A model of replicated asymmetric state machines

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Take-away message

Behavioural specs for the (existing) Actyx industrial platform to develop applications for factory automation

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- feature
 - pub-subscribe (instead of point-to-point)
 - generalised choices
 - arbitrary (and variable) number of instances

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Behavioural specs for the (existing) Actyx industrial platform to develop applications for factory automation

With respect to the state-of-the-art, our models

- feature
 - pub-subscribe (instead of point-to-point)
 - generalised choices
 - arbitrary (and variable) number of instances
- focus on
 - availability (instead of consensus)
 - eventual-consistency (instead of eg. message loss, deadlock, session fidelity, etc.)

Plan

- Challenges in factory automation
- Our behavioural specifications
- Model-driven realisation
- Concluding remarks

Prelude –

[Factory automation]

Industrial scenarios



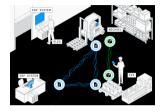
(courtesy of Actyx)

A highly collaborative environment

People + Real-time controllers + IT systems and networks:

- work divided among many autonomous production cells
- efficiency is determined by designing and controlling the flow of resource and information
- local failures must be tolerated for brief time periods

Industrial scenarios



(courtesy of Actyx)

Execution model

 $\mathsf{machine/operator/forklift/}... \; \mapsto \mathsf{Local} \; \mathsf{twin} \; (\mathsf{state} \; \mathsf{machine})$

- twins are replicated where needed
- events have unique IDs and
 - record facts (e.g., from sensors) or
 - decisions (e.g., from an operator)
 - spread asynchronously
- events are kept in local logs used to compute the state of the twin
- logs are replicated and merged

Challenges

Specify application-level protocols where decisions

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Specify application-level protocols where decisions

- don't require consensus
- are based on stale local states
- yet, collaboration has to be successful

Behavioural Specifications –

Decide locally, agree globally...eventually

- Bellavioural Specifications -

Syntax

Global specs

$$\mathsf{G} ::= \mathsf{c}_1 @ \mathsf{R}_1 \langle \mathsf{l}_1 \rangle . \mathsf{G}_1 + \cdots + \mathsf{c}_n @ \mathsf{R}_n \langle \mathsf{l}_n \rangle . \mathsf{G}_n$$

$$G = publish@A\langle p \rangle . G'$$

$$G' = bid@B\langle b \rangle . G'$$

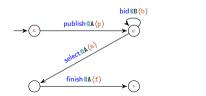
$$+$$

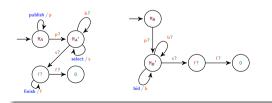
$$select@A\langle s \rangle . finish@A\langle f \rangle . 0$$

Local Specs

$$\mathtt{M} ::= \kappa \cdot [\mathtt{t}_1 ? \mathtt{M}_1 \& \cdots \& \mathtt{t}_n ? \mathtt{M}_n]$$

$$\begin{split} \mathbf{M}_{A} &= \{\mathsf{publish} \, / \, \mathbf{p}\} \cdot \big[\mathbf{p}? \, \mathbf{M}_{A}' \big] \\ \mathbf{M}_{A}' &= \{\mathsf{select} \, / \, \mathbf{s}\} \cdot \big[\mathbf{b}? \, \mathbf{M}_{A}' \, \, \& \, \, \mathbf{s}? \, \{\mathsf{finish} \, / \, \mathbf{f}\} \cdot \mathsf{f}? \, \mathbf{0} \big] \\ \mathbf{M}_{B} &= \mathbf{p}? \, \mathbf{M}_{B}' \\ \mathbf{M}_{B}' &= \{\mathsf{bid} \, / \, \mathbf{b}\} \cdot \big[\mathbf{b}? \, \mathbf{M}_{B}' \, \, \& \, \, \mathbf{s}? \, \mathsf{f}? \, \mathbf{0} \big] \end{split}$$





Syntax

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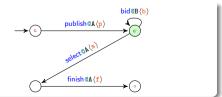
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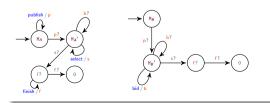
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Semantics of specifications

