



# Optimal Control of Lithium-ion Battery Energy Storage Systems

Scott J. Moura

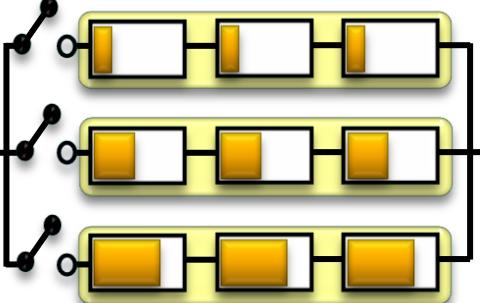
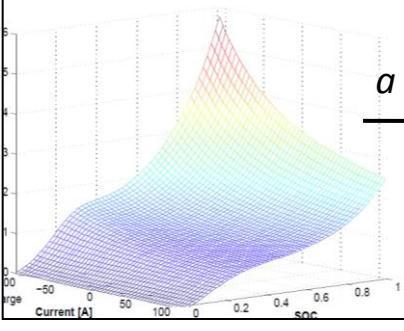
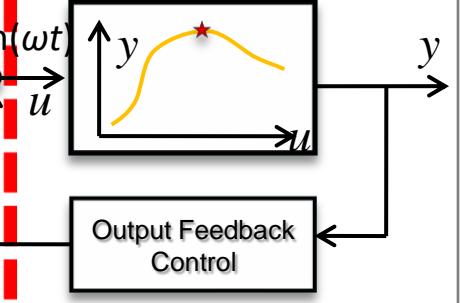
Automated Modeling and Control Optimization Labs  
Department of Mechanical Engineering  
University of Michigan, Ann Arbor, USA

A Seminar Presentation at:

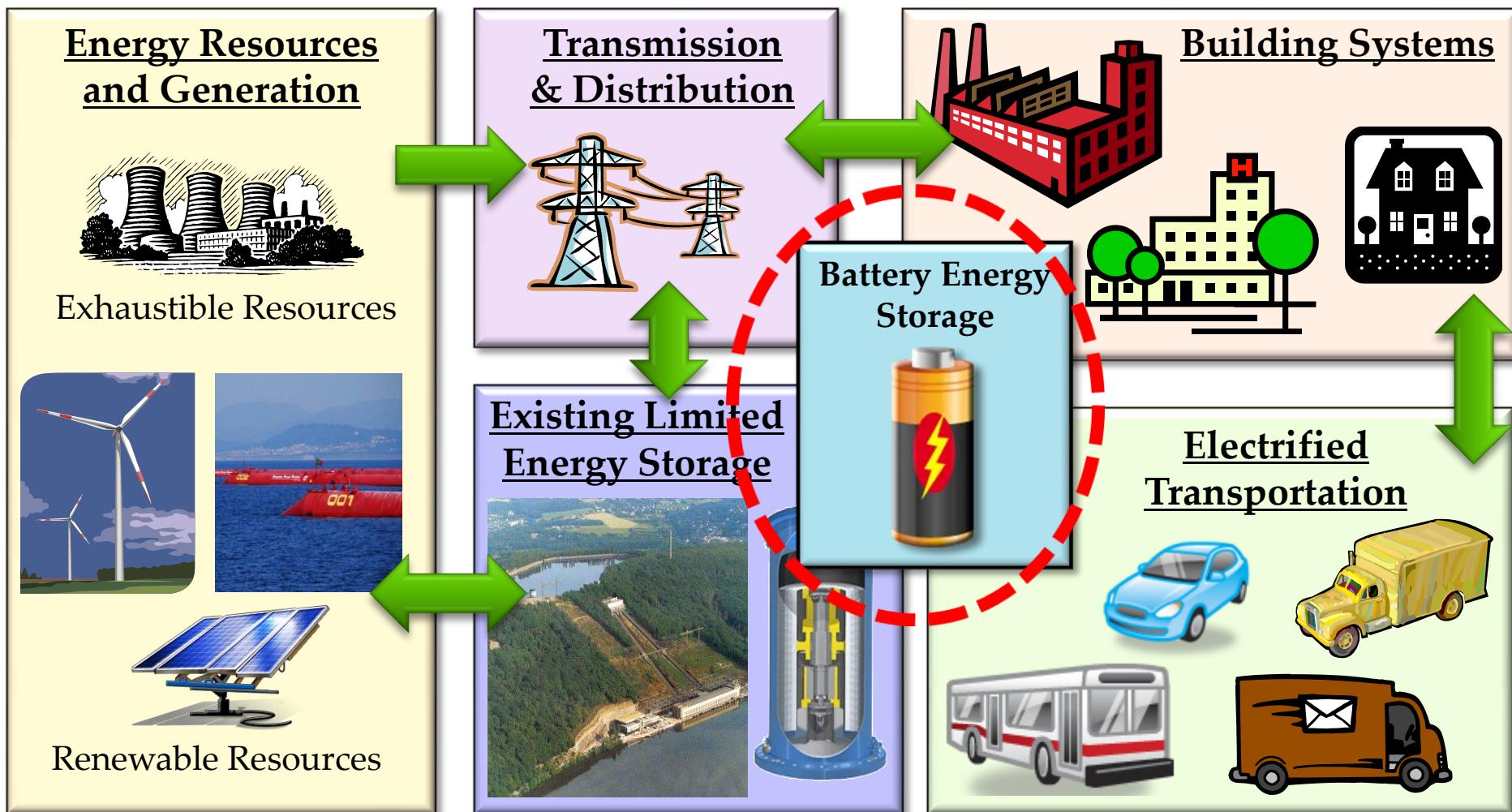


**Ford Motor Company**  
**Friday December 3, 2010**

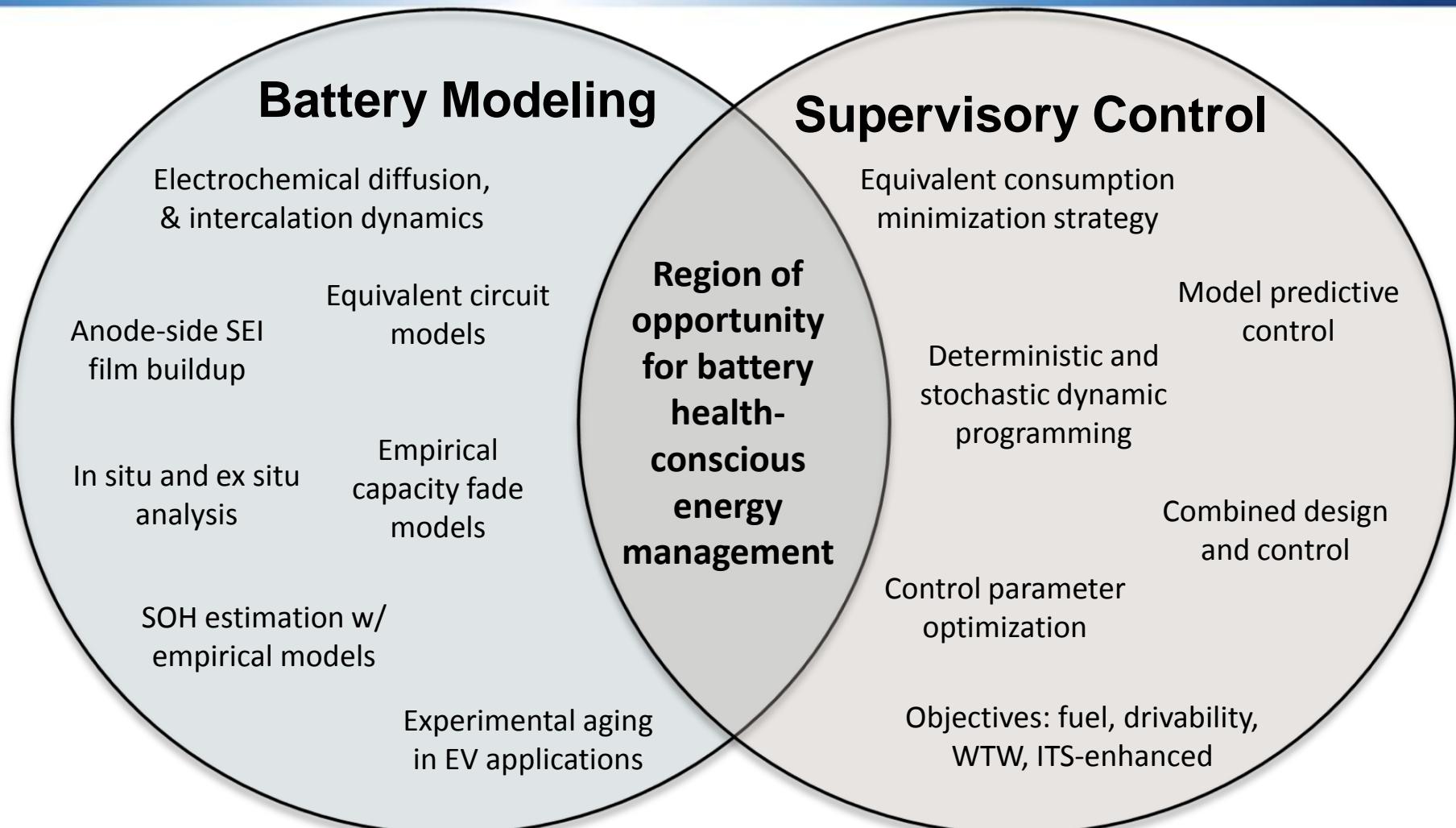
# Overview of Research Contributions

| <u>APPLICATION</u>                    | Li-ion Batteries  | Power Management   | Photovoltaic and Fuel Cells   |
|---------------------------------------|---|--|---|
| <u>THEORY</u>                         |   |  |   |
| Theoretical Modeling & Identification |  A photograph of a green printed circuit board (PCB) labeled "Battery Sensor Board v2.0 : University of Michigan". It has various electronic components, wires, and a white label in the center that reads "+ Param ID - 3.1". |  A photograph of a silver Toyota Prius hybrid car parked and connected to a white charging station via a power cord.   |  A photograph of a large array of dark blue solar panels mounted on a metal frame, likely for a photovoltaic system.   |
| Optimal Control & Estimation          |  A schematic diagram showing three parallel battery cells connected in series. Each cell is represented by a yellow rectangle with two white circles at its ends, representing the positive and negative terminals.           |  A 3D surface plot showing a performance metric (e.g., energy density or efficiency) as a function of Current [A] (x-axis, -50 to 100) and State of Charge (SOC) (y-axis, 0 to 1). The surface shows a complex, multi-peaked structure. |  A block diagram of a control system. It starts with a signal $u = a \sin(\omega t)$ entering a block labeled "Output Feedback Control". The output of this block is $y$ , which is fed back through a feedback line to the input $u$ . |

# Vision of Future Energy Infrastructure



# Literature Review



# Key Research Topics

## Electrochemical Battery Modeling

- Mathematical modeling based on first principles
- Experimental identification

## Advanced Battery Pack Management

- The charge un-equalization concept
- Modeling, optimal control, and analysis

## PHEV Power Management

- PHEV powertrain and daily drive cycle modeling
- Stochastic optimal control
- Tradeoff analysis

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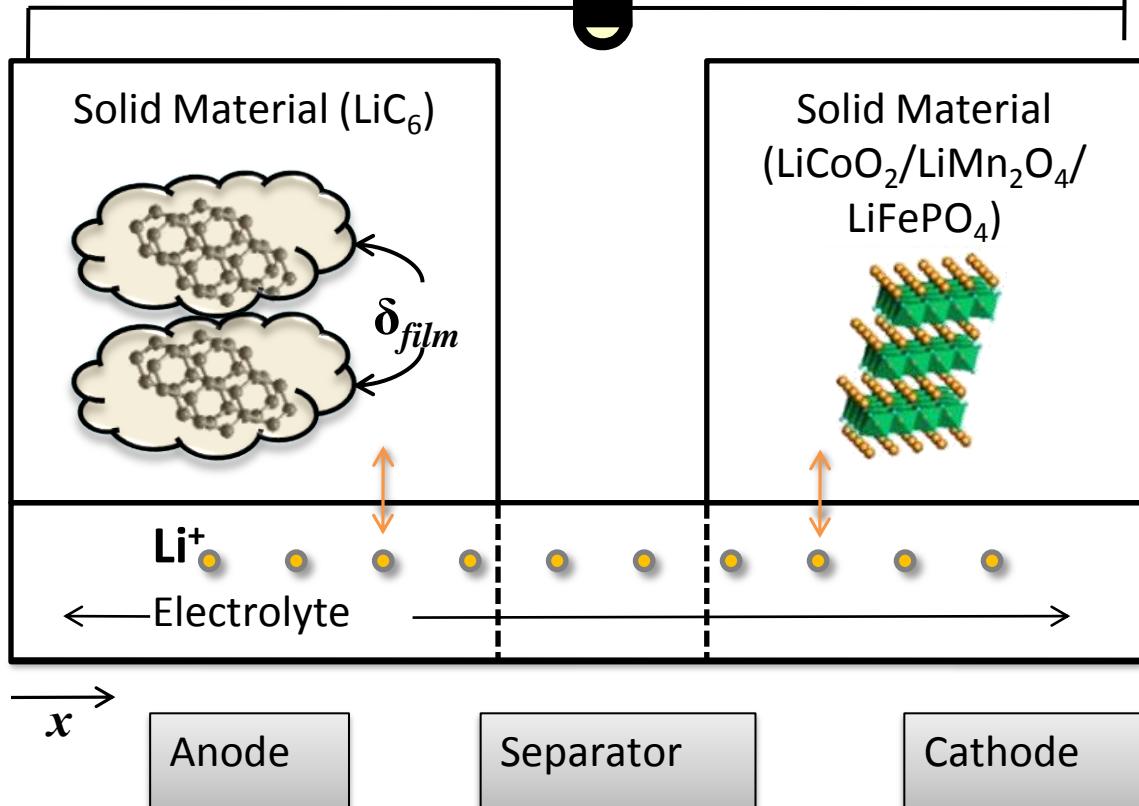
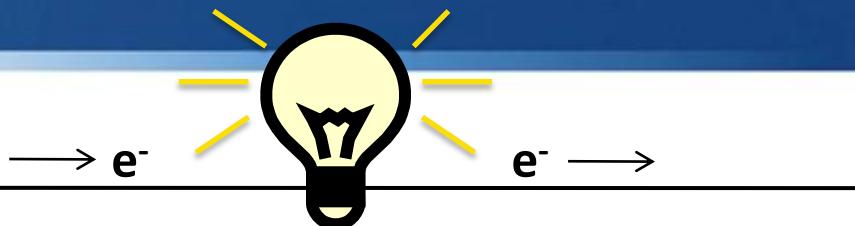
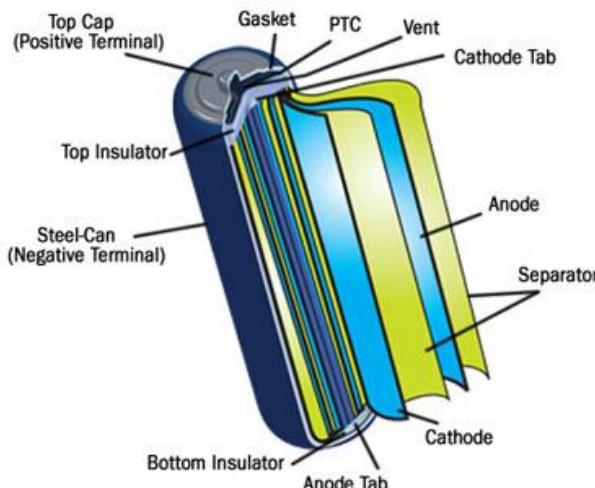
## PHEV Power Management

- PHEV powertrain and daily drive cycle modeling
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- Tradeoff analysis

