MDS-SIM-Partial_21-22Q1: Template for solutions to questions

Your Name and ID Number

November 8th, 2021

Data Description

Available variables:

Nutrient analysis of pizzas (from https://data.world/sdhilip/pizza-datasets). Who likes pizza? I mean, there are so many things to like, let's take a closer look! The data set pizza. Pizza.RData contains measurements that capture the kind of things that make a pizza tasty. Can you determine which pizza brand works best for you and explain why? The variables in the data set are:

- brand: Pizza brand (class label)
- id: Sample analysed
- mois: Amount of water per 100 grams in the sample
- prot: Amount of protein per 100 grams in the sample
- fat: Amount of fat per 100 grams in the sample
- ash: Amount of ash per 100 grams in the sample
- sodium: Amount of sodium per 100 grams in the sample
- carb: Amount of carbohydrates per 100 grams in the sample
- cal: Amount of calories per 100 grams in the sample

List of Questions

Firstly, load dataset and check available variables.

```
# Clear plots
if(!is.null(dev.list())) dev.off()

## null device
## 1

# Clean workspace
rm(list=ls())

setwd("C:/Users/lmontero/Dropbox/DOCENCIA/MUM-DATS/EXAMS/CURS21-22")
pathfile<-"C:/Users/lmontero/Dropbox/DOCENCIA/MUM-DATS/EXAMS/CURS21-22/"
# pizza <- read.table("Pizza.csv", header=T, dec=".", sep=",",stringsAsFa</pre>
```

```
ctors = T)
# df <- pizza
# row.names(pizza) <- paste0(pizza$brand,".",pizza$id)</pre>
# save(list=c("pizza", "df"), file="Pizza.RData")
load(paste0(pathfile, "Pizza.RData"))
summary(df)
##
       brand
                     id
                                   mois
                                                                fat
                                                  prot
         : 33
                      :14003 Min. :25.00
                                             Min. : 6.98 Min.
  Н
                                                                  : 4.38
##
                Min.
                ##
   D
          : 32
                                             1st Ou.: 8.06
                                                           1st Ou.:14.77
##
   J
          : 32
                                             Median :10.44 Median :17.14
                                                  :13.37 Mean :20.23
  В
          : 31
                Mean :20841 Mean
                                    :40.90
                                             Mean
                3rd Qu.:24110 3rd Qu.:49.12
                                                            3rd Qu.:21.43
##
   F
          : 30
                                             3rd Qu.:20.02
                Max. :34045 Max.
##
          : 29
                                     :57.22
                                             Max.
                                                   :28.48
                                                                  :47.20
   Α
                                                            Max.
   (Other):113
##
##
                     sodium
                                      carb
        ash
                                                     cal
## Min.
          :1.170 Min.
                        :0.2500 Min.
                                        : 0.510 Min.
                                                       :2.180
                  1st Qu.:0.4500 1st Qu.: 3.467
                                                1st Qu.:2.910
   1st Qu.:1.450
##
                  Median :0.4900 Median :23.245
   Median :2.225
##
                                                Median :3.215
                                                       :3.271
   Mean
        :2.633
                  Mean
                        :0.6694 Mean
                                       :22.865
                                                Mean
   3rd Qu.:3.592
                  3rd Qu.:0.7025 3rd Qu.:41.337 3rd Qu.:3.520
##
   Max. :5.430
                  Max. :1.7900 Max.
                                       :48.640
                                               Max.
                                                       :5.080
##
names(df)
## [1] "brand"
                "id"
                         "mois"
                                  "prot"
                                           "fat"
                                                    "ash"
                                                             "sodium" "ca
rb"
## [9] "cal"
vars res <- names(df)[c(9)]</pre>
vars_con \leftarrow names(df)[c(3:8)]
vars_dis \leftarrow names(df)[c(10:11)]
```

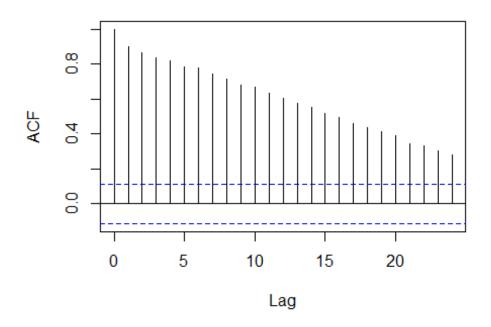
The amount of calories per 100 grams is selected as the numeric target.

1. Determine whether serial correlation is present on dataset or not.

You have seen acf() method to plot autocorrelation in calories. The plot clearly shows a serial correlation. Durbin-Watson test is an inferential tool that addresses whether autocorrelation is present and the null hypothesis is clearly rejected, thus again, autocorrelation is present in the cal column of the pizza dataset.

```
acf(df$cal)
```

Series df\$cal



```
library(lmtest)
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
       as.Date, as.Date.numeric
##
dwtest(df$cal~1)
##
##
    Durbin-Watson test
##
## data: df$cal ~ 1
## DW = 0.1699, p-value < 2.2e-16
## alternative hypothesis: true autocorrelation is greater than 0
```

2. Define a new variable containing the total amount of ingredients (water, protein, fat, ash and carbohydrates). Check consistency.

