

## Introduction

- ▶ Internal brain activity is only modulated, not driven, by sensory input [1].
- ▶ Semantic learning has to result from the interaction of sensory stimuli with an autonomously active network.
- ▶ Clique encoding [2] can be achieved with a network of competing cliques, that has transient state dynamics.
- ▶ We propose a learning rule that correlates such transient states with sensory inputs from the bars and stripes problem, prompted by [3].

## Network architecture

- ▶ A clique is a maximal fully connected sub-graphs.
- ▶ Cliques compete with one another if they have predominantly inhibitory connections across and excitatory ones within.
- ▶ A single active clique is a stable state, as long as other cliques are inhibited.

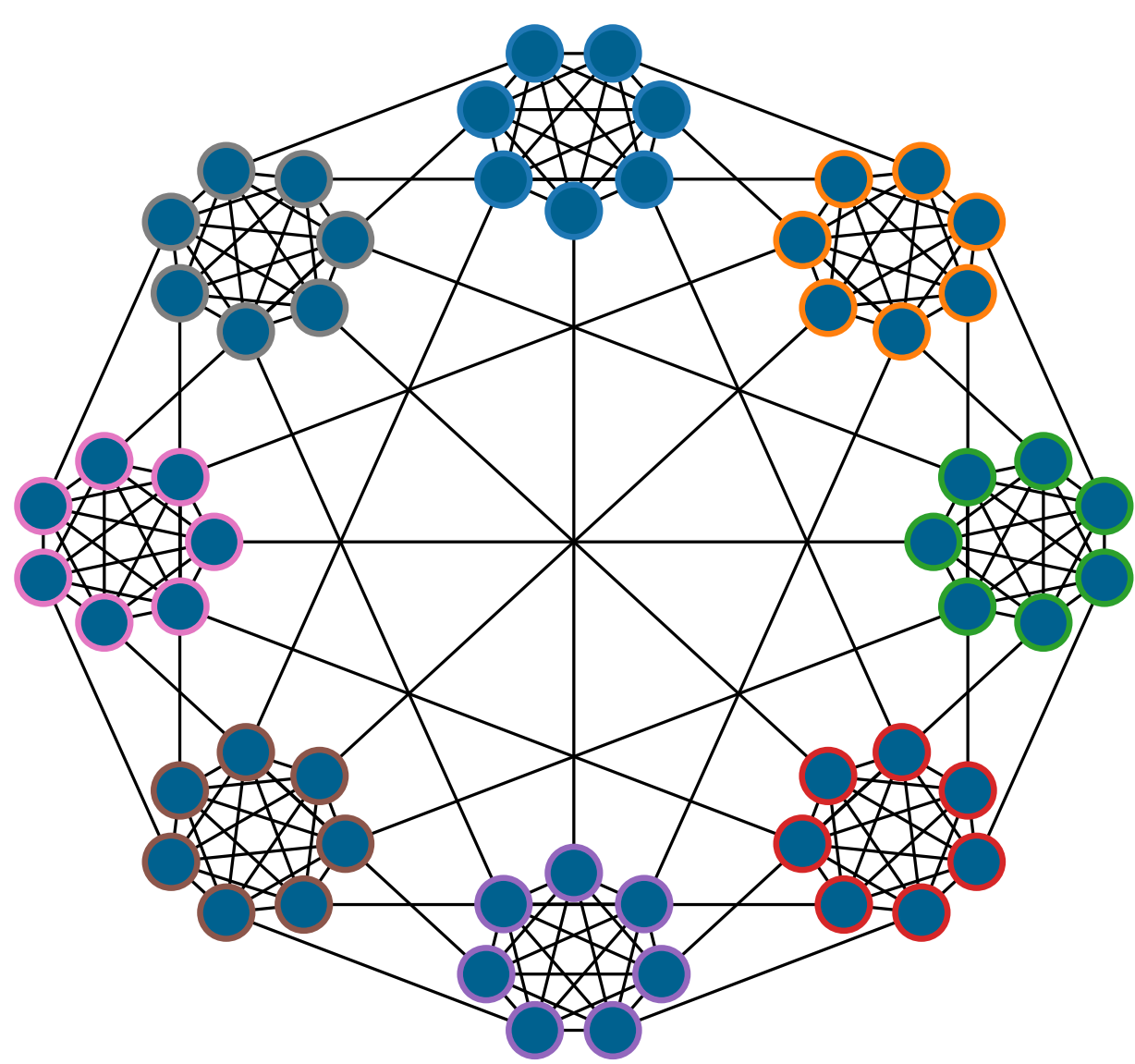


Figure 1: An eight clique network, each with seven nodes. Only excitatory links are shown. Each neuron within a clique excites an extra-clique neuron. The network is completed with inhibitory connections.

