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# PI Tuning via Extremum Seeking Methods for Cruise Control

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# Motivation

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- Automated PID Tuning Method
  - Online control synthesis
  - Achieve optimal performance in some sense
  - Reduces calibration time
  - Does not require knowledge of plant
  - Does not require special experiments
- Can ES be used as an adaptive control law?
  - Real-time controller adaptation
  - Varying plant parameters and dynamics
  - Varying disturbance inputs



# Reference Paper

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## PID Tuning Using Extremum Seeking Online, Model-Free Performance Optimization

Nick J. Killingsworth and Miroslav Krstic

*IEEE Control Systems Magazine*  
February 2006



# Literature Review

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## Closed-loop (model free) PID parameter tuning

### Relay Feedback Tuning

- Åström *et al* (1984)
- Leva (1993)
- Voda *et al* (1995)

### Unfalsified Control

- Jun *et al* (1999)
- Saeki *et al* (2003, 2004)

### Iterative Feedback Tuning

- Hjalmarsson *et al* (1998)
- Lequin *et al* (1999, 2003)



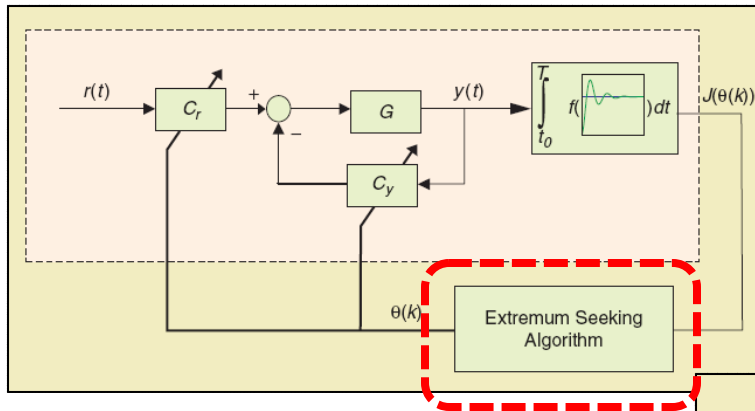
# Outline

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- Motivation & Literature Review
- Paper Reproduction
  - Extremum Seeking (ES) Algorithm
  - PID Tuning on Sample Plant
  - ES Parameter Sensitivity
- Case Study: Adaptive Cruise Control
  - Cruise Control Model
  - PI Tuning
    - Vary Desired Velocity, Fix Road Grade
    - Vary Road Grade, Fix Desired Velocity
    - Vahidi Road Grade Profile (I-15 near San Diego)
- Summary & Conclusions



# Extremum Seeking Algorithm



E.S. Algorithm Design

$\theta$  PID parameters

$J$  Cost

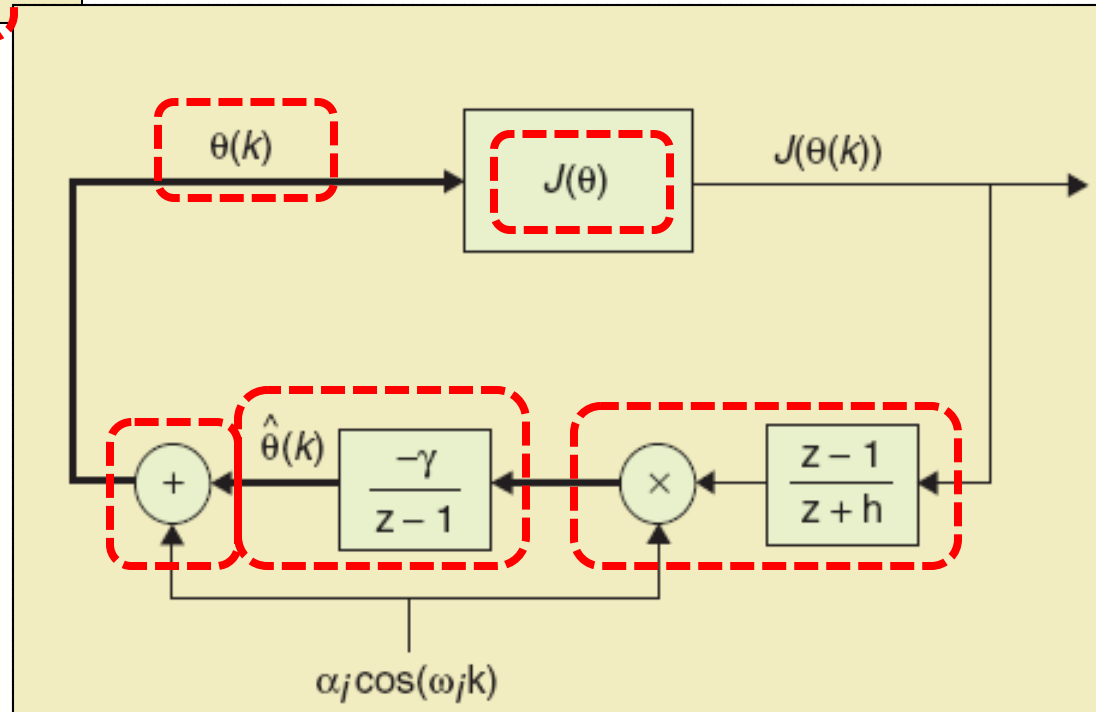
$h$  Washout filter cutoff freq

$\omega_i$  Perturbation freq.

