VIENNA UNIVERSITY OF TECHNOLOGY

105.625 PR ADVANCED ECONOMICS PROJECT

Double Sided Matching

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Contents

1	Intr	oductio	on	2			
	1.1	Motiva	ation and Problem Description	2			
	1.2		nd Objectives				
	1.3		ture				
2	The	Theory					
	2.1	•		4			
	2.2						
	2.3	1					
		2.3.1	General				
		2.3.2	Example for the Application of Game Theory	7			
		2.3.3	Double Sided Matching Problem and Game Theory	7			
		2.3.4	Double Sided Matching Problem and Optimal Stopping	8			
3	Prot	Prototype 9					
	3.1	3.1 Data Model					
	3.2	Data (Generation	10			
	3.3	GUI		11			
	3.4	NetLogo Code					
	3.5	Simulation Runs					
		3.5.1	Simulation Run 1: Small Dataset	14			
		3.5.2	Simulation Run 2: Large Dataset	16			
		3.5.3	Simulation Run 3: Large Dataset and Lower Preferences	18			
4	Sum	mmary					
5	Appendix						
	5.1	Discot	teque code	20			
Lis	st of F	igures		32			
Re	feren	ices		33			

Introduction

Double sided matching is about finding a match between two sets of elements. The first algorithm which should solve this problem was described by David Gale and Lloyd S. Shapley in 1962 [1]. The focus of this report is on the examination of this algorithm and the creation of a simulation model for it, which can be applied to different economic issues. The selected economic issues will be presented in the following chapters. Due to another important project in the course of this lecture only the partner-matching algorithm was implemented. The other two economic issues, the university application and labour supply/demand problem, could not be implemented.

Motivation and Problem Description

Many everyday situations contain hidden double sided matching problems. For example, students usually have the opportunity to apply to a number of schools. In this case students and schools have to be matched together. Both parties have preferences which need to be taken into consideration. Yet, in our everyday life we usually do not have the time to find an appropriate solution for our problems.

In some cases these problems even go by without solving them. In other situations however, it is crucial to solve them, e.g. if we consider medical school graduates and open positions in hospitals. Due to multiple reasons like different preferences or a high number of elements in the two sets this problem cannot be solved intuitively or in linear time.

Aim and Objectives

The aim of this paper is to develop a simulation model prototype which can solve similar problems, like the ones discussed above. Questions, which should be answered with the simulation model are:

- Do there exist "stable" solutions for these kinds of problem?
- How can it be applied to all prospective students and universities in Austria?
- Is there also a solution for the current labour supply and demand in the European Union?

Structure

In the second chapter a theoretical overview is provided regarding the double sided matching problem and what stability means in this context. The focus lies on the Gale and Shapley Algorithm, basic information about the game theory and the relationship between them.

The third chapter describes the prototype of the simulation model, which puts the previously discussed theory into practice. As a simulation environment NetLogo ¹ will be used. The prototype will be firstly evaluated on a simple discotheque example. In the disco example it is assumed, that an equal number of men and women are in a discotheque and the objective is to form couples.

Finally the most important findings and results are summarized and compared in the last chapter. Additionally a short outlook to further research areas will be provided.

¹Available at https://ccl.northwestern.edu/netlogo/, accessed April 28, 2016

Theory

In this chapter the necessary theoretical background for the realization of this project is discussed.

The Double Sided Matching Problem

The double sided matching problem focuses on two groups of elements. These sets are disjoint and may be equal in size, but this condition is not mandatory. The purpose of the double sided matching algorithm is to find a solution, so every element of the first set has a corresponding counterpart in the other set. This can be best described in an example: Assume that the elements are men and women and that individuals have only heterosexuals preferences. Consequently, the two sets are male and female persons. The double sided matching algorithm shall create couples, which consist of a man and woman. Optimally, every person has a partner who has a high position in their list of preferences.

The solutions of the matchings can have different properties, which might be very important (e.g. stability). The output of the algorithm of men and women is not allowed to be unstable, i.e. there are two men α and β who are assigned to women A and B although β prefers A to B and A prefers α to β . If this situation does not occur, the assignment is called *stable*. If there exists more than one stable solution the *optimal* one can be of particular interest.

Optimality means that a solution has the best outcome for an individual or set. In this case optimality can be achieved from the perspective of the first set of elements or from the second one. There can also be a trade-off from the perspective of the both sets. In this case optimality is achieved by weighting the expected value of both sets. These properties have been described in a more detailed way in the paper by Gale and Shapley [1].

Generally in economics this is also known as pareto efficiency [2, p. 46]. Pareto efficiency is a characteristic for a solution where any change which would improve one property on one hand, but will worsen another one on the other hand.

Gale and Shapley Algorithm

In the paper of Gale and Shapley [1] an algorithm was proposed for solving the double sided matching problem. The assumption is that there are two sets of elements: one contains men and the other one women. The size of the two sets is equal, the preferences are heterosexual and there are no polygamies (i.e. one element is only allowed to be matched with one element from the other set). The aim of the algorithm is to find a stable way of marrying men and women. Each man and woman has own preferences of the marriage partner.

First Iteration

In the first iteration each man proposes to the woman who he ranked on the first place. Afterwards a woman has a list of men who proposed to her. This list might not contain anybody. If one man/multiple men proposed to her she rejects every man, except most preferred man on her preference list who proposed to her. If a man is not rejected he and the woman create a temporary couple. All men who are not in a couple are single.

Second Iteration

In the second interaction each man who is single, proposes to his highest ranked woman, to whom he did not propose yet. Each woman now chooses the man she ranked the highest out of her received proposals. If a man is not rejected he and the woman create a temporary couple (Note: after the second iteration some men, who have been in a couple in the first iteration, might be single again).