# Electrochemical Li-ion Battery Modeling

## Doyle-Fuller-Newman (DFN) Model

Cylindrical lithium-ion battery



Diffusion, reaction, intercalation: Doyle, Fuller, Newman, 1993 and 1994  
Anode-side SEI film buildup model: Ramadass *et al.*, 2004

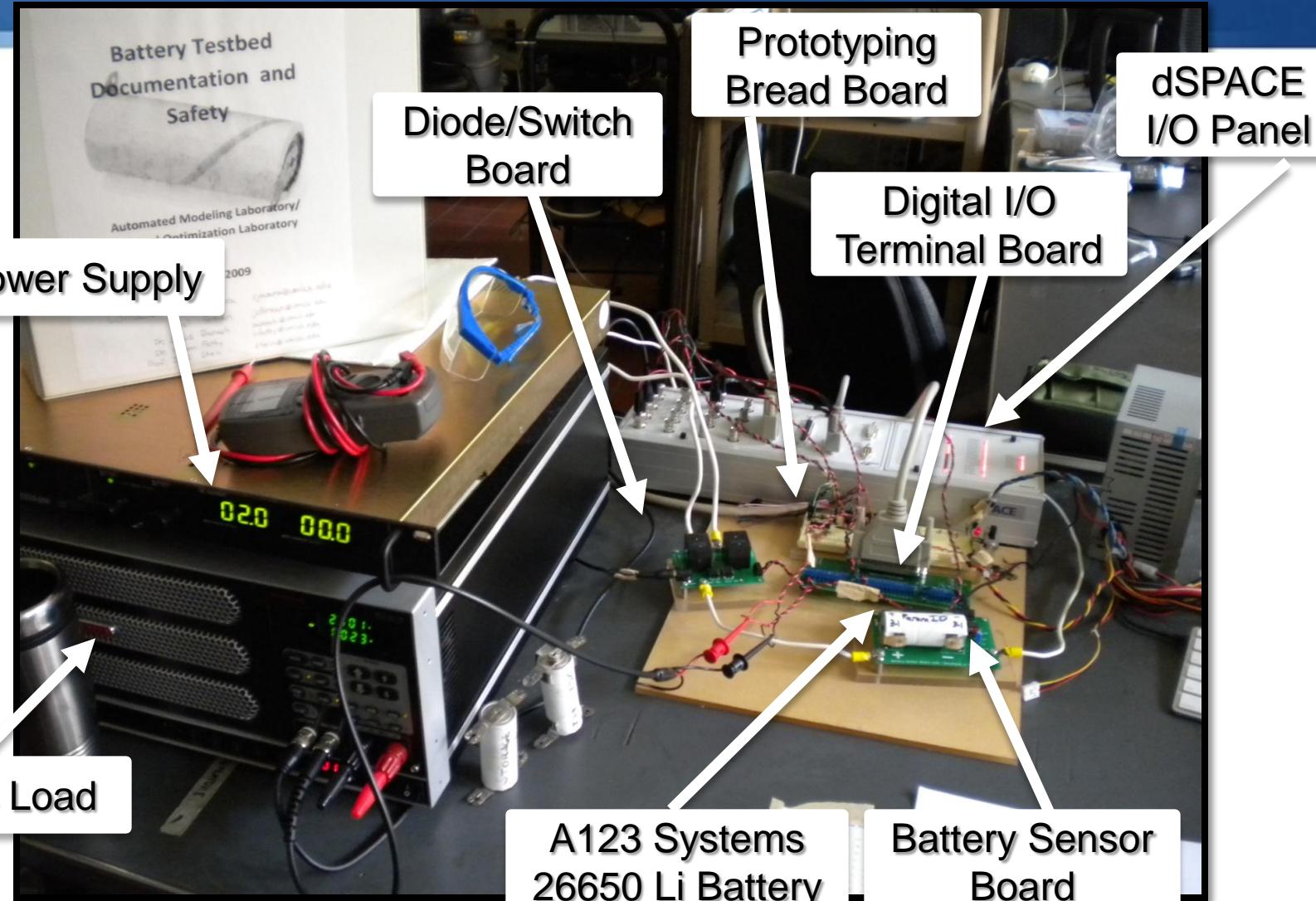
# Electrochemical Battery Model Eqns

A partial differential algebraic equation system (PDAE)

$$\left\{ \begin{array}{ll} \frac{\partial c_{1,j}(r,t)}{\partial t} = \frac{D_{1,j}}{r^2} \frac{\partial}{\partial r} \left( r^2 \frac{\partial c_{1,j}}{\partial r} \right) & \text{Spherical diffusion} \\ \varepsilon_{2,j} \frac{\partial c_{2,j}(x,t)}{\partial t} = \nabla \cdot \left( D_2^{eff} \nabla c_{2,j} \right) + \frac{1-t^+}{F} J_j & \text{Linear diffusion} \\ \frac{\partial \delta_{film}(x,t)}{\partial t} = - \frac{M_P}{a_n \rho_P F} J_{sd} & \text{Resistive film growth} \\ 0 = \nabla \cdot \left( \sigma_j^{eff} \nabla \phi_{1,j}(x,t) \right) - J_j & \text{Ohm's Law} \\ 0 = \nabla \cdot \left( \kappa^{eff} \nabla \phi_{2,j}(x,t) \right) + \nabla \cdot \left( \kappa \nabla \ln c_{2,j} \right) - J_j & \\ 0 = a_j i_{0,j} \sinh \left[ \frac{\alpha_{a,j} F}{RT} \left( \phi_{1,j} - \phi_{2,j} - U_{ref,j} - \frac{J_j}{a_n} R_{film} \right) \right] - J_j(x,t) & \text{Butler-Volmer} \\ 0 = -i_{0,SD} a_n \exp \left[ - \frac{\alpha_n F}{RT} \left( \phi_{1,j} - \phi_{2,j} - U_{ref,SD} - \frac{J_j}{a_n} \cdot R_{film} \right) \right] - J_{sd}(x,t) & \text{Kinetics} \end{array} \right.$$



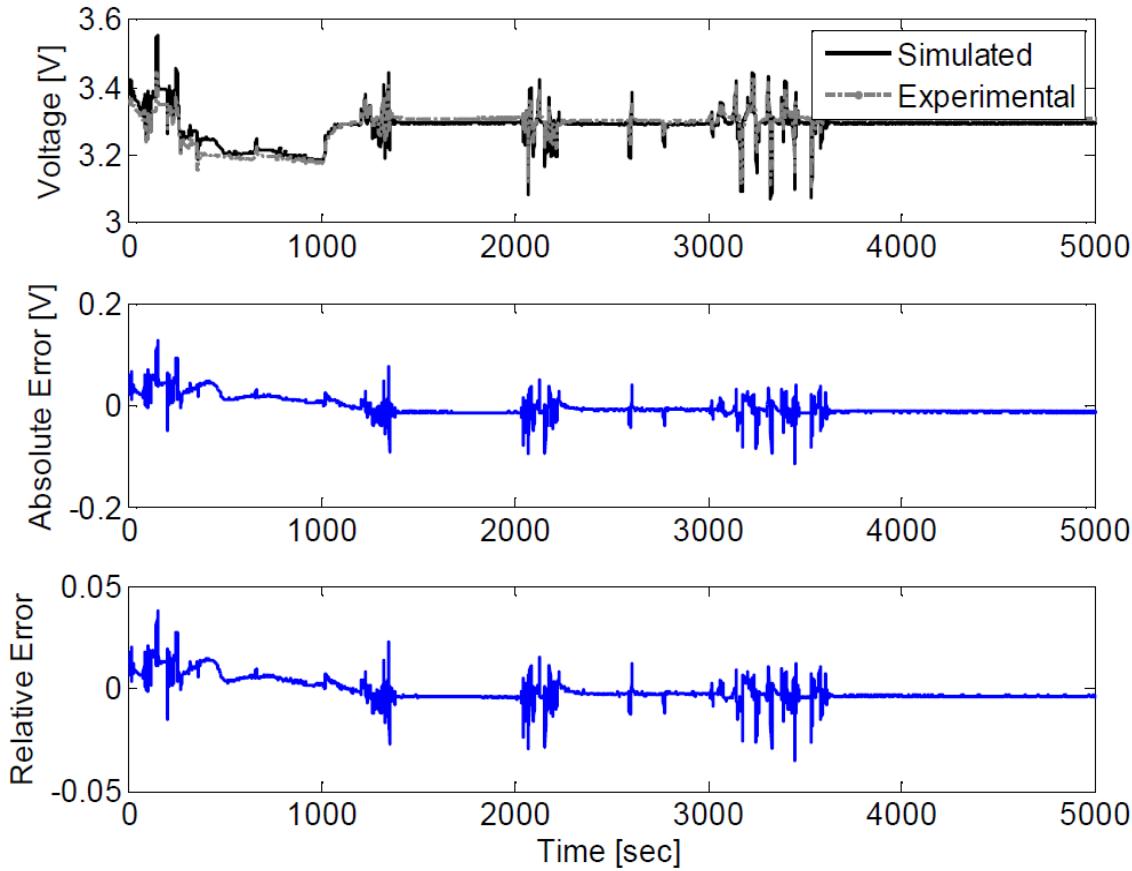
# Battery-in-the-loop Hardware



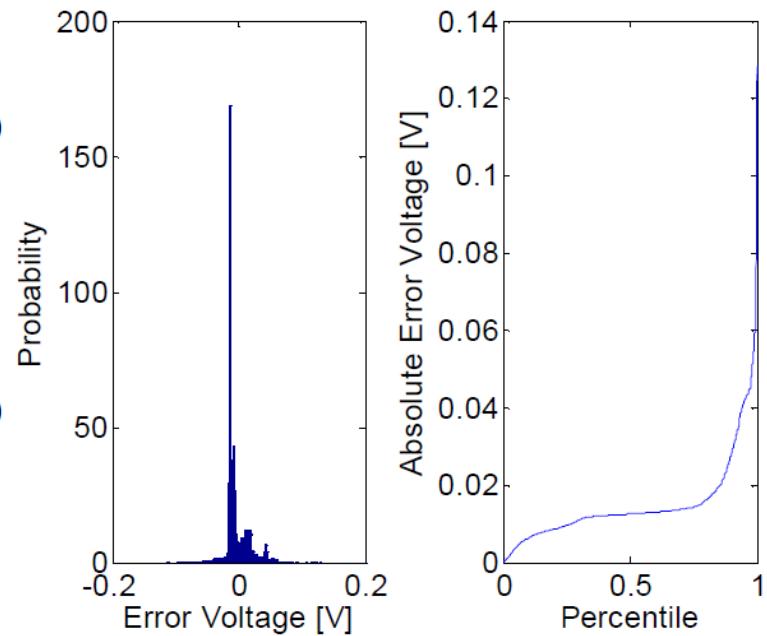
# Parameter Identification Results

collaborative effort with Joel Forman, Ph.D. Candidate @ U-M

## Time Responses of Experimental Validation Data vs. Identified Model for Naturalistic Drive Cycle



## Statistical Analysis of Voltage Error



## Publications

- J. C. Forman, S. J. Moura, J. L. Stein, H. K. Fathy "Parameter Identification of the Doyle-Fuller-Newman Model Based on Experimental Cycling of a Li-ion LiFePO<sub>4</sub> Battery Using a Genetic Algorithm," Submitted to 2011 American Control Conference, San Francisco, CA, 2011.

# Causes of Battery Degradation

## Causes of Battery Degradation

- Particle fracture
- Phase changes
- Active material consumption
- Solid electrolyte film (SEI) growth
- ...

## System-Level Relations to Aging

- SOC level
- Charge/discharge rates
- Temperature
- Time or cycles

| The Cup Analogy                | New | Aged |
|--------------------------------|-----|------|
| Particle Fracture              |     |      |
| Phase Changes                  |     |      |
| Consumption of Active material |     |      |
| SEI film growth                |     |      |

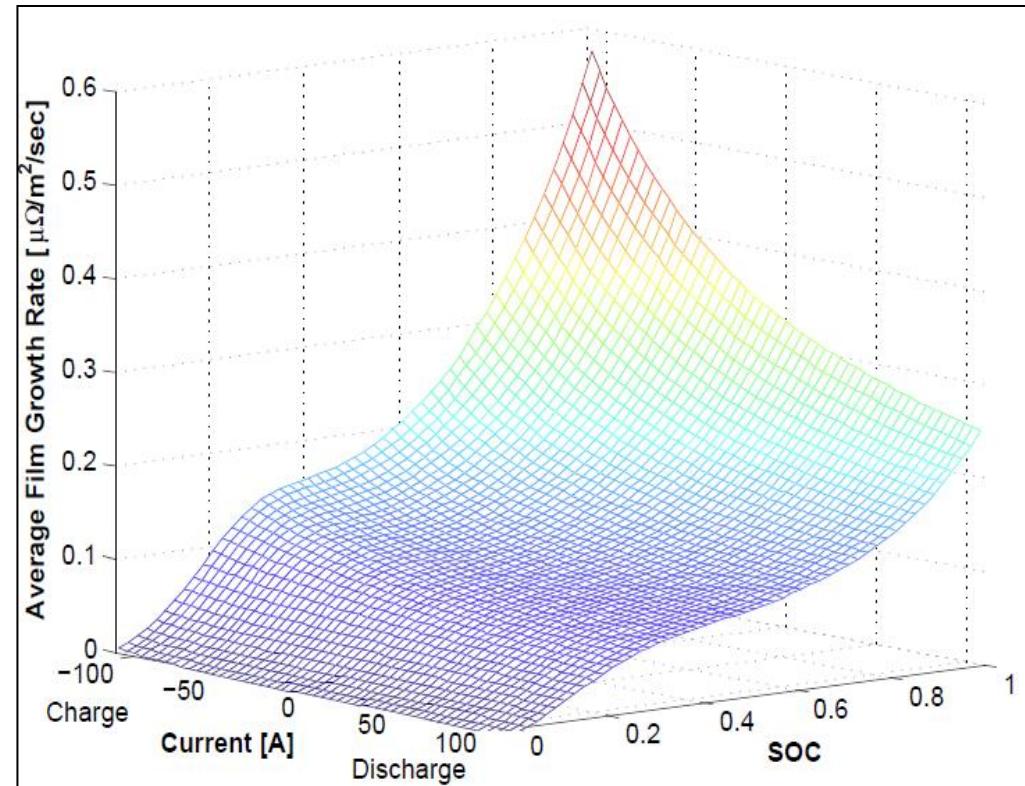
# Anode-Side SEI Film Buildup

Ramadass et al, 2004



$$R_{film}(x,t) = R_{SEI} + \frac{\delta_{film}(x,t)}{K_P}$$

$$\frac{\partial \delta_{film}(x,t)}{\partial t} = -\frac{M_P}{a_n \rho_P F} J_{sd}$$



