

# Adaptive Estimation and Control of Models for Battery Electrochemistry

Scott Moura, Ph.D.

UC President's Postdoctoral Fellow  
Cymer Center for Control Systems and Dynamics  
UC San Diego

MAE Seminar  
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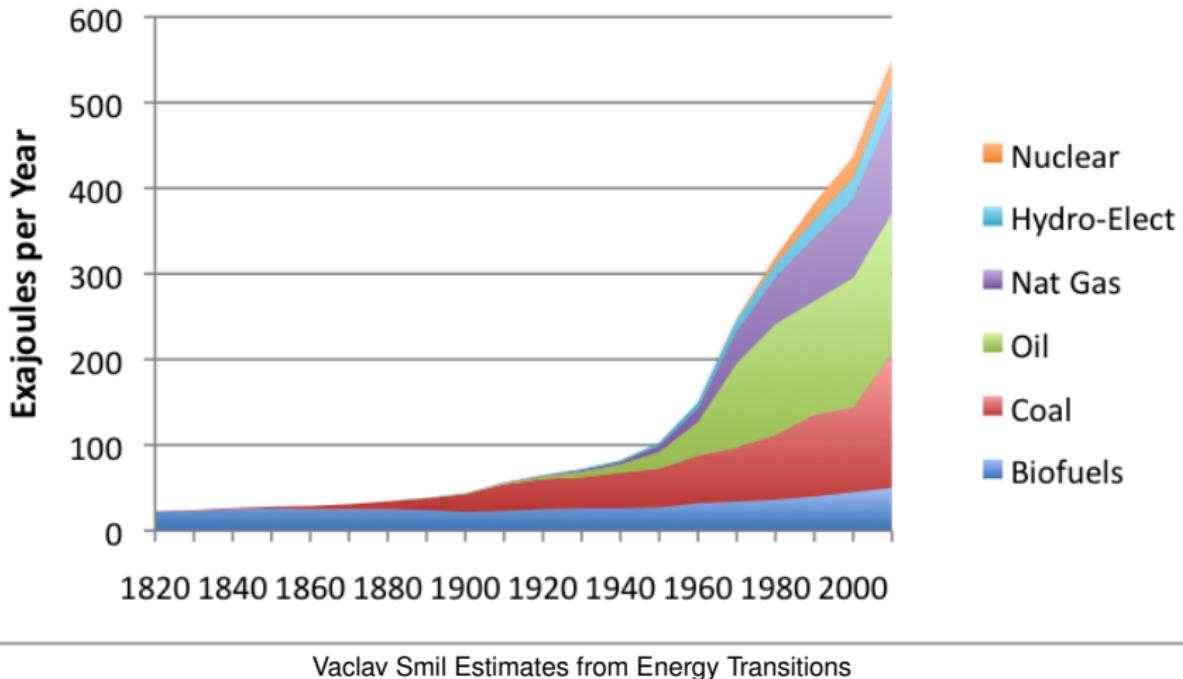
## *Core Philosophy:*

(Dynamical models of physical phenomena)

+ (novel control paradigms)

= (transformative advancements)

## World Energy Consumption



# Energy Initiatives



Denmark 50% wind penetration by 2025  
China leads manufacturing of renewable tech  
Brazil uses 86% renewables

EV Everywhere

SunShot

Green Button

33% renewables by 2020

Go Solar California

20% reduction of bldg. energy by 2015

# Energy Crisis Solutions

Integrate variable renewables



Energy storage

(e.g., batteries)

Decrease energy waste



Intelligent energy management

(e.g., smart grids)

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# Outline

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## Batteries

- [Electrochemical Modeling] Incorporating Physics
- [SOC/SOH Estimation] Looking Inside w/ Models, Meas., and Math
- [Constrained Control] Operate at the Limits, Safely
- [PHEV Power Management] Max eMPG and Max Batt Life

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## Demand Response in Smart Grids

3

## Future

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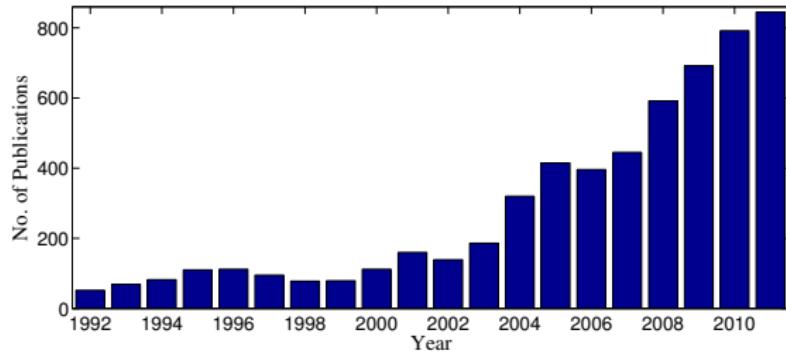
# A Golden Era



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Keyword: “Battery Systems and Control”



# The Battery Problem

**Needs:** Cheap, high energy, high power, long life

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## Some Motivating Facts

EV Batts

\$800 / kWh now (2010)

\$125 / kWh for parity to IC engine

Only 75% of available capacity is used

Range anxiety inhibits adoption

Lifetime risks caused by fast charging

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## Two Solutions

Design better batteries  
(materials science & chemistry)

Make current batteries better  
(estimation and control)

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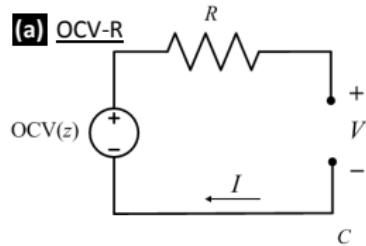
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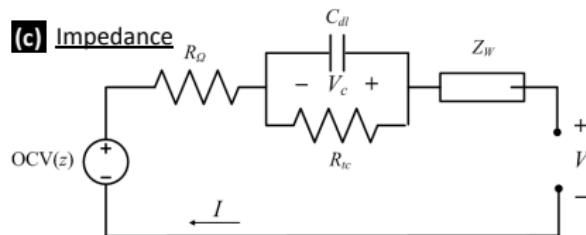
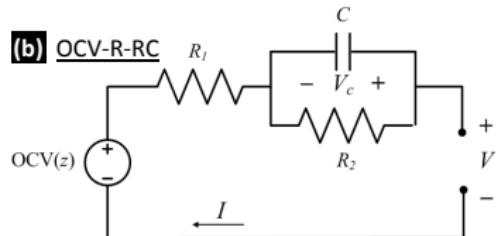
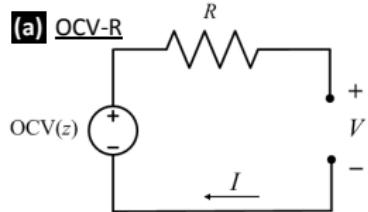
# Battery Models

## Equivalent Circuit Model



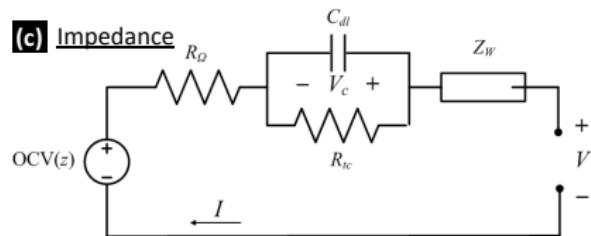
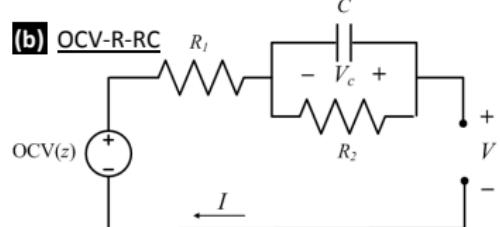
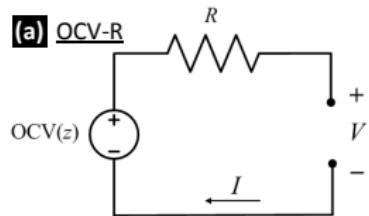
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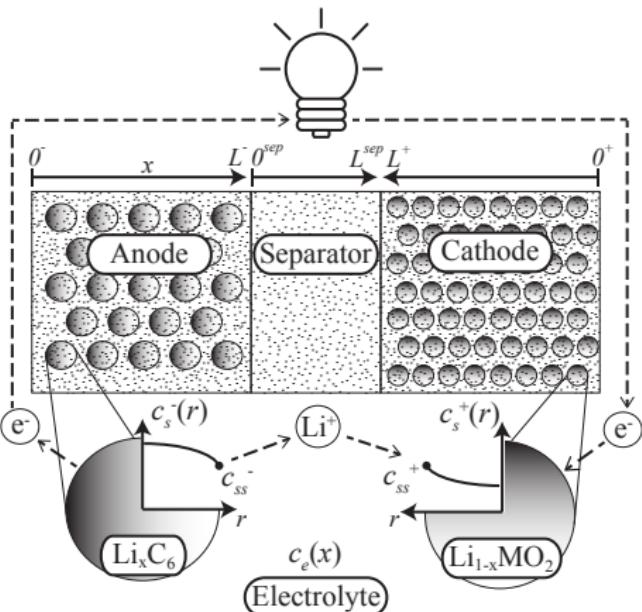


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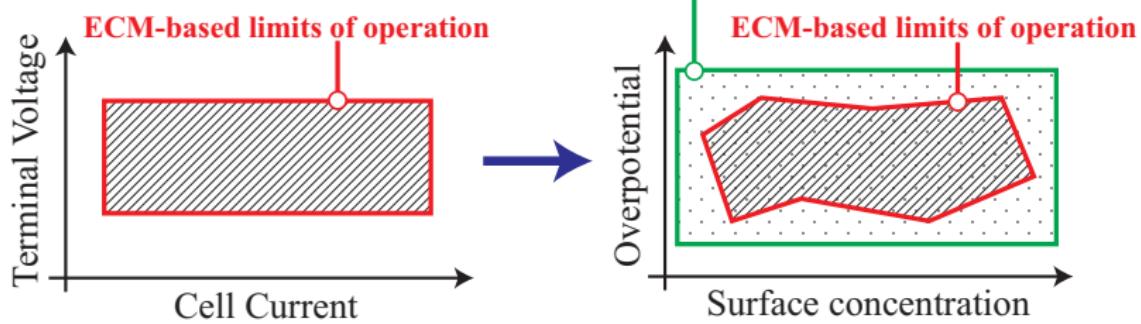


## Electrochemical Model





# Operate Batteries at their Physical Limits



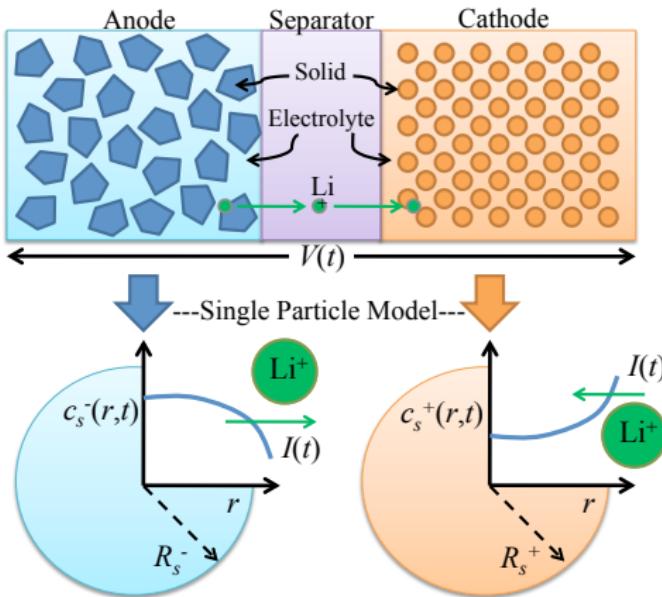
# Electrochemical Model Equations

well, some of them

Description	Equation
Solid phase Li concentration	$\frac{\partial c_s^\pm}{\partial t}(x, r, t) = \frac{1}{r^2} \frac{\partial}{\partial r} \left[ D_s^\pm r^2 \frac{\partial c_s^\pm}{\partial r}(x, r, t) \right]$
Electrolyte Li concentration	$\varepsilon_e \frac{\partial c_e}{\partial t}(x, t) = \frac{\partial}{\partial x} \left[ \varepsilon_e D_e \frac{\partial c_e}{\partial x}(x, t) + \frac{1-t_c^0}{F} i_e^\pm(x, t) \right]$
Solid potential	$\frac{\partial \phi_s^\pm}{\partial x}(x, t) = \frac{i_e^\pm(x, t) - I(t)}{\sigma^\pm}$
Electrolyte potential	$\frac{\partial \phi_e}{\partial x}(x, t) = -\frac{i_e^\pm(x, t)}{\kappa} + \frac{2RT}{F} (1 - t_c^0) \left( 1 + \frac{d \ln f_{c/a}}{d \ln c_e}(x, t) \right) \frac{\partial \ln c_e}{\partial x}(x, t)$
Electrolyte ionic current	$\frac{\partial i_e^\pm}{\partial x}(x, t) = a_s F j_n^\pm(x, t)$
Molar flux btw phases	$j_n^\pm(x, t) = \frac{1}{F} i_0^\pm(x, t) \left[ e^{\frac{\alpha_a F}{RT} \eta^\pm(x, t)} - e^{-\frac{\alpha_c F}{RT} \eta^\pm(x, t)} \right]$
Temperature	$\rho c_P \frac{dT}{dt}(t) = h [T^0(t) - T(t)] + I(t)V(t) - \int_{0^-}^{0^+} a_s F j_n(x, t) \Delta T(x, t) dx$