Further Iterations

The third iteration is the same as the second one. This continues until every man is in a couple. If this condition is satisfied a stable solution is found for the double sided matching problem. The stability of the solution of this algorithm has been proven by contradiction [1].

Relevance to Game Theory

General

"Game theory is about what happens when people - or genes, or nations - interact" [3, p. 1]. An important aspect for the participating parties is to anticipate how the opposite party will react on certain actions. Mathematics shall help to analyse, understand and estimate outcomes of such games. Depending on the information participants have, they decide how to act basing on rules contained in their strategy. Game theory is widely applied in economics. Companies use game theory to estimate e.g. reactions of competitors or behaviour of employees. The major advantages of game theory are its precision and its universal applicability to all kind of games. [3, pp. 1-3]

In addition there are some assumptions which are made during preparation and execution by every individual who is interacting with another one:

- · Well-specified choices
- · Well-defined end-state
- · Specified pay-off
- · Perfect knowledge
- Rationality

However, these perfect preconditions will never be met in real life scenarios. In the context of double sided matching, it is important to have well-specified choices defined.

Nevertheless, there might be chances to get into a nearly worst-case scenario instead. As a consequence of these listed assumptions above, there are two different kind of games:

- · Static ones
- · Dynamic ones

The two items can be combined with the following kinds of knowledge

- Incomplete
- Complete (there is no private information)

Depending on the nature of the game, whether it is static or dynamic and whether the knowledge is complete or incomplete, four different combinations can be made. For a better understanding, following examples only consist of two players (every combination can be used for a higher number of players too):

• Static and (in)complete information

As of complete information, the player's action set can be presented in an N \times M matrix. Therefore all information (also private) is known to every player and each player is able to easily eliminate the pay-offs of the other players. The pay-off is the outcome of a chosen action of a player which depends on the state or previous actions of the game. The pay-off can change dynamically while the game is in progress. As of incomplete information players are forced to be uncertain about the other player's actions and pay-offs. Besides that, there are two basic steps

- 1. Player 1 and 2 are choosing actions out of a set, which was predefined by them before.
- 2. After their actions, they receive their pay-offs.
- Dynamic and complete information

When basic assumptions are made on complete information, players will create a strategy to ensure to get the highest return of each action. Although the strategy might be changed during the game after each turn. Incomplete information leads to communication of uninformed parties (i.e. closed private information) which might end up to under- or overestimate the others pay-offs. In general there will be a Nash Equilibrium between those parties. This equilibrium is created by players because they choose a strategy which do not depend on the other players. There are three basic steps:

- 1. Player 1 chooses an action out of his/her predefined set.
- 2. Player 2 observes player 1's action and chooses an action based on his/her observation.
- 3. After their actions, they receive their pay-offs.

The previously described theory is based on information of the paper "An introduction to applicable game theory" [4].

Example for the Application of Game Theory

Game theory is also very popular in the field of economics. Many companies primarily apply game theory to estimate the reactions of their competitors. In the last auction for broadband internet frequencies in Germany, all major providers hired game theorists out of two reasons. Firstly, they wanted to win the auction for the desired frequency and secondly, they also did not want to overpay for the frequency. The bidding behaviour of a provider indicated the interest rate for a frequency. As a consequence, other providers retained their bids for parts of this frequency so the interested provider did not need to overpay for it. The positive result for the providers was, that the 700-MHz frequency parts were sold for the minimum bidding price. [5]

Double Sided Matching Problem and Game Theory

Like described in chapter 2, the goal of the three main problems, which will be simulated in the course of this project, is to bring different parties together. In the original marriage problem discussed by Shapley, the goal was to match men and women so the overall situation is stable. This idea can also be applied to other areas like the labour market or university applications. In each of these three problems the parties need to have a strategy how to react to moves of the counterpart. If, for example, a university offers a place to a student and this is not the student's favourite one, he/she has to decide whether to accept the place (to be on the safe side) or still hope to get accepted from the favourite university (and as a consequence accept to be on the waiting list there). Not only the student needs to have a strategy how to deal with these situations but also universities have to incorporate different reactions of students into their application process (e.g. how many students to invite) [1].

The double sided matching problem is a dynamic game. The players of the two sets have incomplete information. The algorithm uses the information of both sets, therefore it has complete information.

An important aspect of the game or matching is that the rules have to be clear, which was mentioned by Roth and Sotomayor. The way agents are matched to each other influences the analysis of the problem. A possible rule might be that individuals like a student and university are only brought together if both parties agree to the matching. Other norms of a game might contain the way an individual proposes to another one or whether there exists a moderating individual [6, p. 492].

Double Sided Matching Problem and Optimal Stopping

The double sided matching problem also relates to the optimal stopping problem. The optimal stopping problem deals with choosing the optimal time to stop an undertaken action and at the same time minimize the expected costs and maximize the profit. A concrete example for the optimal stopping problem could be a man trying to find a woman to spend the rest of his life with. He can meet several different women but when is the optimal time to stop looking?

A few algorithms leading to a possible solution for the optimal stopping problem have been presented by Christian & Griffiths 2016 [7]. For the previously mentioned example of partner search, one algorithm proposes to spend 37% of the time in building standards. Afterwards, the man should immediately propose/choose the next woman he meets who satisfies or over-exceeds his standards. 37% is the provably optimal solution [7, p. 2]. This algorithm is recommended in the case of *no-information games* (e.g. in the case of a partner search, it is hard to quantify the information, because it is hard to compare people to each other. There is no concrete criteria, one can only assume that one person is better or more suitable than another person, but not by how much) [7, p. 18].

