

Abstract argumentation frameworks - overview and illustration

Patrick Bellositz

1 Introduction

2 Definitions

To work with argumentation frameworks, first we must define their properties. This section will lay out the basic structure of argumentation frameworks as well as provide extension types for further analysis.

Definition 1. An *argumentation framework* F is a pair (A, R) , where A is a set of arguments and R is a set of attack relations.

Definition 2. *Attack relations* $R \subseteq A \times A$ represent attacks. The pair (a, b) , where $a, b \in A$ means a attacks b .

Example 1. Imagine we have 3 arguments a_1 , a_2 , and b .

a_1	= "Blue is the most beautiful of all colors."
b	= "No, black is much more beautiful!"
a_2	= "That's wrong, black isn't even a color."

These arguments obviously contain 2 attacks. Argument b attacks argument a_1 and in turn argument a_2 attacks argument b .

This results in the framework $F = (A, R)$, where $A = \{a_1, a_2, b\}$ and $R = \{(b, a_1), (a_2, b)\}$.

As writing an argument framework in sets might become hard to read with increasing set sizes, it is also possible to write every framework as a graph (V, E) , where $V = A$ and $E = R$. The graph in our example looks like this:

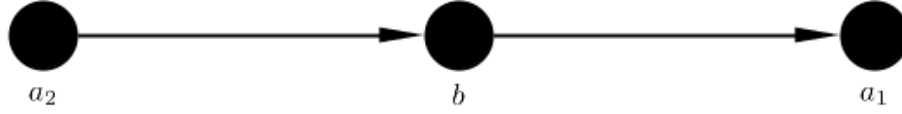


Figure 1: An argument framework about colors.

Remark 1. Let S be a set of arguments. If $a \in S$ and there is an attack $(a, b) \in R$ we say S *attacks* b .

Definition 3. Let S be a set of arguments. It is *conflict-free*, if $\forall a \forall b$ $a, b \in S, (a, b) \notin R$.

Example 2. (Continuation of Example 1) As no argument attacks itself, $\{a_1\}$, $\{a_2\}$ and $\{b\}$ each are conflict-free. $\{a_1, a_2\}$ is also a conflict-free set, since there exists no attack relation containing a_1 and a_2 . The empty set is always conflict-free.

Since there is an attack relation between b and each of the other arguments, there are no other conflict-free sets.

Thus the set of conflict-free sets is $cf(F) = \{\emptyset, \{a_1\}, \{a_2\}, \{b\}, \{a_1, a_2\}\}$.

Definition 4. An argument a is *defended* by a set S , if for every attack $(b, a) \in R$ there is an attack (c, b) , where $c \in S$. If this is the case S *defends* a .

Definition 5. Let S be a conflict-free set. It is called an *admissible extension* if it defends each $a \in S$.

Example 3. (Continuation of Example 2) Of the conflict-free sets only $\{a_2\}$ and \emptyset don't get attacked. They are admissible. $\{a_1, a_2\}$ gets attacked via the attack relation (b, a_1) , but a_1 gets defended through (a_2, b) , making it also admissible. $\{b\}$ and $\{a_1\}$ are not admissible since they don't defend their arguments.

Thus the set of admissible extensions is $adm(F) = \{\emptyset, \{a_1, a_2\}, \{a_2\}\}$.

Definition 6. Let S be an admissible extension. It is called a *preferred extension* if for each $S' \subseteq A$, that is an admissible extension, $S \not\subseteq S'$.

Example 4. (Continuation of Example 3) Since $\emptyset \subset \{a_2\}$, \emptyset is not a preferred extension. $\{a_2\} \subset \{a_1, a_2\}$, therefore $\{a_2\}$ is not a preferred extension. Since all other admissible extensions are proper subsets of $\{a_1, a_2\}$, it is a preferred extension.

Thus the set of preferred extensions is $prf(F) = \{\{a_1, a_2\}\}$.

Definition 7. Let S be a conflict-free set. It is called a *stable extension* if for each $a \notin S$ there exists an attack $(b, a) \in R$ where $b \in S$.

Example 5. (Continuation of Example 2) The conflict-free sets \emptyset and $\{a_1\}$ don't attack any of the other arguments, $\{a_2\}$ only attacks $\{b\}$, missing an attack on $\{a_1\}$. $\{b\}$ misses an attack on $\{a_2\}$. They are not stable extensions. $\{a_1, a_2\}$ attacks all other arguments in $\{b\}$ (attack relation (a_2, b)) and therefore is a stable extension.

Thus the set of stable extensions is $st(F) = \{\{a_1, a_2\}\}$.

Definition 8. Let S be an admissible extension. It is called a *complete extension* if for each $a \notin S$, $S \cup \{a\}$ is not an admissible extension.

Example 6. (Continuation of Example 3) The admissible extension \emptyset is not a complete extension because it defends a_2 which it doesn't contain. $\{a_2\}$ defends a_1 and is therefore also not a complete extension. $\{a_1, a_2\}$ attacks b and as there are no other arguments which could be defended it is a complete extension.

Thus the set of complete extensions is $co(F) = \{\{a_1, a_2\}\}$.

Definition 9. The (unique) *grounded extension* is defined by $\bigcap_{i=1}^n S_i$, where $\{S_1, \dots, S_n\}$ is the set of all complete extensions.

Example 7. (Continuation of Example 6) Since there is only one complete extension $\{a_1, a_2\}$, it also is the grounded extension $gr(F)$.