# Animation of Li Ion Evolution

# Single Particle Model (SPM)

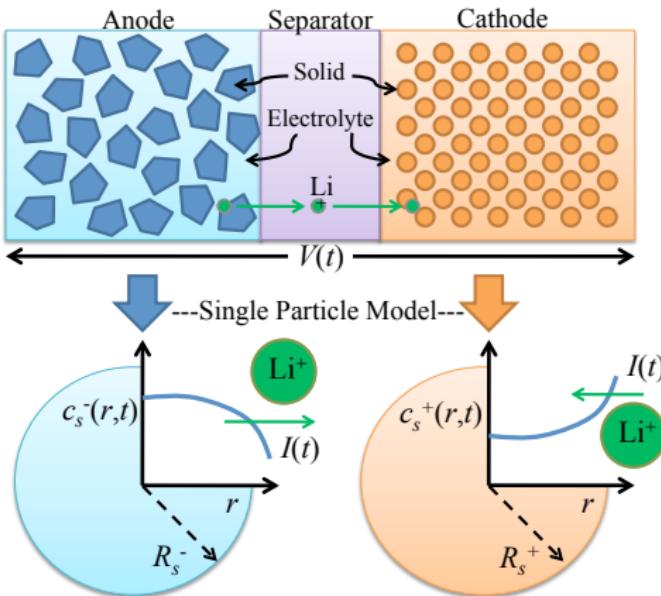


# Single Particle Model (SPM)

Diffusion of Li in solid phase:

$$\frac{\partial c_s^-}{\partial t}(r, t) = \frac{D_s^-}{r^2} \frac{\partial}{\partial r} \left[ r^2 \frac{\partial^2 c_s^-}{\partial r^2}(r, t) \right]$$

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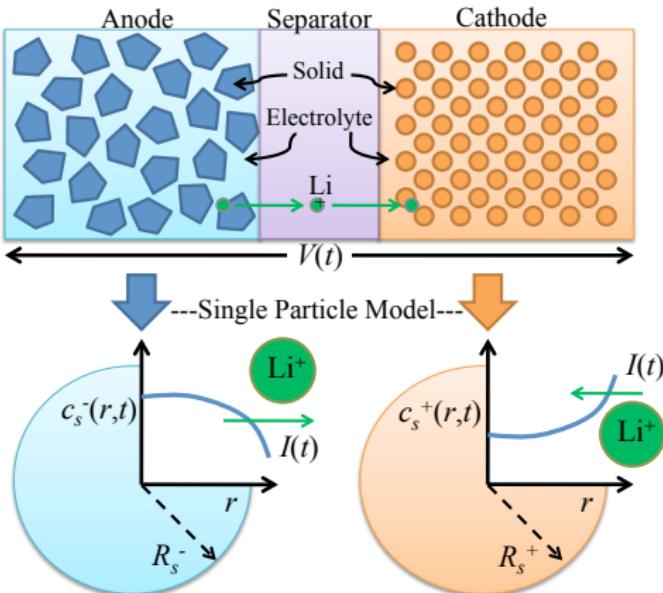
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Boundary conditions:

$$\frac{\partial c_s^-}{\partial r}(R_s^-, t) = -\rho^+ I(t)$$

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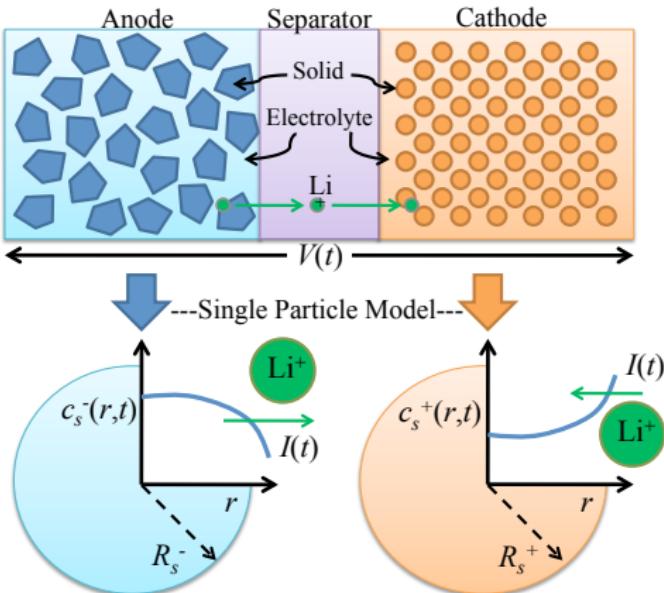
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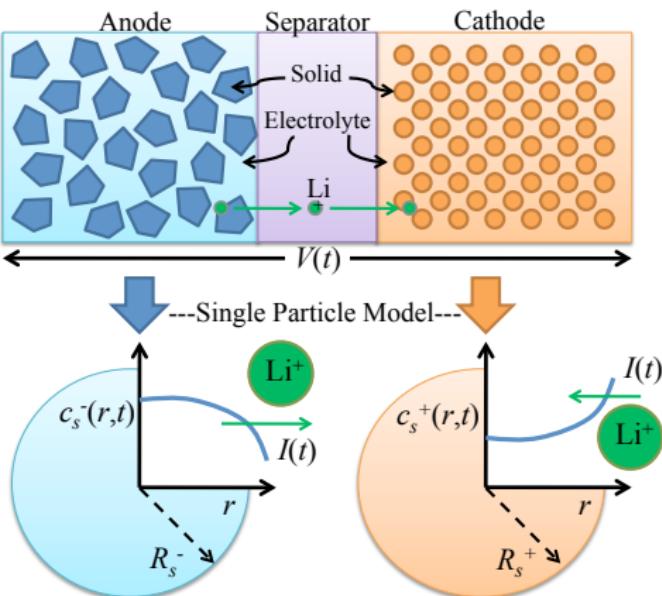
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Definitions

- SOC: Bulk concentration  $SOC_{bulk}$ , Surface concentration  $c_{ss}^-(t)$
- SOH: Physical parameters, e.g.  $\varepsilon$ ,  $q$ ,  $n_{Li}$ ,  $R_f$



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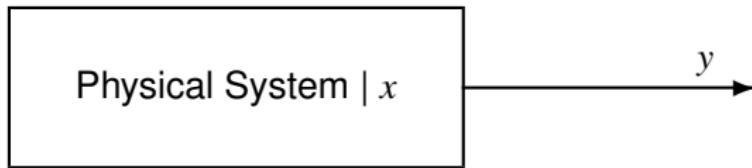
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# The **SOC** Estimation Problem

## Problem Statement

Estimate states  $c_s^-(r, t), c_s^+(r, t)$  from measurements  $I(t), V(t)$  and SPM

### Intro to Estimation

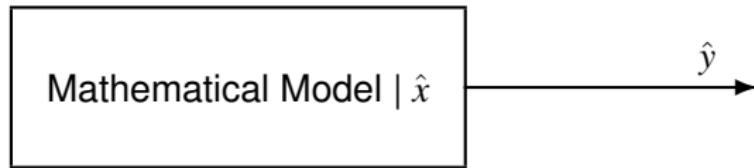
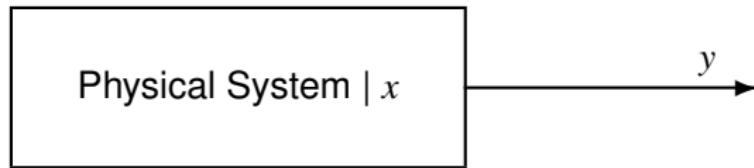


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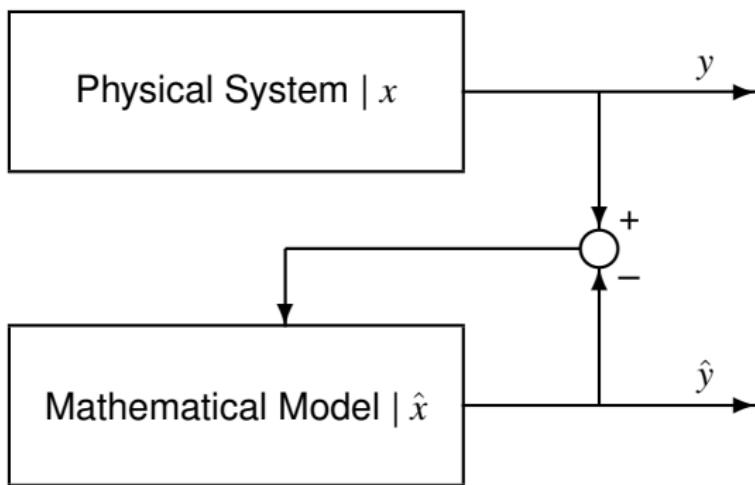


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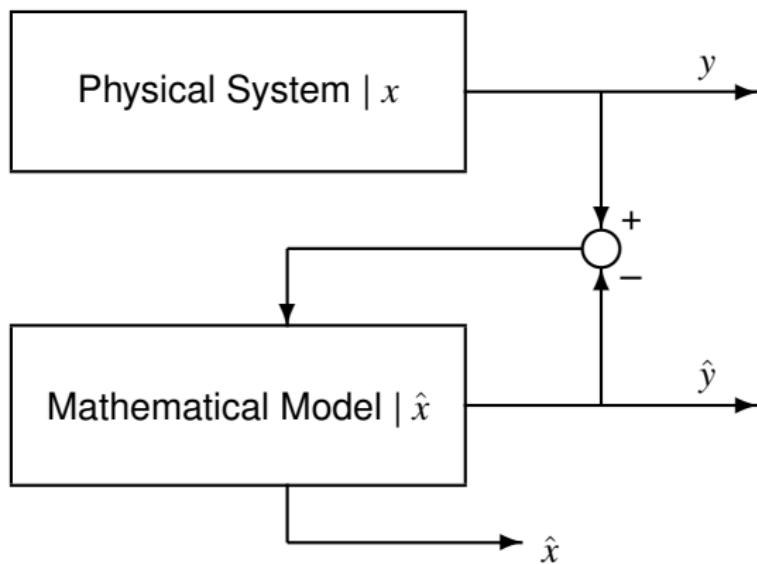


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# Backstepping PDE Estimator

## Simplify the Math

- Model reduction to achieve observability
- Normalize time and space
- Scale spatial dimension

# Backstepping PDE Estimator

Model Eqns. for Observer Design:  $c(r, t)$

$$\begin{aligned}\frac{\partial c}{\partial t}(r, t) &= \varepsilon \frac{\partial^2 c}{\partial r^2}(r, t) && \text{Heat PDE} \\ c(0, t) &= 0\end{aligned}$$

$$\frac{\partial c}{\partial r}(1, t) - c(1, t) = -q\rho I(t)$$

$$\text{Measurement} = c(1, t) = \check{c}_{ss}^-(t)$$

# Backstepping PDE Estimator

Estimator:  $\hat{c}(r, t)$

$$\frac{\partial \hat{c}}{\partial t}(r, t) = \varepsilon \frac{\partial^2 \hat{c}}{\partial r^2}(r, t) + p_1(r) [c(1, t) - \hat{c}(1, t)]$$

$$\hat{c}(0, t) = 0$$

$$\frac{\partial \hat{c}}{\partial r}(1, t) - \hat{c}(1, t) = -q\rho I(t) + p_{10} [c(1, t) - \hat{c}(1, t)]$$

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Estimation Error Dynamics:  $\tilde{c}(r, t) = c(r, t) - \hat{c}(r, t)$

$$\begin{aligned}\frac{\partial \tilde{c}}{\partial t}(r, t) &= \varepsilon \frac{\partial^2 \tilde{c}}{\partial r^2}(r, t) - p_1(r) \tilde{c}(1, t) \\ \tilde{c}(0, t) &= 0 \\ \frac{\partial \tilde{c}}{\partial r}(1, t) - \tilde{c}(1, t) &= -p_{10} \tilde{c}(1, t)\end{aligned}$$

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## The Concept

$$\tilde{c}(r, t) = \tilde{w}(r, t) - \int_r^1 p(r, s) \tilde{w}(s) ds \quad \text{Backstepping Transformation}$$

$$\frac{\partial \tilde{w}}{\partial t}(r, t) = \varepsilon \frac{\partial^2 \tilde{w}}{\partial r^2}(r, t) + \lambda \tilde{w}(r, t) \quad \text{Exp. Stable Target System}$$

$$\tilde{w}(0, t) = 0 \quad W(t) = \frac{1}{2} \int_0^1 \tilde{w}^2(x, t) dx$$

$$\frac{\partial \tilde{w}}{\partial r}(1, t) = \frac{1}{2} \tilde{w}(1, t) \quad \dot{W}(t) \leq -\gamma W(t)$$