Global (protocol spec)

$$\frac{\delta(\mathsf{G}, I) \xrightarrow{\mathsf{c}/\mathsf{1}} \mathsf{G}' \qquad \vdash I' : \mathsf{1} \qquad I' \text{ fresh}}{(\mathsf{G}, I) \xrightarrow{\mathsf{c}/\mathsf{1}} (\mathsf{G}, I \cdot I')}$$

where

/ is an (idealised) global/shared log

$$\cdots + c_i @R_i \langle \mathbf{1}_i \rangle \cdot G_i + \cdots \xrightarrow{c_i / \mathbf{1}_i} G_i$$

$$\delta(\mathsf{G},\epsilon) = \mathsf{G}$$

$$\delta(\mathsf{G}, \ell) = \begin{cases} \delta(\mathsf{G}', \ell \cdot \ell') & \text{if } \mathsf{G} \xrightarrow{\mathsf{C}/1} \mathsf{G}', \ell \neq \epsilon, \vdash \ell' : 1 \\ \bot & \text{otherwise} \end{cases} \qquad \delta(\mathsf{M}, e \cdot \ell) = \begin{cases} \delta(\mathsf{M}_j, \ell) & \text{if } \vdash e : \mathsf{t}_j, \\ \mathsf{M} = \kappa \cdot [\dots \& \mathsf{t}_j? \mathsf{M}_j \& \dots] \\ \delta(\mathsf{M}, \ell) & \text{otherwise} \end{cases}$$

Local (components' spec)

$$\frac{\delta(\mathtt{M}, \mathit{I}) = \mathtt{M}' \qquad \mathtt{M}' \downarrow_{c / 1} \quad \vdash \mathit{I}' : 1 \qquad \mathit{I}' \text{ fresh}}{(\mathtt{M}, \mathit{I}) \xrightarrow{c / 1} (\mathtt{M}, \mathit{I} \cdot \mathit{I}')}$$

where

/ is the local log accessible to M

$$M' \downarrow_{c/1} \iff c/1$$
 enabled at M'

$$\delta(\mathbf{M}, \epsilon) = \mathbf{M}$$

$$\delta(\mathbf{M}, \mathbf{e} \cdot \mathbf{I}) = \begin{cases} \delta(\mathbf{M}_j, \mathbf{I}) & \text{if } \vdash \mathbf{e} : \mathbf{t}_j, \\ \mathbf{M} = \kappa \cdot [\dots \& \mathbf{t}_j? \mathbf{M}_j \& \dots] \end{cases}$$

Events are univocally associated to the machines generating them.

Machines with local logs & a global one

$$\mathbf{S} = (\mathbf{M}_1, \mathbf{I}_1) \mid \ldots \mid (\mathbf{M}_n, \mathbf{I}_n) \mid \mathbf{I}$$

(Recall: the global log is an optical illusion)

Well-formedness

$$(M_1, I_1) | \dots | (M_n, I_n) | I$$
 is well-formed if $I = I_1 \cup \dots \cup I_n$ and for all $i, I_i \sqsubseteq I$

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e₁

where
$$I_i \sqsubseteq I \iff I_i =$$

: = 1

 e_m

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 e_1

where $I_i \sqsubseteq I \iff I_i = \underbrace{\vdots}_{e_{i,n}} = \underbrace{\vdots}_{e_m}$

formally, there is an order-preserving and

where

Events are univocally associated to the machines generating them.

Machines with local logs & a global one
$$S = (M_1, I_1) | \dots | (M_n, I_n) | I$$
 (Recall: the global log is an optical illusion)
$$| I_1 | \dots | I_n | | I$$

formally, there is an order-preserving and downward-total morphism from /; into /

 $I_i \sqsubseteq I \iff I_i =$

 e_1

 e_m

Specs describe how to "produce/consume" events

Global: how/when roles produce events

Local: how/when instances consume events

"skipping" irrelevant events

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First: Events' generation

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Communication is non-deterministic

The semantics of systems consists of two phases:

First: Events' generation

The local log of a machine is extended with the fresh events generated by the machine

