# BIT-PAIR RECODED MULTIPLIER

LAB REPORT 4 FOR ECE327
DIGITAL SYSTEMS DESIGN

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APRIL 11, 2014

## **Abstract**

Bit-pair recoding is an efficient algorithm to perform quick multiplication calculations in hardware. The bit-pair algorithm is useful because it is guaranteed to reduce the number of shift/add operations to half of that of a normal shift/add multiplier. The task of this lab was to implement a bit-pair recoding multiplier in VHDL code. The entire lab was done in simulation and no actual FPGA programming was done. The most difficult aspect of this simulation was timing between the different modules. In order to assuage some of this issues, I implemented a clock to synchronize the operations.

Note: All clocks generated for simulation were built using Morten Zilmers clock gen package [?].

#### Introduction

The purpose of this lab is to simulate a complicated 32-bit multiplier. The multiplier will implement the bit-pair decoding algorithm. A diagram of the system can be seen in Figure 1.1. The signals, registers, and modules are labeled similarly in the code (see appendices).

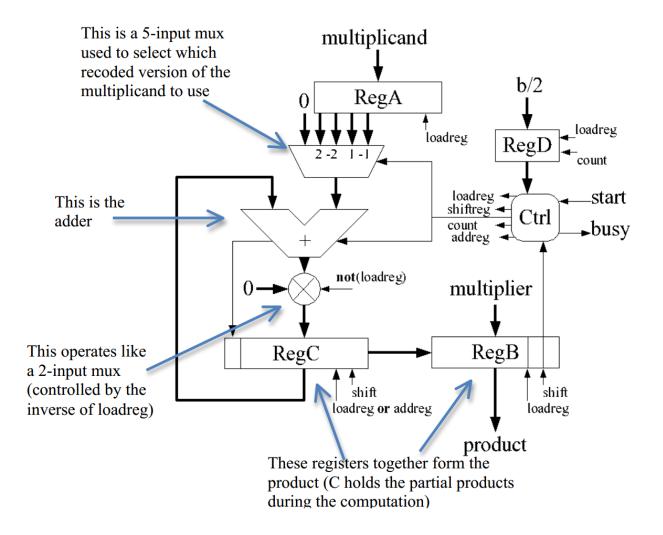


Figure 1.1: Multiplier Circuit

There are five main components to this design: the control module and registers A, B, C, and D. There is also a 32-bit adder module. The "2-input mux" is integrated into register C and the 5-input mux is integrated into register A. This was done to simplify the VHDL coding process.

### 1.1 LAB 4 SYSTEM DESIGN

#### 1.1.1 REGISTER DESIGN

Each register is slightly different than the others. The registers range in complexity as well. Register A is the arguably the second most complicated register in this lab. It stores the multiplicand and outputs the recoded version based upon the code signal (which is the lowest three bits of register B). The output from register A is tied into the 32-bit adder.

The other line that is tied into the adder is the output from register C. Interestingly the input from C is connected to its output. The only way to prevent serious data integrity loss is to control when the registers load and send values. The loadreg signal is what controls this synchronization. Register C accepts input from the adder and will shift the results to the right by two bits. The shifting only occurs when the shift signal is high. The shifted values are sent into the MSBs of register B.

Register B is the closest to a "pure" register. It only stores data and sends the lowest three bits as the code signal. It is also capable of shifting, but instead of shifting in sign bits, register B will shift in the bits that register C just shifter out.

All of these processes and signals are controlled by the control unit. This module is the entry point for the outside world. It interfaces directly with register D to keep track of the calculations needed to finish multiplication. The only signals that interface with the control unit from the outside are the start signal and the busy signal. Once the registers are loaded (A with the multiplicand and B with the multiplier) the start signal can be set high. This will start the multiplication process and will in turn, bring the busy signal high. The start signal will do nothing until the busy signal is reset. Once the busy signal is reset, register C will hold the upper 32 bits of the product and register B will hold the lower 32 bits.

#### 1.1.2 TESTING OF REGISTER A

Each unit was tested in groups. This is due to the reliance of one unit upon signals from other units. It may have been simpler to test units individually, but the method chosen proved to provide quicker results (although, debugging was more difficult). Below are the simulation results for the different unit tests.

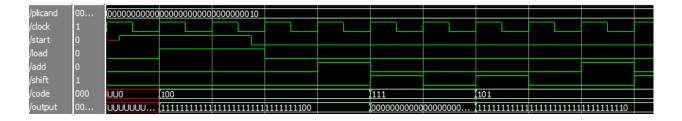


Figure 1.2: Register A Results

The test shown in Figure 1.2 shows the manipulations that are performed on the multiplicand via register A. Notice that as the load value goes high, the first code is produced: 100. This code, and the following codes shown, align perfectly with the expectations for a bit-pair coding scheme.