# Backstepping PDE Estimator

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## Kernel PDE

$$p(r, s) : \mathcal{D} \rightarrow \mathbb{R}, \quad \mathcal{D} = \{(r, s) | 0 \leq r \leq s \leq 1\}$$

$$\begin{aligned}p_{rr}(r, s) - p_{ss}(r, s) &= \frac{\lambda}{\varepsilon} p(r, s) & p_1(r) &= -p_s(r, 1) - \frac{1}{2} p(r, 1) \\ p(0, s) &= 0 & p_{10} &= \frac{3 - \lambda/\varepsilon}{2} \\ p(r, r) &= \frac{\lambda}{2\varepsilon} r\end{aligned}$$

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## Explicit Solution to Estimator Gains

$$p_1(r) = \frac{-\lambda r}{2\varepsilon z} \left[ I_1(z) - \frac{2\lambda}{\varepsilon z} I_2(z) \right] \quad \text{where } z = \sqrt{\frac{\lambda}{\varepsilon}(r^2 - 1)}$$
$$p_{10} = \frac{1}{2} \left( 3 - \frac{\lambda}{\varepsilon} \right)$$

# The SOH Estimation Problem

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Estimate physical parameters from measurements  $I(t)$ ,  $V(t)$  and SPM

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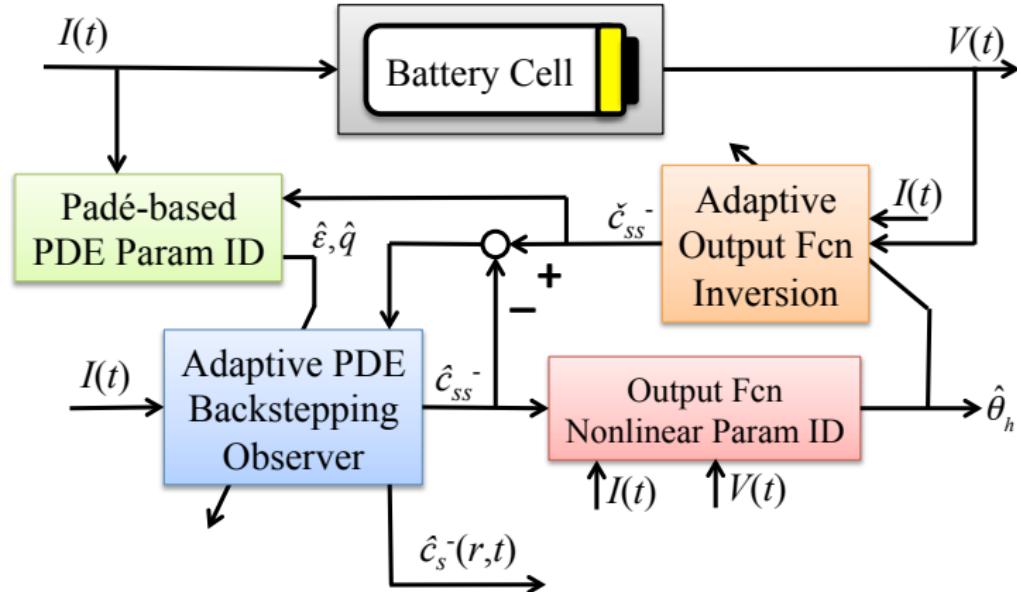
Estimate physical parameters from measurements  $I(t)$ ,  $V(t)$  and SPM

Relate uncertain parameters to SOH-related concepts

- Capacity fade
- Power fade

# Adaptive Observer

Combined State & Parameter Estimation



## Nonlinearly Parameterized Output

$$V(t) = h(c_{ss}^-(t), I(t); \theta)$$

- $\theta$  contains many parameters
- Linear dependence b/w parameters?

# Output Function Nonlinear Parameter ID

## Nonlinearly Parameterized Output

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## Identifiability Analysis

- Linearly independent parameter subset :  $\theta_h = [n_{Li}, R_f]^T$ 
  - $n_{Li}$  : Moles of cyclable Li (Capacity Fade)
  - $R_f$  : Resistance of current collectors, electrolyte, etc. (Power Fade)

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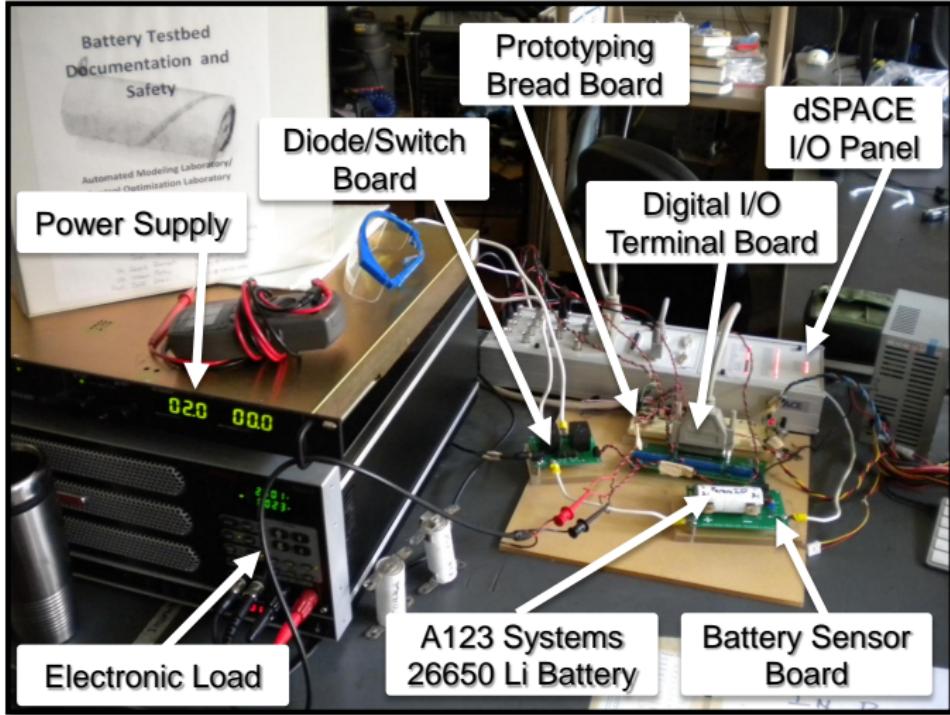
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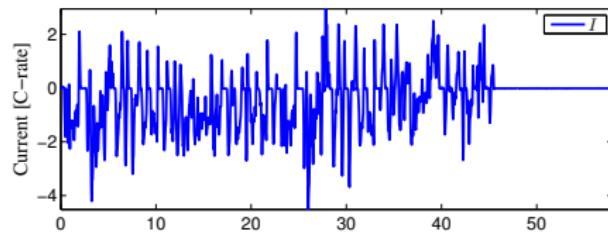
Apply nonlinear recursive least squares to  $\theta_h$