## Neuronal dynamics

- ▶ A rate-encoding model is used.
- ▶ The  $j$ -th neuron has membrane potential  $x_j$ , activity  $y_j$  and excitatory and inhibitory input,  $E_j$  and  $I_j$ .

$$\tau_x \dot{x}_j = -x_j + E_j + I_j$$

$$y_j = \sigma(x_j) = \frac{1}{1 + \exp(-ax_j)}$$

$$E_j = \sum_k w_{jk} y_k$$

$$I_j = \sum_k z_{jk} y_k.$$

- ▶ With these equation the system rapidly relaxes to a stable active clique state.
- ▶ The inclusion of presynaptic short-term plasticity, transforming  $y_k \rightarrow \tilde{y}_k$ , gives transient state dynamics, as in Fig. 2.

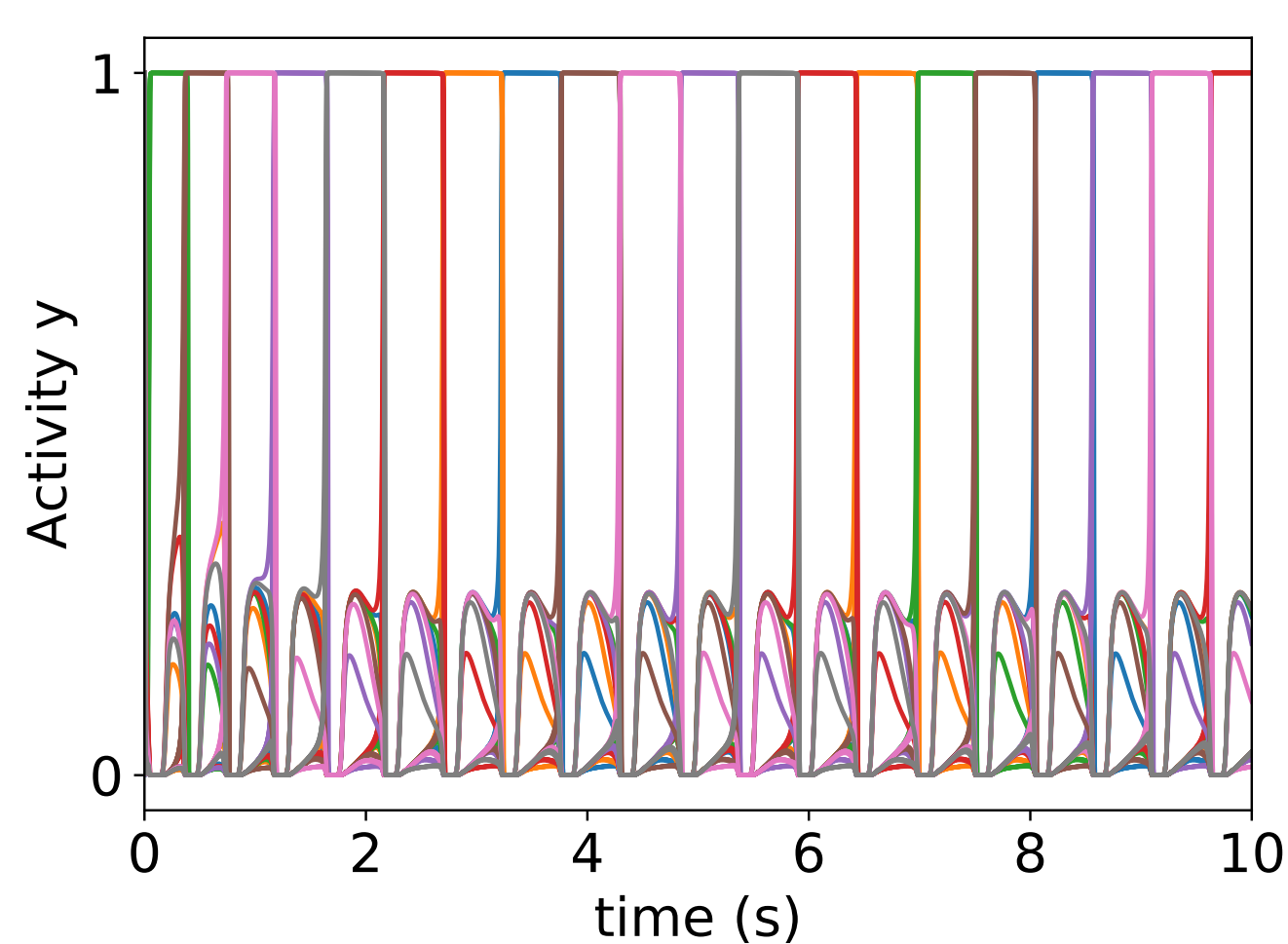


Figure 2: Internal activity in the network shown above, with the full depletion model. Neurons belonging to the same clique share plotting colours, as in Fig. 1.