#### 1.1.3 TESTING OF REGISTERS B AND D

Registers B and D were tested at the same time to show that the counter will stop when the maximum number of shifts have occurred. This was not necessary to do, but it aids the user in understanding why the counter is needed, as the controller has no other way of keeping track of the amount of shifts performed.

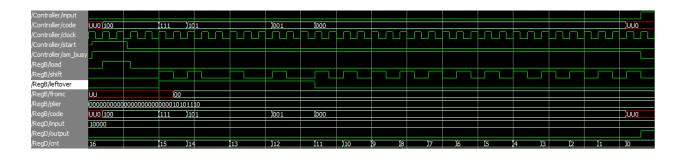


Figure 1.3: Register D and B Test

Notice that the shifts are spaced slightly. This occurs when an add operation is warranted. Later on in the register C test, you will be able to see the add signal being used. The disparity between clock cycles used per operation is the reason for the counter. Without it there would be know way to know preemptively how many clock cycles would be needed for a given multiplication.

#### 1.1.4 TESTING OF REGISTER C

Register C was fairly simple to implement, once the other units were designed. In the test, you will notice that the registers values change based upon the signal changes that occur upon the signals shift, add, and load. Register C performed the same operations as B except it did not send off the lowest three bytes for coding purposes.

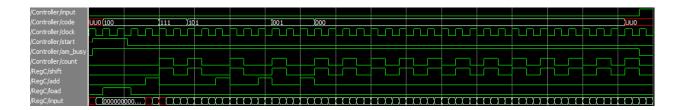


Figure 1.4: FSM State Diagram

### 1.2 CONCLUSIONS

There are definite changes that could be made to this project to increase the efficiency and decrease the overall runtime of the algorithm. Mainly making the system asynchronous. Do do that, more signals would need to be added to the control unit. In particular, bus read signals would be needed to make sure register C doesn't stomp out its own value through the adder loop.

Overall, this lab shows that complex algorithms can be implemented in VHDL by creating small modules, one piece at a time. If anything else can be taken away, it is that testing is best done on INDIVIDUAL units, not groups. By testing entities individually, debugging is greatly simplified and overall development time and stress are reduced.