# Custom-Built Battery-in-the-Loop Testbed



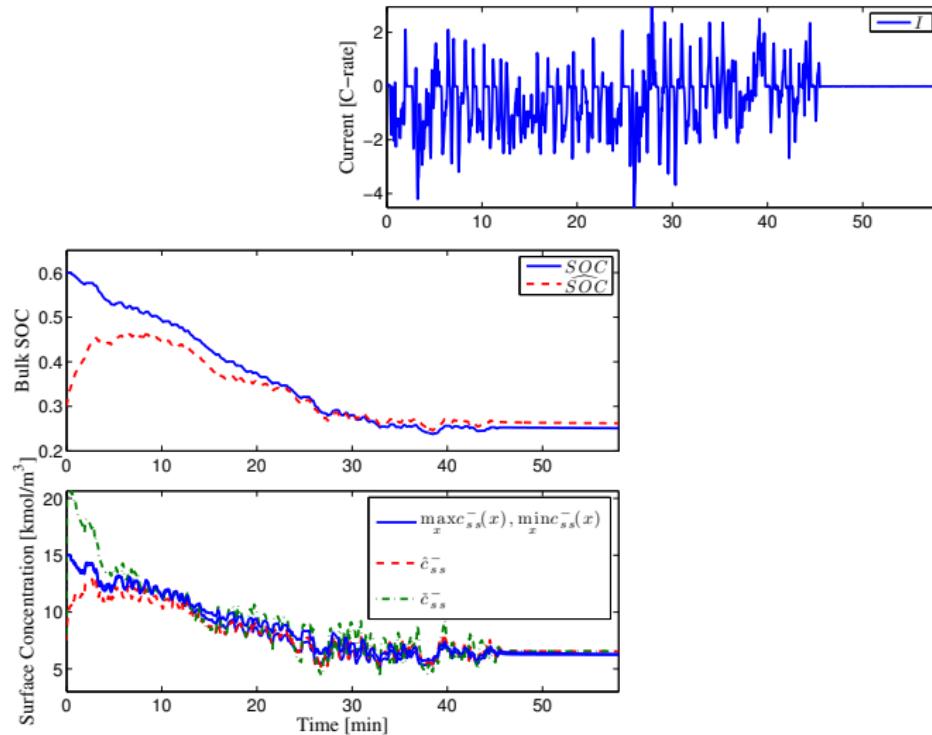
# Results

## UDDS Drive Cycle Input



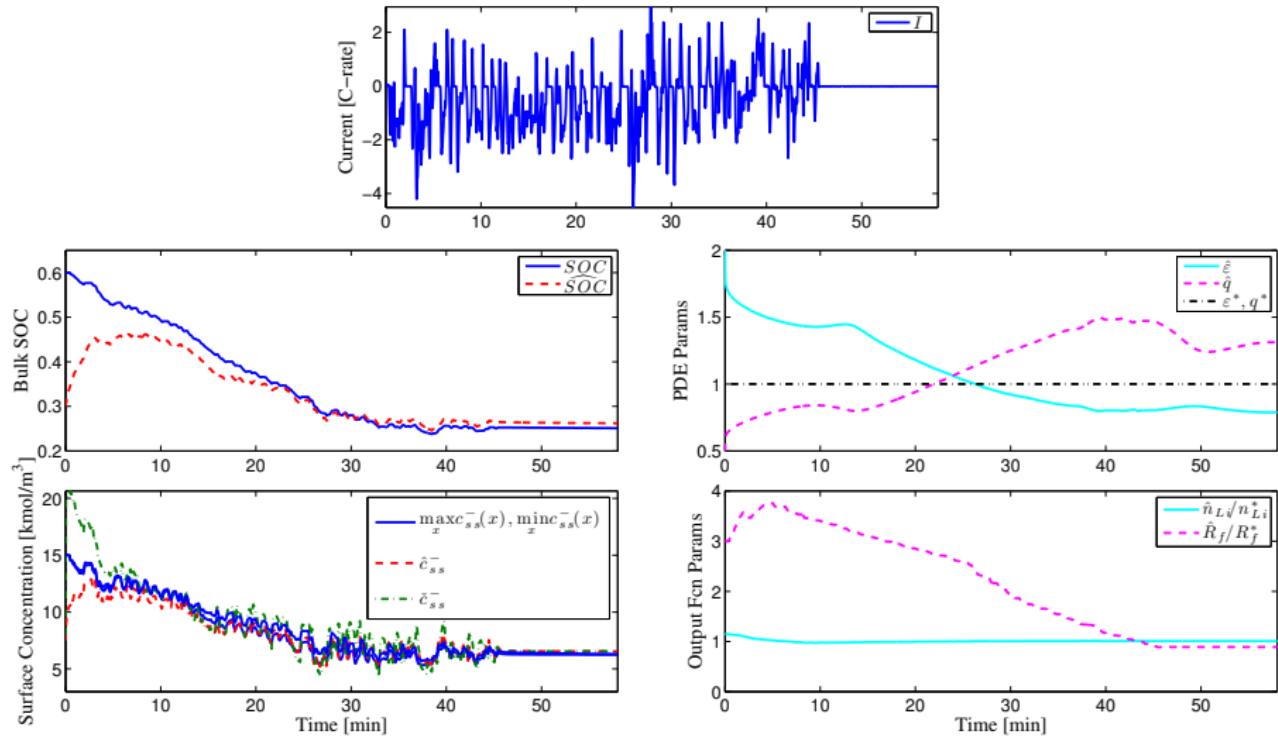
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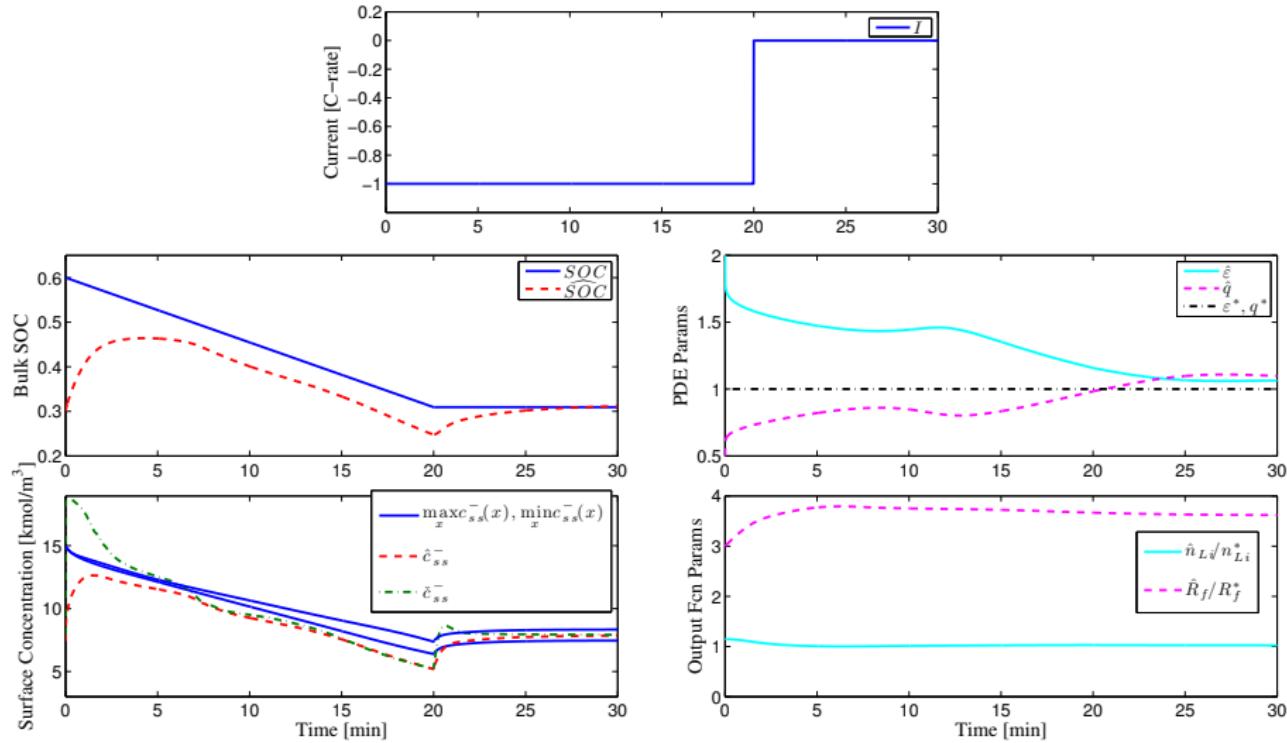
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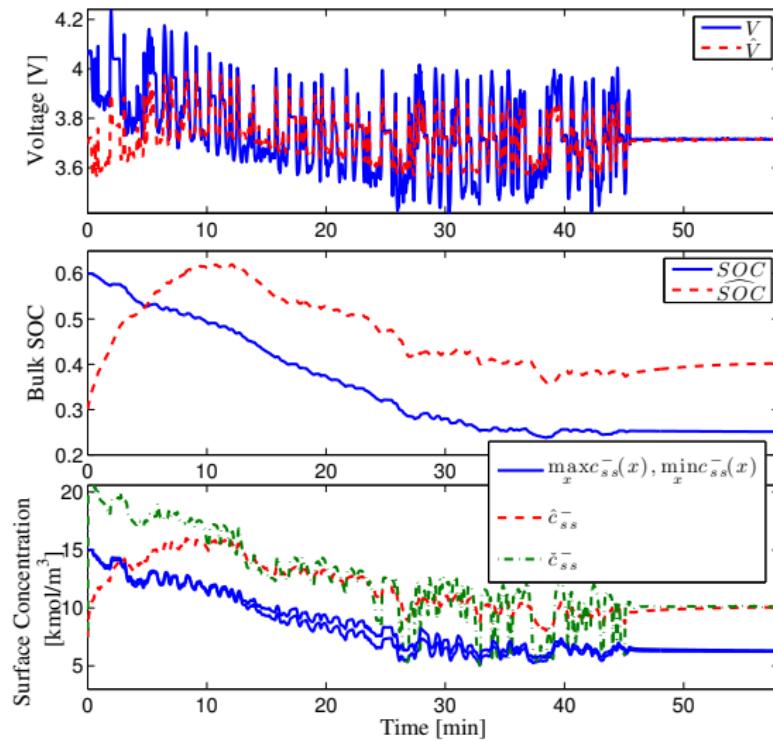
# Results

## Constant 1C Discharge



# Results

No Parameter Adaption - Bias in State Estimates



# Experimental Testing | ARPA-E AMPED Program



**BOSCH**



**COBASYS**

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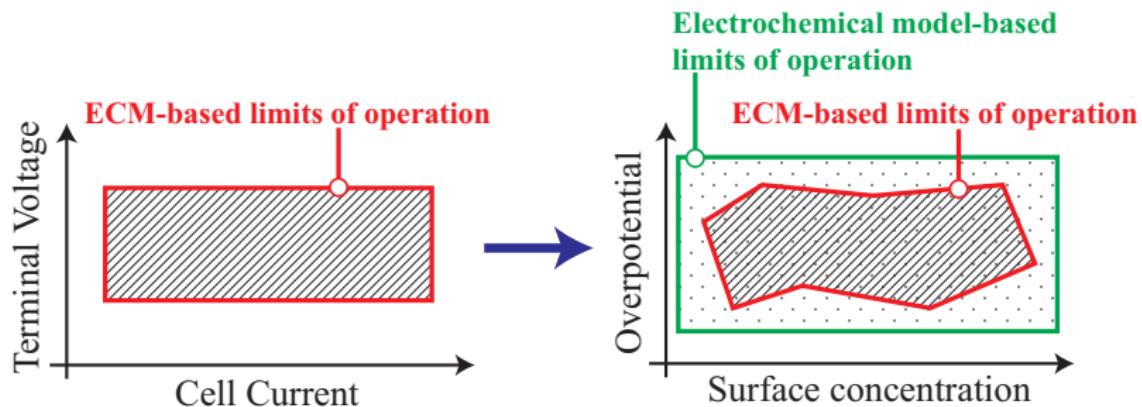
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## Problem Statement

Given accurate state estimates, govern the electric current such that safe operating constraints are satisfied.

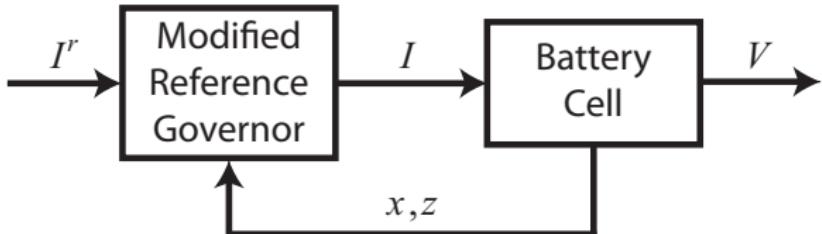


# Constraints

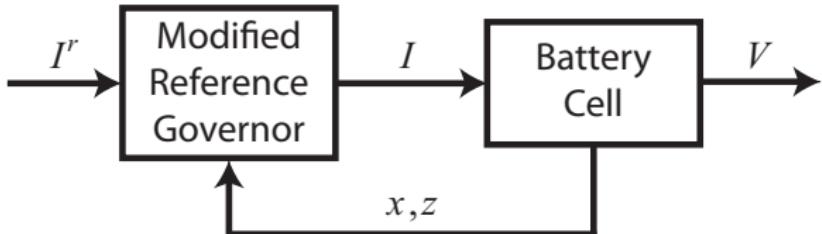
Variable	Definition	Constraint
$I(t)$	Current	Power electronics limits
$c_s^\pm(x, r, t)$	Li concentration in solid	Saturation/depletion
$\frac{\partial c_s^\pm}{\partial r}(x, r, t)$	Li concentration gradient	Diffusion-induced stress
$c_e(x, t)$	Li concentration in electrolyte	Saturation/depletion
$T(t)$	Temperature	High/low temps accel. aging
$\eta_s(x, t)$	Side-rxn overpotential	Li plating, dendrite formation

Each variable,  $y$ , must satisfy  $y_{\min} \leq y \leq y_{\max}$ .

# The Algorithm: Modified Reference Governor (MRG)



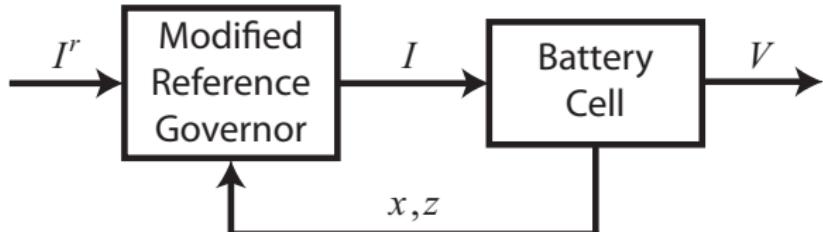
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## MRG Equations

$$I[k+1] = \beta^*[k]I^r[k], \quad \beta^* \in [0, 1],$$
$$\beta^*[k] = \max \{\beta \in [0, 1] : (x(t), z(t)) \in \mathcal{O}\}$$

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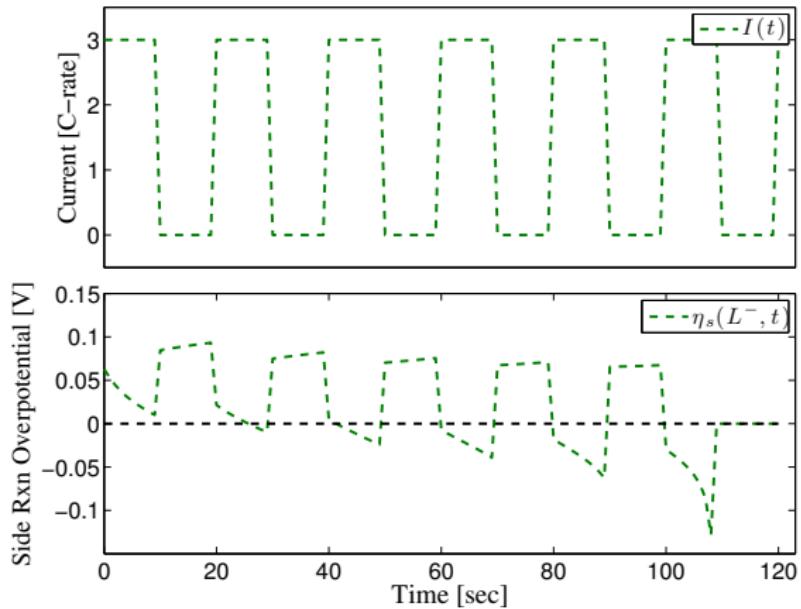
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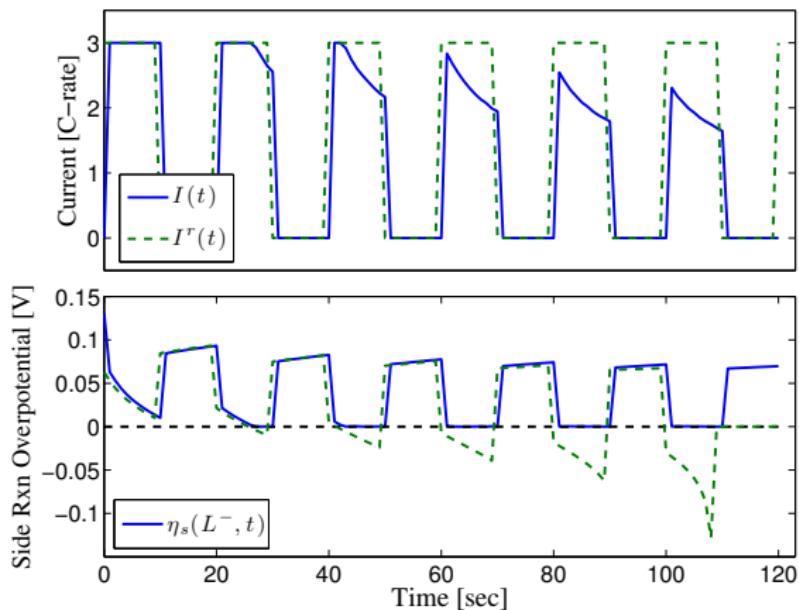
## Def'n: Admissible Set $\mathcal{O}$

$$\mathcal{O} = \{(x(t), z(t)) : y(\tau) \in \mathcal{Y}, \forall \tau \in [t, t + T_s]\}$$
$$\begin{aligned} \dot{x}(t) &= f(x(t), z(t), \beta I^r) \\ 0 &= g(x(t), z(t), \beta I^r) \\ y(t) &= C_1 x(t) + C_2 z(t) + D \cdot \beta I^r + E \end{aligned}$$