## References

- [1] Fiser, J., Chiu, C. & Weliky, M. Small modulation of ongoing cortical dynamics by sensory input during natural vision. *Nature* 431, 573 (2004).
- [2] Lin, L., Osan, R. & Tsien, J. Z. Organizing principles of real-time memory encoding: neural clique assemblies and universal neural codes. *Trends in Neurosciences* 29, 48–57 (2006).
- [3] Gros, C. & Kaczor, G. Semantic learning in autonomously active recurrent neural networks. *Log J IGPL* 18, 686–704 (2010).
- [4] Mongillo, G., Barak, O. & Tsodyks, M. Synaptic Theory of Working Memory. *Science* 319, 1543–1546 (2008).

## Full depletion model

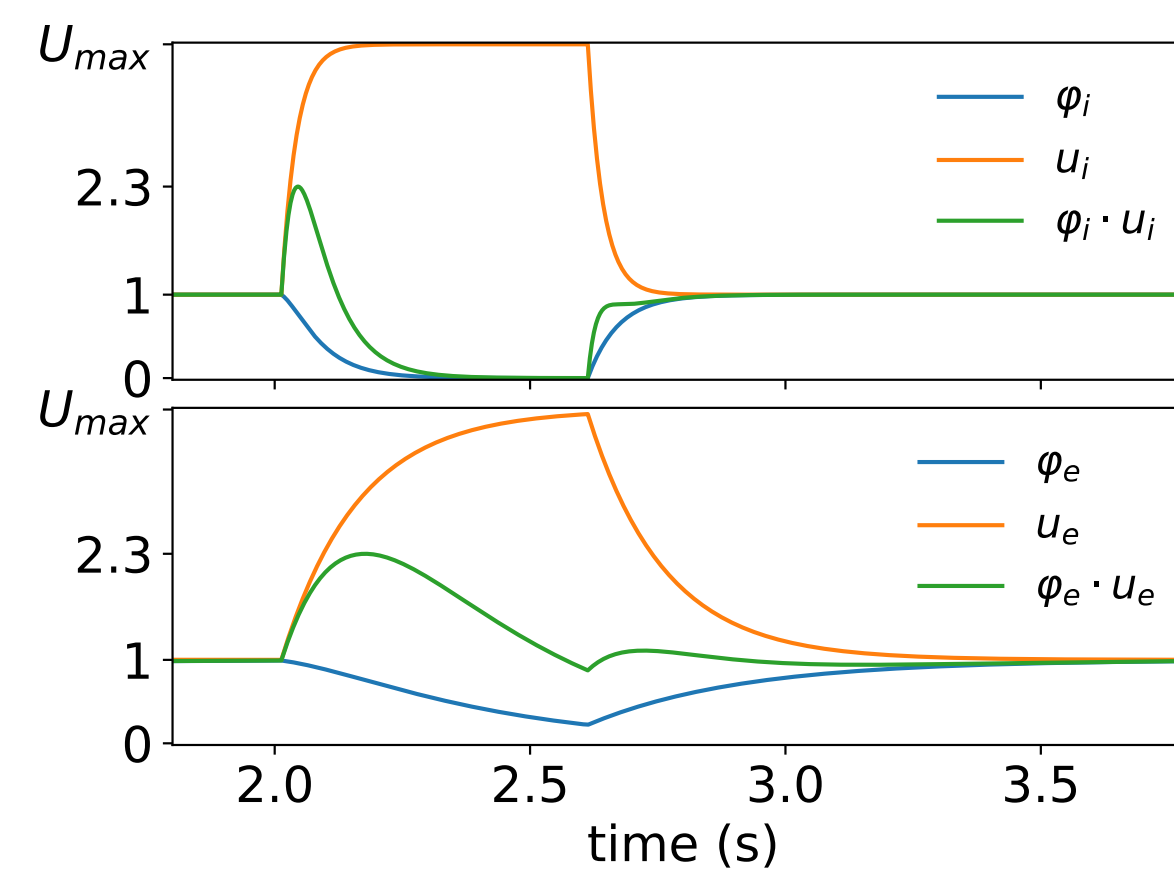


Figure 3: Dynamics of the full depletion model, with high presynaptic activity, for inhibitory (top) and excitatory (bottom) synapses.