3 Observations

As we have seen in the previous section, often there may be overlaps between the different extension types beyond what their definitions explicitly state. In this section we will discuss those relations between extension types.

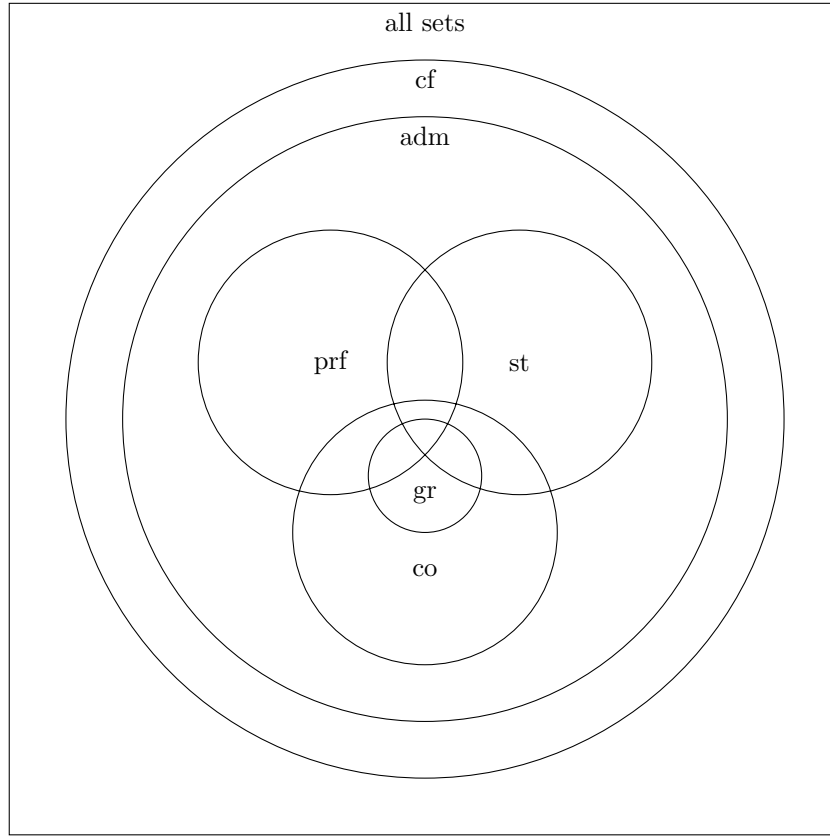


Figure 2: Relations between extension types

4 Application

4.1 Introduction

In this section the usage and implementation details of the aforementioned program illustrating the computation of the different extension types is provided.

4.2 Creation of a framework

On starting the application the user is presented with an input mask. It consists of ten rows, each representing an argument and a button labeled "show graph".

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use?	argument description:	attacks:
<input checked="" type="checkbox"/> A	<input type="text"/>	b <input type="text"/>
<input checked="" type="checkbox"/> B	<input type="text"/>	c <input type="text"/>
<input checked="" type="checkbox"/> C	<input type="text"/>	a <input type="text"/>
<input checked="" type="checkbox"/> D	<input type="text"/>	b <input type="text"/>
<input type="checkbox"/> E	<input type="text"/>	<input type="text"/>
<input type="checkbox"/> F	<input type="text"/>	<input type="text"/>
<input type="checkbox"/> G	<input type="text"/>	<input type="text"/>
<input type="checkbox"/> H	<input type="text"/>	<input type="text"/>
<input type="checkbox"/> I	<input type="text"/>	<input type="text"/>
<input type="checkbox"/> J	<input type="text"/>	<input type="text"/>

Figure 3: Input mask

4.3 Argumentation graph

Once a framework is created and "show graph" was clicked a graphical representation of it is shown alongside buttons to compute extensions and an area dedicated to showing computation results.

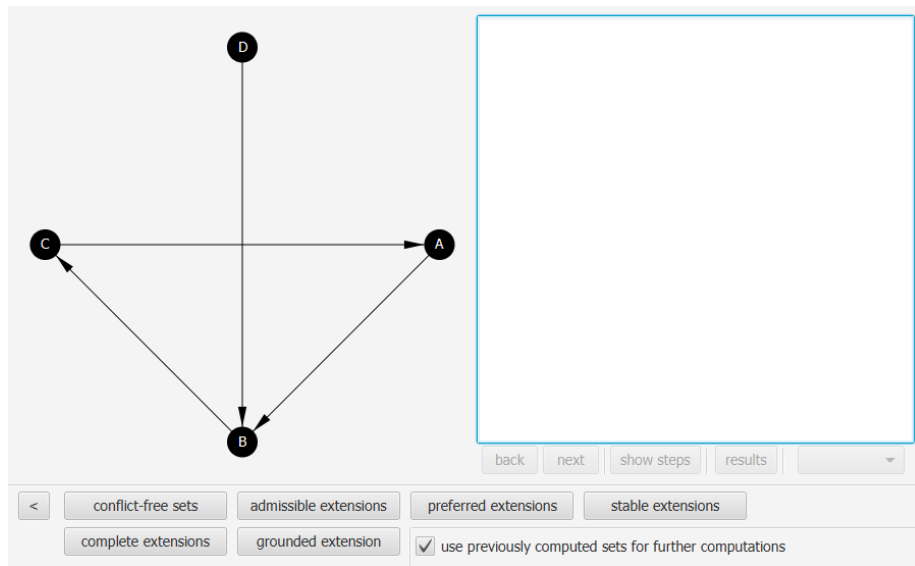


Figure 4: Demonstration view

4.4 stuff comes here