## APPENDIX A: LAB 4 CODE

```
-- Lab 4 Main Code --
library ieee,work;
use ieee.std_logic_1164.all;
use work.all;
entity Lab4 is
 port (
   MULTIPLICAND : in std_logic_vector(31 downto 0);
   MULTIPLIER : in std_logic_vector(31 downto 0);
   START
           : in std_logic;
   CLOCK
          : in std_logic;
   BUSY
            : out std_logic;
   PRODUCT
            : out std_logic_vector(63 downto 0));
end entity Lab4;
architecture behav of Lab4 is
 -- Schignuls
 signal loadreg : std_logic;
 signal shiftreg : std_logic;
 signal addreg : std_logic;
 signal count : std_logic;
 signal code : std_logic_vector(2 downto 0);
 signal fromc : std_logic_vector(1 downto 0);
 signal rega_out : std_logic_vector(31 downto 0);
 signal regb_out : std_logic_vector(31 downto 0);
 signal regc_out : std_logic_vector(31 downto 0);
 signal addr_out : std_logic_vector(31 downto 0);
```

```
signal twom_out : std_logic_vector(31 downto 0);
signal regd_out : std_logic;
component reg_a is
 port( load : in
                   std_logic;
     plicand : in std_logic_vector(31 downto 0);
     code : in std_logic_vector( 2 downto 0);
     output : buffer std_logic_vector(31 downto 0));
end component reg_a;
component reg_b is
 port( load : in
                   std_logic;
     shift : in std_logic;
     fromc : in std_logic_vector( 1 downto 0);
     plier : in std_logic_vector(31 downto 0);
     code : out std_logic_vector( 2 downto 0);
     output : buffer std_logic_vector(31 downto 0));
end component reg_b;
component reg_c is
 port( clock : in std_logic;
     load : in std_logic;
     shift : in std_logic;
     add : in std_logic;
     input : in std_logic_vector(31 downto 0);
     output : buffer std_logic_vector(31 downto 0);
     fromc : out std_logic_vector( 1 downto 0));
end component reg_c;
component reg_d is
 port( load : in std_logic;
     count : in std_logic;
     input : in std_logic_vector(4 downto 0);
     output : out std_logic);
end component reg_d;
```

```
component two_mux is
   port ( clock : in std_logic;
       load : in std_logic;
       input : in std_logic_vector(31 downto 0);
       output : out std_logic_vector(31 downto 0));
  end component two_mux;
  component add_32 is
   port( right : in std_logic_vector(31 downto 0);
       left : in std_logic_vector(31 downto 0);
       add : in std_logic;
       output : out std_logic_vector(31 downto 0));
 end component add_32;
  component control is
   port( input : in std_logic;
       code : in std_logic_vector(2 downto 0);
       clock : in std_logic;
       start : in std_logic;
       load : out std_logic;
       shift : out std_logic;
       count : out std_logic;
       add : out std_logic;
       busy : out std_logic);
  end component control;
begin
 PRODUCT(63 downto 32) <= regc_out;
 PRODUCT(31 downto 0) <= regb_out;
 RegA : reg_a PORT MAP (
   load => loadreg,
   plicand => MULTIPLICAND,
   code => code,
   output => rega_out
 );
```

```
RegB : reg_b PORT MAP (
 load => loadreg,
 shift => shiftreg,
 fromc => fromc,
 plier => MULTIPLIER,
 code => code,
 output => regb_out
);
RegC : reg_c PORT MAP (
 clock => CLOCK,
 load => loadreg,
 shift => shiftreg,
 add => addreg,
 input => twom_out,
 output => regc_out,
 fromc => fromc
);
RegD : reg_d PORT MAP (
 load => loadreg,
 count => count,
 input => "10000",
 output => regd_out
);
TwoMux : two_mux PORT MAP (
 clock => CLOCK,
 load => loadreg,
 input => addr_out,
 output => twom_out
);
Adder : add_32 PORT MAP (
 right => rega_out,
```

```
left => regc_out,
   add => addreg,
   output => addr_out
 );
 Controller : control PORT MAP(
   input => regd_out,
   code => code,
   clock => CLOCK,
   start => START,
   load => loadreg,
   shift => shiftreg,
   count => count,
   add => addreg,
   busy => BUSY
 );
end architecture behav;
```

```
-- Registah Eyyyyyyy (A) --
_____
-- i phut zee mux in zee --
   registah!
library ieee,work;
use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
use work.all;
entity reg_a is
 port( load : in std_logic;
     plicand : in std_logic_vector(31 downto 0);
     code : in std_logic_vector( 2 downto 0);
     output : buffer std_logic_vector(31 downto 0));
end entity reg_a;
architecture b_reg_a of reg_a is
begin
 loader : process (load,code)
   variable comp : std_logic_vector(31 downto 0);
 begin
   comp := not plicand; -- invert
   comp := std_logic_vector(unsigned(comp) + 1); -- add one
   case code is
     when "000" | "111" => -- 0xM
       output <= X"00000000"; -- bit 32 is unneeded but I'm weird
     when "001" | "010" => -- +1xM
       output <= plicand;</pre>
     when "011" => -- +2xM
       output(0) <= '0';
```

```
output(31 downto 1) <= output(30 downto 0);
when "100" => -- -2xM
output(0) <= '0';
output(31 downto 1) <= comp(30 downto 0);
when "101"|"110" => -- -1xM
output(31 downto 0) <= comp;
when others =>
    -- ya dun &*@#ed up, son
    -- dis iz impossibru
end case;
end process loader;
end architecture b_reg_a;
```

```
-- Registah Bee (B) --
_____
library ieee,work;