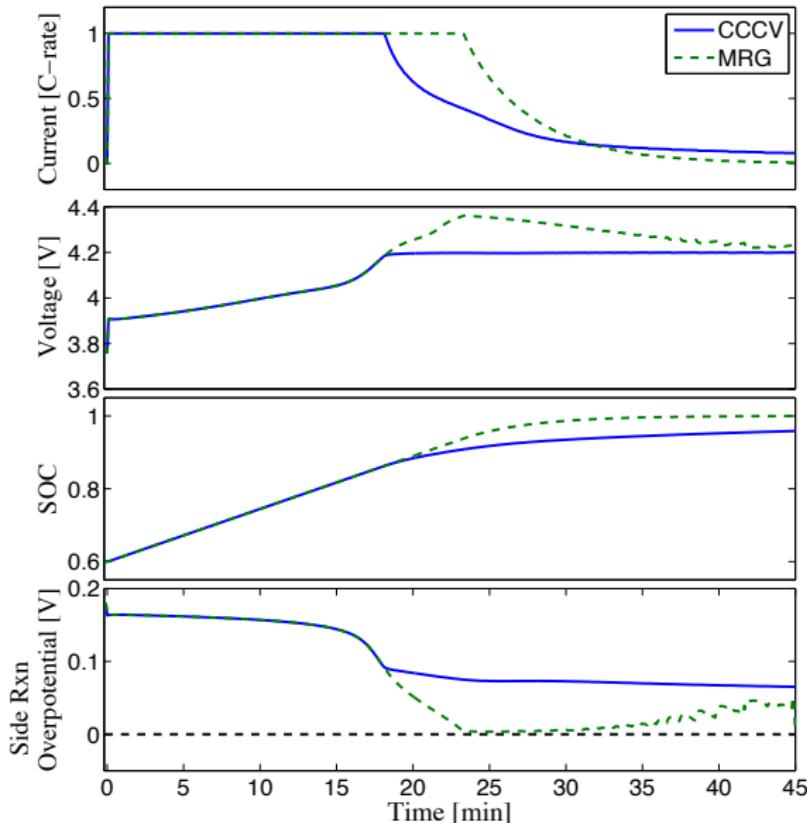
# Constrained Control of EChem States



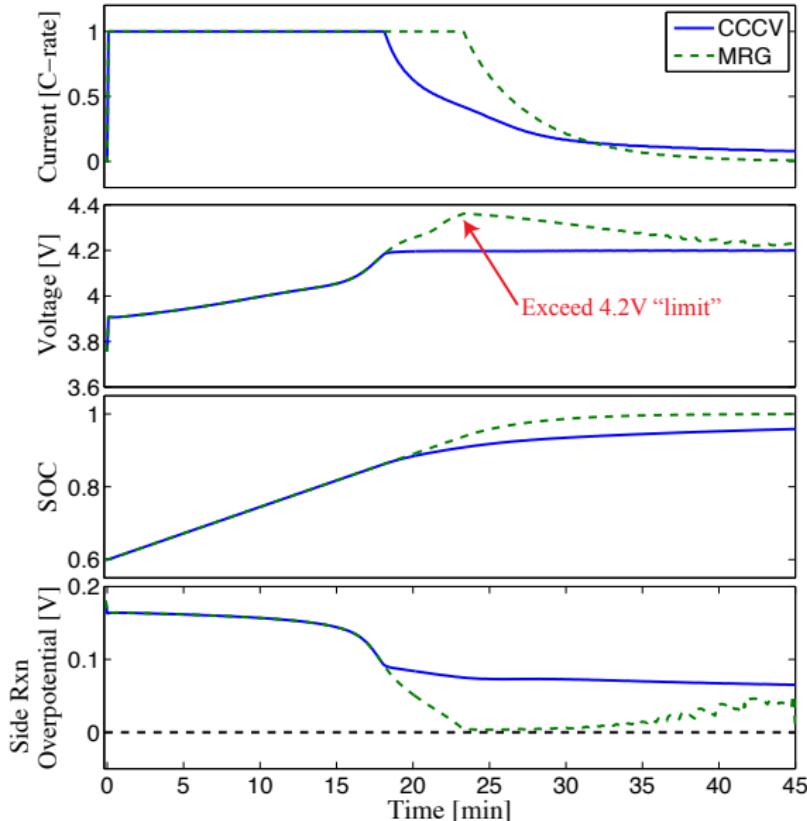
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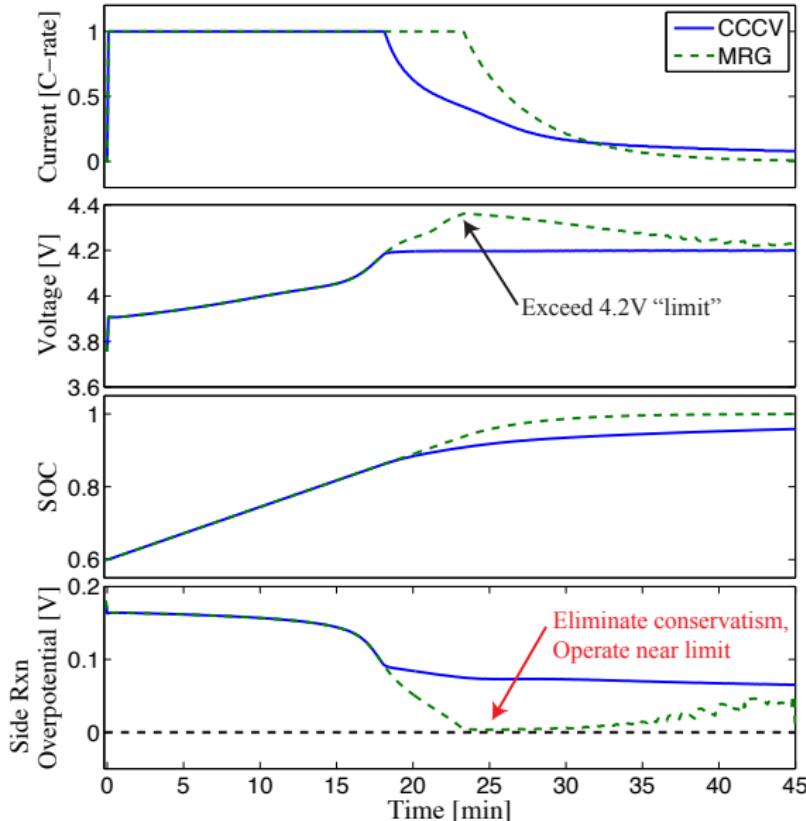
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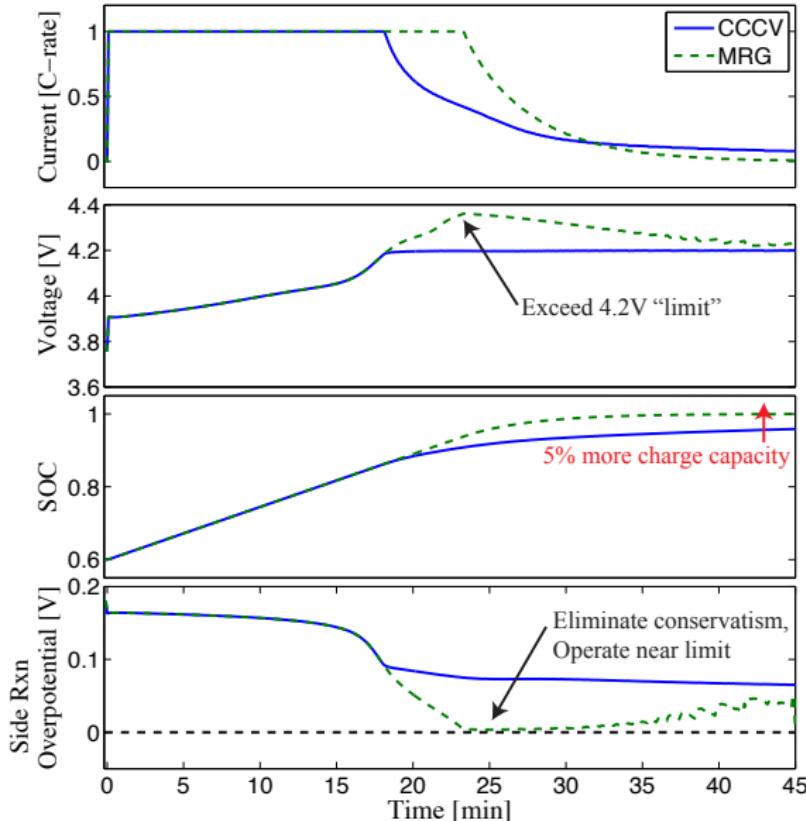
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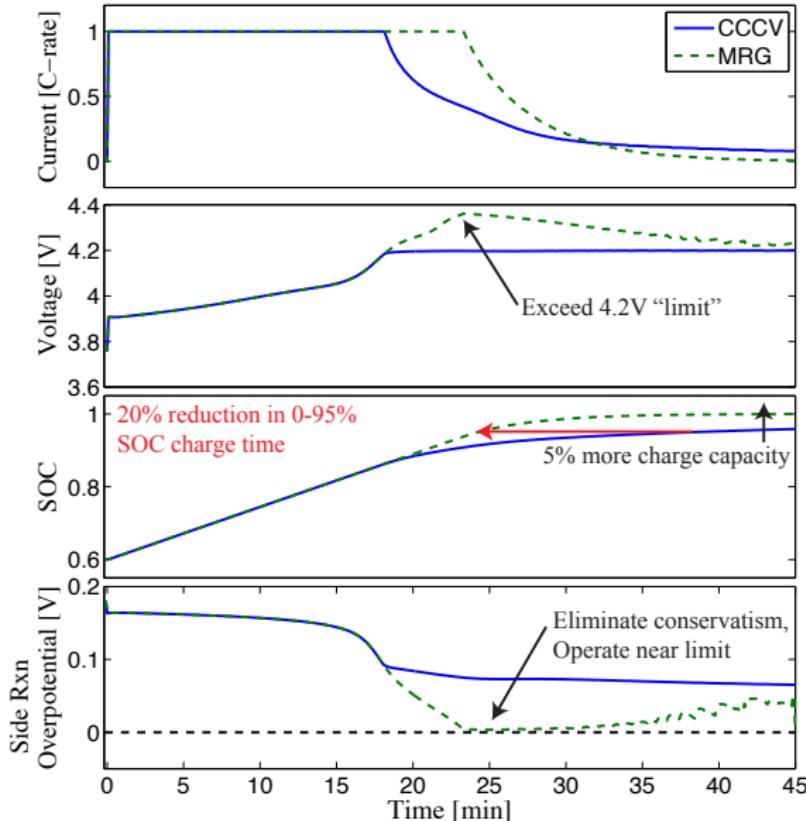
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# Outline

1

## Batteries

- [Electrochemical Modeling] Incorporating Physics
- [SOC/SOH Estimation] Looking Inside w/ Models, Meas., and Math
- [Constrained Control] Operate at the Limits, Safely
- [PHEV Power Management] Max eMPG and Max Batt Life

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## Demand Response in Smart Grids

3

## Future

# PHEV Power Management

## Problem Statement

Design a supervisory control algorithm for plug-in hybrid electric vehicles (PHEVs) that splits **engine** and **battery** power **in some optimal sense**.



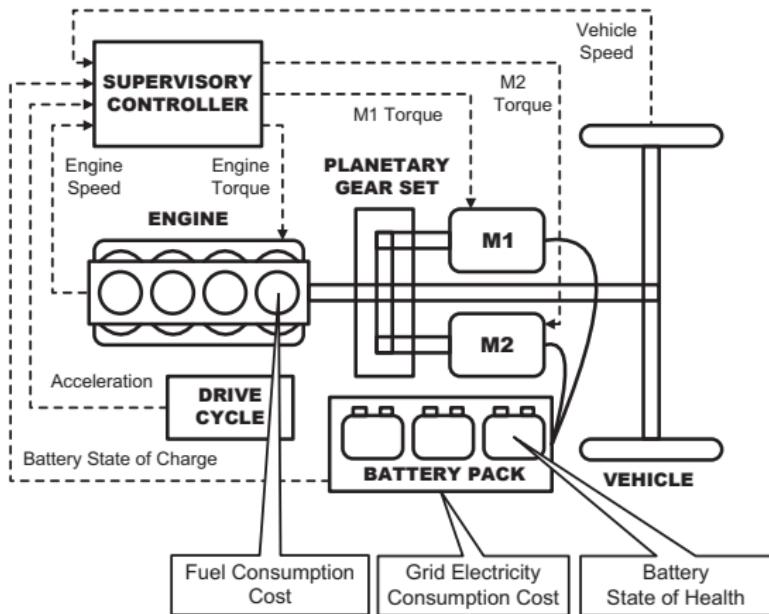
J. Voelcker, "Plugging Away in a Prius," *IEEE Spectrum*, vol. 45, pp. 30-48, 2008.



