
476 end
477 ;; http://stackoverflow.com/questions/22462168/netlogo-export-
        tableau-issues
478 to-report quote [ #thing ]
479
      ifelse is-number? #thing
      [ report #thing ]
480
      [ report (word "\"" #thing "\"") ]
481
482 end
483
484 ;; https://groups.yahoo.com/neo/groups/netlogo-users/conversations/
        topics/6490
485 ;; intersperse listA with delim
486 to-report list-concat-with-delim [listA delim]
487
      if length listA > 0 [report reduce [(word ?1 delim ?2)] listA]
      report ""
488
489 end
```

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