Another possible solution for the previously mentioned problem is to set a threshold from the beginning on and to take the first option who exceeds it. Christian & Griffiths 2016 [7] recommended this approach in the case of *full-information games*. A suitable example for this case is the sale of a house: the value of the house can be specified clearly and there exists also information about the state of the market. The combined knowledge allows to predict a range of offers. In this case a threshold is set and the first offer that exceeds this threshold can be accepted. This example does not include waiting costs. If waiting costs exist, they also have to be taken into account. Therefore, it is recommended to decline an offer if the chance of a better offer multiplied by how much better it is compensates the waiting costs.

Finally Christian & Griffiths 2016 [7, pp. 28-30] recommend to always stop looking at a certain point.

Prototype

A prototype for solving the double sided matching problem was developed in NetLogo². In this chapter the prototype is evaluated on a discotheque example. In this case, it is assumed that an equal number of men and women are in a discotheque and the objective is to form couples based on the individual preferences. In the following, the data model, the data generation script, the graphical user interface (GUI) and code from NetLogo will be described.

Data Model

According to the problem description a generic data model for every individual was defined. This data model is valid for the discotheque example, the university and labour market example, and contains the following attributes:

- id: unique object identifier
- name: object name (e.g. male1 or female1)
- maxMatchesInt: integer value representing the maximum number of matchings for this individual (e.g. in the disco example each person is maximally matched with one other person)
- sideInt: integer helper variable assigning an individual to one of the two participant groups
- partnerList: list of identifiers of the partners, ordered according to the preference of an individual
- rankList: list of ranks (values between 1 to 0) for the partners from the partnerList; the list is ordered from highest to lowest preferences. If the value is equal to 1 this partner is a perfect match.
- hasProposedToList: list of identifiers representing the individuals to which an individual has proposed
- gotProposedByList: list of identifiers representing the individuals from which an individual received proposals. The gotProposedByList is only valid for one iteration.
- tmpMatchList: list containing the identifiers of individuals to whom a temporary match was established
- activeFlag: boolean value stating if an individual is matched or not respectively if
 the individual gave up (they already proposed to all individuals from the partnerList
 but only received rejections)

²Available at https://ccl.northwestern.edu/netlogo/, accessed April 28, 2016

Data Generation

In order to generate random data, which represents the individuals and their preferences the statistical computing language R³ was used. The generated data is exported as a CSV list, which is then read by NetLogo. The R script accepts the following parameters:

- seed: integer value, which is used as a seed by the number generator. The default value is 123.
- numberOfMen: integer value representing the number of men which should be created. The default value is 10.
- numberOfWomen: integer value representing the number of women which should be generated. The default value is 10.
- pickyLower: float value between 0 and 1 representing the lower bound which will be used in order to generate a number that represents how picky a person is. The value 0 means accepts every possible match, the value 1 excepts none.
- pickyUpper: float value between 0 and 1 representing the upper bound which will be used in order to generate a number that represents how picky a person is. The value 0 means excepts every possible match, the value 1 excepts none.

The script can be called as follows from the command line:

```
Rscript initDisco.R 123 10 10 0 0
```

The script generates a CSV which looks as follows:

³Available at https://www.r-project.org/, accessed April 28, 2016

GUI

One of the main goals in the design phase was to keep the GUI simple and clear. The GUI was structured in two main parts - the control and the information section.

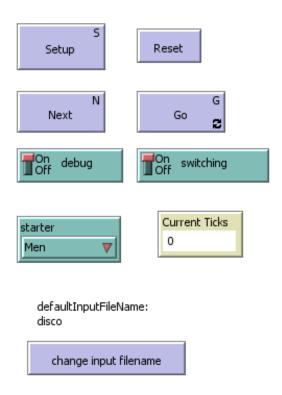


Figure 3.1: The control section for the disco example

Figure 3.1 shows the control section in the GUI. With the buttons **Setup** and **Reset** the simulation model can be initialized or reset after a simulation run. The button Next advises the program to perform one simulation step, if Go is activated the simulation continues until a termination criterion is met. In the disco example the main termination criterion is if every proposing person is already matched to another person. Another criterion for termination is if the proposing person already proposed to every person in his partnerList but got rejected every time. The debug switch enables or disables debug messages which are printed during the setup phase and simulation run. The speed of a simulation run can be increased if the **debug** switch is set to Off. The second switch, switching, controls, if the two parties propose to each other alternatively (On) or if only one party proposes to the other one (Off). With the drop-down list **starter** the user can determine which party starts proposing. The reporting box Current Ticks shows the current number of simulation steps. The button change input file name raises a dialogue box where the user can enter the filename of an input file which shall be used in the simulation. Together with the number of ticks the file name will also be used as the name for the CSV export file.

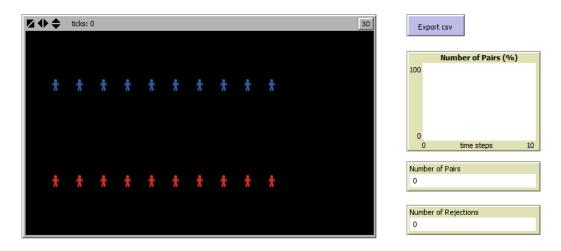


Figure 3.2: The information section for the disco example

Figure 3.2 shows the information section of the disco example GUI. All created humans are shown in the world area. Men are coloured blue and women are red. On setup of the simulation the proposing site is shown in the top row. As soon as two people are matched their colour changes to green and a link between the two is established. If a couple is divorced the link is removed and the colour changes back to the original one. The plot named **Number of Pairs** (%) illustrates at each point in time how many of the possible couples exist. If the simulation contains 10 men and 10 women and currently 4 couples exist, the plot shows that 40% are matched. The reporting box **Number of Pairs** shows the absolute number of couples. The other reporting box, **Number of Rejections**, indicates how many couples were divorced over time. With the button **Export CSV** the current properties of all humans are exported to a CSV file. The file name is a combination of the input file name, the starting side, if the switching is activated and the current number of ticks.