# Power-Split PHEV Model

Ex: Toyota Prius, Ford Escape Hybrid

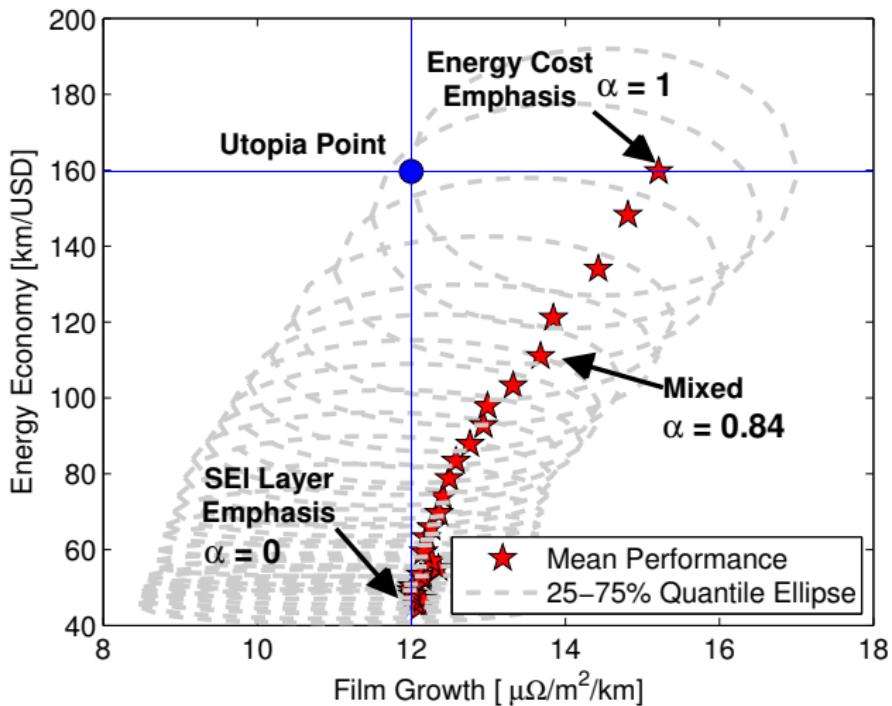
- Control Inputs
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Control Optimization: Minimize energy consumption cost AND battery aging

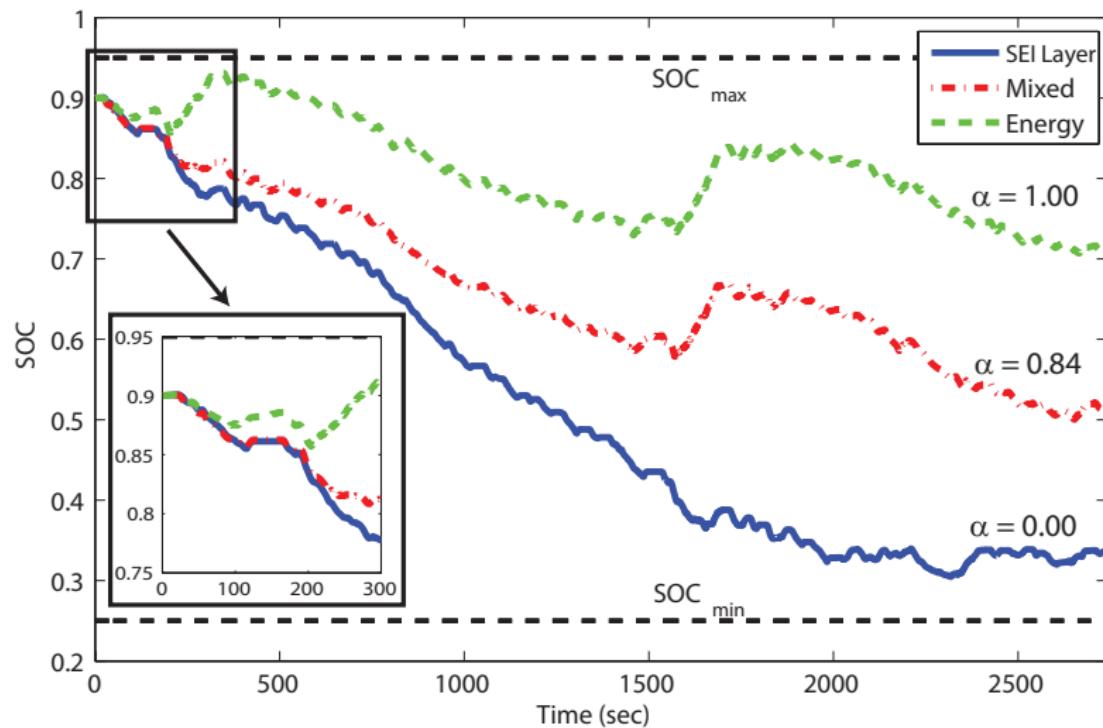
# Pareto Set of Optimal Solutions

Anode-side SEI Layer Growth



# SOC Trajectories

Anode-side SEI Layer Growth | UDDSx2



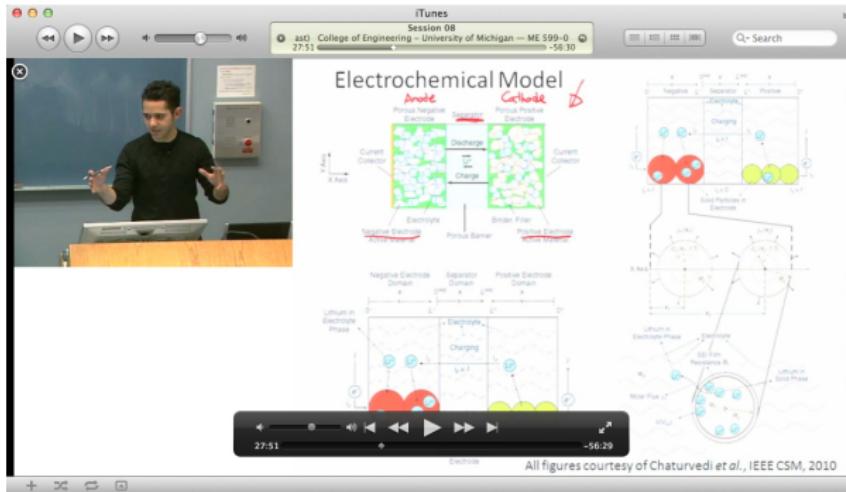
# Battery Systems and Control Course

Funded by DOE-ARRA, University of Michigan

## Enrollment

- Winter 2010: 59 + 5 distance
- Winter 2011: 50 + 26 distance
- ME, EE, ChemE, CS, Energy Systems, MatSci, Physics, Math

- Undergraduates
- Graduate students
- Professionals
  - Tesla Motors, General Motors, Roush, US Army



# Summary of Contributions

Simultaneous SOC/SOH estimation  
of physically meaningful variables via electrochemical models,  
PDE estimation theory, and adaptive control.

Constrained control of batteries  
via an electrochemical model  
and reference governors.

PHEV power management  
using electrochemical models  
and stochastic optimal control.

Impact through education.

# Energy Crisis Solutions

Integrate variable renewables



Energy storage

(e.g., batteries)

Decrease energy waste



Intelligent energy management

(e.g., smart grids)

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## 3 Future

# The Renewable Integration Problem

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50% of U.S. electricity consumption is TCLs  
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## The Punchline

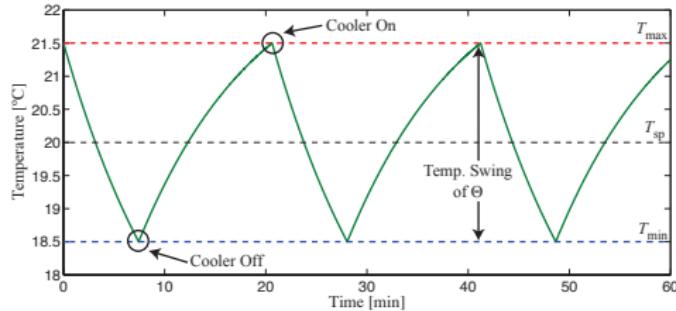
Flexible loads (e.g. TCLs) can absorb variability in renewable generation

# Modeling Aggregations of TCLs

Individual TCL  
models



(Tens of) Thousands  
of hybrid ODEs

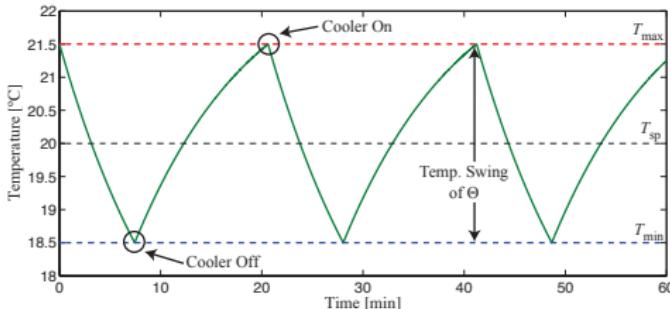


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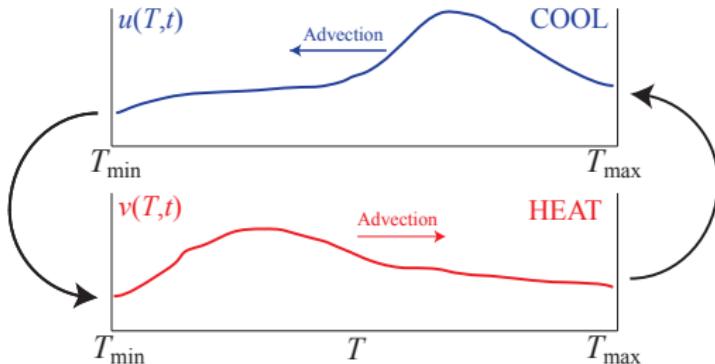
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Model aggregations  
of TCLs



Two coupled linear  
PDEs



$u(T, t)$	# TCLs/°C, in COOL state, @ temp $T$ , time $t$
$v(T, t)$	# TCLs/°C, in HEAT state, @ temp $T$ , time $t$

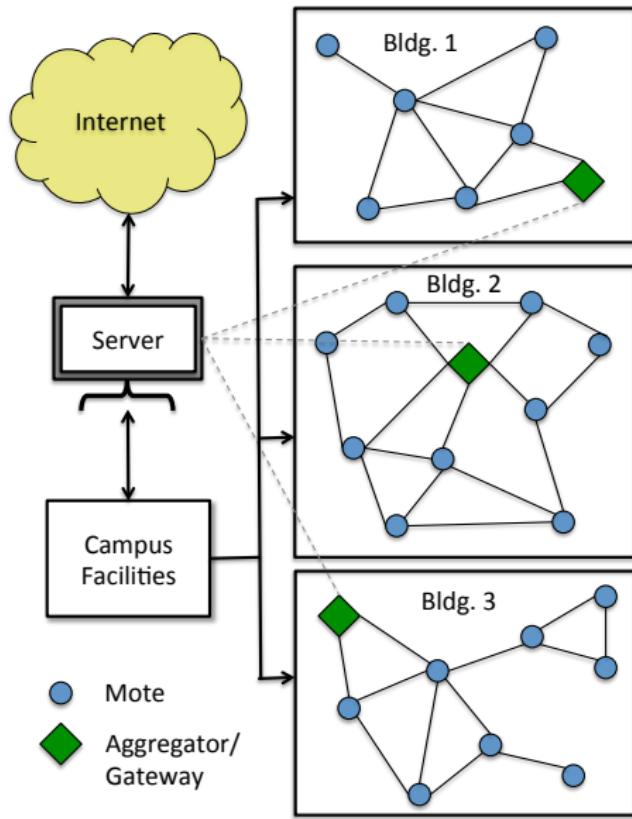
# UCSD Campus: A Living Laboratory

## Goal: Smart Campus

- ① Deploy temp. wireless sensor network
- ② Verify models and estimation algorithms
- ③ Derive control algorithms
- ④ Implement via UCSD facilities & management



Libelium Waspmotes and Meshlium Gateway

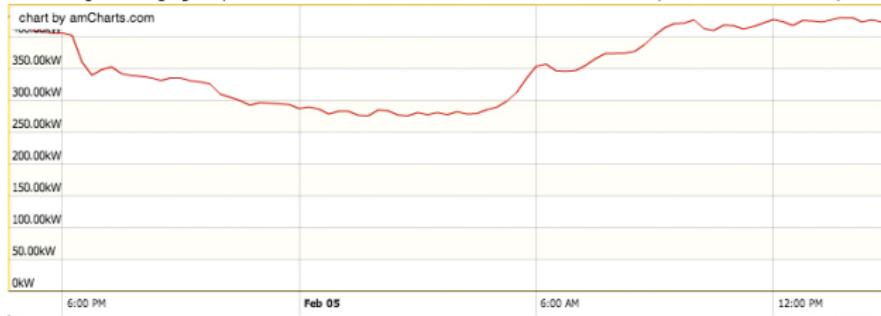


[Login](#)[Home](#) | [My Dashboard](#) | [Campus Meters](#) | [Research](#) | [About](#)

CSE Building / EBU3B &gt; Campus Meter

[Fast version](#) | [Meter Graph](#) | [Time Comparison](#) | [Add to compare list](#)**Device Information****Name:** EBU3B Total Power Usage**Description:** Total power usage for the CSE building through the two sub station meters. Combined mechanical, lighting, plug, and server room.**Overall Energy Statistics****kW-Hours:** 60162.96 kW-H**Average kW:** 358.11 kW**Energy costs:** \$7821.18**Power consumption for EBU3B Total Power Usage****From:** Jan, 29, 2013 05:12:49 PM    **Resolution:** Every 15 minutes (averaged)  
**To:** Feb, 05, 2013 05:12:49 PM    **Timespan:** 7 days

- 1st Average kW in highlighted period: 358.11 kW



energy.ucsd.edu

Fuse data from Dr. Yuvraj Agarwal's Energy Dashboard project

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# Future: EChem-based Battery Management Systems

