

# Introduction to the Stack ADT

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**Stack:** a LIFO (last in, first out) data structure

Examples:

- plates in a cafeteria serving area
- return addresses for function calls

# Stack Basics

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Stack is usually implemented as a list, with additions and removals taking place at one end of the list

The active end of the list implementing the stack is the **top** of the stack

Stack types:

- Static – fixed size, often implemented using an array
- Dynamic – size varies as needed, often implemented using a linked list

# Stack Operations and Functions

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## Operations:

- **push**: add a value at the top of the stack
- **pop**: remove a value from the top of the stack

## Functions:

- **isEmpty**: true if the stack currently contains no elements
- **isFull**: true if the stack is full; only useful for static stacks

# Static Stack Implementation

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Uses an array of a fixed size

Bottom of stack is at index 0. A variable called top tracks the current top of the stack

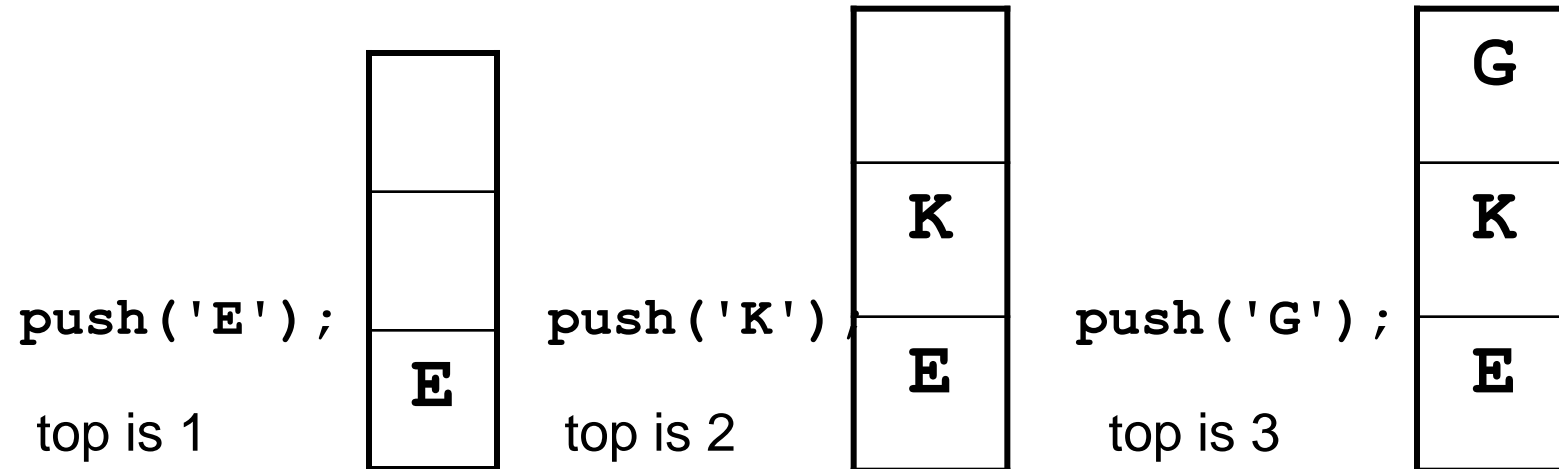
```
const int STACK_SIZE = 3;  
char s[STACK_SIZE];  
int top = 0;
```