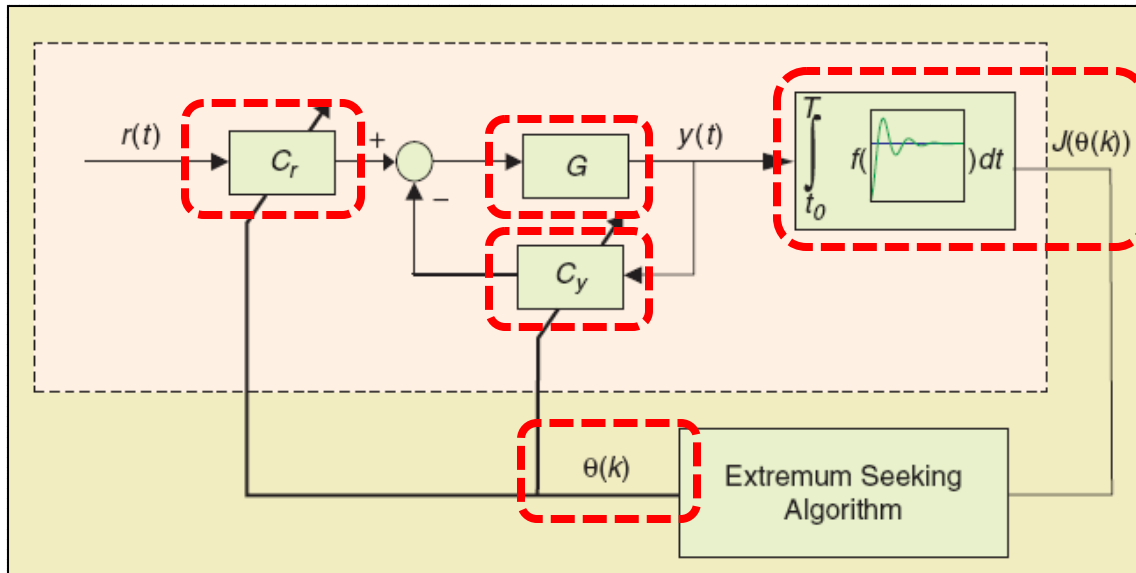
$\alpha_i$  Perturbation amplitude

$\gamma$  Adaptation gain

$\hat{\theta}$  PID parameters estimate



# Control Problem Formulation



Plant:

$$G(s) = \frac{1}{1 + 20s} e^{-20s}$$

Controller:

$$C_r(s) = K \left( 1 + \frac{1}{T_i s} \right)$$

$$C_y(s) = K \left( 1 + \frac{1}{T_i s} + T_d s \right)$$

Cost Function:

$$J(\theta) = \frac{1}{T - t_0} \int_{t_0}^T e^2(t, \theta) dt$$

$$e(t, \theta) = r(t) - y(t, \theta)$$

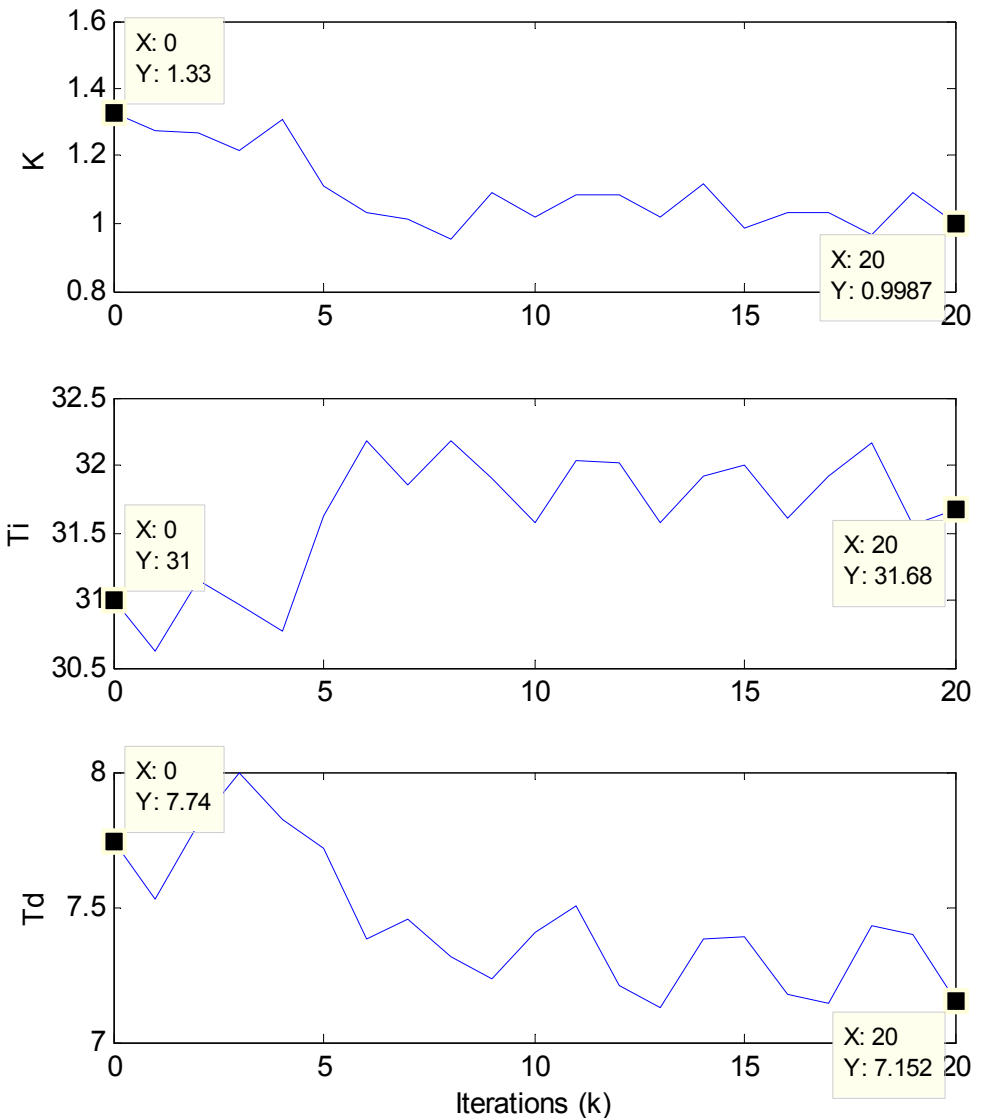
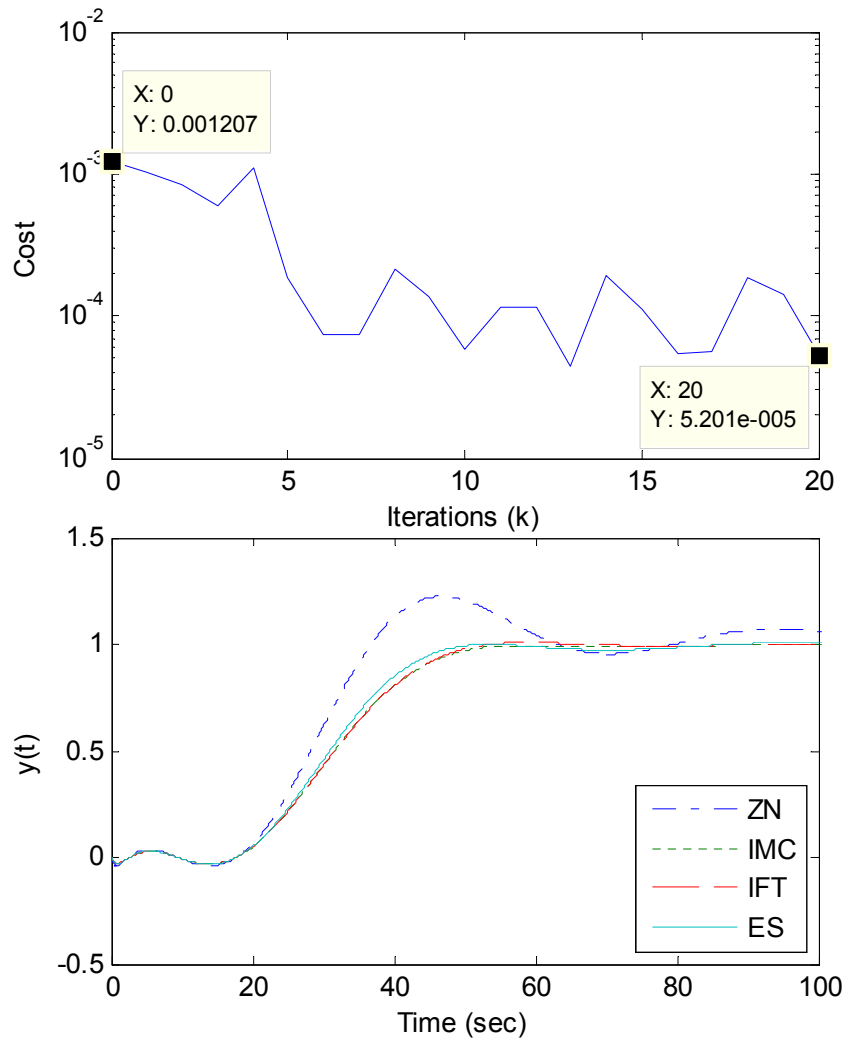
Tuning Parameters:

$$\theta = [K \quad T_i \quad T_d]^T$$



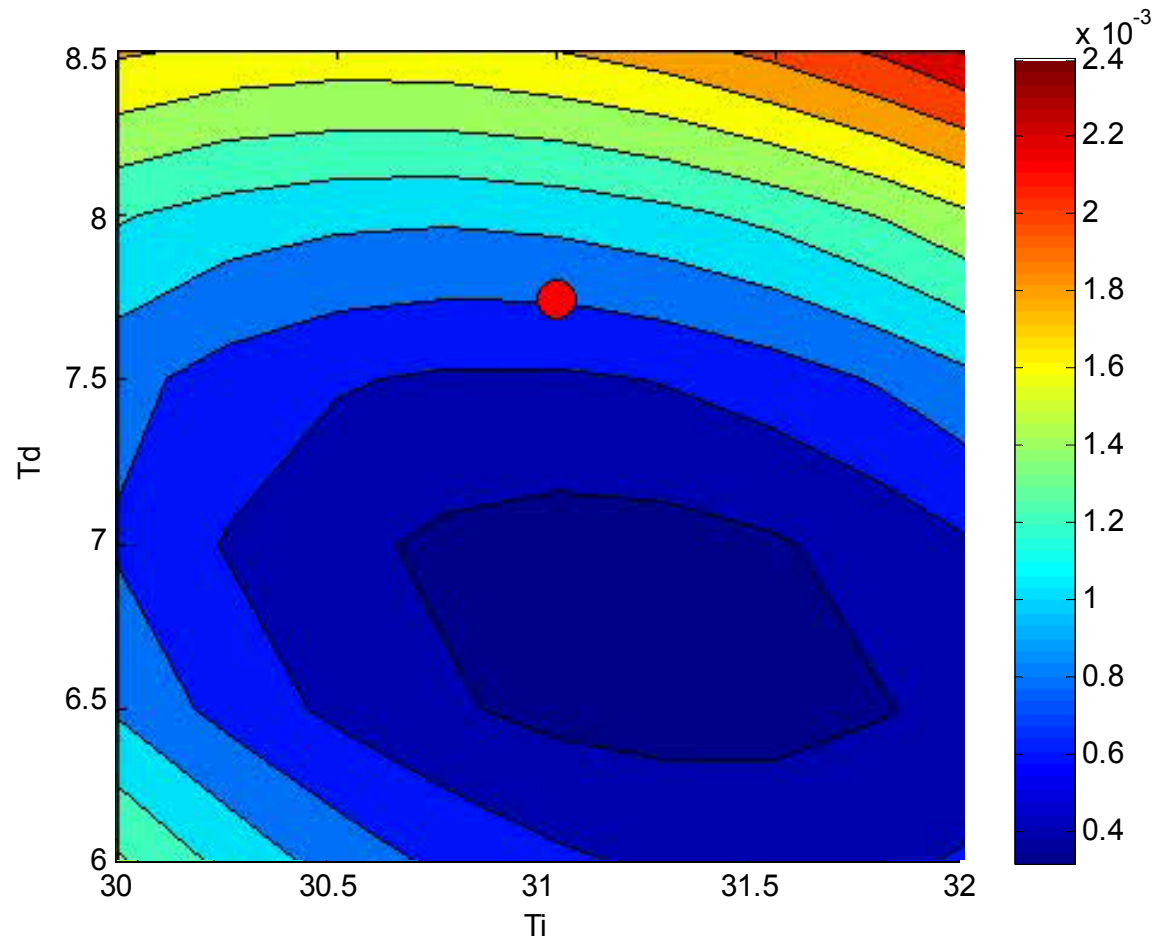
# PID Tuning on Sample Plant

Use Ziegler-Nichols as initial gains





# PID Gain Trajectories wrt Cost

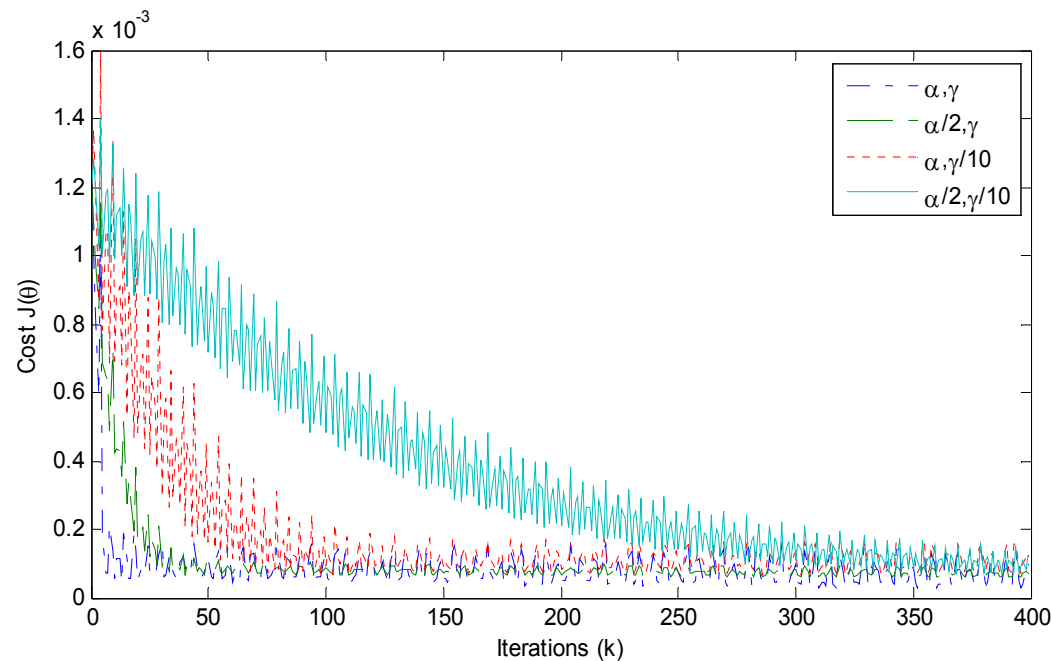


Cross-section of cost as a function of  $T_d$  and  $T_i$   
Fixed  $K$



# Varying ES Parameters

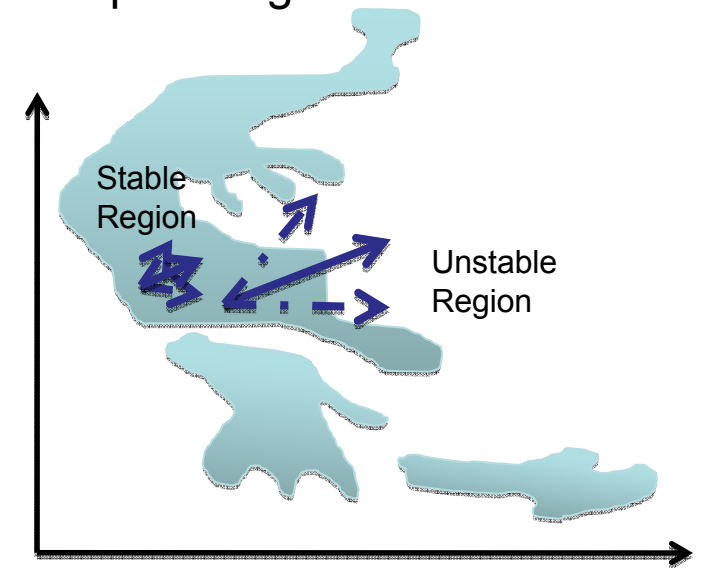
How sensitive are the results to the choice of the ES parameters?



## Recall

$\alpha_i$  Perturbation amplitude

$\gamma$  Adaptation gain



## Killingsworth's Answer      Our Answer

"fairly insensitive"

- Insensitive for more conservative values