**Vision:** Enhanced energy, power, chg times, life from existing batts.

**Open technical problems for BMS:**

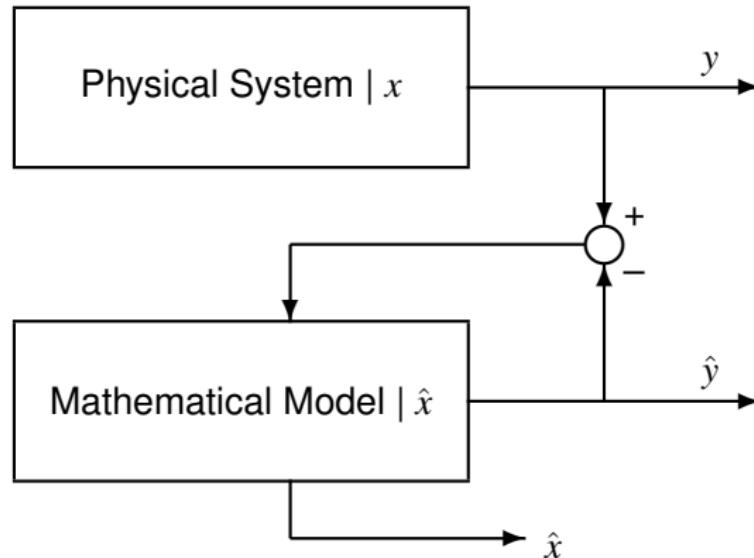
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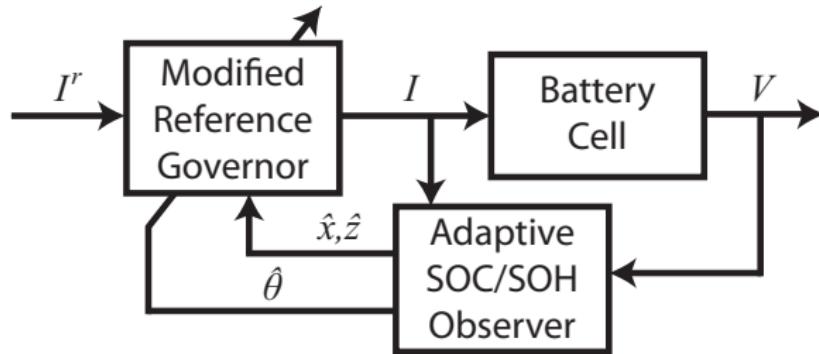


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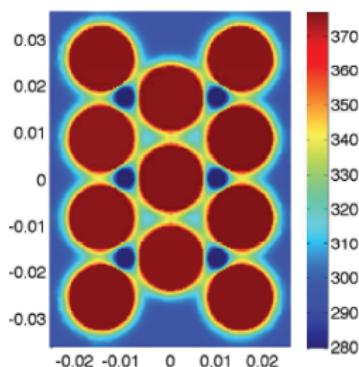
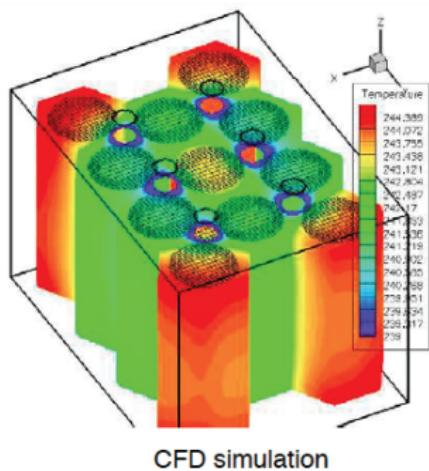


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## **Funding:**

- ARPA-E AMPED
- DoD HESM

# Future: EV Urban Mobility

**Goal:** Solve range anxiety

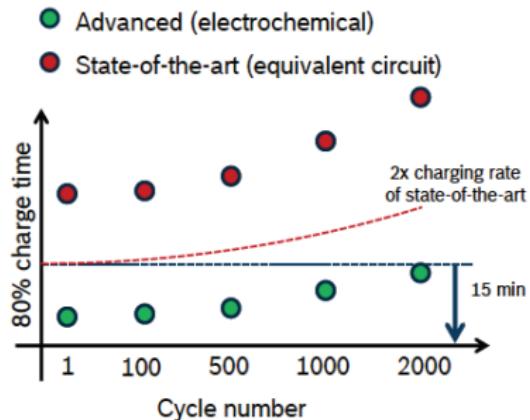
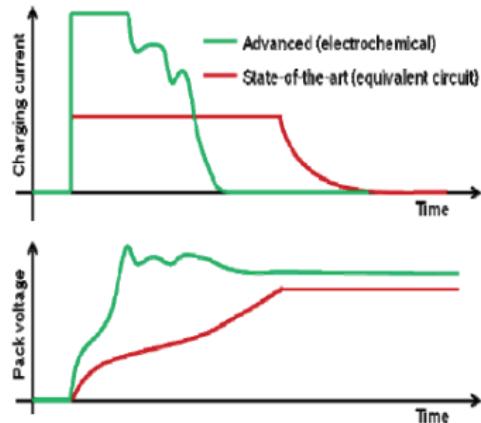
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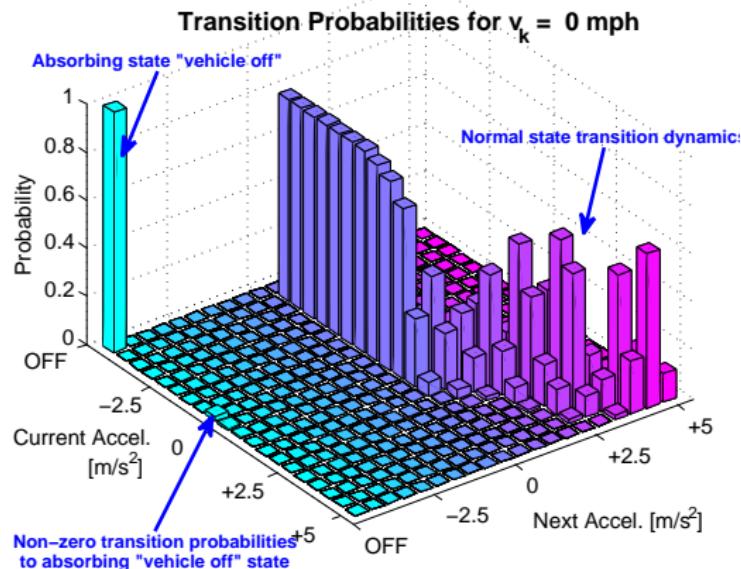
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Adaptive Markov chain model:  $p_{ijm} = \Pr(a_{k+1} = j | a_k = i, v_k = m)$



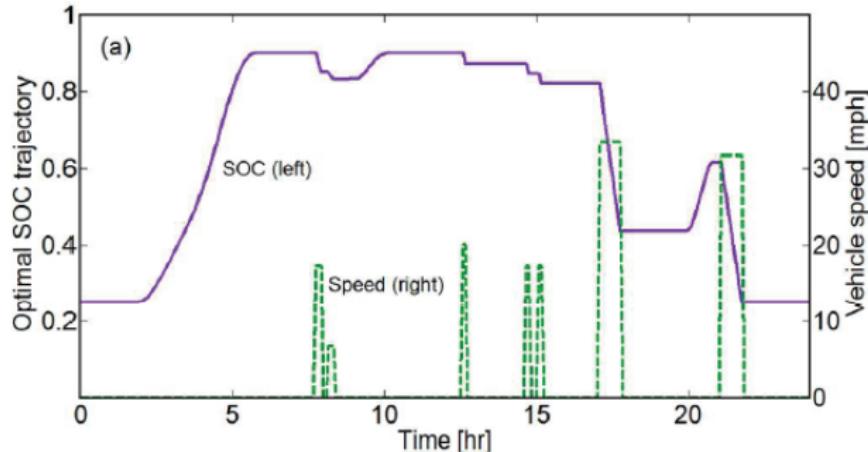
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- Satisfy range req.
- Max health, min energy consumption
- Grid interface for city-wide resilience



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**Vision:** Fully automated and adaptive building energy management.

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$$u_t(x, t) = \alpha\lambda(x)u_x + \alpha u + \beta u_{xx}$$

$$v_t(x, t) = -\alpha\mu(x)v_x + \alpha v + \beta v_{xx}$$

$$u(1, t) = q_1 v(1, t), \quad u_x(0, t) = -v_x(0, t)$$

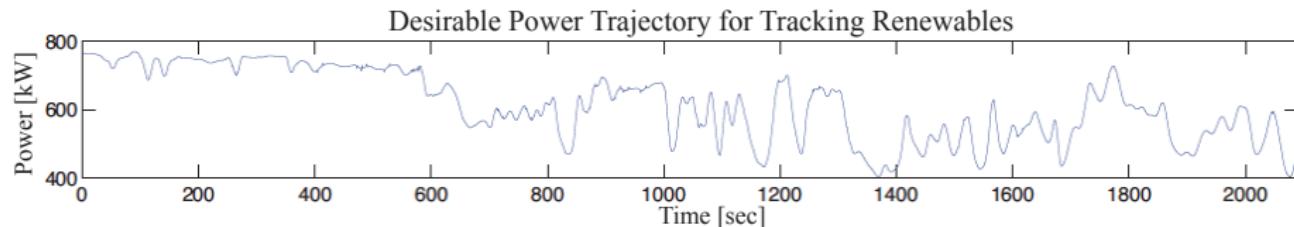
$$v(0, t) = q_2 u(0, t), \quad v_x(1, t) = -u_x(1, t)$$

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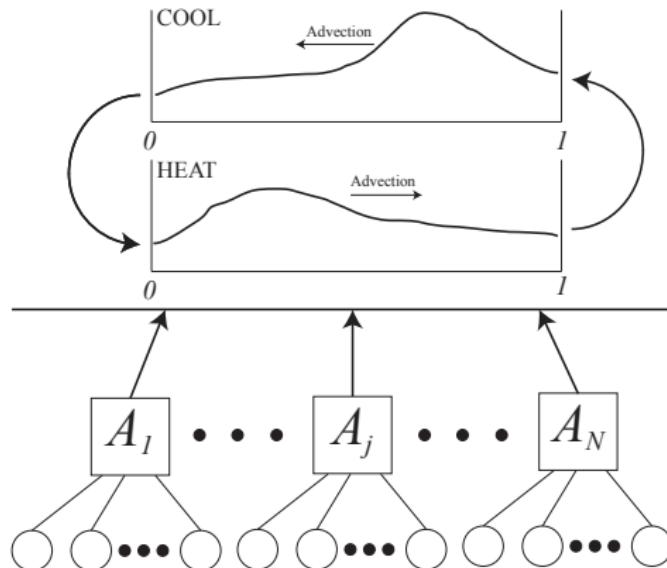


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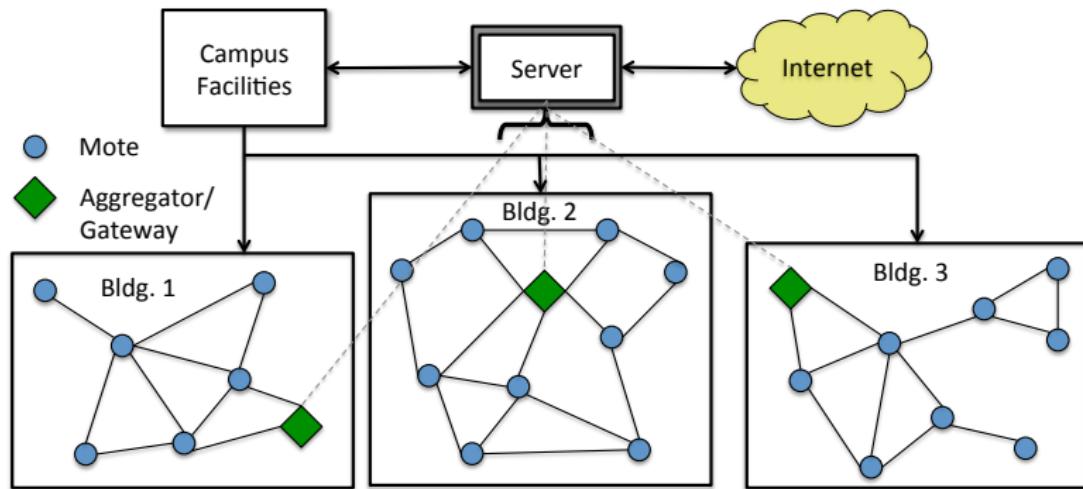


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- Nest Labs, Palo Alto
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## Funding:

- California Energy Commission
- NSF EPAS, CPS

# Courses I could teach

## **Undergrad**

MAE 154 - Mechatronics

MAE 171 - Analysis, Simulation and Design of Mechatronic Systems

MAE 172 - Automatic Control of Engineering Systems

## **Graduate**

MAE 218 - Advanced Energy Systems

MAE 272 - Theory and Design of Control Systems

MAE 274 - Analysis and Design of Digital Control Systems

# Energy Systems and Control Laboratory

**Themes:** Energy | Control systems

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## Key Tools:

- PDE modeling
- Lyapunov stability
- Adaptive control
- Optimization

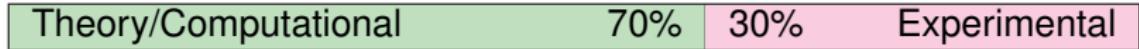
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## Outreach, Diversity, and Inclusion

- SHPE, NSBE, SWE
- C-STEM, UC LEADs

The background of the slide is a composite image. At the top, a wind turbine stands against a clear blue sky with a few wispy clouds. A bright sun is positioned to the right of the tower, casting a lens flare. Below the wind turbine, several large blue solar panels are arranged in a row. In the foreground, there is a cluster of vibrant yellow sunflowers. The overall theme of the image is renewable energy and sustainable development.