# Key Research Topics

## Electrochemical Battery Modeling

- Mathematical modeling based on first principles
- Experimental identification

## Advanced Battery Pack Management

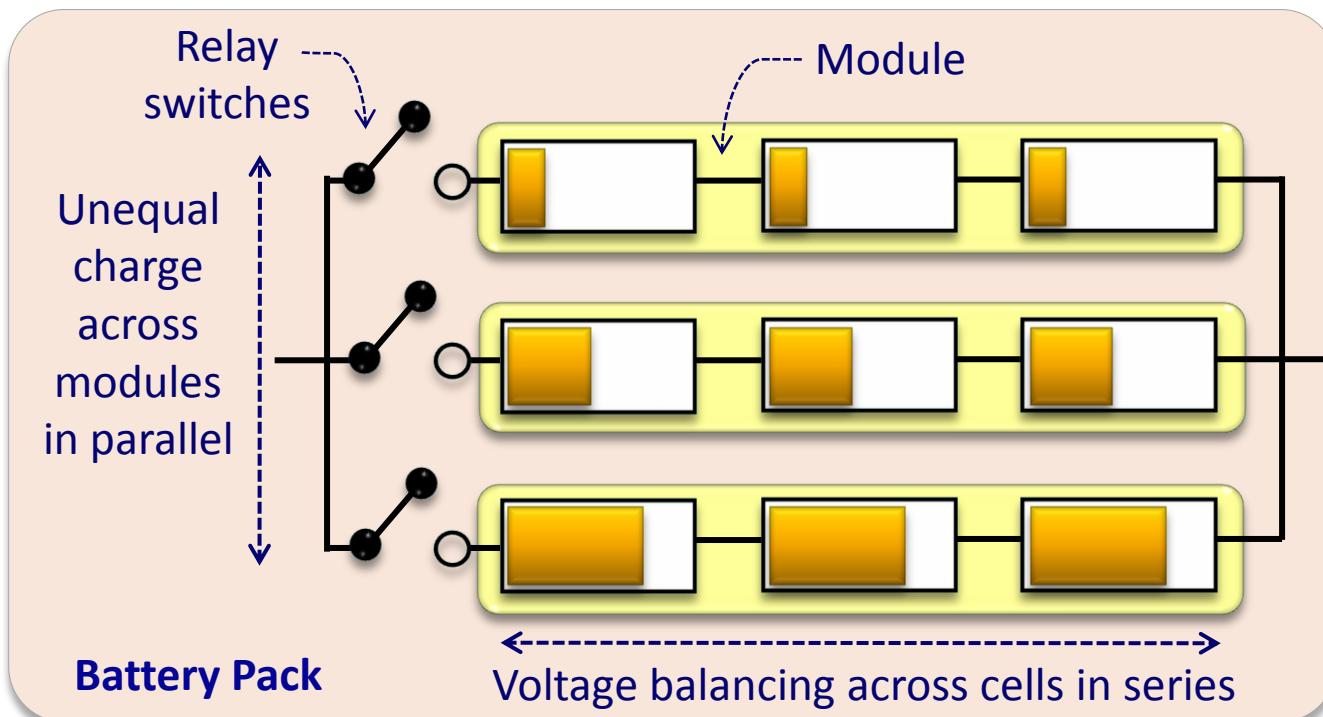
- The charge un-equalization concept
- Modeling, optimal control, and analysis

## PHEV Power Management

- PHEV powertrain and daily drive cycle modeling
- Stochastic optimal control
- Tradeoff analysis

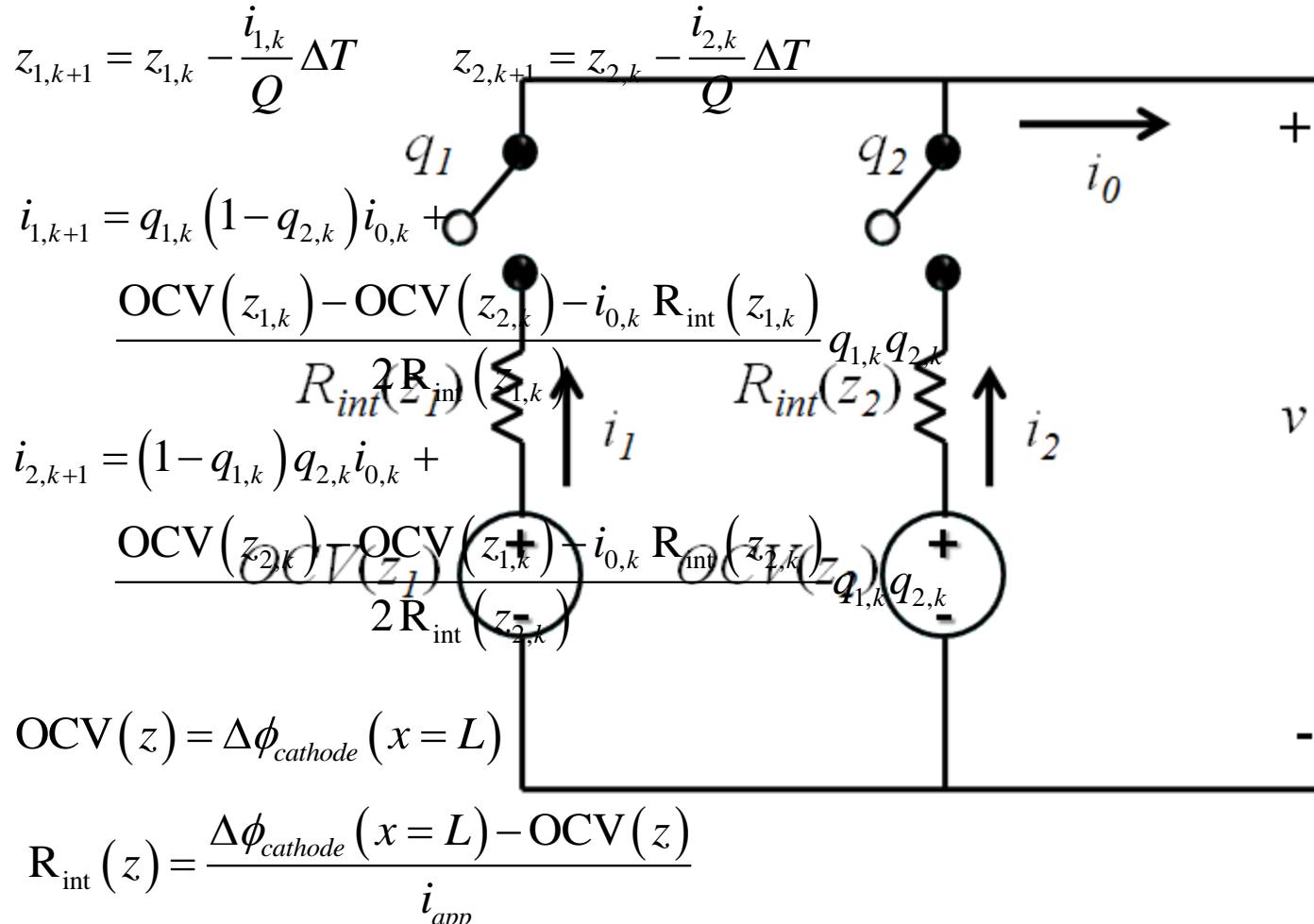
# Unbalanced Charge Management

Objective: Explore unequal but controlled charge levels in battery packs for enhancing health



Theoretical Approach: Optimal control and reduced order models

# Battery Pack Model



# Problem Formulation

Minimize total spatially-averaged film growth over the charge cycle

$$\min_{q_1, q_2} J = \sum_{k=1}^N \left[ \dot{\delta}_{film}(z_{1,k}, i_{1,k}) + \dot{\delta}_{film}(z_{2,k}, i_{2,k}) + g_z(z_k) \right] + \alpha_N \|z_N - 0.95\|_2^2$$

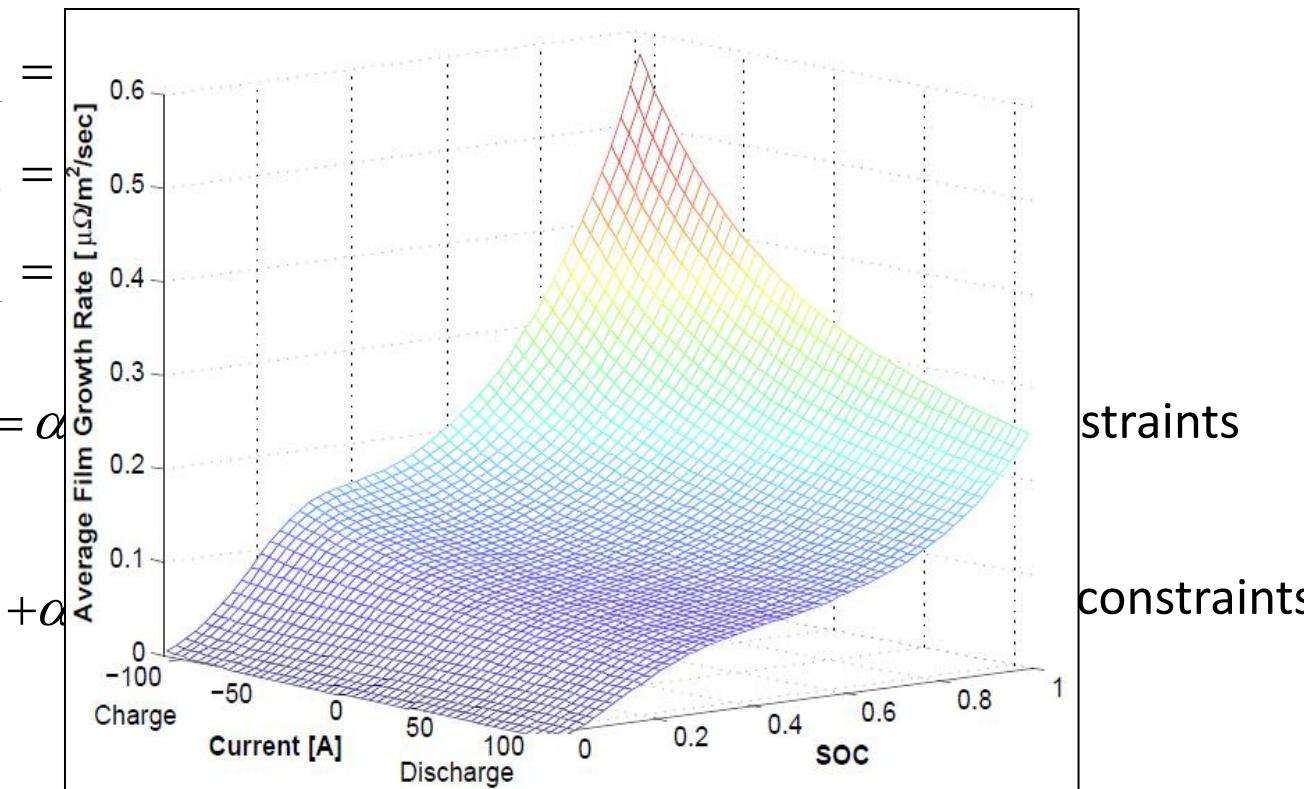
subject to

$$z_{k+1} =$$

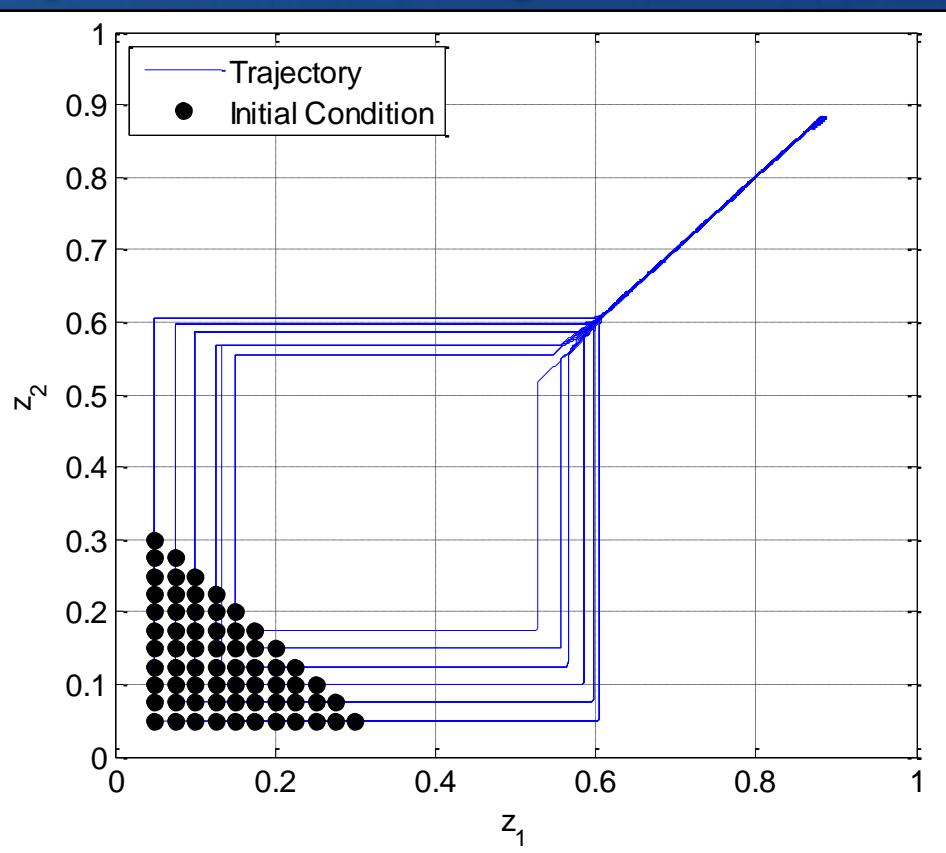
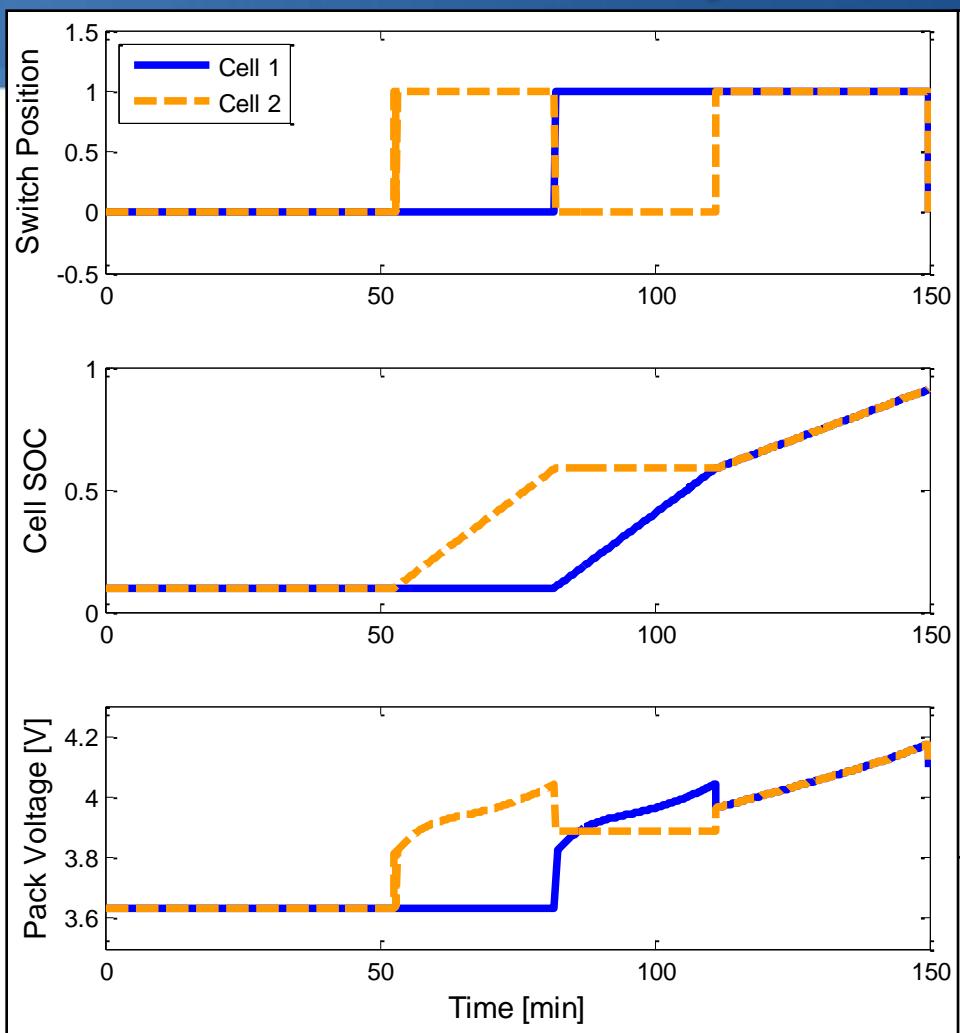
$$i_k =$$