- VERY sensitive for more aggressive values



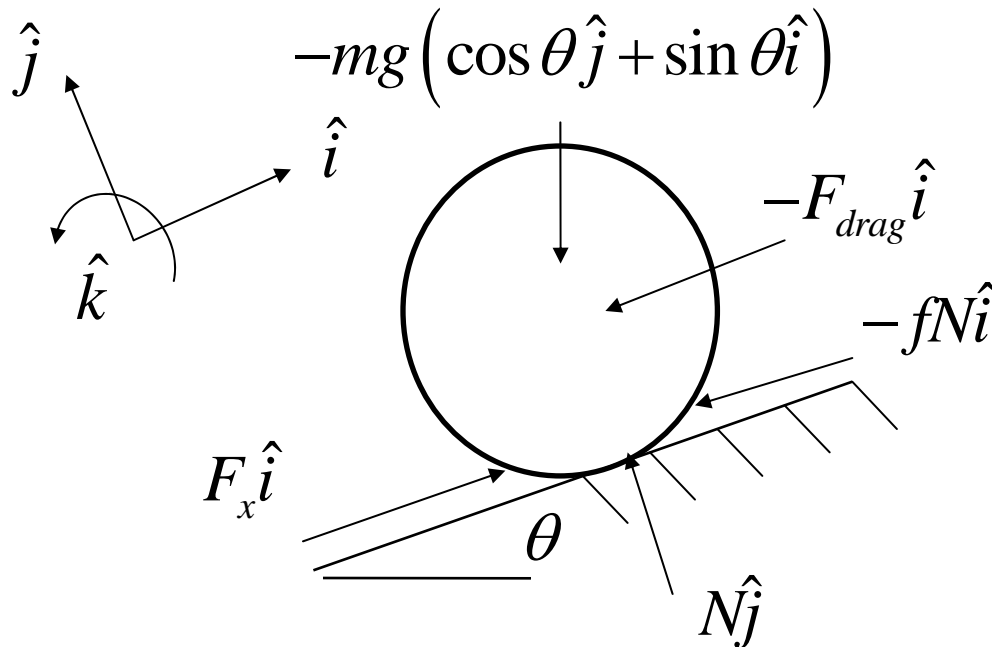
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# Case Study

## Adaptive Cruise Control



# Vehicle Dynamics Model



## Assumptions

- Rolling disk dynamics
- No wheel slip
- No actuator dynamics
- Coulomb friction

$$m\mathbf{a} \cdot \hat{i} = F_x - mg \sin \theta - fN - F_{drag}$$

$$m\mathbf{a} \cdot \hat{j} = N - mg \cos \theta = 0$$

$$F_{drag} = 0.5 \rho A C_d (v + v_w)^2$$

$$N = mg \cos \theta$$

Wind Speed

$$m \frac{dv}{dt} = F_x - mg \sin \theta - fmg \cos \theta - 0.5 \rho A C_d (v + v_w)^2$$