NetLogo Code

At the beginning of the NetLogo code the extensions, the data model and the needed global variables are defined. The rest of the code is based on procedures (i.e. a sequence of NetLogo commands which begins with *to* and ends with *end*). The most important procedures are the following:

- *setup* and *reset*: both clear all results and reset the whole model (especially the needed variables) to an initial empty state.
- *open-file*: procedure used to open and import a CSV list which represents the individuals and their preferences. The turtles for the simulation are then created based on the read information.
- *setup-globals*: procedure used to set up all global variables (e.g., current number of pairs, shape of the humans, etc.)
- *step*: procedure which represents going one step in the double sided matching algorithm. Within this step one side proposes to the other one. The proposal-receiving site processes (accepts/rejects) the proposals.
- *go*: calls the procedure step until a termination criterion is met.
- *calc-stats*: calculate some statistical information (e.g., number of pairs, number of rejections).
- *clear-before-match*: empties the list of the proposals as a preparation for the next matching round.
- *propose-to[sender receiver]*: sends the proposals (e.g. manages lists containing IDs of individuals an individual already proposed to/an individual got proposed by).
- process-proposals [tmpId]: processes the proposals (e.g. orders incoming proposals according to the own preference, calls the method create-tmpCouples to form a couple with the most desired partner, calls method reject-proposals to reject the other proposers).
- reject-proposals [tmpId rejectList]: rejects the proposals (e.g. removes the partner-ID from the tmpMatchList, sets the status of the turtle to active the individual shall try to find another partner in the next round, sets the colour of the rejected individual to the original one and removes an existing link).
- *create-tmpCouples [tmpId acceptList]*: creates temporary couples (e.g. puts the ID of the partner in the tmpMatchList, sets the colour of the individual to green, creates a link to the partner).

The Netlogo program itself contains comments which explain the procedures and performed steps in a more detailed way.

Simulation Runs

The discotheque problem was simulated three times: one time with a simple and small dataset of 20 persons (10 men and 10 women) and twice with a dataset of 200 persons (100 men and 100 women).

Simulation Run 1: Small Dataset

In the first simulation run a dataset containing 20 individuals (10 males and 10 females) was used. This dataset was generated using the previously described R script. After the first simulation step already 6 couples were formed (see figure 3.3).

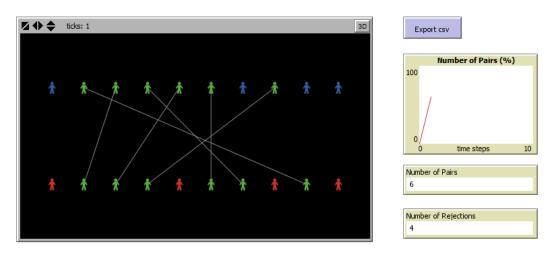


Figure 3.3: Simulation 1, step 1

In the next few steps the number of couples continued to increase by 1 at each step. After the third step 8 couples were formed (see figure 3.4).

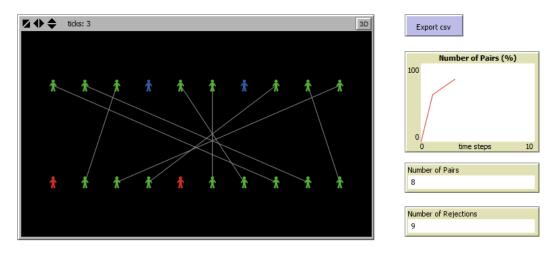


Figure 3.4: Simulation 1, step 3

Afterwards the number of couples continued to increase slowly and some of them changed according to the individual's preferences. As we can see in figure 3.5 the male number 10 (upper right corner) was in a couple with female number 3. However, male number 10 is now single, because female number 3 changed the partner and is now a couple with male number 6. Female number 3 changed partner because male number 6 better suits her preferences.

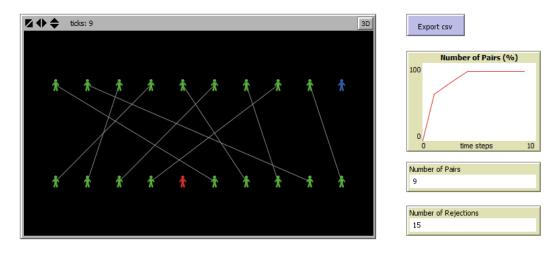


Figure 3.5: Simulation 1, step 9

In the further steps, the couples continued to change according to the individual's preferences. Finally, after 27 steps the double sided matching problem was solved and 10 couples have been created (see figure 3.6).

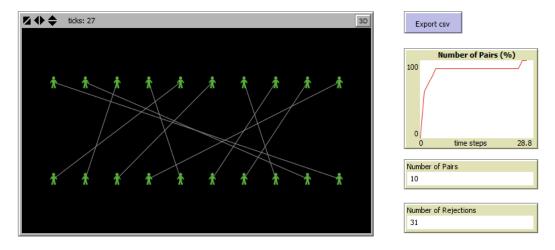


Figure 3.6: Simulation 1, step 27

Simulation Run 2: Large Dataset

In the second simulation run, the algorithm was applied to a dataset containing 100 men and 100 women. In the first step of the simulation 49 couples were formed (see figure 3.7).

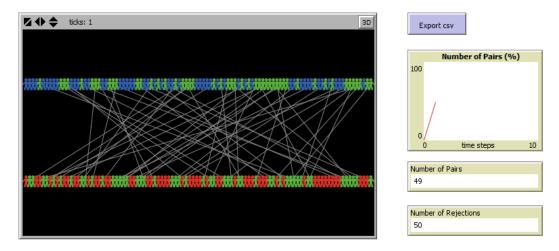


Figure 3.7: Simulation 2, step 1

As observed in the previous simulation, in the next few steps the number of formed couples continued to increase (see figure 3.8).