$$z_1 =$$

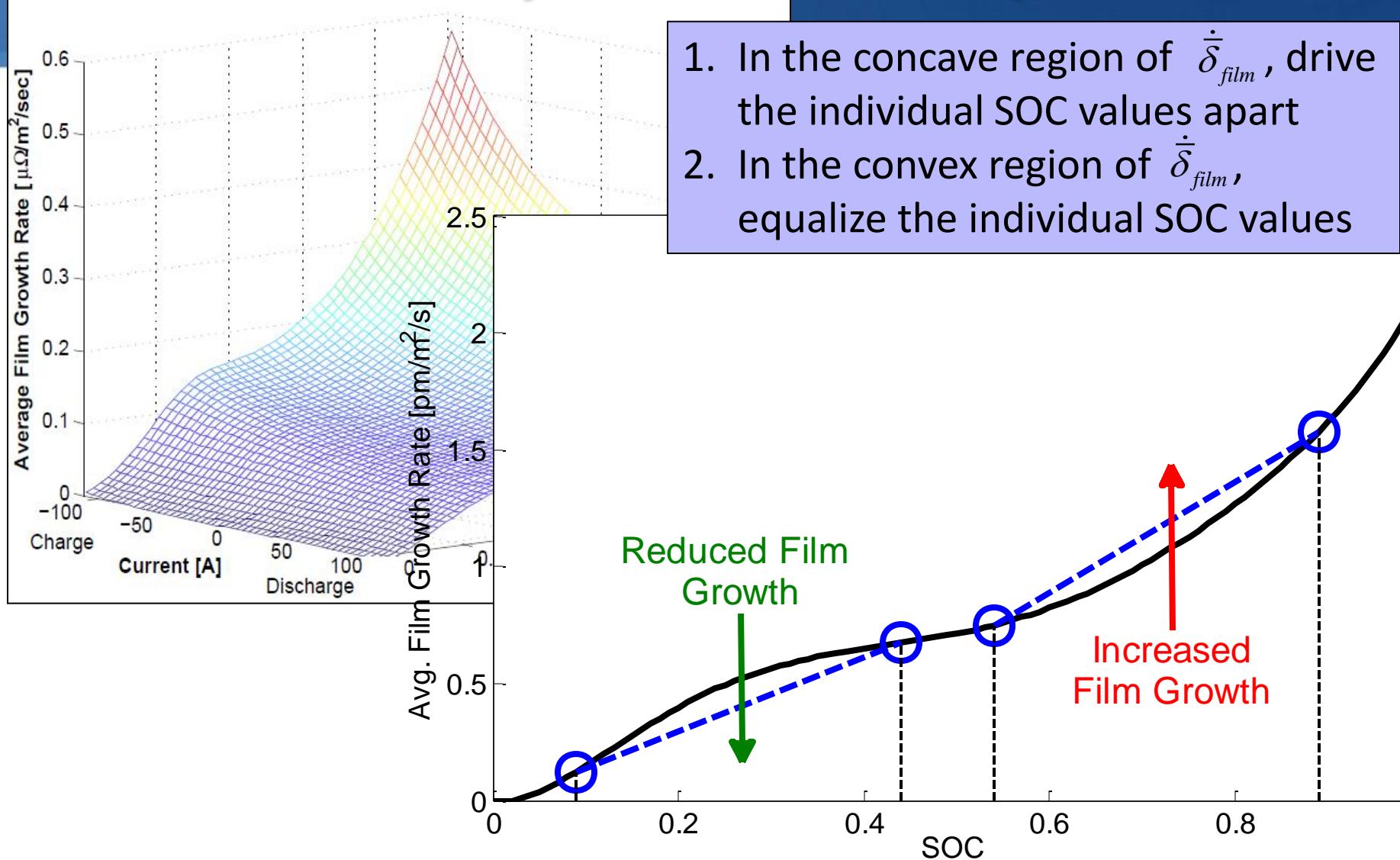
where  $g_z(z_k) = \alpha$



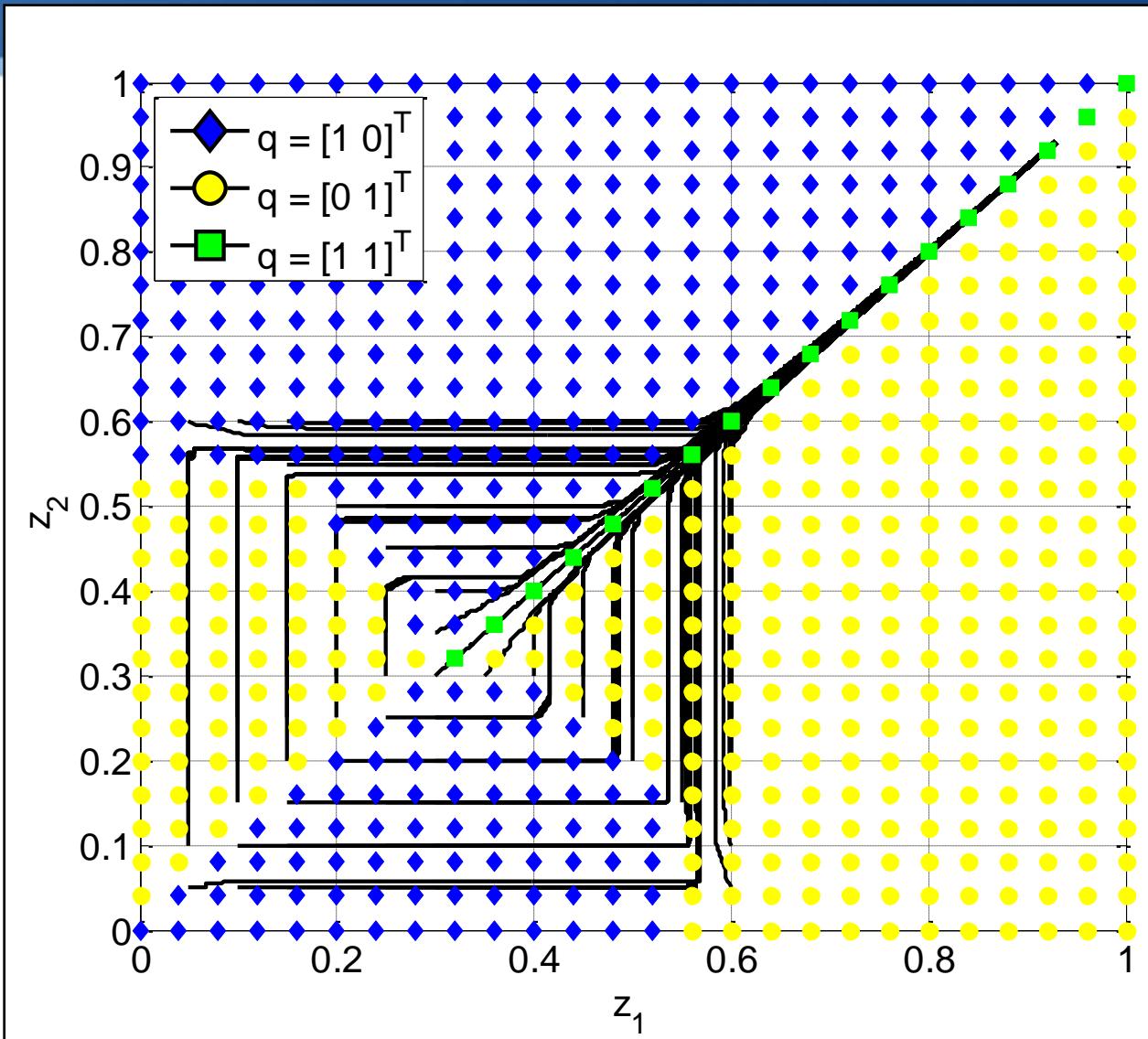
# Solution Analysis: Optimal Trajectories



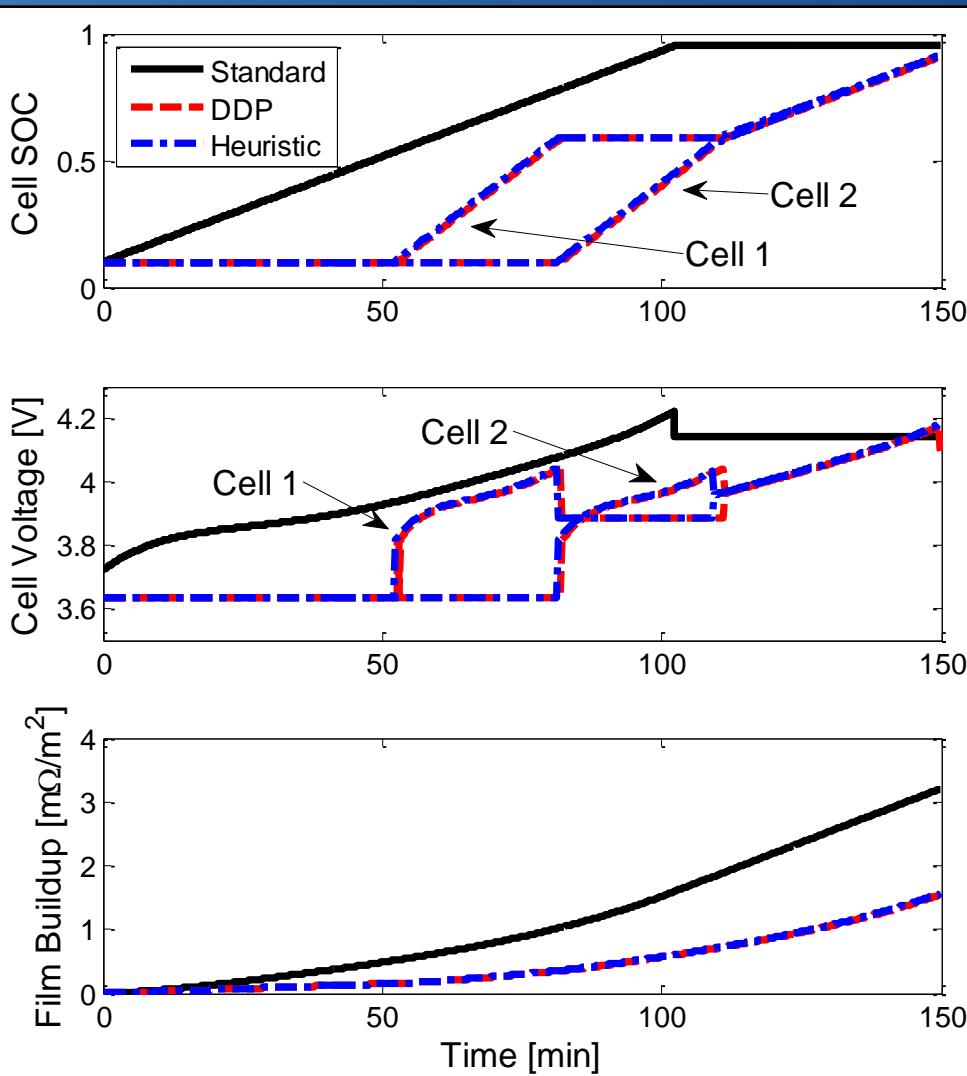
# Solution Analysis: Convexity



# Solution Analysis: Heuristic Control

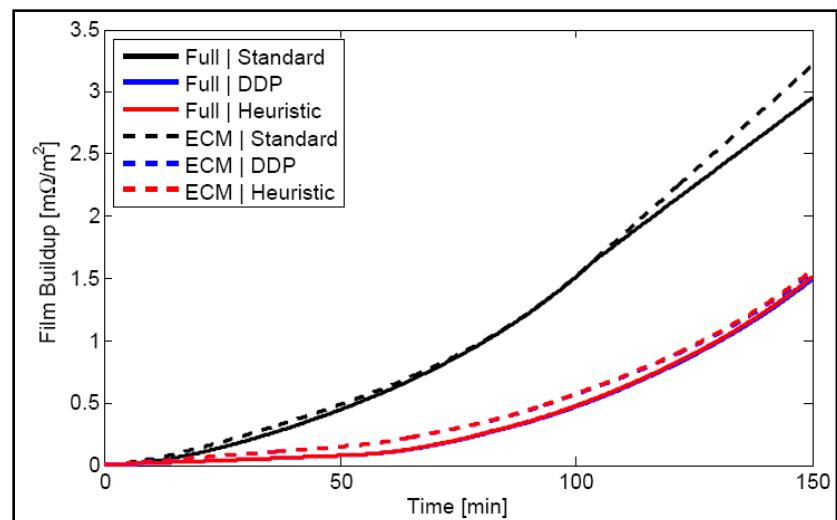


# Simulation Results: Controller Comparison



| Control Scheme | Resistance of Total Film Buildup | Reduction in Film Buildup |
|----------------|----------------------------------|---------------------------|
| Standard       | 3.20 $\text{m}\Omega/\text{m}^2$ | 0%                        |
| DDP            | 1.55 $\text{m}\Omega/\text{m}^2$ | 51.8%                     |
| Heuristic      | 1.56 $\text{m}\Omega/\text{m}^2$ | 51.2%                     |

## Validation on Full Electrochemical Model



# Key Research Topics

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## PHEV Power Management

- PHEV powertrain and daily drive cycle modeling
- Stochastic optimal control
- Tradeoff analysis

# Research Objective

Design supervisory control algorithms that optimally balance battery health degradation and energy consumption cost in PHEVs



J. Voelcker, "Plugging Away in a Prius," *IEEE Spectrum*, vol. 45, pp. 30-48, 2008.



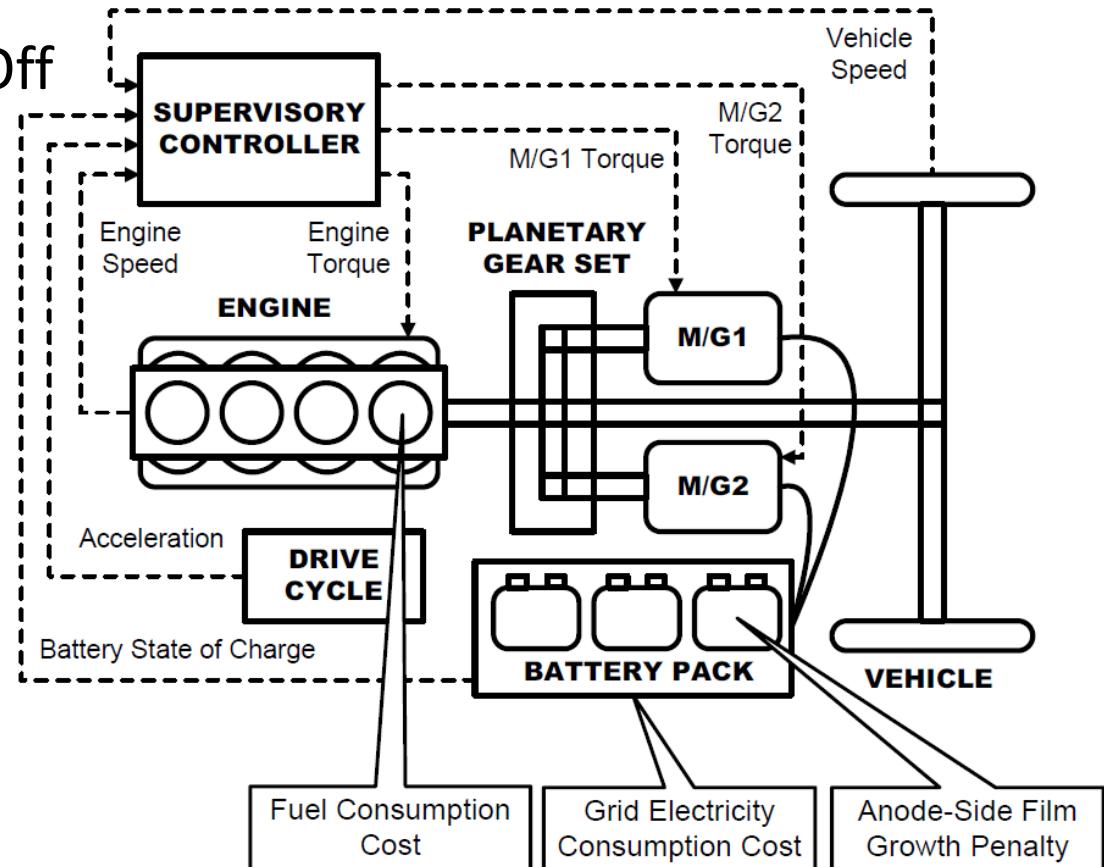
# Power-Split PHEV Model

- Control Inputs

- Engine Torque w/ Eng. Off
- M/G1 Torque

- State Variables

- Engine speed
- Vehicle speed
- Battery SOC
- Vehicle acceleration  
(Markov chain)