top is where the next item will be added

# Array Implementation Example

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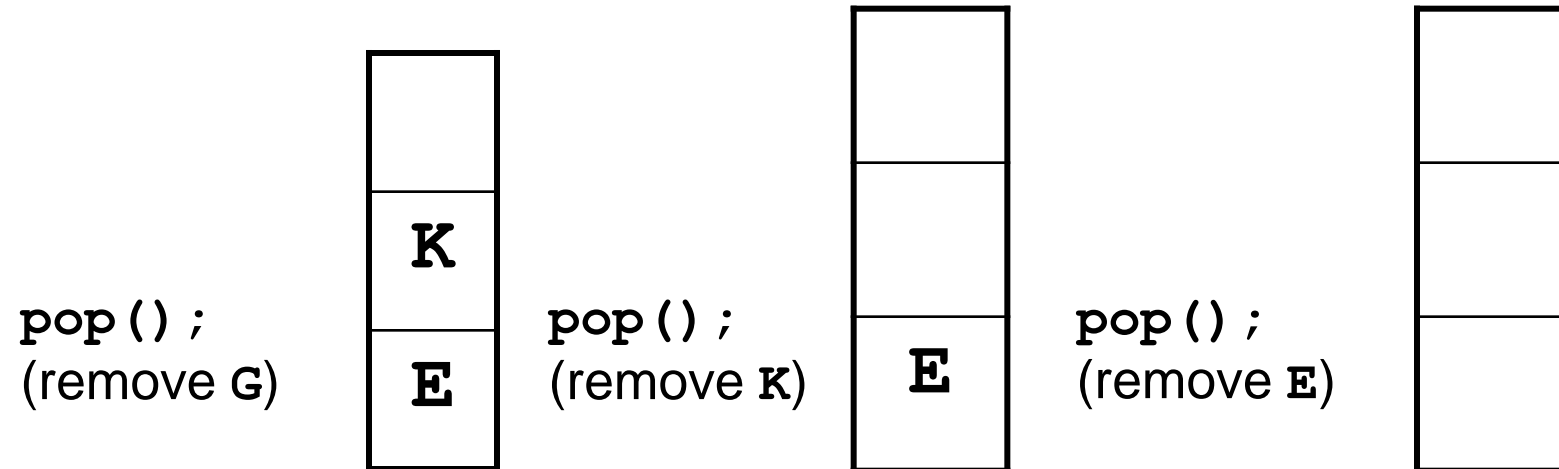
This stack has max capacity 3, initially  $\text{top} = 0$  and stack is empty.



# Stack Operations Example

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After three pops, `top == 0` and the stack is empty



# Array Implementation

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```
char s[STACK_SIZE];  
int top=0;
```

To check if stack is empty:

```
bool isEmpty()  
{  
    if (top == 0)  
        return true;  
    else return false;  
}
```



# Array Implementation

---

```
char s[STACK_SIZE];  
int top=0;
```

To check if stack is full:

```
bool isFull()  
{  
    if (top == STACK_SIZE)  
        return true;  
    else return false;  
}
```

# Array Implementation

---

To add an item to the stack

```
void push(char x)
{
    if (isFull())
        {error(); exit(1);}
    // or could throw an exception
    s[top] = x;
    top++;
}
```

# Array Implementation

---

To remove an item from the stack

```
void pop(char &x)
{
    if (isEmpty())
        {error(); exit(1);}
    // or could throw an exception
    top--;
    x = s[top];
}
```

# Class Implementation

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```
class STACK
{
private:
    char *s;
    int capacity, top;
public:
    void push(char x);
    void pop(char &x);
    bool isFull(); bool isEmpty();
    STACK(int stackSize);
    ~STACK()
};
```

# Exceptions from Stack Operations

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Exception classes can be added to stack object definition to handle cases where an attempt is made to push onto a full stack (overflow) or to pop from an empty stack (underflow)

Program that uses **push** and **pop** operations should do so from within a **try** block.

**catch** block(s) should follow the **try** block, interpret what occurred, and inform the user.

# Dynamic Stacks

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Implemented as a linked list

Can grow and shrink as necessary

Can't ever be full as long as memory is available

# Linked List Implementation

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Node for the linked list

```
struct LNode
{
    char value;
    LNode *next;
    LNode(char ch, LNode *p = 0)
        { value = ch; next = p; }
};
```

Pointer to beginning of linked list, which will serve as top of stack

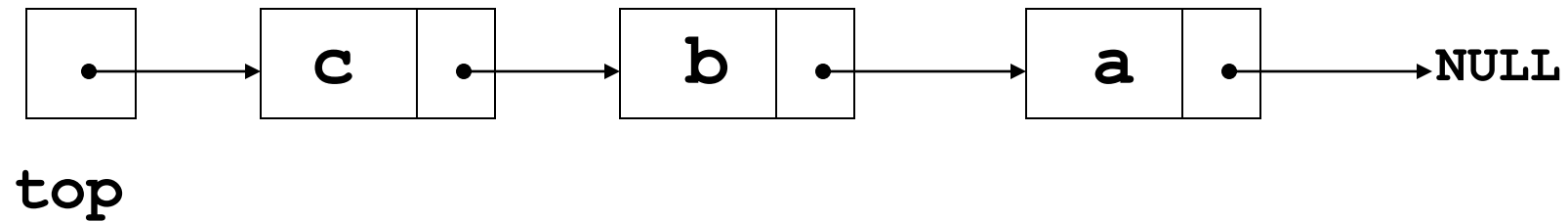
```
LNode *top = NULL;
```

# Linked List Implementation

---

A linked stack after three push operations:

```
push('a'); push('b'); push('c');
```