Second: Events' propagation

Emitted events propagate asynchronously & non-deterministically

Semantics of systems: formally

$$\frac{i \in \operatorname{dom} S}{(S, l) = (M, l_i)} \xrightarrow{(M, l_i)} \xrightarrow{c/1} (M, l'_i) \xrightarrow{l' \in l \bowtie l'_i} (S, l) \xrightarrow{c/1} (S[i \mapsto (M, l'_i)], l')$$

where

$$|_{1} \bowtie |_{2} = \{ | \mid | \subseteq |_{1} \cup |_{2} \land |_{1} \sqsubseteq | \land |_{2} \sqsubseteq | \}$$

$$\frac{i \in \mathsf{dom}\,\mathsf{S}}{(\mathsf{S},\mathit{I}) \xrightarrow{\tau} (\mathsf{S}[i \mapsto (\mathsf{M},\mathit{I}')],\mathit{I})}$$













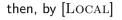








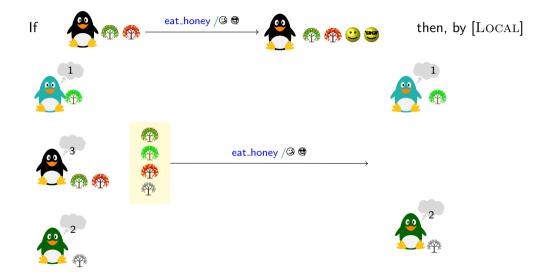


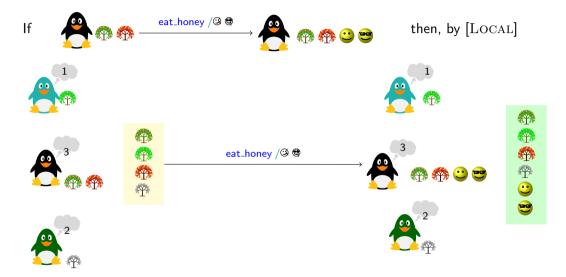


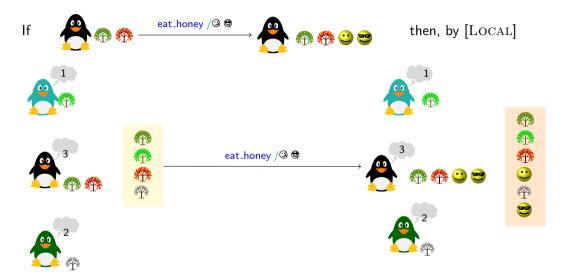


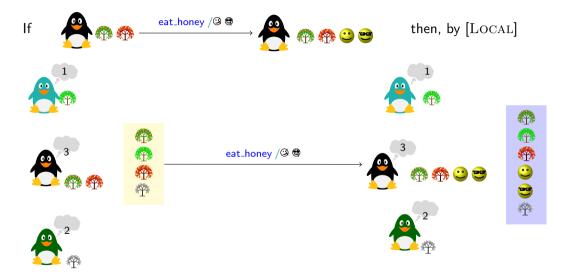


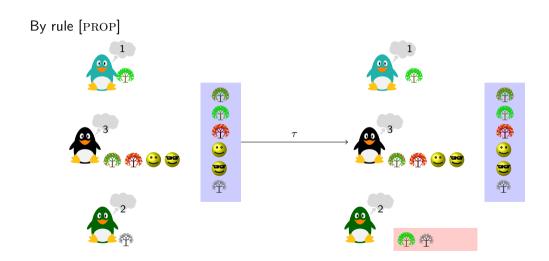












By rule [PROP] 4 τ

By rule [PROP] τ

By rule [PROP] τ WRONG!

Properties of our semantics

```
Theorem: Well-Formedness preservation

If

S is well-formed and S \xrightarrow{[Local]/[Prop]}^* S'
then
S' is well-formed
```

Theorem: Eventual Consistency

```
If \mathbf{S} = (\mathbf{M}_1, \mathbf{I}_1) \mid \dots \mid (\mathbf{M}_n, \mathbf{I}_n) \mid \mathbf{I} \text{ is well-formed then} then \mathbf{S} \xrightarrow{\tau}^{\star} (\mathbf{M}_1, \mathbf{I}) \mid \dots \mid (\mathbf{M}_n, \mathbf{I}) \mid \mathbf{I}
```

From models to implementations –

On realisation

Exercise on realisation

It is hard to get realisation right (even without multi-instances or choices!)