# Markov chain model of Drive Cycles

## Drive cycle dynamics

Normal state transition dynamics

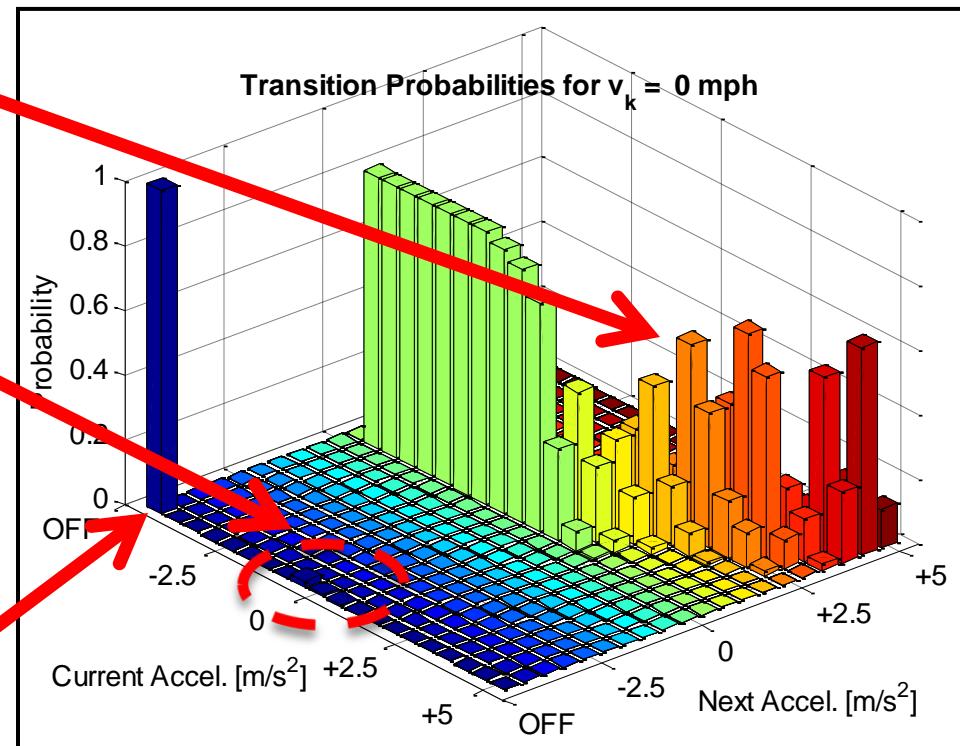
$$p_{ijm} = \Pr(a_{k+1} = j | a_k = i, v_k = m)$$

Transition to “vehicle off”  
denoted  $a_{k+1} = t$

$$p_{itm} = \Pr(a_{k+1} = t | a_k = i, v_k = 0)$$

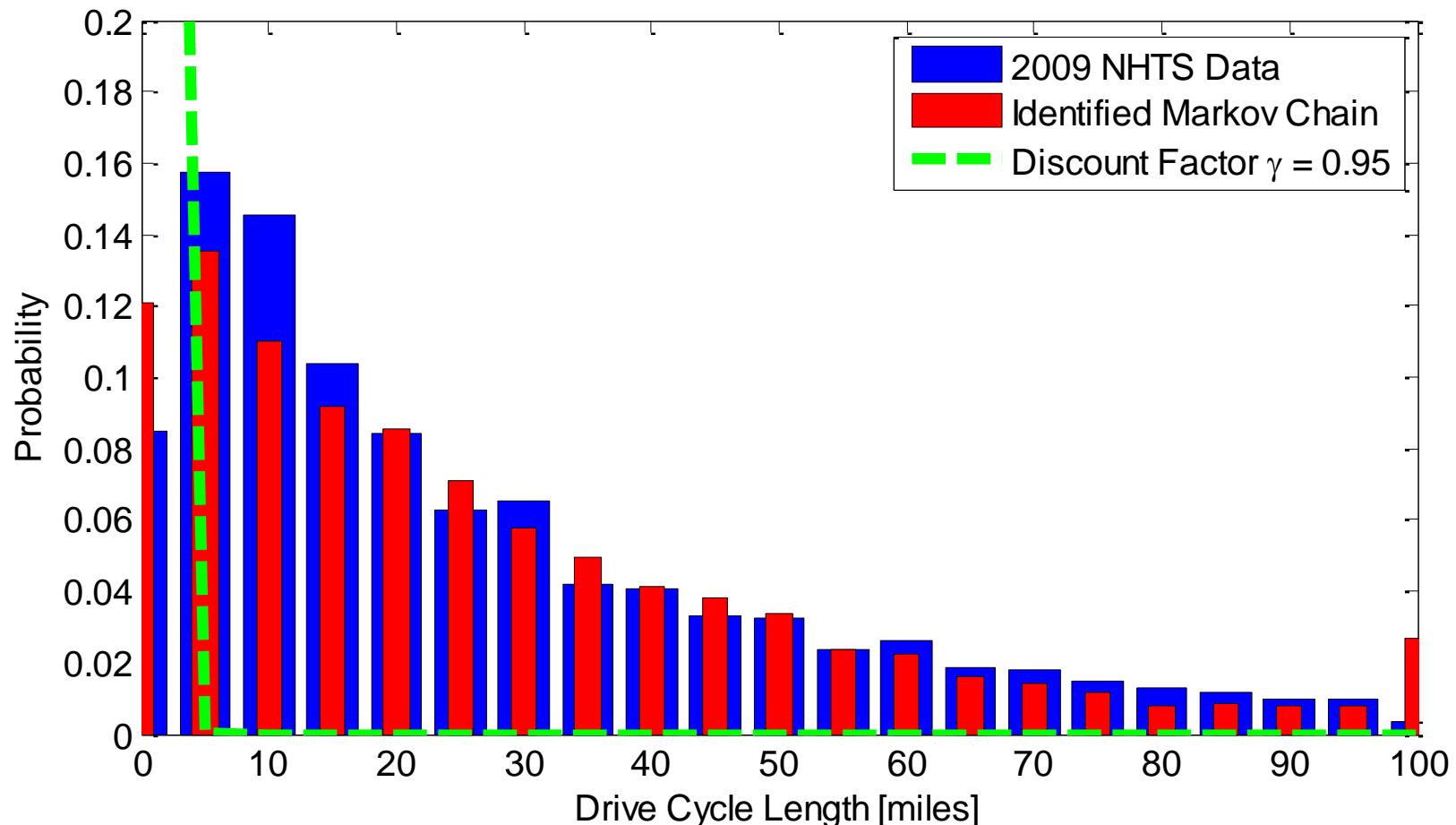
Absorbing state “vehicle off”

$$1 = \Pr(a_{k+1} = t | a_k = t, v_k = 0)$$



# Markov chain model of Drive Cycles

## Daily Trip Length Distribution



# Optimal Control Problem Formulation

Multiobjective Shortest-Path Stochastic Dynamic Program

Cost Functional:

$$J^g = \lim_{N \rightarrow \infty} \mathbb{E} \left[ \sum_{k=0}^N c(x_k, u_k) \right]$$



Constraints:

$$\begin{aligned} x_{k+1} &= f(x_k, u_k, w_k) \\ x &\in X \end{aligned}$$

$$u \in U(x)$$

Objective:

$$g^* = \arg \inf_{g \in G} J^g$$

Combine two objectives into a single linear-weighted objective:

$$c(x_k, u_k) = \alpha \cdot c_{energy}(x_k, u_k) + (1 - \alpha) \cdot c_{film}(x_k, u_k)$$

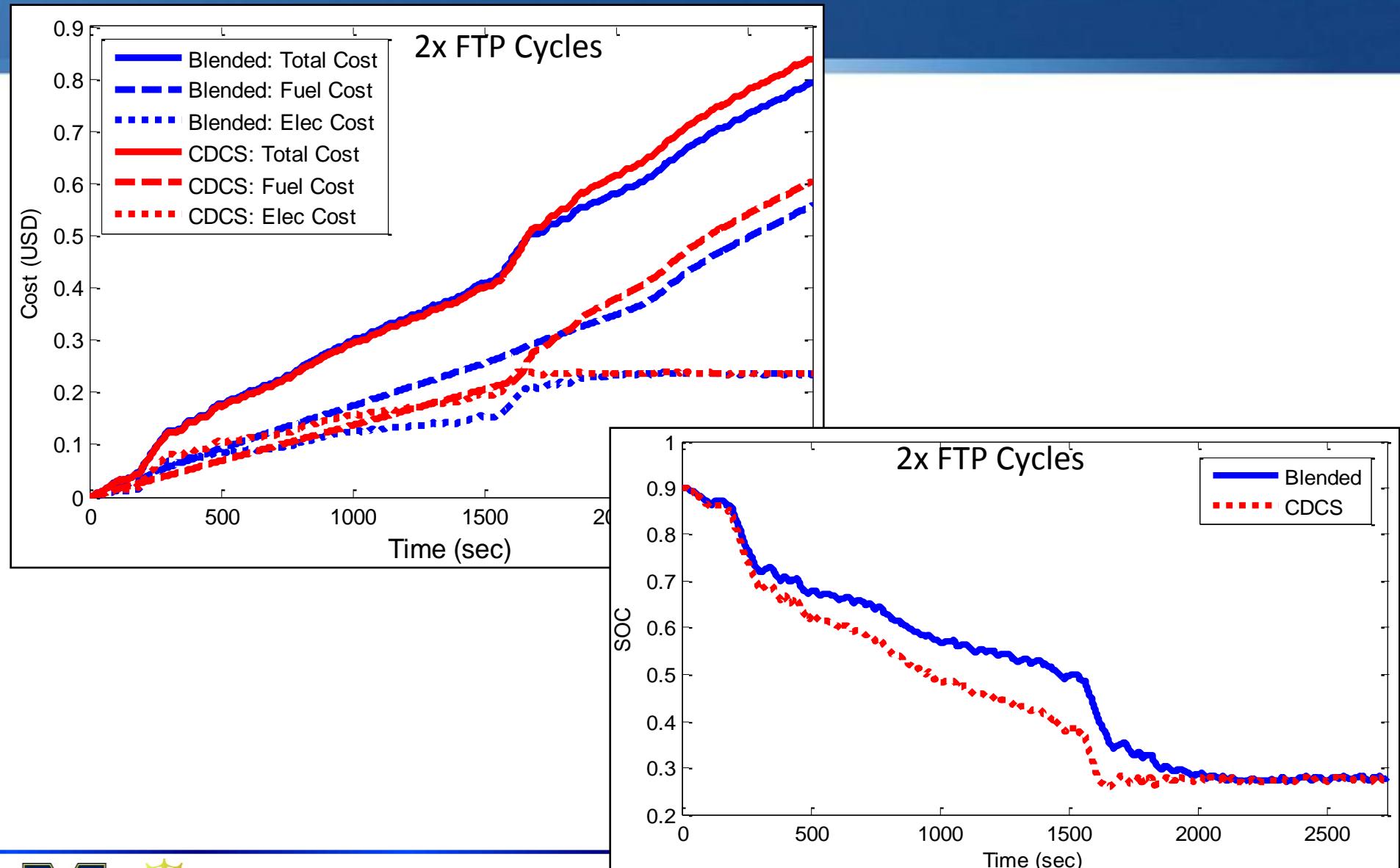
where  $c_{energy}(x_k, u_k) = \beta \alpha_{fuel} W_{fuel} + \alpha_{fuel} \frac{-V_{oc} Q_{batt} \dot{SOC}}{\eta_{grid}}$

$$c_{film}(x_k, u_k) = \dot{\delta}_{film}(I, SOC) \quad \beta = \frac{\text{Price of Gasoline per MJ}}{\text{Price of Grid Electricity per MJ}}$$

Remark: Normalize individual objectives by scaling the range of their natural values to [0,1].