# Operations on a Linked Stack

---

Check if stack is empty:

```
bool isEmpty()  
{  
    if (top == NULL)  
        return true;  
    else  
        return false;  
}
```

# Operations on a Linked Stack

---

Add a new item to the stack

```
void push(char x)
{
    top = new LNode(x, top);
}
```

# Operations on a Linked Stack

---

Remove an item from the stack

```
void pop(char &x)
{
    if (isEmpty())
    { error(); exit(1); }
    x = top->value;
    LNode *oldTop = top;
    top = top->next;
    delete oldTop;
}
```

# The STL **stack** Container

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Stack template can be implemented as a **vector**, **list**, or a **deque**

Implements **push**, **pop**, and **empty** member functions

Implements other member functions:

- **size**: number of elements on the stack
- **top**: reference to element on top of the stack (must be used with **pop** to remove and retrieve top element)

# Defining an STL-based Stack

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Defining a stack of **char**, named **cstack**, implemented using a **vector**:

```
stack< char, vector<char> > cstack;
```

Implemented using a list:

```
stack< char, list<char> > cstack;
```

Implemented using a **deque** (default):

```
stack< char > cstack;
```

Spaces are required between consecutive > > symbols to distinguish from stream extraction

# Introduction to the Queue ADT

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**Queue**: a FIFO (first in, first out) data structure.

Examples:

- people in line at the theatre box office
- print jobs sent to a printer

Implementation:

- static: fixed size, implemented as array
- dynamic: variable size, implemented as linked list

# Queue Locations and Operations

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**rear**: position where elements are added

**front**: position from which elements are removed

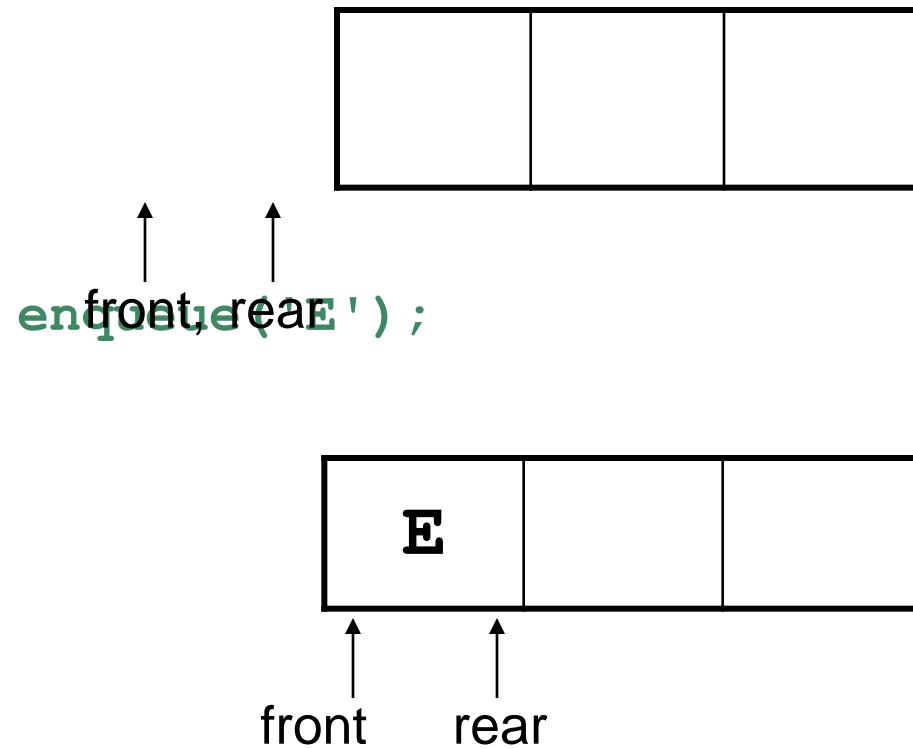
**enqueue**: add an element to the rear of the queue