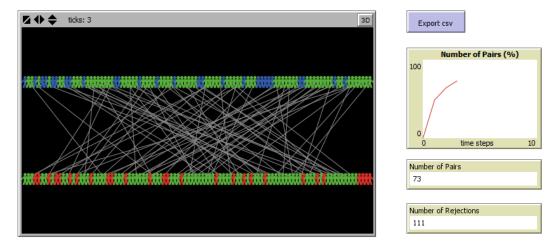


Figure 3.8: Simulation 2, step 3

As the number of steps increased, the number of couples increased only slowly and a change of couples could be observed (see figure 3.9).

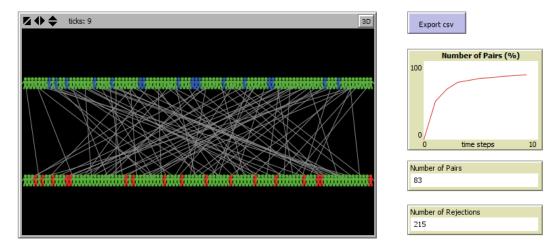


Figure 3.9: Simulation 2, step 9

As the simulation went on, the model started to reach a stable point, where the number of couples increased only slowly and the number of rejections increased much faster. Finally, after 127 steps, the model has reached a final state where 94 couples were formed. Not every individual could find a partner. This might happen if a person was in a partnership, got rejected and could not find another partner who was not already in a partnership with a higher-ranked person. The final state of the model is illustrated in figure 3.10.

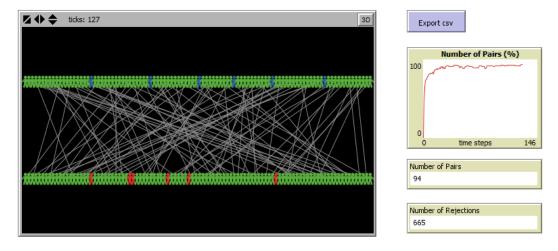


Figure 3.10: Simulation 2, step 127

Simulation Run 3: Large Dataset and Lower Preferences

The second simulation was repeated with a similar dataset. This time however, the individuals did not have too many preferences (i.e., they were not so picky) regarding their partner. During this simulation the couples were formed faster. After the first step (see figure 3.11) there were 59 couples formed (compared to 49 from the previous simulation - see figure 3.7).

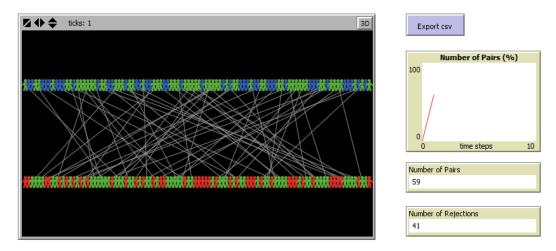


Figure 3.11: Simulation 3, step 1

After the third step there were 79 (compared to 73 from the previous simulation) and after the ninth step there existed already 90 (compared to 83) couples. Finally the model reached a stable state after 118 steps, where 100 couples were formed. Another observation with the new dataset was, that the number of rejections was much lower than with the other data set. In the end 465 rejections (see figure 3.12) were counted compared to 665 from the previous run (see figure 3.10).

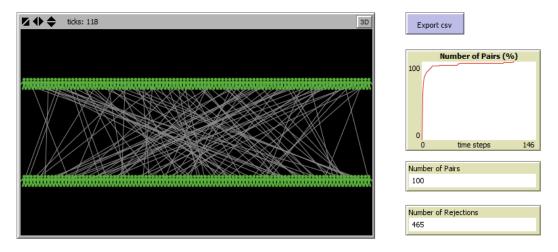


Figure 3.12: Simulation 3, step 118

Summary

The algorithm by Gale and Shapley is very versatile and can be applied to different problems. It would be interesting to also apply it to the labour market to pair supply and demand. Furthermore, it would also be interesting to see how good the simulation model performs with real life data (e.g. matching students and universities).

The major difficulty will probably be the data gathering and preprocessing. Statistics about university preferences are not available (for public use). One possibility to overcome this problem would be to use data about students who finished certain studies. Then, assumptions about their preference and other factors (like the place of residence or previous education) need to be taken.

Another aspect which has to be considered is the performance of the simulation model. Even though the code was written with runtime in mind the size of the data set had major impacts on the runtime.

As mentioned above, it would be very interesting to test the model in further research projects with other data sets and areas of application. Maybe, also extensions (like the optimal stopping) could be incorporated in future, more advanced versions of the simulation model.