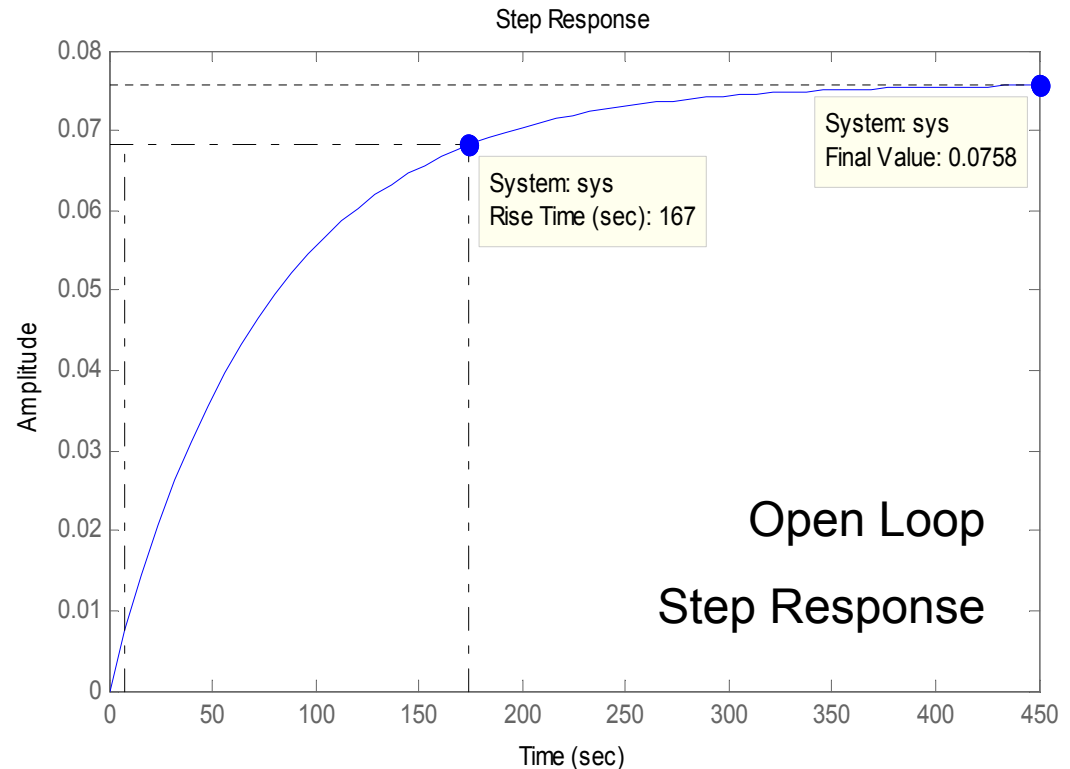


# Linearization and Ziegler-Nichols

$$\delta \dot{v} = -\frac{1}{m} \rho A C_d (v_0 + v_w) \delta v + \frac{1}{m} \delta F_x + \frac{1}{m} [-mg \cos \theta_0 + fmg \sin \theta_0] \delta \theta$$

Variable	Nominal Value
Traction Force, $F_x$	293 N
Road Grade, $\theta$	0 radians
Wind Speed, $v_w$	2 m/s
Vehicle Speed, $v$	20 m/s $\approx$ 45 mph

$$\frac{Y(s)}{U(s)} = \frac{0.0758}{75.75s + 1} = \frac{K}{\tau s + 1}$$



PI Controller:

$$C(s) = K_{PI} \frac{\tau_{PI}s + 1}{s}$$

Ziegler-Nichols

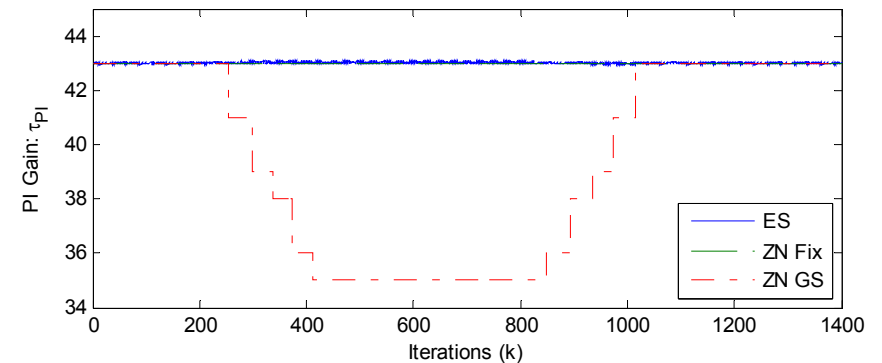
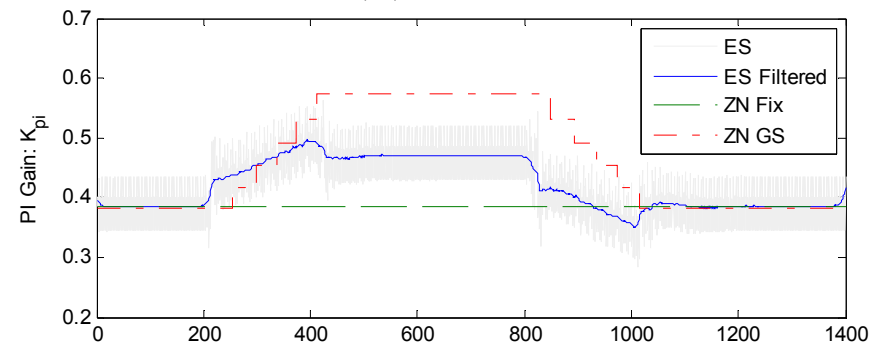
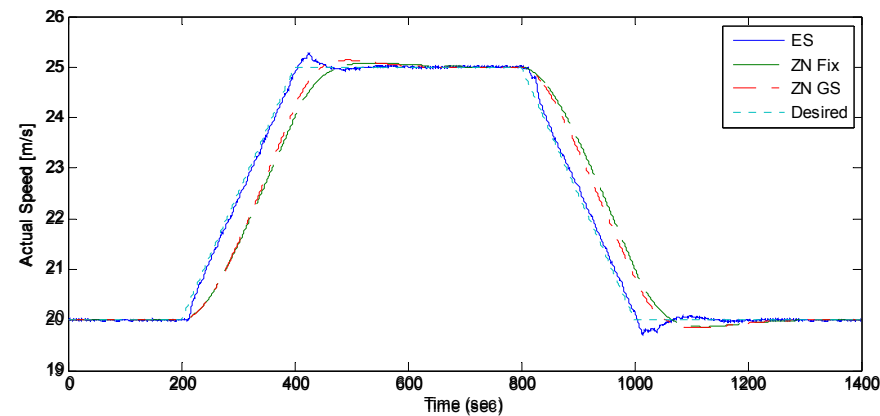
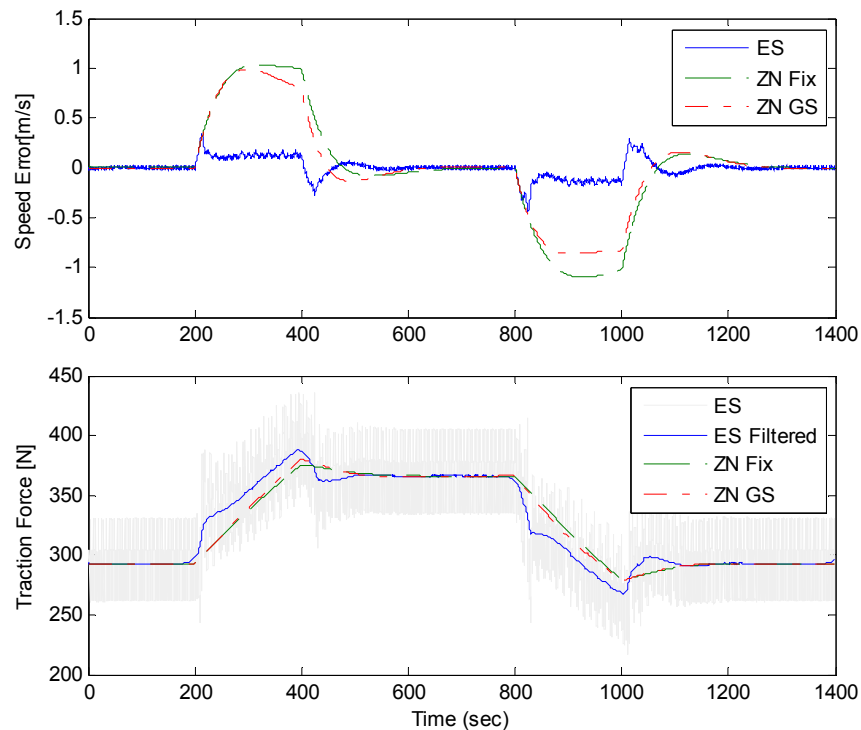
$$C(s) = (0.3845) \frac{43s + 1}{s}$$



# PI Tuning for Cruise Control

## Control Methods

- Extremum Seeking (ES)
- Fixed Ziegler-Nichols Gains (ZN Fix)
- Gain Scheduling (ZN GS)



# Summary & Conclusions

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- Tunes PID controllers by minimizing a cost function characterizing the desired closed-loop behavior
- Achieves better or comparable results relative to other popular tuning methods
- Improper ES parameters may produce instability
- Successfully performs adaptation for time-varying systems
- Online adaptation does not require models



# References

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- [1] N.J. Killingsworth, M. Krstic, “PID tuning using extremum seeking,” *IEEE Control Systems Magazine*, pp 70-79, Feb. 2006.
- [2] K.J. Åström, B. Wittenmark, *Computer Controlled Systems: Theory and Design*, 3<sup>rd</sup> ed. Upper Saddle River, NJ: Prentice-Hall, 1997.
- [3] O. Lequin, E. Bosmans, T. Triest, “Iterative feedback tuning of PID parameters: Comparison with classical tuning rules,” *Contr. Eng. Pract.*, vol. 11, no. 9, pp. 1023-1033, 2003.
- [4] A. Vahidi, A. Stefanopoulou, H. Peng, “Recursive least squares with forgetting for online estimation of vehicle mass and road grade: theory and experiments,” *International Journal of Vehicle Mechanics and Mobility*, Jan 2005.





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# QUESTIONS?