**dequeue**: remove an element from the front of a queue

# Array Implementation of Queue

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An empty queue that can hold **char** values:

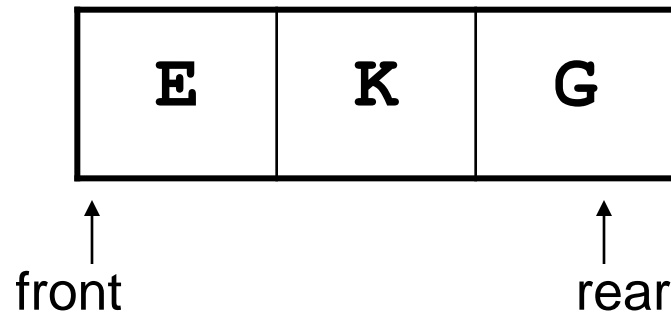
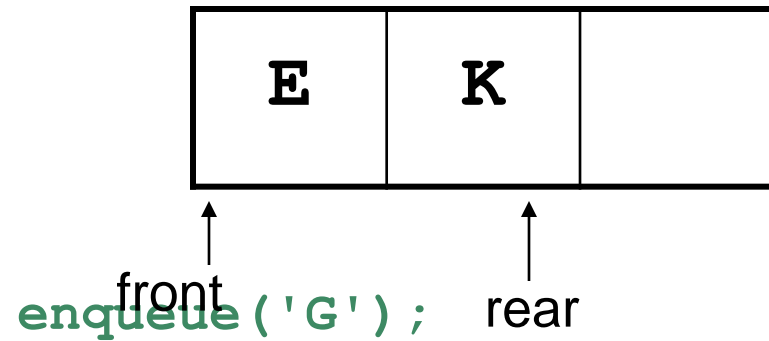




# Queue Operations - Example

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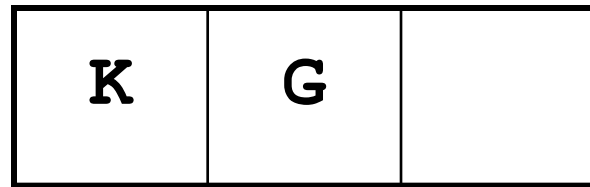
`enqueue('K');`



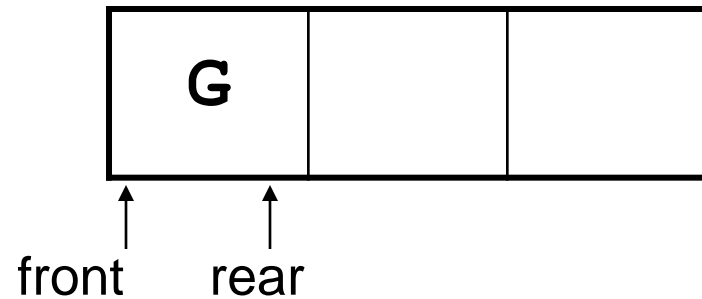
# Queue Operations - Example

---

`dequeue(); // remove E`



`dequeue(), // remove K`



# Array Implementation Issues

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In the preceding example, Front never moves.

Whenever **dequeue** is called, all remaining queue entries move up one position. This takes time.

Alternate approach:

- Circular array: **front** and **rear** both move when items are added and removed. Both can 'wrap around' from the end of the array to the front if warranted.

Other conventions are possible

# Array Implementation Issues

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Variables needed

- `const int QSIZE = 100;`
- `char q[QSIZE];`
- `int front = -1;`
- `int rear = -1;`
- `int number = 0; //how many in queue`

Could make these members of a queue class, and queue operations would be member functions

# isEmpty Member Function

---

Check if queue is empty

```
bool isEmpty()  
{  
    if (number > 0)  
        return false;  
    else  
        return true;  
}
```

# isFull Member Function

---

Check if queue is full

```
bool isFull()
{
    if (number < QSIZE)
        return false;
    else
        return true;
}
```

# enqueue and dequeue

---

To enqueue, we need to add an item **x** to the rear of the queue

Queue convention says **q[rear]** is already occupied. Execute

```
if(!isFull)
{
    rear = (rear + 1) % QSIZE;
    // mod operator for wrap-around
    q[rear] = x;
    number++;
}
```