Appendix

Discoteque code

```
extensions [array]
2 extensions [string]
3 breed [humans human]
5; used for drawing a line between the couples
  undirected-link-breed [ pairs pair ]
   ; humans are turtles (common breed)
8
9
10 ; NetLogo is case-insensitive
11
12 humans-own [
13
     id
14
     name
15
     maxMatchesInt
     sideInt
16
17
     partnerList
18
     rankList
19
     has Proposed To List\\
20
     gotProposedByList
     tmpMatchList
21
22
     activeFlag
23 ]
24
25 ;; global variables
26 globals [
27
     csv fileList; fileList named csv
     startSideInt; set in setup-globals from GUI-slider
28
29
     switchingFlag; set in setup-globals from GUI-switch
     debugFlag; set in setup-globals from GUI-switch
30
     user-input-filename;
31
32
     input-filename; set default in setup-globals or from GUI-button
     current_nr_of_pairs
33
     current_nr_of_pairs_percent
34
35
     current_nr_of_rejects
36 ]
37
38 ;; method which is called from the setup button
39 to setup
40
     clear-all
      if debugFlag = true [
41
42
       show "after clear-all"
       show "clear-all"
43
```

```
show count humans]
44
45
      setup-globals
      if debugFlag = true [show "after open-file"
46
47
         show "count humans after open-file"
48
         show count humans]
49
      reset-ticks
50
   end
51
52 to reset
53
      clear-ticks
      clear-turtles
54
55
      clear-patches
      clear-drawing
56
      clear-all-plots
57
      clear-output
58
      if debugFlag = true [show "after clear-all"
59
60
         show "clear-all"
61
         show count humans]
62
      setup-globals
63
      if debugFlag = true [show "after open-file"
64
         show "count humans after open-file"
65
         show count humans]
      reset-ticks
66
67
   end
68
69
70
   ;; stackoverflow.com/questions/27096948/how-to-read-a-csv-filve-with
       -netlogo
71
   to open-file
72
      file -open (word input-filename ".csv")
73
      set fileList []
74
      while [not file-at-end?] [
75
        set csv file-read-line
76
77
        set csv word csv ";" ; add comma for loop termination
78
        let mylist [] ; list of values
79
        let i 0
80
        while [not empty? csv]
81
82
          let $x position ";" csv
83
          if i > 0
84
85
            let $item substring csv 0 $x ; extract item
            carefully [set $item read-from-string $item][]; convert if
86
               number
87
            set mylist lput $item mylist ; append to list
88
          set csv substring csv ($x + 1) length csv ; remove item and
89
```

```
comma
           set i i + 1
90
91
92
        if debugFlag = true [show mylist]
         if item 0 mylist != "id"[
93
94
           create-humans 1 [
95
             set id item 0 mylist
             set name item 1 mylist
96
97
             set maxMatchesInt item 2 mylist
             set sideInt item 3 mylist
98
             let tmpPartnerListString string:split-string item 4 mylist
99
             set partnerList read-from-string (word tmpPartnerListString)
100
101
                   set partnerList string:split-int item 4 mylist "#"
102
             let tmpRankListString string:split-string item 5 mylist "#"
             set rankList read-from-string (word tmpRankListString)
103
104
                   set rankList string:split-int item 5 mylist "#"
105
             set hasProposedToList []
             set gotProposedByList []
106
             set tmpMatchList []
107
108
             set activeFlag true
109
           1
110
        1
111
        set fileList lput mylist fileList
         if debugFlag = true [show "count humans at end of open-file"
112
         show count humans
113
114
         show "fileList at end of open-file"
115
         show fileListl
116
117
      file-close
118 end
119
120
    to setup-globals
      ifelse starter = "Men" [set startSideInt 1] [set startSideInt 2]
121
122
      set debugFlag debug
      set switchingFlag switching
123
      ifelse user-input-filename = 0 [set input-filename "
124
          disco100NotPicky"] [set input-filename user-input-filename]
125
      set current_nr_of_rejects 0
      set current_nr_of_pairs 0
126
127
      set current_nr_of_pairs_percent 0
      let current world width world-width
128
129
130
      open-file; and read initialisation data from csv file
131
      ; define starting position and start color
132
      let number_women count humans with [sideInt = 2]
      let xposHumansStart current_world_width / 2; starting position
133
          for humans
```

```
134
      let i 1
135
      foreach sort humans with [sideInt = startSideInt] [
136
        ask? [
137
           let number_starting count humans with [sideInt = startSideInt]
138
           set shape "person"
139
           set size 1
140
           set heading 0
           ; positioning and color
141
142
           set vcor 4
           ifelse sideInt = 1 [set color blue] [set color red]
143
144
           let xposHumans i / (number_starting + 1) * current_world_width
               xposHumansStart
145
           set xcor xposHumans
146
           set i i + 1
147
        ]
148
      1
149
      set i 1
      foreach sort humans with [sideInt != startSideInt] [
150
151
152
           let number_notstarting count humans with [sideInt !=
              startSideInt]
153
           set shape "person"
154
           set size 1
155
           set heading 0
           ; positioning and color
156
157
           set vcor -4
158
           ifelse sideInt = 1 [set color blue] [set color red]
159
           let xposHumans i / (number_notstarting + 1) *
              current_world_width - xposHumansStart
160
           set xcor xposHumans
161
           set i i + 1
162
        ]
163
      1
164 end
165
166
    to go
       if count humans with [activeFlag = true and (sideInt =
167
          startSideInt or switchingFlag = true)] = 0 [stop]
168
      step
169
    end
170
171
172
173
    to step
174
      if debugFlag = true [show "----- begin of step
          show "count humans at begin of step"
175
176
         show count humans]
```

```
177
      clear-before-match
      foreach sort humans with [activeFlag = true and sideInt =
178
          startSideInt] [ ; start of proposing
179
         ask ? [
180
           if debugFlag = true [show "count humans at begin of ask humans
               with activeFlag=true and sideInt=startSideInt"
             show count humans with [activeFlag = true and sideInt =
181
                startSideInt]
182
             show "myId"