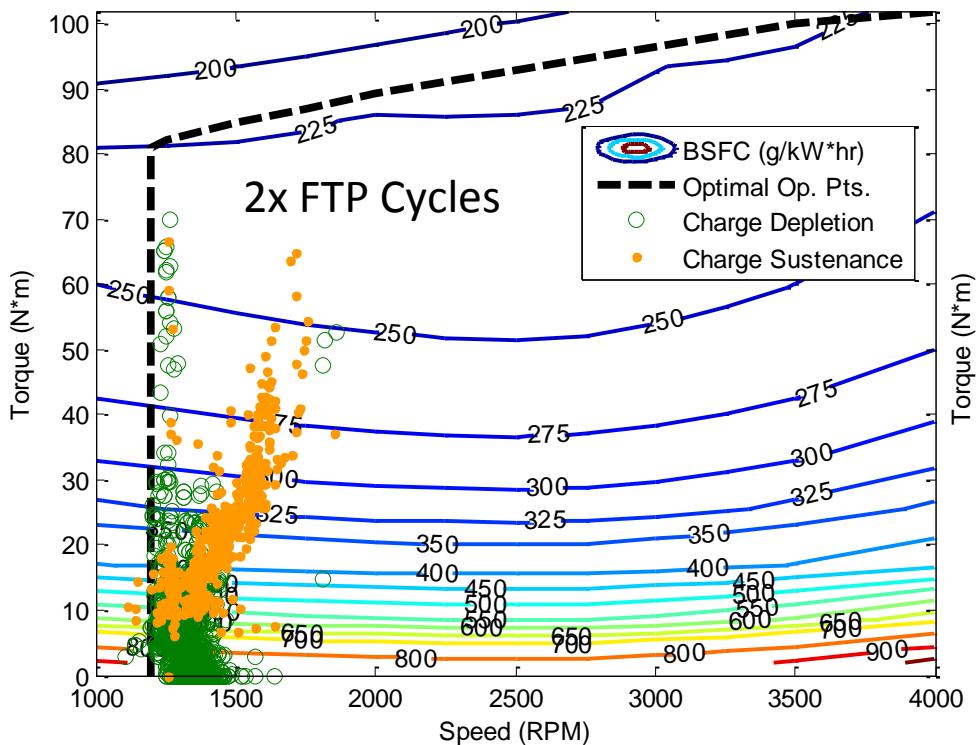


# Power Management Results w/o Aging

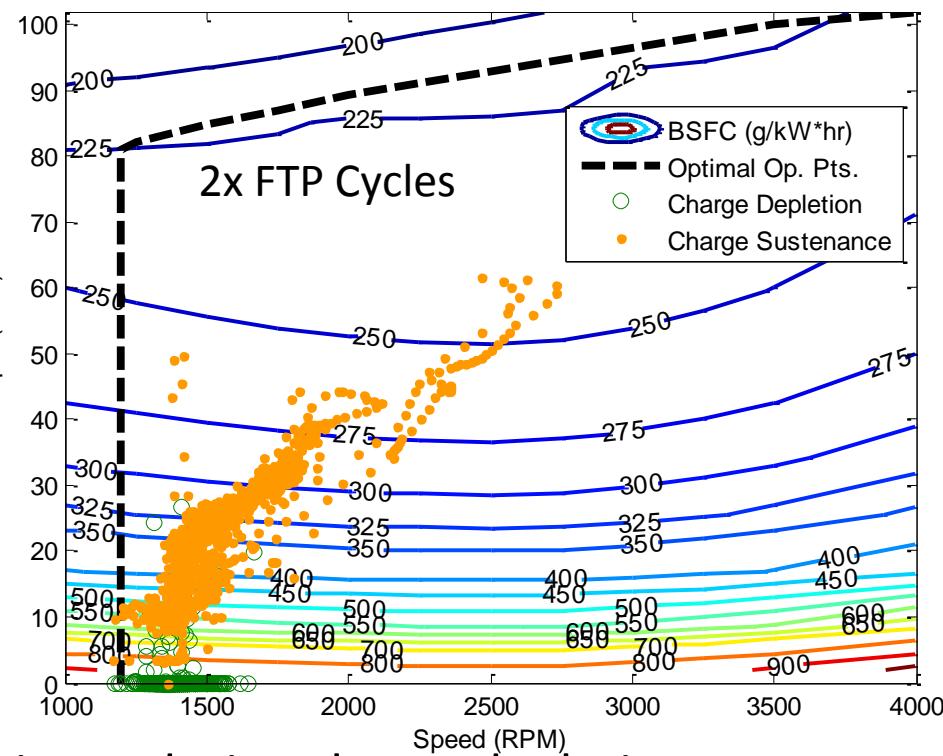


# Engine Operating Point Analysis

## Optimal Blending

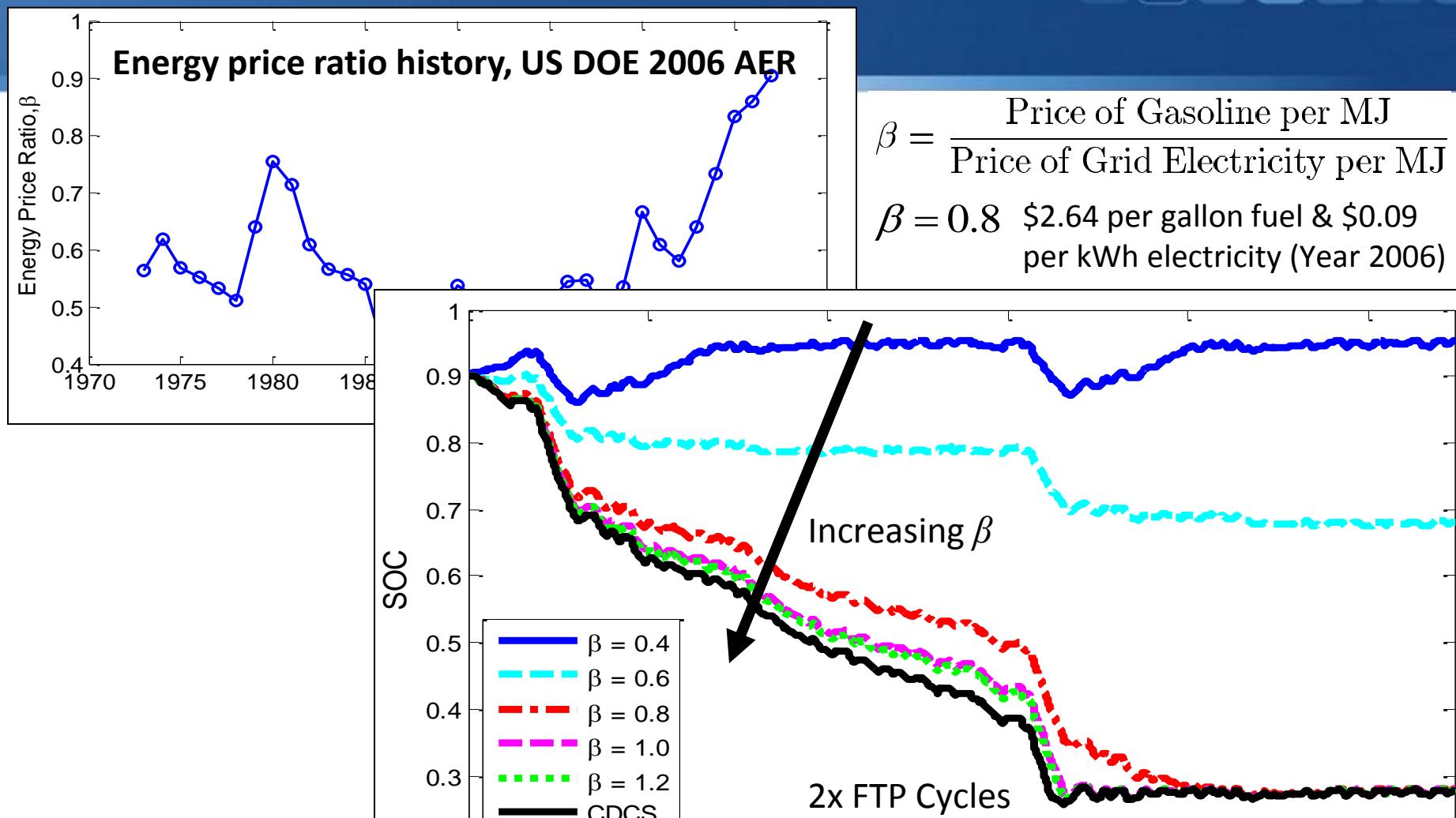


## Charge Depletion, Charge Sustenance



- Blended operates at higher engine efficiency during charge depletion
- Excess power goes to battery charge regeneration

# Energy Price Ratio Analysis

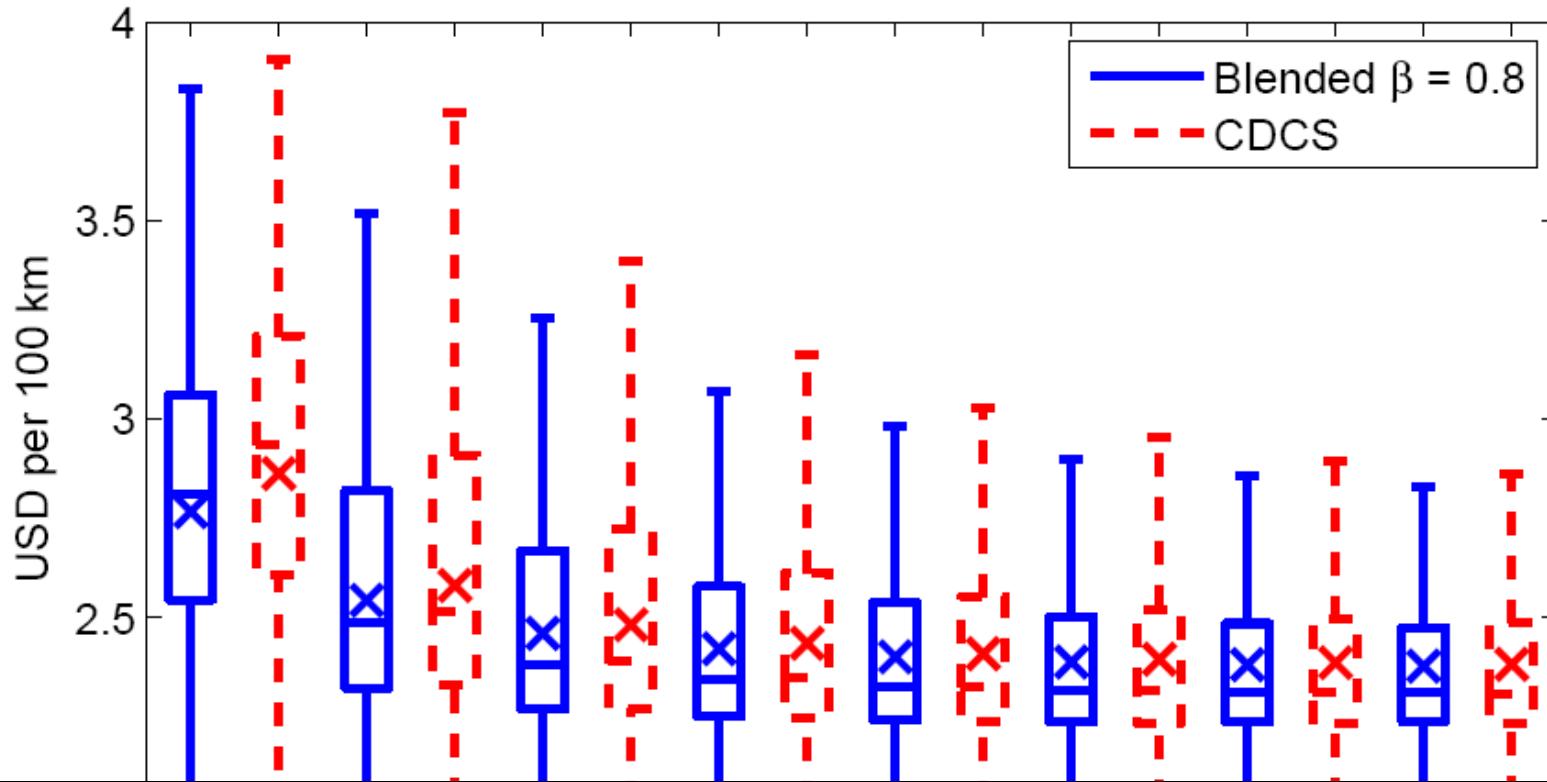


## Publications

- S. J. Moura, H. K. Fathy, D. S. Callaway, and J. L. Stein, "A Stochastic Optimal Control Approach for Power Management in Plug-In Hybrid Electric Vehicles," *IEEE Transactions on Control Systems Technology*, vPP, n 99, 2010.
- S. J. Moura, H. K. Fathy, D. S. Callaway, and J. L. Stein, "A Stochastic Optimal Control Approach for Power Management in Plug-In Hybrid Electric Vehicles," *Proceedings of the 2008 ASME Dynamic Systems and Control Conference*, p 1357-1366, Ann Arbor, MI, 2008.

# Sensitivity Analysis of Battery Size

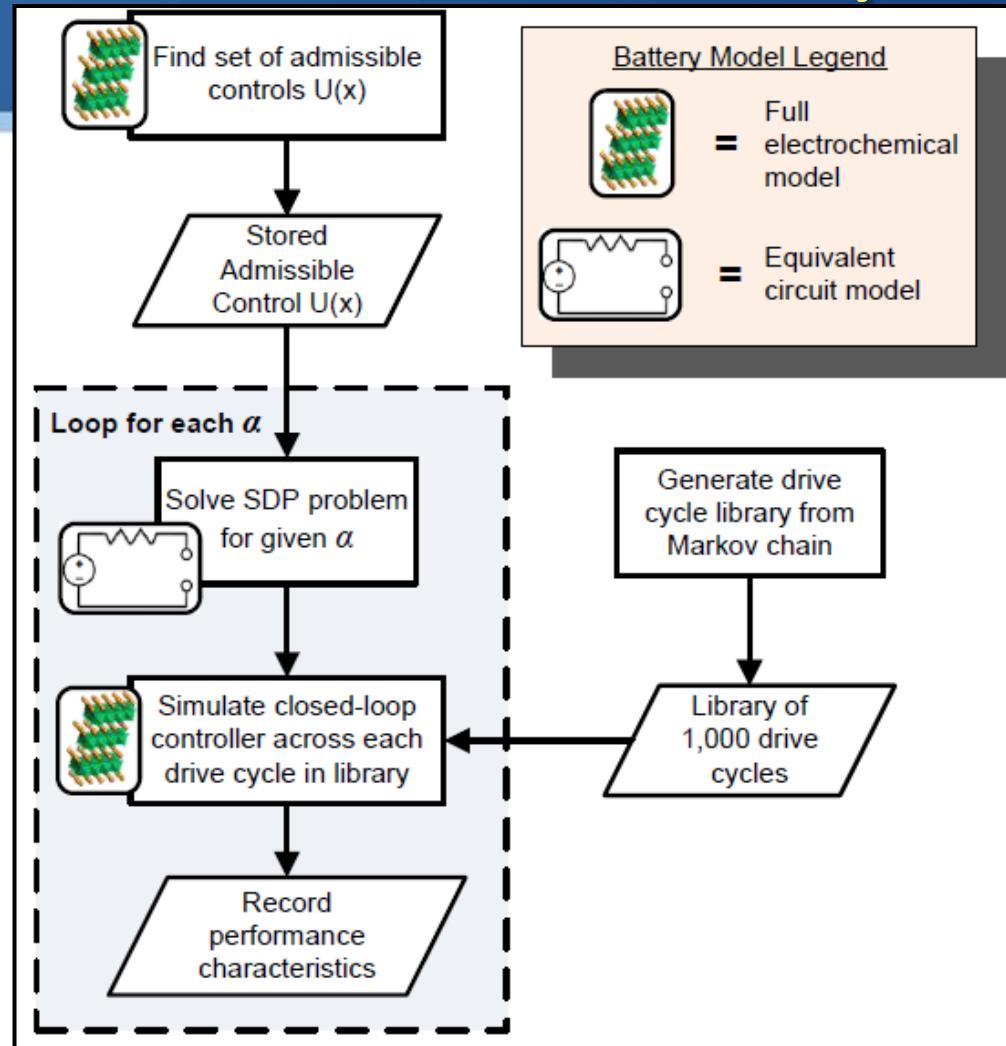
How sensitive is Blending vs. CDCS to battery size?