## Sensory input

- ▶ Cognitive systems must identify objects in a noisy environment, performing independent component analysis.
- ▶ Sensory input consists of vertical and horizontal bars presented on a retina of  $L \times L$  pixels
- ▶ Each bar is independently drawn with probability  $p = 1/2L$ .
- ▶ Inactive pixels have output  $y_l^{\text{ext}} = 0$ , and active pixels  $y_l^{\text{ext}} = 1$ , even at the intersection of two bars.
- ▶ Therefore, *non linear* independent component analysis has to be performed to separate bars.
- ▶ At regular intervals, the all-to-all sensory connections transmit the extra excitatory input

$$\Delta E_j = \sum_l v_{jl} y_l^{\text{ext}}$$

## Learning rule

- ▶ The sensory weights  $v_{jl}$  must change so that different cliques respond mostly to single different bars.
- ▶ We hypothesize that learning occurs during the transitions from one winning clique to another.

$$\dot{v}_{jl} = (\dot{y}_j c_j / \tau_v - 1 / \tau_d) y_l^{\text{ext}} v_{jl}$$

$$c_j = \tanh[a(V_t - \Delta E_j)]$$

$$V_t = V^{\text{inact}} + y_j (V^{\text{act}} - V^{\text{inact}})$$

$$\tau_v \ll \tau_d, \quad V^{\text{inact}} < V^{\text{act}}.$$

- ▶  $v_{jl}$  ensures that the weights do not change sign,
- ▶ sensory input  $y_l^{\text{ext}}$  is necessary,
- ▶  $\dot{y}_j = 0$  during winning clique states,
- ▶  $c_j$  prevents runaway synapses dynamics, through the sliding activity level target  $V_t$ ,
- ▶ the slow decay term  $-1/\tau_d$  shrinks orthogonal synapses.

## Results

We use two performance measures:

$$R(\alpha, \beta) = \frac{1}{S_\alpha} \sum_{\substack{i \in C_\alpha \\ l \in P_\beta}} v_{il} y_l^{\text{ext}}$$

$$F(\alpha, l) = \frac{1}{S_\alpha} \sum_{i \in C_\alpha} v_{il}$$

- ▶ The response  $R(\alpha, \beta)$  is the clique averaged input received by clique  $\alpha$  of size  $S_\alpha$ , when bar  $\beta$  is active.
- ▶ Ideally,  $R(\alpha, \beta)$  would have a single maximum, that would be different across cliques.
- ▶ The receptive field  $F(\alpha, l)$  is the clique averaged sensory synaptic weight from the  $j$ -th pixel.
- ▶ Ideally,  $F(\alpha, l)$  would mirror the input from the most important bar.

## Conclusions

- ▶ In neural networks designed for feature extraction activity usually dies out without input. This is not, however, how actual brains operate.
- ▶ This work is a proof of concept showing how feature extraction with an autonomously active network can be achieved.
- ▶ Internal activity is characterized by transient states and competitive dynamics, and learning occurs during transitions between active cliques.
- ▶ More work is needed to improve performance and robustness of the algorithm.