use ieee.std_logic_1164.all;
use work.all;
entity reg_b is
 port( load : in std_logic;
     shift : in std_logic;
     fromc : in std_logic_vector( 1 downto 0);
     plier : in std_logic_vector(31 downto 0);
     code : out std_logic_vector( 2 downto 0);
     output : buffer std_logic_vector(31 downto 0));
end entity reg_b;
architecture b_reg_b of reg_b is
 signal leftover : std_logic := '0';
begin
 loader : process (load, shift)
 begin
   if (load = '1') then
     output <= plier;</pre>
     leftover <= '0';</pre>
   end if;
   if (shift = '1') then
     leftover <= output(1);</pre>
     output(29 downto 0) <= output(31 downto 2); -- shift right by 2</pre>
     output(31 downto 30) <= fromc; -- pull in bits from reg_c</pre>
   end if;
  end process loader;
 code(2 downto 1) <= output(1 downto 0);</pre>
 code(0) <= leftover;</pre>
```

```
-- Registah See (C) --
_____
library ieee,work;
use ieee.std_logic_1164.all;
use work.all;
entity reg_c is
 port( clock : in std_logic;
     load : in std_logic;
     shift : in std_logic;
     add : in std_logic;
     input : in std_logic_vector(31 downto 0);
     output : buffer std_logic_vector(31 downto 0);
     fromc : out std_logic_vector( 1 downto 0));
end entity reg_c;
architecture b_reg_c of reg_c is
 signal buff : std_logic_vector(31 downto 0);
begin
  load_input : process (clock,load,add)
 begin
   if (rising_edge(clock) and (load ='1' or add ='1')) then
     buff <= input;</pre>
   end if;
  end process load_input;
 output <= buff;</pre>
 shiftah : process (clock,shift)
   variable old_bit : std_logic;
 begin
   if (rising_edge(clock) and shift = '1') then
     fromc <= buff(1 downto 0);</pre>
```

```
old_bit := buff(31);
buff(29 downto 0) <= buff(31 downto 2); -- buff = output >> 2
buff(31) <= old_bit; -- sign in the bits
buff(30) <= old_bit;
end if;
end process shiftah;
end architecture b_reg_c;</pre>
```

```
-- Registah Dee (D) --
_____
library ieee,work;
use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
use work.all;
entity reg_d is
 port( load : in std_logic;
     count : in std_logic;
     input : in std_logic_vector(4 downto 0);
     output : out std_logic := '0');
end entity reg_d;
architecture b_reg_d of reg_d is
 signal cnt : integer range 0 to 16 := 16;
begin
 decrement : process (count)
 begin
   if (cnt = 0) then
     output <= '1';</pre>
   elsif (count = '1') then
     cnt <= cnt - 1;</pre>
     output <= '0';
   end if;
 end process decrement;
end architecture b_reg_d;
```

```
-- Derty Too Bit Adduh --
_____
-- Notez:
-- no need for carry --
-- out bit in mah
-- implementashun
______
library ieee,work;
use ieee.std_logic_1164.all;
use ieee.numeric_std.all;
use work.all;
entity add_32 is
 port( right : in std_logic_vector(31 downto 0);
     left : in std_logic_vector(31 downto 0);
     add : in std_logic;
     output : out std_logic_vector(31 downto 0));
end entity add_32;
architecture b_add_32 of add_32 is
 signal buff : std_logic_vector(31 downto 0);
begin
 adder : process (add)
 begin
   if (add = '1') then
     buff <= std_logic_vector(unsigned(left)</pre>
        + unsigned(right));
   end if;
   output <= buff;</pre>
 end process adder;
end architecture b_add_32;
```

```
-- Two Input Multiplex --
-----
-- Two Inpuht Mucksh --
-- this file was deemed obsolete and move into register b
library ieee,work;
use ieee.std_logic_1164.all;
use work.all;
entity two_mux is
 port ( clock : in std_logic;
     load : in std_logic;
     input : in std_logic_vector(31 downto 0);
     output : out std_logic_vector(31 downto 0));
end entity two_mux;
architecture b_two_mux of two_mux is
 signal buff : std_logic_vector(31 downto 0) := (others => '0');
begin
 process (clock,load)
 begin
   if (rising_edge(clock) and load = '0') then
     output <= input;</pre>
   else
     output <= X"00000000";</pre>
   end if;
 end process;
end architecture b_two_mux;
```

```
-- TEST BENCH CODE FOR LAB 4 --
_____
library ieee,work;
use ieee.std_logic_1164.all;
use work.clk_package.all;
use work.all;
entity test4 is --test-bench
end entity test4;
architecture behav of test4 is
 component Lab4 is
   port (
     MULTIPLICAND : in std_logic_vector(31 downto 0);
     MULTIPLIER : in std_logic_vector(31 downto 0);
     START
            : in std_logic;
     CLOCK
           : in std_logic;
     BUSY
             : out std_logic;
     PRODUCT : out std_logic_vector(63 downto 0));
 end component;
 signal plicand : std_logic_vector(31 downto 0);
 signal plier : std_logic_vector(31 downto 0);
 signal start : std_logic;
 signal clockt : std_logic;
 signal busyt : std_logic;
 signal prod : std_logic_vector(63 downto 0);
 signal run : std_logic := '1';
begin
 labtest : Lab4
```

```
port map (plicand, plier, start, clockt, busyt, prod);

clk_gen(clockt, 50.000E6, 0 fs, run);

test : process is

begin
  plicand <= X"000000001";
  plier <= X"000000002"; wait for 5 ns;
  start <= '1'; wait for 50 ns;
  start <= '0'; wait;
  end process;

end architecture behav;</pre>
```