## Publications

- S. J. Moura, D. S. Callaway, H. K. Fathy, and J. L. Stein, "Tradeoffs between Battery Energy Capacity and Stochastic Optimal Power Management in Plug-in Hybrid Electric Vehicles," *Journal of Power Sources*, v 195, n 9, p 2979-2988, May 2010.
- S. J. Moura, D. S. Callaway, H. K. Fathy, and J. L. Stein, "Impact of Battery Sizing on Stochastic Optimal Power Management in Plug-in Hybrid Electric Vehicles," *Proceedings of the 2008 IEEE International Conference on Vehicular Electronics and Safety*, p 96-102, Columbus, OH, 2008. (Invited Paper)

# Battery-Health Conscious Analysis Procedure

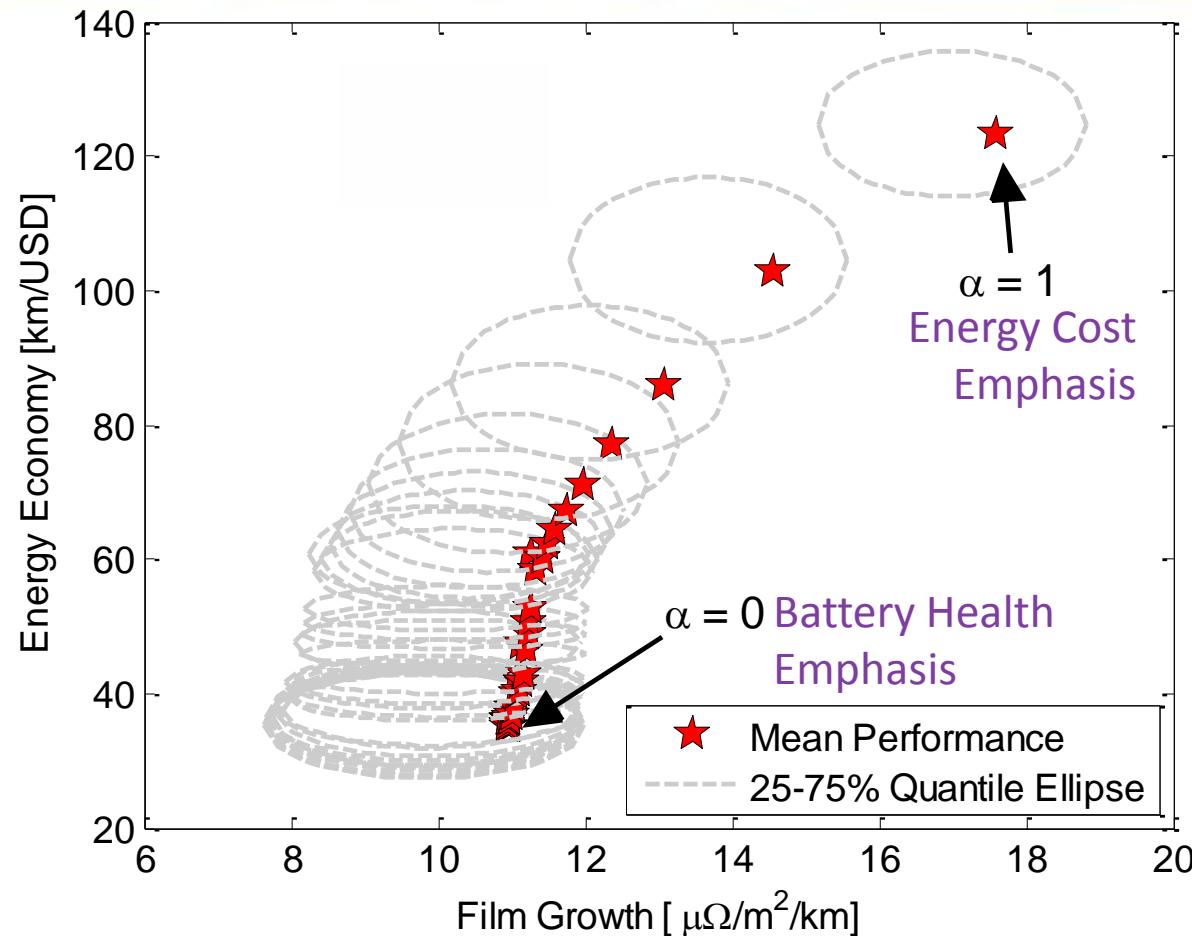


$$c(x_k, u_k) = \alpha \cdot c_{energy}(x_k, u_k) + (1 - \alpha) \cdot c_{film}(x_k, u_k)$$

**Remark:** This study leveraged parallel computing resources at the University of Michigan Center for Advanced Computing to perform 32 SDP optimizations and 32,000 drive cycle simulations.

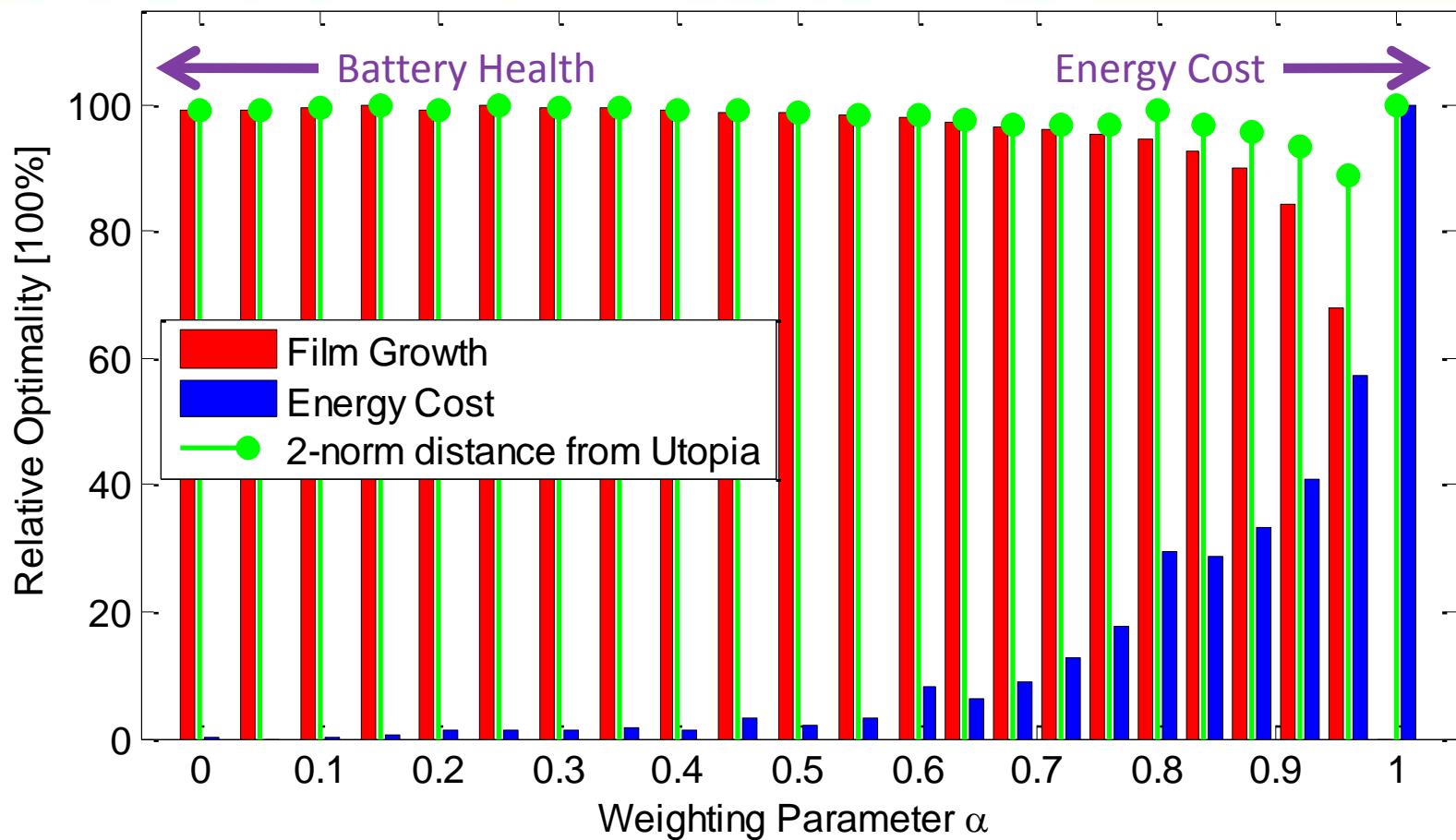
# Pareto\* Set of Optimal Solutions

\*convex subset



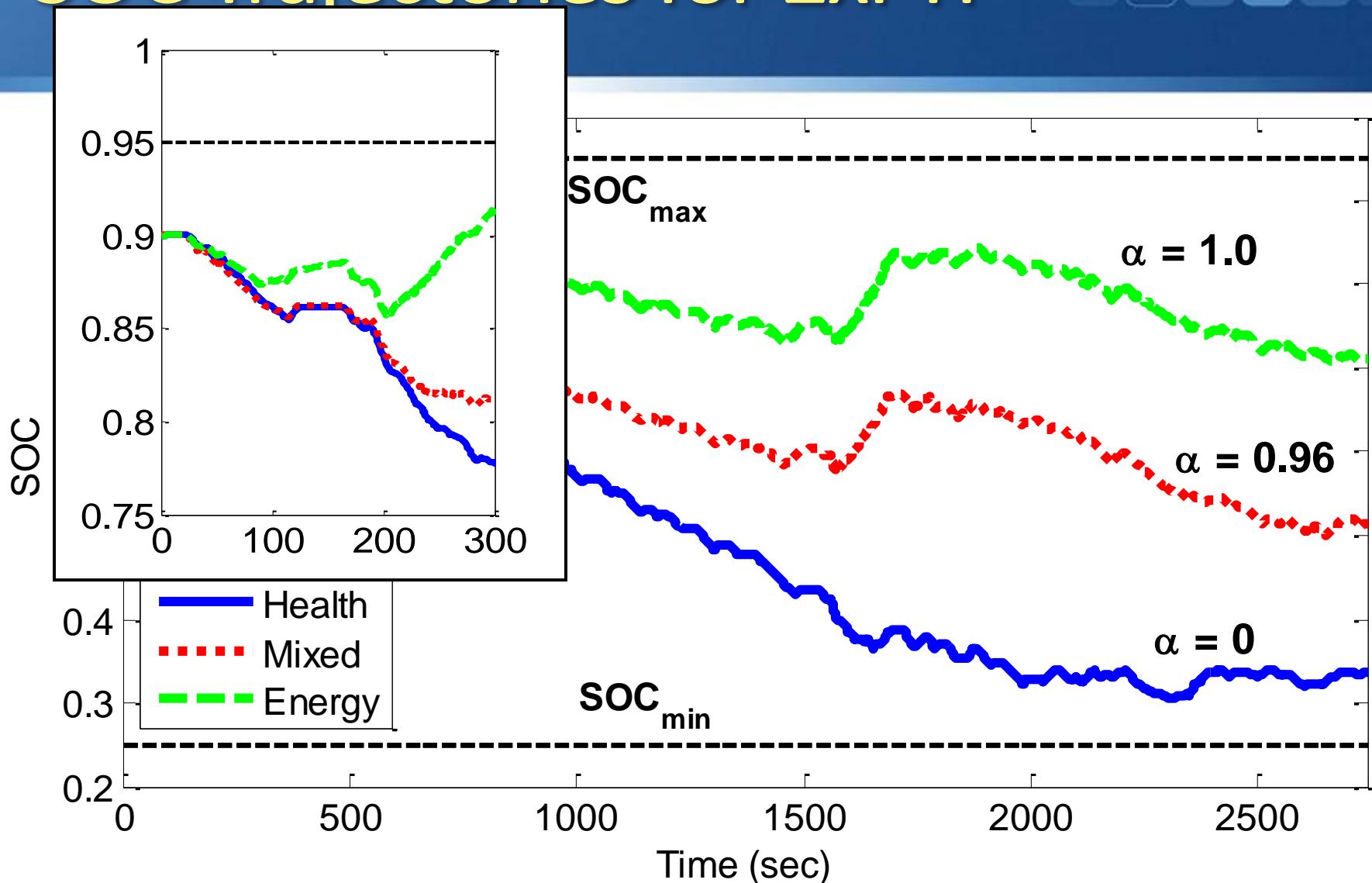
$$c(x_k, u_k) = \alpha \cdot c_{energy}(x_k, u_k) + (1 - \alpha) \cdot c_{film}(x_k, u_k)$$

# Relative Optimality Analysis

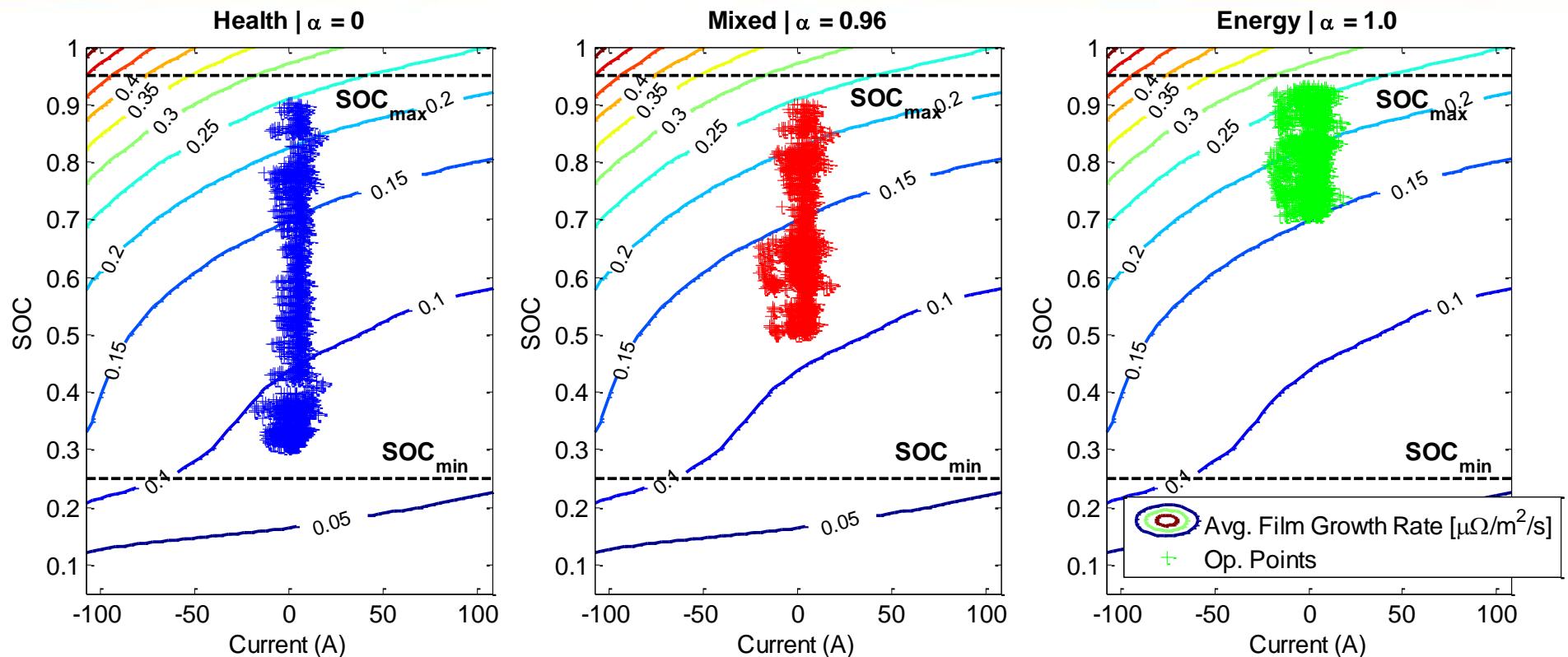


$$c(x_k, u_k) = \alpha \cdot c_{energy}(x_k, u_k) + (1 - \alpha) \cdot c_{film}(x_k, u_k)$$

# SOC Trajectories for 2xFTP



# Film Growth Map Operating Points



**Aggressively deplete battery charge to reduce film growth**

- (1) **Aggressively deplete charge to escape fast film growth region**
- (2) **Ration charge to reduce CS mode**

**Conservatively ration charge to reduce charge sustenance**

## Publications

- S. J. Moura, J. L. Stein, and H. K. Fathy, "Battery Health-Conscious Power Management for Plug-in Hybrid Electric Vehicles via Stochastic Control," *Proceedings of the 2010 ASME Dynamic Systems and Control Conference*, Cambridge, MA, 2010.

# Ongoing / Future Work:

## Optimal Control & Estimation of Distributed Param. Systems

Develop practical extensions of LQR and optimal estimation results for distributed parameter systems

Relevant applications for Ford Motor Company:

- Advanced batteries and fuel cells
- Intelligent building systems
- Stochastic distributions of PEV's and grid loads
- ...