183
             show id
             show "myName"
184
185
             show name
             show "partnerList"
186
187
             show partnerList
             show "hasProposedToList"
188
189
             show hasProposedToList]
190
           let tmpPotentialPartnersList list-difference partnerList
              hasProposedToList; set-difference of partnerList \
              hasProposedToList
191
           if length tmpPotentialPartnersList = 0 [
192
             set activeFlag false; this human has no potential partners
                to propose to
             stop; break
193
194
           if length tmpMatchList >= maxMatchesInt [
195
             set activeFlag false; this human has enough current matches
196
197
             stop
198
           ]
199
           let myPreferredPartner item 0 tmpPotentialPartnersList; most
              preferred partner from tmp...List
200
          propose-to id myPreferredPartner
201
        ]
202
      ]; end of proposing
203
      if debugFlag = true [show "end of proposing"]
204
      foreach sort humans with [length gotProposedByList > 0 and sideInt
           != startSideInt] [
205
         ask ? [
206
           process-proposals id
207
        1
208
      1
      if switchingFlag = true [set startSideInt ((startSideInt + 1) mod
209
210
      if startSideInt = 0 [set startSideInt 2]
        if debugFlag = true [show "switchingFlag"
211
212
         show switchingFlag
213
         show "startSideInt"
214
         show startSideInt]
215
      calc-stats
```

```
216
      tick
217
      if debugFlag = true [show "########### end of step
          ############"<u>]</u>
218 end
219
220
   to calc-stats
221
       set current_nr_of_pairs 0
222
      ask humans with [sideInt = startSideInt] [
223
         if length tmpMatchList = maxMatchesInt [
224
            set current_nr_of_pairs current_nr_of_pairs + 1
225
        1
226
      1
227
     let countedHumans count humans with [sideInt = startSideInt]
228
      ifelse countedHumans = 0 [
229
         set current_nr_of_pairs_percent 0
230
      ] [
        set current_nr_of_pairs_percent current_nr_of_pairs /
231
            countedHumans
232
         set current_nr_of_pairs_percent current_nr_of_pairs_percent *
            100
233
         if current_nr_of_pairs = 0 [set current_nr_of_pairs_percent 0]
234
235
       if debugFlag = true [ show "Current Nr of Pairs"
236
       show current nr of pairs
237
       show "Current Nr of Pairs Percent"
       show current_nr_of_pairs_percent
238
239
     1
240 end
241
242
   to clear-before-match
243
      ask humans [
244
         set gotProposedByList []; delete gotProposedbyList (in
            preparation for next matching-round)
245
246
    end
247
    to propose-to [sender receiver]
248
       if debugFlag = true [show "----- begin of propose-to
249
                     ----"1
      ask humans with [id = sender] [
250
251
         set hasProposedToList lput receiver hasProposedToList
252
         if debugFlag = true [show "hasProposedToList"
253
           show hasProposedToList
           show "receiver"
254
255
           show receiver]
        ask humans with [id = receiver] [
256
257
           set gotProposedByList lput sender gotProposedByList
258
           if debugFlag = true [show "female side"
```

```
259
              show "gotProposedByList"
260
              show gotProposedByList]
261
        ]
262
      1
       if debugFlag = true [show "########### end of propose-to
263
          ##########"]
264
   end
265
266
    to process-proposals [tmpId]
                                          ----- begin of process-
267
       if debugFlag = true [show "----
          proposals -----
          show "count humans at begin of process-proposals"
268
269
          show count humans]
270
      ask humans with [id = tmpId] [
271
         if debugFlag = true [show "gotProposedByList"
272
           show gotProposedByList
273
           show "sideInt"
274
           show sideInt
           show "maxMatchesInt"
275
276
           show maxMatchesInt]
277
         let tmpPotentialCoupleList []
278
         ifelse length tmpMatchList = 0 [
           set tmpPotentialCoupleList gotProposedByList
279
280
281
         set tmpPotentialCoupleList list-union-set tmpMatchList
            gotProposedByList
282
         ]
283
         if debugFlag = true [show "tmpPotentialCoupleList"
284
            show tmpPotentialCoupleList]
285
         let tmpRejectList []
286
         let tmpCoupleList []
         ifelse length tmpPotentialCoupleList > maxMatchesInt [
287
288
           set tmpCoupleList list-order tmpPotentialCoupleList rankList
              partnerList maxMatchesInt
289
           if debugFlag = true [show "has more proposals than willing to
              accept"
290
              show "tmpCoupleList"
291
              show tmpCoupleList]
           set tmpRejectList list-difference tmpPotentialCoupleList
292
              tmpCoupleList
293
         ] [
294
         set tmpCoupleList tmpPotentialCoupleList
295
296
         if length tmpRejectList > 0 [
297
           reject-proposals id tmpRejectList
298
        1
299
         if length tmpCoupleList > 0 [
           create-tmpCouples id tmpCoupleList
300
```

```
301
        1
302
303
      if debugFlag = true [show "########### end of process-
         proposals ###########"]
304
   end
305
306
   to reject-proposals [tmpId rejectList]
      if debugFlag = true [show "----- begin of reject-
307
         proposals ----"
308
      let rejecter 0
309
      ask humans with [id = tmpId] [
310
        set rejecter self
        set tmpMatchList list-difference tmpMatchList rejectList
311
312
        if debugFlag = true [show "tmpMatchList"
           show tmpMatchList]
313
314
        foreach rejectList [
315
          ask humans with [id = ?] [
            set tmpMatchList list-difference tmpMatchList lput tmpId []
316
317
            set activeFlag true
            ifelse sideInt = 1 [set color blue] [set color red]
318
319
            set current_nr_of_rejects current_nr_of_rejects + 1
            remove-link self rejecter
320
321
          1
322
          ifelse sideInt = 1 [set color blue] [set color red]
323
        1
324
325
      if debugFlag = true [show "############ end of reject-proposals
          #########"]
326
   end
327
328
   to create-tmpCouples [tmpId acceptList]
      if debugFlag = true [show "----- begin of create-
329
         ask humans with [id = tmpId] [
330
331