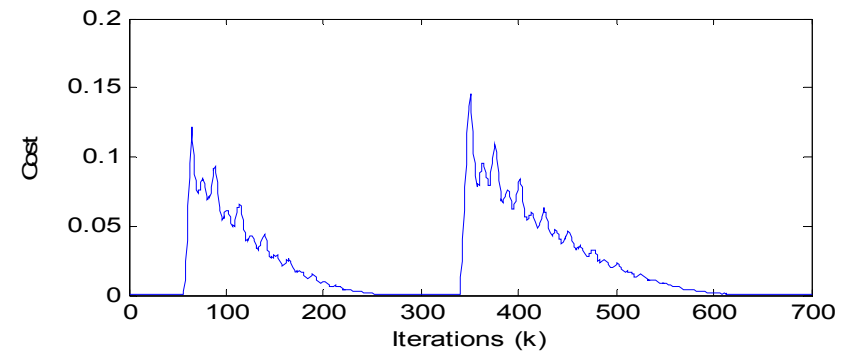
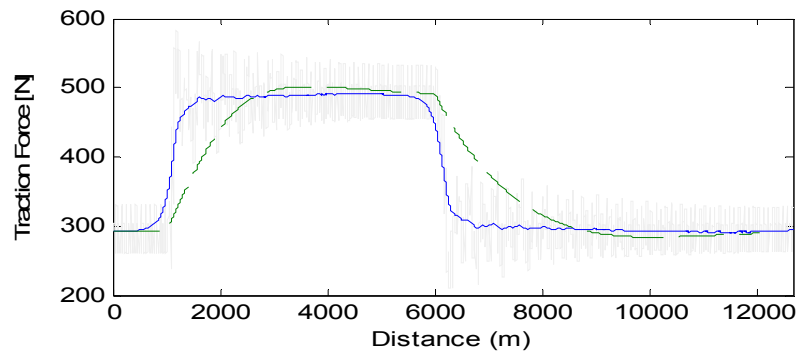
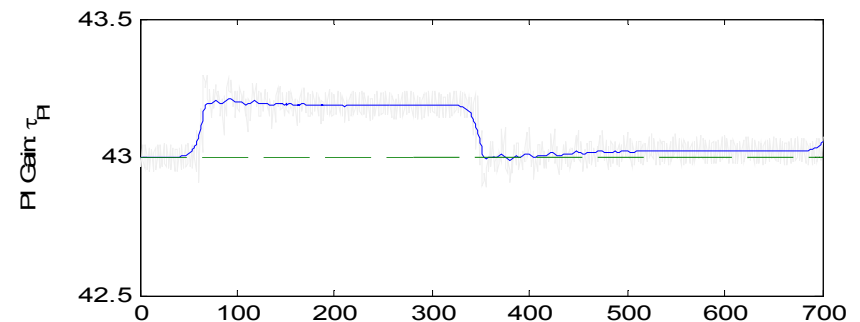
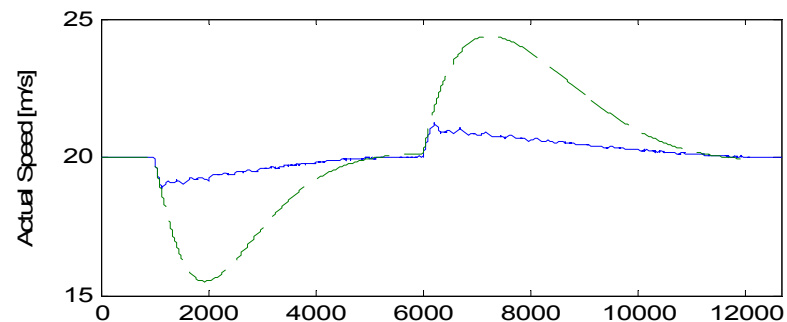
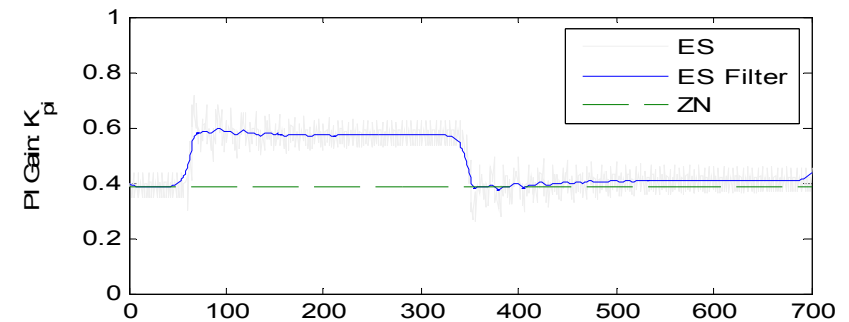
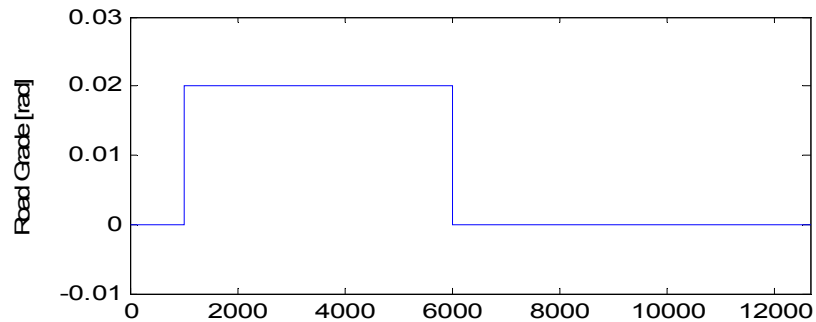


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# APPENDIX SLIDES



# Results: Road Grade Steps



# Results: Vahidi Road Grade Profile (Linear Model)