A trivial protocol

Take

$$G = prepare@P(piece) . pack@A(product) . 0$$

Do the following machines realise G?

```
M_P = \{ prepare / piece \} \cdot 0 and M_A = piece ? \{ pack / product \} \cdot 0
```

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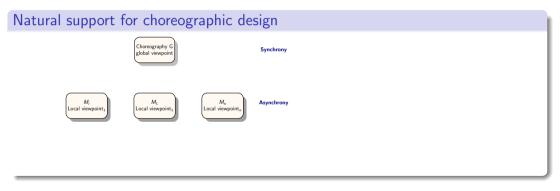
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```
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```

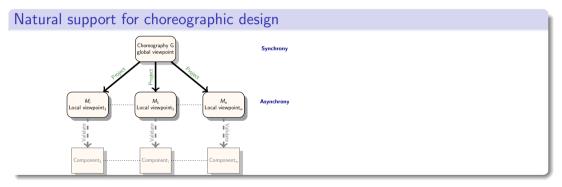
Do they do that "correctly"?

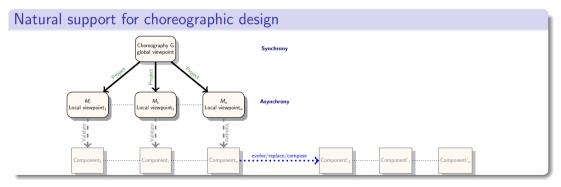


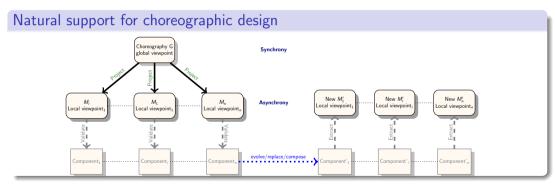
Choreographies provide a principled development approach

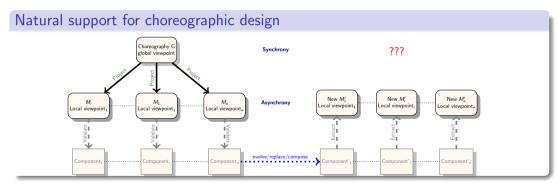
Natural support for choreographic design

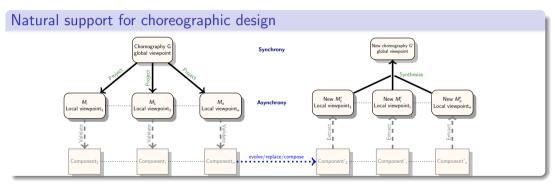












Realisation...choreographically

Well-formedness of global specs

Each guard, say l_i , should be

- causal consistent
 - each selector in (the continuation of) l_i reacts to l_i
 - each role involved in the continuation of l_i cannot react to more events on l_i than selectors on the branch
- determined
 - each role in the continuation of $\mathbf{1}_i$ reacts to $\mathbf{1}_i[0]$
 - selectors in the continuation of $\mathbf{1}_i$ react to the same set of event types in $\mathbf{1}_i$
- confusion-free
 - guards of different branches start with distinct event types
 - an event type cannot occur in more than one guard

A glimpse of top-down design

Definition (Projection)

Given a global type G and a subscription σ , the projection of G over a role R with respect to σ , written $G \downarrow_R^{\sigma}$, is co-inductively defined as follows:

$$(\sum_{i \in I} c_i @R_i \langle \mathbf{l}_i \rangle . G_i) \downarrow_{R}^{\sigma} = \kappa \cdot [\&_{i \in I} (c_i @R_i \langle \mathbf{l}_i \rangle . G_i) \downarrow_{R}^{\sigma}]$$

where $\kappa = \{(c_i, l_i) \mid i \in I \land R_i = R\}$ and

$$(c_i@R_i\langle \mathbf{1}_i\rangle . G_i) \downarrow_R^{\sigma} = \begin{cases} \text{filter}(\mathbf{1}_i, \sigma(R))? (G_i\downarrow_R^{\sigma}) & \text{if filter}(\mathbf{1}_i, \sigma(R)) \neq \epsilon \\ 0 & \text{otherwise} \end{cases}$$

– Wrapping up –

Conclusions

We have a useful basis to take design decisions

- a formal model ensuring relevant properties
- projectable global specs
- a prototype implementation for top-down engineering

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We would like to have

- our models as reference documentation for Actyx's developers
- "minimal" subscriptions
- tools / develop behavioral typing / inference (ie going bottom-up)
- compensations (hence causality tracking) / active monitoring?
- failure handling (in event propagation)

Thank you!