

$$\begin{array}{l} k=18prt z\#E()=p+1-trzss\\ \textcolor{blue}{????}\chi?\\ 123?1\times 2\rightarrow 3123 \end{array}$$

$$\begin{array}{l} \alpha F_{p^k}pk embedding E(F_{p^k})krp^k r\#E(F_p)\log_2 r\approx 256\log_2 p^k\approx 30005000\rho=(\log_2 p)/(\log_2 r)k1220?k=18????2s21211\\ s(s-1)2pk\pi:(x,y)\mapsto (x^p,y^p)p(x,y)F_{p^k}tt=p+1-\#E(F_p)?z\equiv -3p+p^4\bmod rzzrzszs\\ ?E'2'2F_{p^{18}}2'F_{p^3}22'2F_{p^{18}}z\\ k=18? \end{array}$$

$$\begin{array}{l} 4a^3+27b^2\neq 0a,b\in_curve are known as rational points on the curve.\\ E(p)\mathcal{O}E(F_p)\# \bar{E}(F_p)E(F_p)L=(x_l,y_l)M=(x_m,y_m)N=L+MN=(x_n,y_n)L,M,N\in E()xyN \end{array}$$

$$\lambda$$

$$\lambda \mathcal{O}E(p)L\neq ML+ML=ML+M=2Ls0\leq s<rrM[s]M(s-1)M$$

$$\begin{array}{l} s=rr[r]M=\mathcal{O}[s]M=NssMN\\ ?F_{p^{18}} \end{array}$$

$$b\neq 0X,Y\in F_{p^{18}}ptrz$$

$$zz\equiv 1442\rho=(\log_2 p/\log_2 r)4/3\#E(F_{p^{18}})$$

$$\begin{array}{l} t_{18}=\alpha^{18}+\beta^{18}\alpha\beta\alpha+\beta=t\alpha\beta=p??prp=511\\ E(F_{p^{18}})(x,y)E(F_{p^{18}})\pi_p:(x,y)\mapsto (x^p,y^p)pF_{p^{18}}??k=12\\ F_{p^{18}}F_{p^k}k??\\ F_{p^{18}}?(p-1)\theta?k=18F_{p^{18}} \end{array}$$

$$\begin{array}{l} \theta=2\\ \frac{2}{2}-i),\\ p18=p6[w]/(w^3-v).\\ (11) \end{array}$$

$$\begin{array}{l} ?F_{p^3} sextic twist\\ 22123Q\in 2Q_{rel}2relation.Next,ascalarwillbeconsideredforscalarmultiplicationof.Afterthat,asFigure??,-adicre\\ ??(t-1)s_a dic.eps-adicrepresentation of scalar.\\ ??zs_a dic.eps-adicand-adicrepresentation of scalar.\\ ??_sm.epsMulti-scalarmultiplication of with Frobenius mapping.\\ 1,2G_3?123 \end{array}$$

$$\begin{array}{l} \alpha 1,2G_3F_{p^{18}}r\\ Q\in 2\subset E(p18)Q \end{array}$$