# enqueue and dequeue

---

To dequeue, we need to remove an item **x** from the front of the queue

Queue convention says **q[front]** has already been removed. Execute

```
    if (!isEmpty)
    {   front = (front + 1) % QSIZE;
        x = q[front];
        number--;
    }
```



# enqueue and dequeue

---

**enqueue** moves **rear** to the right as it fills positions in the array

**dequeue** moves **front** to the right as it empties positions in the array

When **enqueue** gets to the end, it wraps around to the beginning to use those positions that have been emptied

When **dequeue** gets to the end, it wraps around to the beginning use those positions that have been filled

# enqueue and dequeue

---

Enqueue wraps around by executing

```
rear = (rear + 1) % QSIZE;
```

Dequeue wraps around by executing

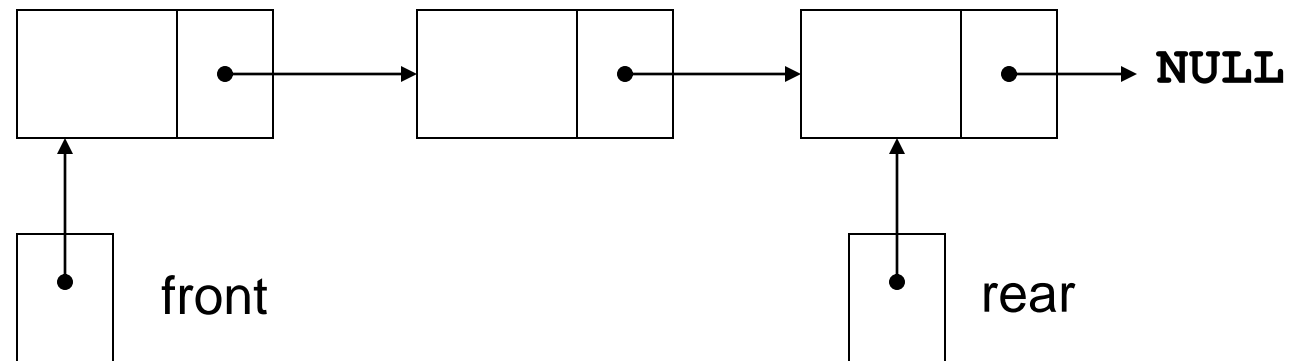
```
front = (front + 1) % QSIZE;
```

# Dynamic Queues

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Like a stack, a queue can be implemented using a linked list

Allows dynamic sizing, avoids issue of wrapping indices



# Dynamic Queue Implementation Data Structures

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```
struct QNode
{
    char value;
    QNode *next;
    QNode(char ch, QNode *p = NULL);
    {value = ch; next = p;}
}

QNode *front = NULL;
QNode *rear = NULL;
```

# isEmpty Member Function

---

To check if queue is empty:

```
bool isEmpty()  
{  
    if (front == NULL)  
        return true;  
    else  
        return false;  
}
```

# enqueue Member Function

---

To add item at rear of queue

```
void enqueue(char x)
{
    if (isEmpty())
    { rear = new QNode(x);
      front = rear;
      return;
    }
    rear->next = new QNode(x);
    rear = rear->next;
}
```

# dequeue Member Function

---

To remove item from front of queue

```
void dequeue(char &x)
{
    if (isEmpty())
        { error(); exit(1); }
    x = front->value;
    QNode *oldfront = front;
    front = front->next;
    delete oldfront;
}
```

# The STL **deque** and **queue** Containers

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**deque**: a double-ended queue. Has member functions to enqueue (**push\_back**) and dequeue (**pop\_front**)

**queue**: container ADT that can be used to provide a queue based on a **vector**, **list**, or **deque**. Has member functions to enqueue (**push**) and dequeue (**pop**)



# Defining a Queue

---

Defining a queue of **char**, named **cQueue**, based on a **deque**:

```
deque<char> cQueue;
```

Defining a **queue** with the default base container

```
queue<char> cQueue;
```

Defining a queue based on a **list**:

```
queue<char, list<char> > cQueue;
```

Spaces are required between consecutive > > symbols to distinguish from stream extraction

# Eliminating Recursion

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Recursive solutions to problems are often elegant but inefficient

A solution that does not use recursion is more efficient for larger sizes of inputs

Eliminating the recursion: re-writing a recursive algorithm so that it uses other programming constructs (stacks, loops) rather than recursive calls