Publications available at <http://flyingv.ucsd.edu/smoura/>  
[smoura@ucsd.edu](mailto:smoura@ucsd.edu)

# Managing Overparameterization

$$\hat{\theta}_{pde} = \begin{bmatrix} \widehat{q\varepsilon^2} \\ \widehat{q\varepsilon} \\ \widehat{\varepsilon} \end{bmatrix} \rightarrow \begin{bmatrix} \hat{\varepsilon} \\ \hat{q} \end{bmatrix} = \hat{\theta}_{\varepsilon q}$$

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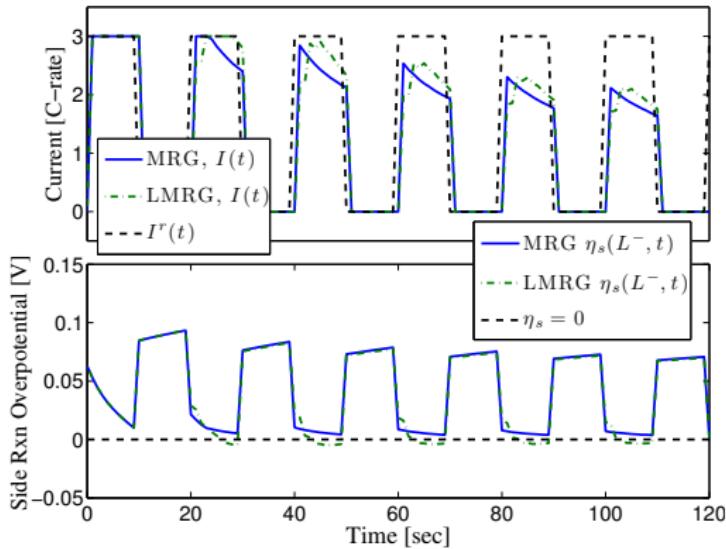
$$\log(\hat{\theta}_{\varepsilon q}) = A_{\varepsilon q}^+ \log(\hat{\theta}_{pde})$$

Remark:  $A_{\varepsilon q}^+ = (A_{\varepsilon q}^T A_{\varepsilon q})^{-1} A_{\varepsilon q}^T$  is the Moore-Penrose pseudoinverse of  $A_{\varepsilon q}$

# Linear Reference Governor

Modified Reference Governor (MRG) : Simulations

Linearized MRG (LMRG) : Explicit function evaluation



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## Problem Statement

Design a supervisory control algorithm for plug-in hybrid electric vehicles (PHEVs) that splits **engine** and **battery** power **in some optimal sense**.



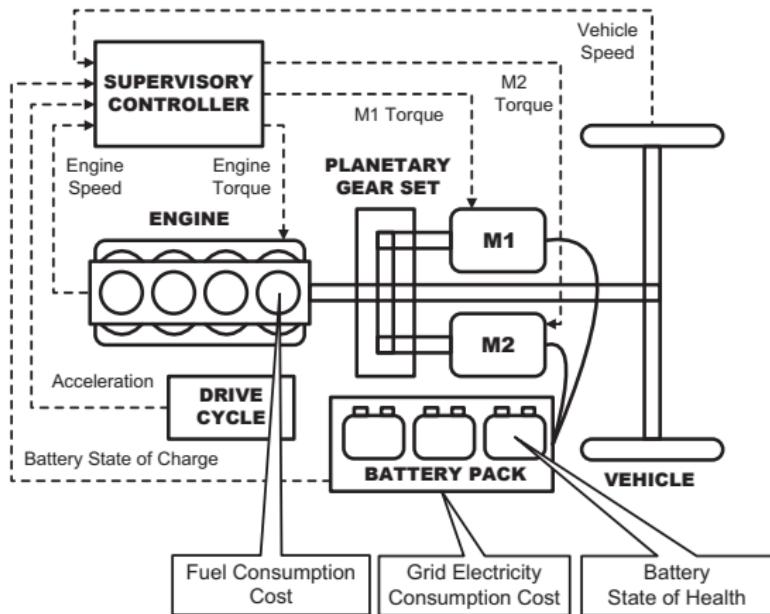
J. Voelcker, "Plugging Away in a Prius," *IEEE Spectrum*, vol. 45, pp. 30-48, 2008.



# Power-Split PHEV Model

Ex: Toyota Prius, Ford Escape Hybrid

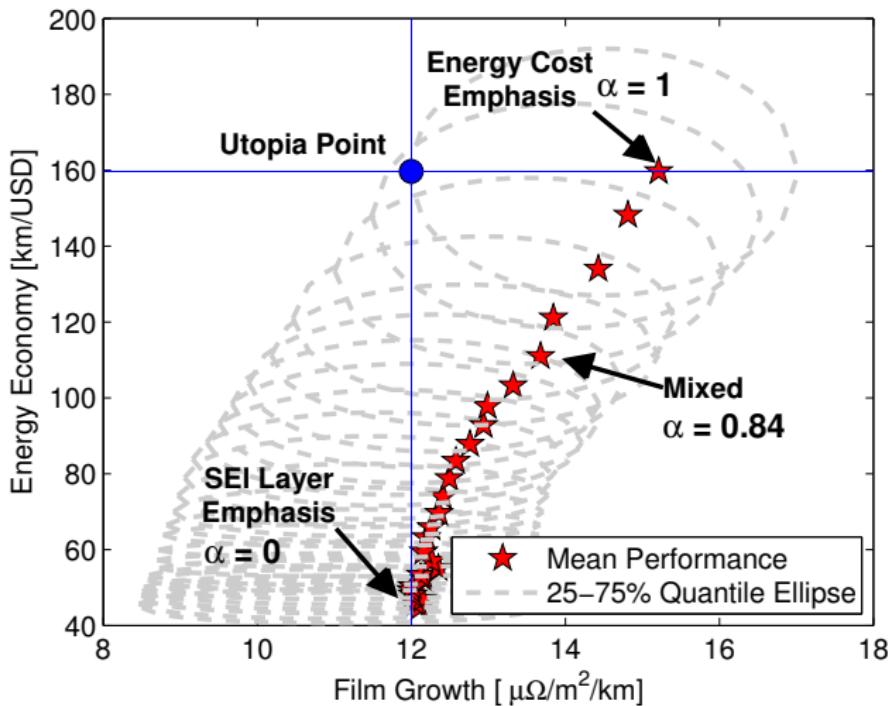
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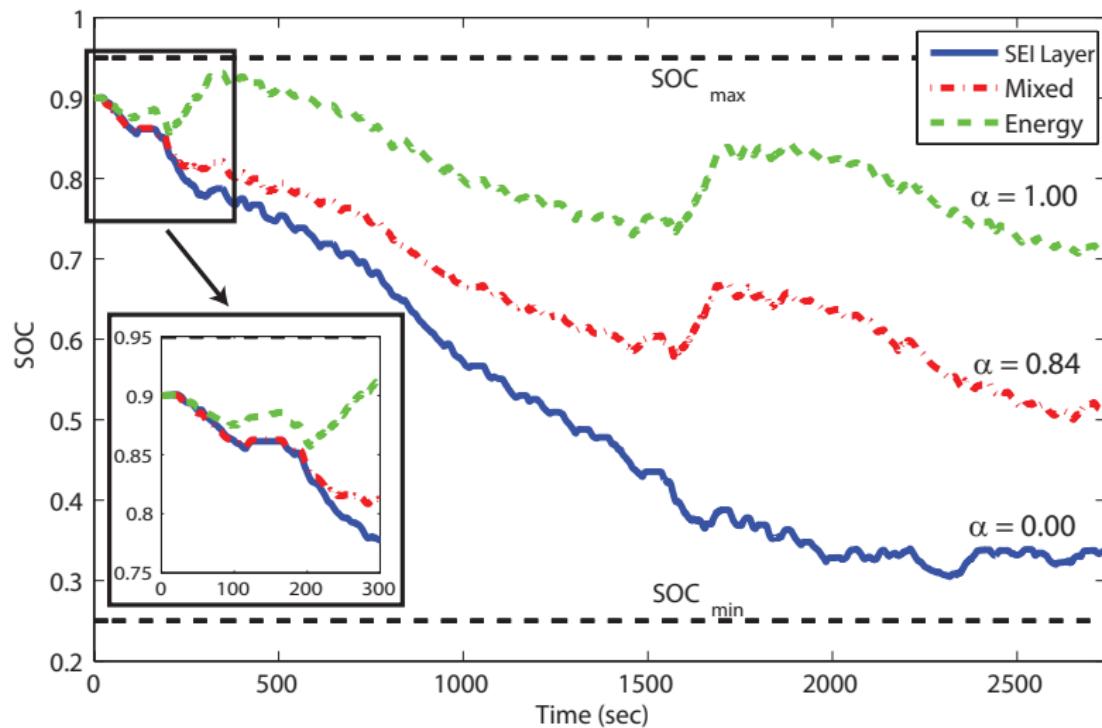
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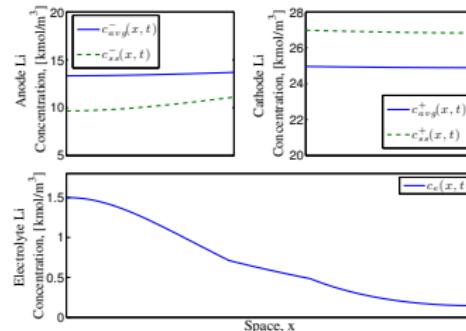
Anode-side SEI Layer Growth | UDDSx2



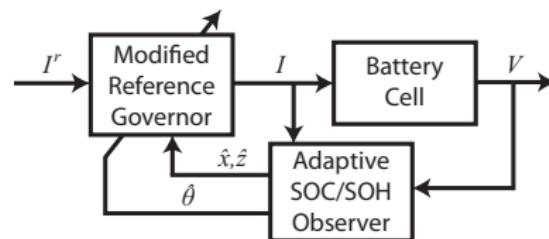
# Advanced Battery Management Systems

ARPA-E

## State Estimation w/ Electrolyte



## Estimator + Reference Governor



## Optimal charge/discharge

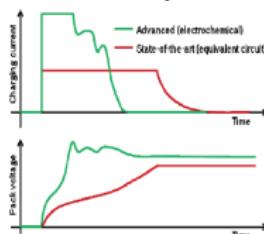


Figure 2: Charging phase of each duty cycle for BMS validation

## Thermal Management

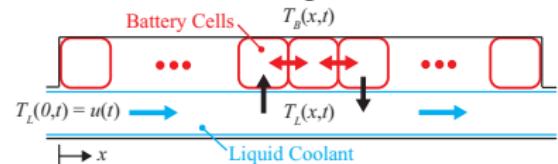


Figure 3: Comparison of charging time on a cycle to cycle basis for conventional BMS and advanced BMS

# Optimal Control of Distributed Parameter Systems

## Models

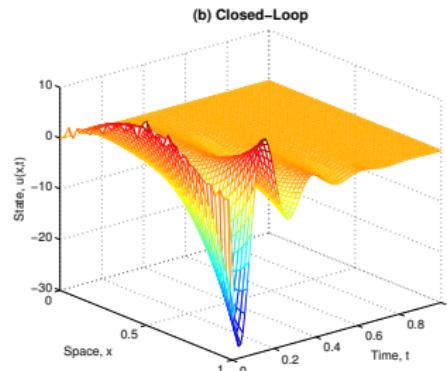
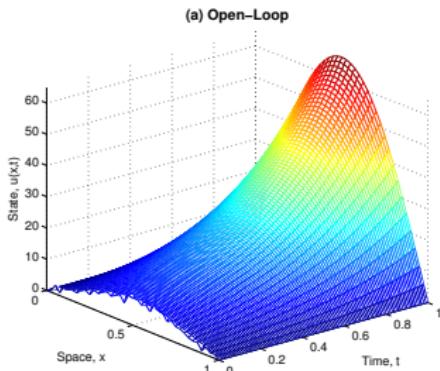
- Diffusion-Reaction-Advection
- Transport, Delays
- Waves, Beams, Nonlinear
- ...

## Apps

- Fluid Dynamics
- Contaminant transport
- Solar Forecasting
- Heat Transfer
- ...

## Control Results

- LQR
- Reference tracking
- Estimation
- Actuator/Sensor placement
- ...



# Demand Response of Aggregated Storage

Joint Work with Jan Bendsten, Aalborg University, Denmark