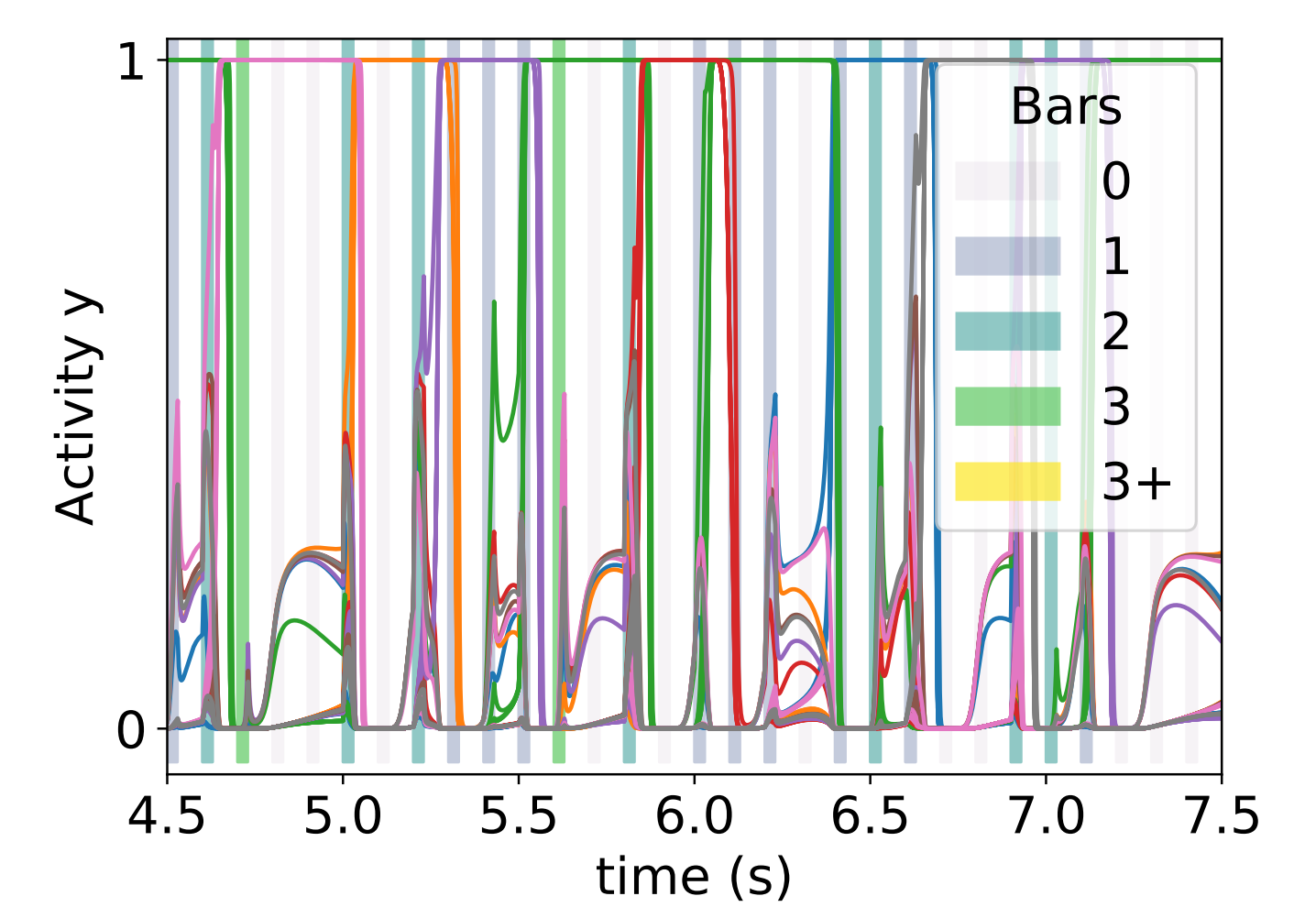
- ▶ Winning clique states become unstable with the STP *full depletion model*, that is inspired by the Tsodyks-Markram model [4].
- ▶ Transient states are obtained by modelling neurotransmitter vesicles with:
  - ▷  $u_k$ : likelihood of neurotransmitter release, increases with input
  - ▷  $\varphi_k$ : concentration of vesicles, that deplete while firing.
- ▶ Inhibitory synapses deplete faster than excitatory ones.

$$y_k \rightarrow \tilde{y}_k = y_k u_k \varphi_k$$

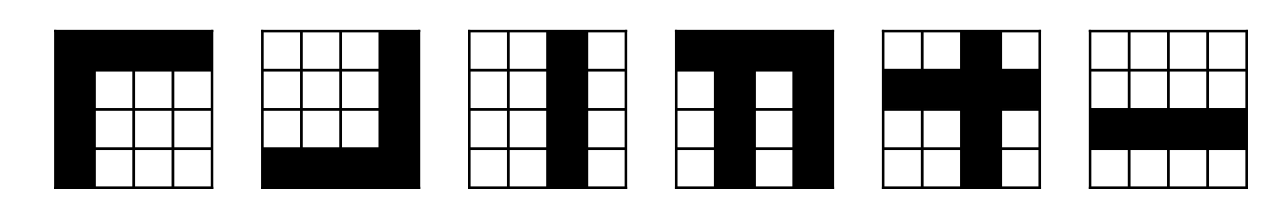
$$\dot{u}_k = \frac{U_y - u_k}{T_u}, \quad U_y = 1 + (U_{\text{max}} - 1) y_k$$

$$\dot{\varphi}_k = \frac{\Phi_u - \varphi_k}{T_\varphi}, \quad \Phi_u = 1 - \frac{u_k y_k}{U_{\text{max}}}$$

$$T^{\text{exc}} = 5 \cdot T^{\text{inh}}.$$



(a) Activity with sensory input shown by vertical stripes.