### Publications

- S. J. Moura and H. K. Fathy "Optimal Boundary Control & Estimation of Diffusion-Reaction PDEs," Submitted to the *2011 American Control Conference*, San Francisco, CA, 2011

# LQR Problem Formulation

## Linear parabolic diffusion-reaction system

Dynamics:  $u_t(x, t) = u_{xx}(x, t) + cu(x, t)$

Boundary conditions:  $u_x(0, t) = 0 \quad u(1, t) = U(t)$

Initial condition:  $u(x, 0) = u_0(x)$

Minimize:  $J = \frac{1}{2} \int_0^T [\langle u(x), Q(u(x)) \rangle + RU^2(t)] dt + \frac{1}{2} \langle u(x, T), P_f(u(x, T)) \rangle$

## Derivation of optimal state-feedback:

- Weak-variation necessary conditions
- Linear operator theory

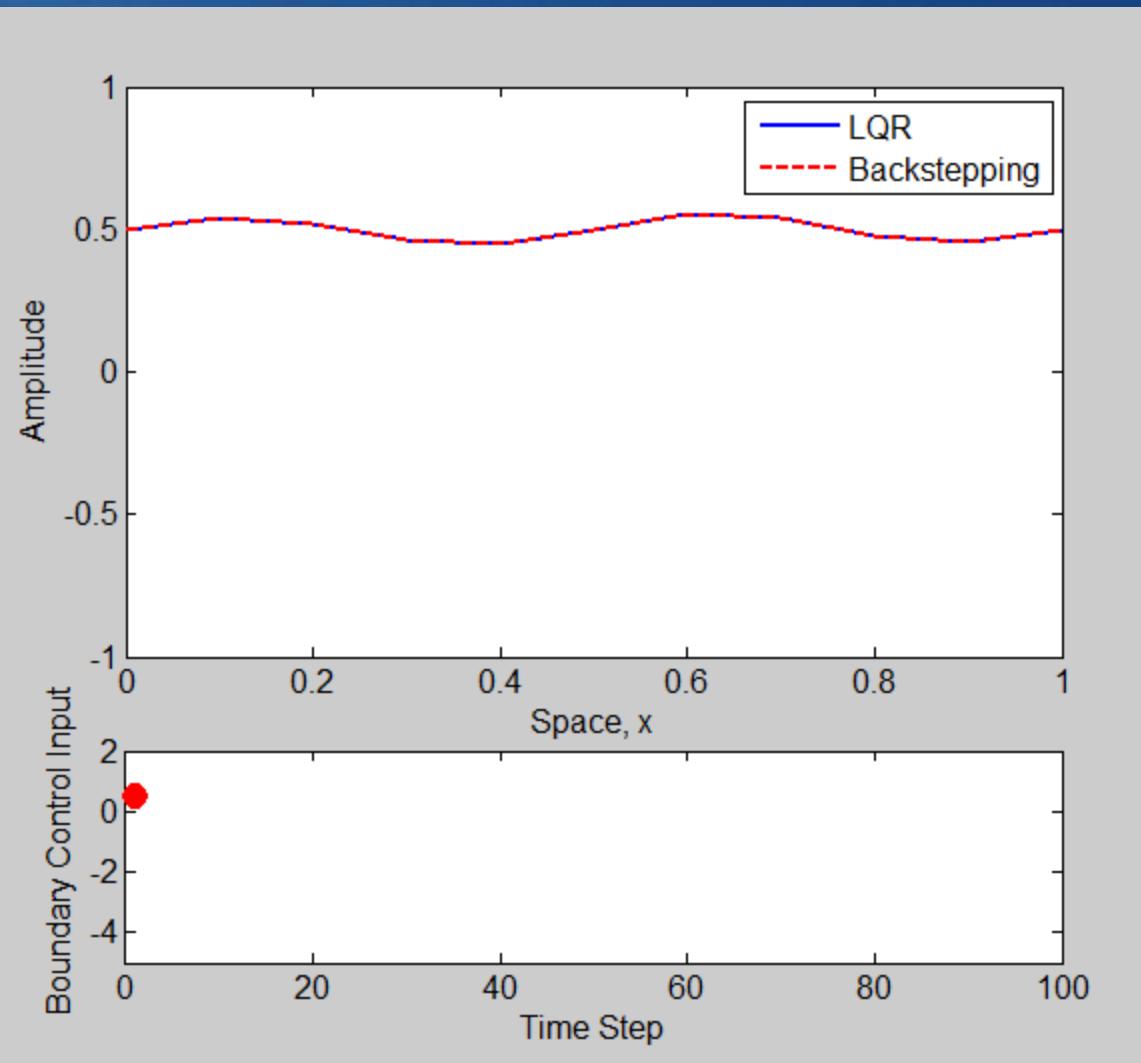
# LQR Results: A partial differential Riccati equation

State-feedback

Riccati

Boundary Condition

Final condition



$$\begin{aligned} & \psi(1, y) \\ & \psi(x, t) = 0 \end{aligned}$$



# Optimal Estimator Problem Formulation

## Linear parabolic diffusion-reaction system

Dynamics:  $u_t(x, t) = u_{xx}(x, t) + cu(x, t) + w(x, t)$

Boundary conditions:  $u_x(0, t) = 0 \quad u(1, t) = U(t)$

Initial condition:  $u(x, 0) = u_0(x)$

Measurement:  $y(t) = u(0, t) + v(t)$

## Observer

Dynamics:  $\hat{u}_t(x, t) = \hat{u}_{xx}(x, t) + c\hat{u}(x, t) + L^t(y(t) - \hat{u}(0, t))$

Boundary conditions:  $\hat{u}_x(0, t) = L_0^t(y(t) - \hat{u}(0, t)) \quad \hat{u}(1, t) = U(t)$

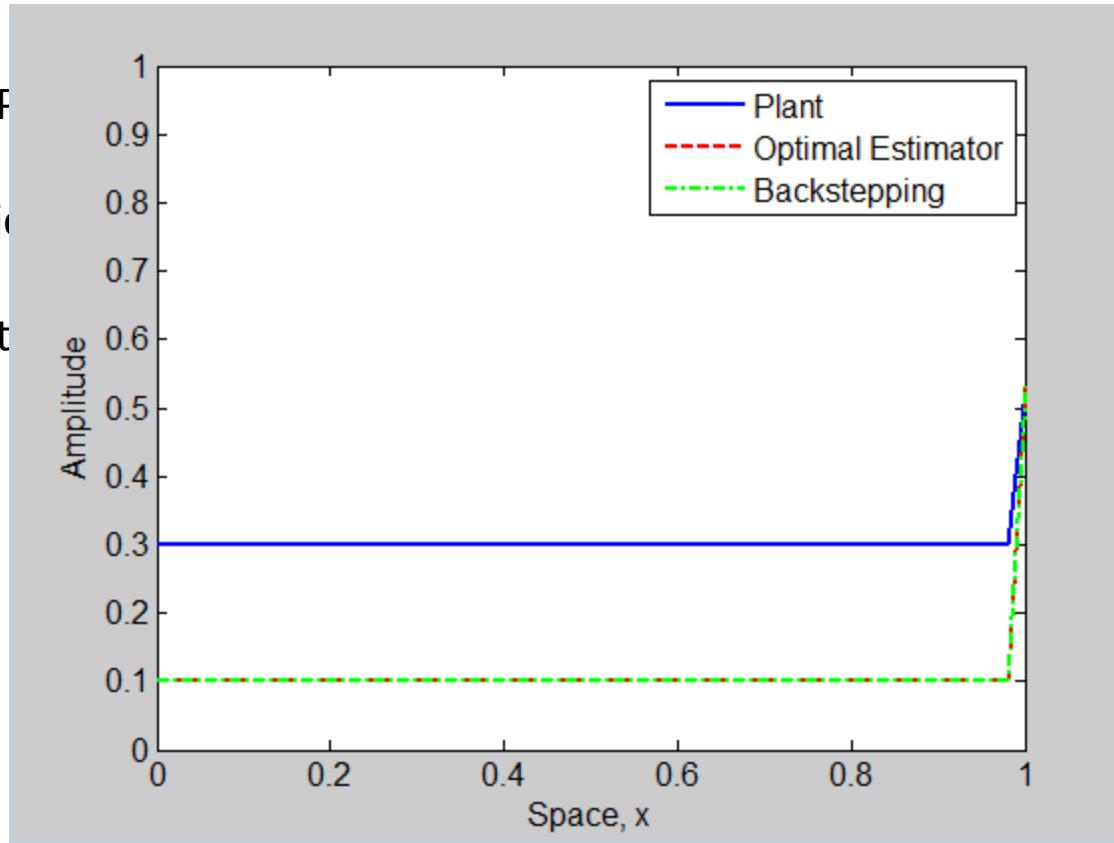
Initial condition:  $\hat{u}(x, 0) = \hat{u}_0(x)$

# Estimation Results: A dual Riccati PDE

Output injection gain:  $L^t = \frac{1}{V} S(x, t)$      $L_0^t = -\frac{1}{V} S(0, t)$

Dual Riccati P  
Boundary Condition  
Initial condition

$$+ W(x, 0)$$



# Seminar Summary



- Battery Modeling and Experimentation
  - Modeling battery electrochemical dynamics from first principles
  - Battery-in-the-loop tester for parameter ID and control design
- Advanced Battery Pack Management Systems
  - Charge unequalization
  - Relationship between SOH convexity properties and charge management
- Power Management in Plug-in Hybrid Electric Vehicles
  - Stochastic drive cycle modeling
  - Multi-objective, constrained
  - Fundamental tradeoffs between energy consumption and battery health

# Teaching Experience:

## Battery Systems and Control Course

- **Winter 2010 Enrollment:**  
59 (including 5 distance learning students)
- **Teaching Winter 2011**

Professional engineers  
(e.g. GM, US Army)

Graduate Students

Undergraduates

ME

ChemE

ESE

EECS

CSE

MatSci



Michigan Engineering **Online Learning**

Winter 2011 Online Graduate Courses

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- Online Learning Home

MECHENG 599-886 Vehicle Electrification:  
Battery Systems and Control

Course Number  
MECHENG 599-886

Offered  
MW 3-4:30 p.m.

Sample Syllabus

Register Here

Video Preview



Course Description

This course covers battery modeling, control and diagnostic methodologies associated to battery electric

## Publications

- S. J. Moura, J. B. Siegel, D. J. Siegel, H. K. Fathy, A. G. Stefanopoulou "Education on Vehicle Electrification: Battery Systems, Fuel Cells, and Hydrogen," *Proceedings of the 2010 IEEE Vehicle Power and Propulsion Conference*, Lille, France, 2010. (**Invited Paper**).

# Publications

## Peer-Reviewed Journals (Accepted)

1. S. J. Moura, H. K. Fathy, D. S. Callaway, and J. L. Stein, "A Stochastic Optimal Control Approach for Power Management in Plug-in Hybrid Electric Vehicles," *IEEE Transactions on Control Systems Technology*, v PP, n 99, p 1-11, March 2010.
2. S. J. Moura, D. S. Callaway, H. K. Fathy, and J. L. Stein, "Impact of Battery Sizing on Stochastic Optimal Power Management in Plug-in Hybrid Electric Vehicles," *Journal of Power Sources*, v 195, n 9, p 2979-2988, May 2010.
3. S. Bashash, S. J. Moura, J. C. Forman, and H. K. Fathy, "Plug-in hybrid electric vehicle charge pattern optimization for energy cost and battery longevity," *Journal of Power Sources*, v 196, n 1, p 541-549, January 2011.
4. S. J. Moura, J. C. Forman, S. Bashash, J. L. Stein, and H. K. Fathy, "Optimal Control of Film Growth in Lithium-Ion Battery Packs via Relay Switches," *accepted to IEEE Transactions on Industrial Electronics* in September 2010.

## Peer-Reviewed Journals (Submitted or In Preparation)

5. S. Bashash, S. J. Moura, and H. K. Fathy, "Battery Health-Conscious Plug-in Hybrid Electric Vehicle Grid Load Prediction," (in review).
6. S. J. Moura and Y. A. Chang, "Lyapunov-Based Switched Extremum Seeking for Maximum Power Point Tracking in Photovoltaic Systems," (in preparation).
7. S. J. Moura, J. L. Stein, and H. K. Fathy, "Battery Health-Based Power Management for Plug-in Hybrid Vehicles via Trip Length Aware Stochastic Control," (in preparation).
8. S. J. Moura, J. B. Siegel, H. K. Fathy, A. G. Stefanopoulou, "Education on Vehicle Electrification: Battery Systems and Control," (in preparation).
9. J. C. Forman, S. J. Moura, J. L. Stein, H. K. Fathy, "Parameter Identification of the Doyle-Fuller-Newman Model for a LiFePO<sub>4</sub> Battery with Fisher Information-Based Identifiability Analysis," (in preparation).
10. S. J. Moura, J. L. Stein, and H. K. Fathy, "Optimal Boundary Control and Estimation of Diffusion-Reaction PDEs," (in preparation).

## Conferences Proceedings (Accepted)

1. S. J. Moura, H. K. Fathy, D. S. Callaway, J. L. Stein, "A Stochastic Optimal Control Approach for Power Management in Plug-in Hybrid Electric Vehicles," *Proceedings of the 2008 ASME Dynamic Systems and Control Conference*, Ann Arbor, MI, 2008.
2. S. J. Moura, D. S. Callaway, H. K. Fathy, and J. L. Stein, "Impact of Battery Sizing on Stochastic Optimal Power Management in Plug-in Hybrid Electric Vehicles," *Proceedings of the 2008 IEEE International Conference on Vehicular Electronics and Safety*, pp. 96-102, Columbus, OH, 2008. (Invited Paper)
3. Y. A. Chang, S. J. Moura, "Real-Time Air-Flow Control in Fuel Cell Systems: An Extremum Seeking Approach," *Proc. of the 2009 American Control Conference*, St. Louis, MO, 2009.
4. S. J. Moura, J. C. Forman, J. L. Stein, H. K. Fathy, "Control of Film Growth in Lithium Ion Battery Packs via Switches," *Proceedings of the 2009 ASME Dynamic Systems and Control Conference*, Hollywood, CA, 2009. **Best Student Paper Finalist**
5. S. J. Moura, Y. A. Chang, "Asymptotic Convergence through Lyapunov-Based Switching in Extremum Seeking with Application to Photovoltaic Systems," *Proceedings of the 2010 American Control Conference*, Baltimore, MD, 2010.
6. S. Bashash, S. J. Moura, H. K. Fathy, "Charge Trajectory Optimization of Plug-in Hybrid Electric Vehicles for Energy Cost Reduction and Battery Life Enhancement," *Proceedings of the 2010 American Control Conference*, Baltimore, MD, 2010.
7. S. J. Moura, J. B. Siegel, D. J. Siegel, H. K. Fathy, A. G. Stefanopoulou, "Education on Vehicle Electrification: Battery Systems, Fuel Cells, and Hydrogen," *Proceedings of the 2010 IEEE Vehicle Power and Propulsion Conference*, Lille, France, 2010.
8. S. J. Moura, J. L. Stein, H. K. Fathy, "Battery Health-Conscious Power Management for Plug-in Hybrid Electric Vehicles via Stochastic Control," *Proceedings of the 2010 ASME Dynamic Systems and Control Conference*, Cambridge, MA, 2010.
9. S. Bashash, S. J. Moura, H. K. Fathy, "Battery Health-Conscious Plug-in Hybrid Electric Vehicle Power Demand Prediction," *Proceedings of the 2010 ASME Dynamic Systems and Control Conference*, Cambridge, MA, 2010.

## Conferences Proceedings (Submitted)

10. S. J. Moura, H. K. Fathy, "Optimal Boundary Control & Estimation of Diffusion-Reaction PDEs," Submitted to the *2011 American Control Conf.*, San Francisco, CA, 2011.
11. J. C. Forman, S. J. Moura, J. L. Stein, H. K. Fathy, "Genetic Parameter Identification of the Doyle-Fuller-Newman Model From Experimental Cycling of a Li-ion LiFePO<sub>4</sub> Battery," Submitted to the *2011 American Control Conference*, San Francisco, CA, 2011.



# Relevant Honors

- National Science Foundation (NSF) Graduate Research Fellowship
- University of Michigan Rackham Merit Fellowship (RMF)
- Distinguished Leadership Award, College of Engineering,  
University of Michigan
- Best Student Paper Finalist at the 2009 ASME Dynamic Systems  
and Control Conference, Hollywood, CA USA
- 1st Place Technical Paper Competition, 2008 Society of  
Hispanic Professional Engineers Conference, Phoenix, AZ



“I’m convinced that the country that leads in clean energy is also going to be the country that leads in the global economy. And I want America to be that nation.”

– President Barack Obama, March 2, 2010

Thank you for your attention!

Questions?

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