        set tmpMatchList acceptList
        if debugFlag = true [show "tmpMatchList"
332
333
           show tmpMatchList]
        foreach acceptList [
334
335
          ask humans with [id = ?] [
            set tmpMatchList list -union-set tmpMatchList lput tmpId []
336
337
            set color green
            create-link-with myself
338
339
          ]
340
          set color green
341
        ]
342
343
      if debugFlag = true [show "############ end of create-
         tmpCouples ###########"]
```

```
344 end
345
346
347
    to-report list-order [listToOrder ranking partners maxMatches]
                                     ----- begin of list-order
       if debugFlag = true [show "----
348
      set listToOrder list-overlap listToOrder partners
349
350
      if debugFlag = true [show "listToOrder"
351
          show listToOrder]
352
      if length listToOrder > maxMatches [
         let tmpRanking get-rating-of-list partnerList listToOrder
353
            ranking
354
         let tmpList listToOrder
         if debugFlag = true [show "tmpRanking"
355
356
           show tmpRanking
357
           show "tmpList"
           show tmpList]
358
359
         set listToOrder []
        let i 0
360
        loop [
361
362
           if i >= maxMatches [report listToOrder]
363
           let j position (max tmpRanking) tmpRanking
           if debugFlag = true [show "j"
364
365
              show j
              show "item j tmpList"
366
              show item j tmpList
367
              show "tmpList"
368
369
              show tmpList]
370
           set listToOrder lput item j tmpList listToOrder
371
           set tmpRanking remove-item j tmpRanking
372
           set tmpList remove-item j tmpList
           if debugFlag = true [show "listToOrder"
373
374
              show listToOrder
              show "tmpList"
375
376
              show tmpList]
           set i i + 1
377
378
        1
379
380
      report listToOrder
381
382
       if debugFlag = true [show "############ end of list-order
          #########"]
383 end
384
385
    ;; symmetrical difference: fullList \ toRemoveList
    to-report list-difference [fullList toRemoveList]
386
387
      report filter [not member? ? toRemoveList] fullList
388
   end
```

```
389
390 ;; intersection of listA and listB
391
   to-report list-overlap [listA listB]
      if debugFlag = true [show "########### begin of list-overlap
392
         ##########"
393
        show listA
        show listB
394
395
        show filter [member? ? listB] listA]
396
      if debugFlag = true [show "########### end of list-overlap
         ##########"]
397
      report filter [member? ? listB] listA
398 end
399
400 ;; union of listA and listB
401 to-report list-union-set [listA listB]
      let tmpList list-difference listB listA
402
403
      foreach tmpList [ set listA lput ? listA]
404
      report listA
405 end
406
407
408 ;; gets ranking associated with fullList for partialList
409 to-report get-rating-of-list [fullList partialList ranking]
410
      let tmpList []
      foreach partialList [
411
        set tmpList lput item (position ? fullList) ranking tmpList
412
413
414
      report tmpList
415 end
416
417
418
420 ;;; Input filename ;;;
421
    422
423 to change-input
424
      set user-input-filename user-input "Type input filename (without
         extension)."
425
      if debugFlag = true [show "user-input-filename"
426
         show user-input-filename]
427 end
428
429
430
431
433 ;;; Output matches
```

```
434
    435
436
437 ;; write-to-file taken from
    ;; Wilensky, U. (1999). NetLogo. http://ccl.northwestern.edu/netlogo
439
   ;; Center for Connected Learning and Computer-Based Modeling,
       Northwestern University, Evanston, IL
   ;; code from File/Models Library/Code Examples/File Output Example
440
441
    to export-to-csv
442
      let output-filename (word input-filename "_Starter_" starter "
443
          Switch " switching " Ticks " ticks ".csv")
444
      foreach sort humans [
445
        ask? [
446
          let delimPartnerList list-concat-with-delim partnerList "#"
447
          let delimRankList list-concat-with-delim rankList "#"
448
          let delimHasProposedToList list-concat-with-delim
              hasProposedToList "#"
          let delimGotProposedByList list-concat-with-delim
449
              gotProposedByList "#"
450
          let delimTmpMatchList list-concat-with-delim tmpMatchList "#"
          write-csv output-filename (list (id) (name) (maxMatchesInt) (
451
              sideInt) (delimPartnerList) (delimRankList) (
              delimHasProposedToList) (delimGotProposedByList) (
              delimTmpMatchList) (activeFlag))
452
        ]
453
454
    end
455
456
457
    ;; http://stackoverflow.com/questions/22462168/netlogo-export-
        tableau-issues
    to write-csv [ #filename #items ]
458
459
      ;; #items is a list of the data (or headers!) to write.
      if is-list? #items and not empty? #items
460
461
      [ file -open #filename
462
        ;; quote non-numeric items
463
        set #items map quote #items
        ;; print the items
464
        ;; if only one item, print it.
465
        ifelse length #items = 1 [ file-print first #items ]
466
        [file-print reduce [ (word ?1 ";" ?2) ] #items]
467
468
        ;; close-up
469
        file-close
470
471
    end
472
```

```
473 to remove—link [human1 human2]
474
      ask links with [(end1 = human1 and end2 = human2) or (end1 =
         human2 and end2 = human1) ] [
475
        diel
476 end
477 ;; http://stackoverflow.com/questions/22462168/netlogo-export-
        tableau-issues
478 to-report quote [ #thing ]
479
      ifelse is-number? #thing
      [ report #thing ]
480
      [ report (word "\"" #thing "\"") ]
481
482 end
483
484 ;; https://groups.yahoo.com/neo/groups/netlogo-users/conversations/
        topics/6490
485 ;; intersperse listA with delim
486 to-report list-concat-with-delim [listA delim]
487
      if length listA > 0 [report reduce [(word ?1 delim ?2)] listA]
488
      report ""
489 end
```

List of Figures

3.1	The control section for the disco example	11
3.2	The information section for the disco example	12
3.3	Simulation 1, step 1	14
3.4	Simulation 1, step 3	14
3.5	Simulation 1, step 9	15
3.6	Simulation 1, step 27	15
3.7	Simulation 2, step 1	16
3.8	Simulation 2, step 3	16
3.9	Simulation 2, step 9	17
3.10	Simulation 2, step 127	17
3.11	Simulation 3, step 1	18
3.12	Simulation 3, step 118	18

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