(b) Examples of input patterns.

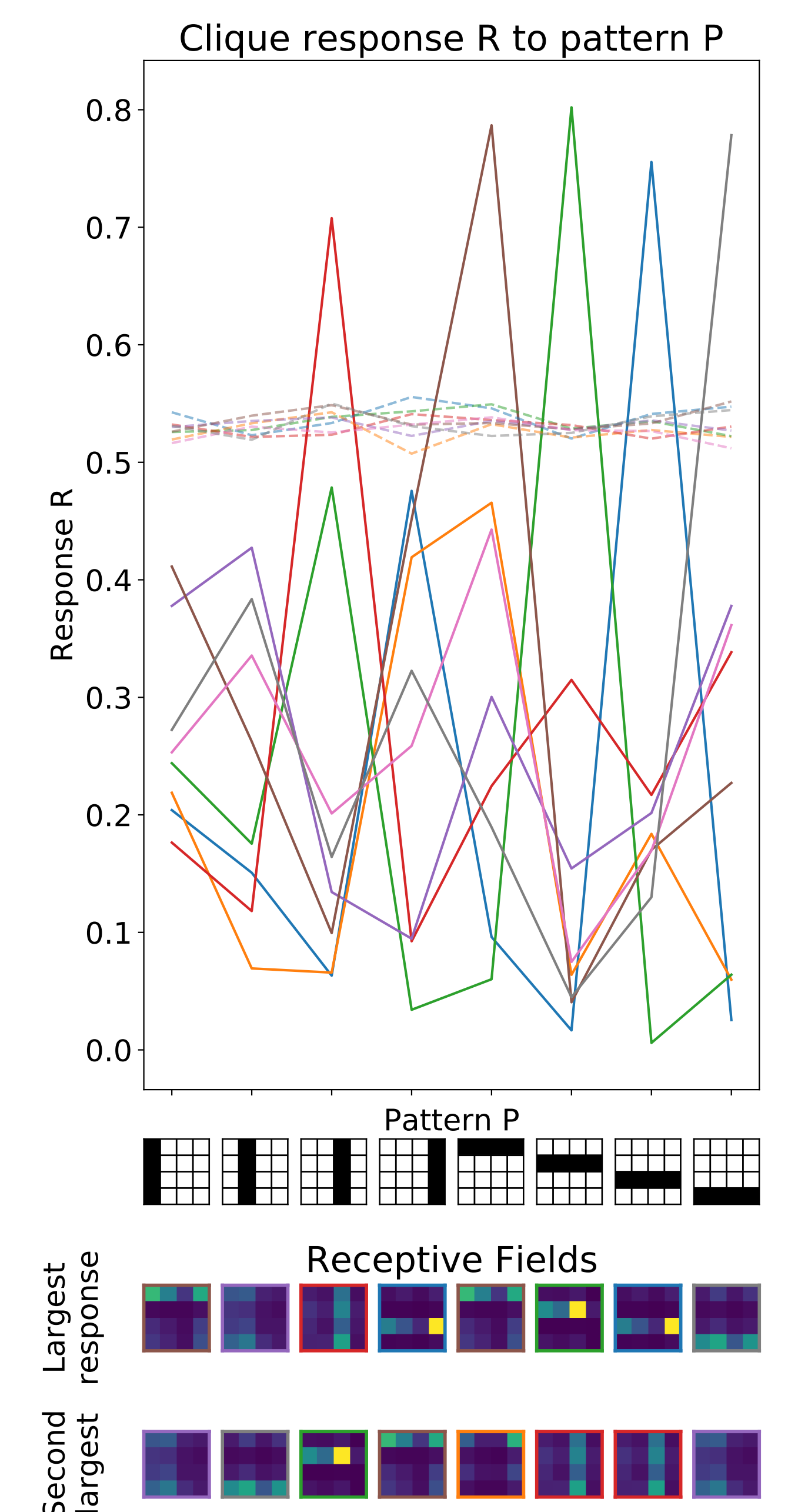


Figure 4: Performance of the learning rule. Top: clique response for every bar, dashed lines show initial responses. Bottom: receptive fields of the two cliques that respond the most to given patterns. The colour coding increases from violet to yellow.