Total sum of indicated ingredients accounts for 100 g in 292 observations and a less than 1 g deviation (above/below) can be seen in the rest of observations.

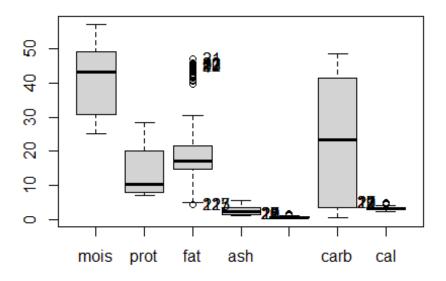
```
names(df)
```

```
## [1] "brand" "id"
                          "mois"
                                   "prot"
                                             "fat"
                                                      "ash"
                                                               "sodium" "ca
rb"
## [9] "cal"
df$ingredients <- rowSums(df[,c(3:6,8)])</pre>
summary( df$ingredients )
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                               Max.
     99.37 100.00 100.00
##
                            100.00 100.00
                                             100.83
table( df$ingredients )
##
    99.37
           99.99
                     100 100.01 100.05
##
                                       100.1 100.27 100.63 100.83
##
        1
               1
                     292
                              1
                                     1
                                             1
                                                    1
                                                           1
```

3. Univariant severe outliers are also present in some variables. Determine them.

Univariate severe outlier checking is addressed for all variables. There 271 observation without any outlier, 4 observations having 1 outlier (in sodium) and 25 observations having 2 outliers (on fat and sodium).

```
Boxplot( df[,c(3:9)])
```



```
## [1] "123" "125" "217" "21" "3" "11" "22" "10" "27" "13" "9" "12" "13" "9" "20" "20" "22" "25" "17" "29"
```

```
"21"
## [25] "11" "12" "22" "3" "10" "1"
                                           "9" "13" "27"
unidesfat <- summary( df$fat ); unidesfat</pre>
##
      Min. 1st Qu. Median
                             Mean 3rd Qu.
                                              Max.
##
      4.38
             14.77
                     17.14
                             20.23
                                     21.43
                                             47.20
thrusout <- unidesfat[5]+3*( unidesfat[5]-unidesfat[2]);thrusout
## 3rd Ou.
## 41.43
llusout <- which( df$fat > thrusout ); llusout
## [1] 1 2 3 4 5 6 8 9 10 11 12 13 14 15 16 20 21 22 23 24 25 26
27 28 29
df$sevout <- 0
df$sevout[ llusout ] <- 1</pre>
unidesash <- summary( df$ash ); unidesash</pre>
##
      Min. 1st Qu.
                    Median
                              Mean 3rd Qu.
                                              Max.
##
     1.170
             1.450
                     2.225
                             2.633
                                     3.592
                                             5.430
thrusout <- unidesash[5]+3*( unidesash[5]-unidesash[2]);thrusout
## 3rd Qu.
     10.02
##
llusout <- which( df$ash > thrusout ); llusout
## integer(0)
if (length(llusout) > 0 ) df$sevout[ llusout ] <- df$sevout[ llusout ] +</pre>
1
unidessod <- summary( df$sodium ); unidessod</pre>
##
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                              Max.
## 0.2500 0.4500 0.4900 0.6694 0.7025 1.7900
thrusout <- unidessod[5]+3*( unidessod[5]-unidessod[2]);thrusout
## 3rd Qu.
##
      1.46
llusout <- which( df$sodium > thrusout ); llusout
## [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22
23 24 25
## [26] 26 27 28 29
```

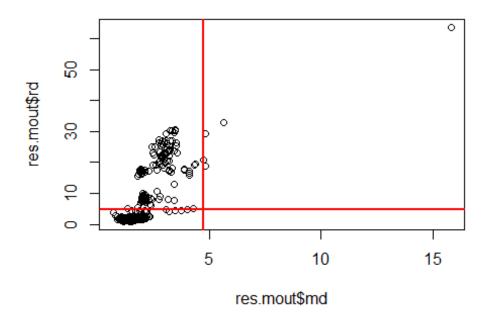
```
if (length(llusout) > 0 ) df$sevout[ llusout ] <- df$sevout[ llusout ] +</pre>
unidescal <- summary( df$cal ); unidescal</pre>
##
      Min. 1st Ou.
                    Median
                               Mean 3rd Ou.
                                                Max.
##
     2.180
             2.910
                      3.215
                              3.271
                                      3.520
                                               5.080
thrusout <- unidescal[5]+3*( unidescal[5]-unidescal[2]);thrusout
## 3rd Qu.
      5.35
##
llusout <- which( df$cal > thrusout ); llusout
## integer(0)
if (length(llusout) > 0 ) df$sevout[ llusout ] <- df$sevout[ llusout ] +</pre>
summary( df$sevout )
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Ou.
                                                Max.
##
      0.00
              0.00
                       0.00
                               0.18
                                       0.00
                                                2.00
table( df$sevout )
##
##
     0
             2
         1
## 271
            25
```

4. Are there multivariant outliers? Find them. Try to explain their singularity. Multivariant outliers,if present, are not going to be treated in this exercise: keep them as suplementary observations in the rest of the exercise. Which is the cutoff at 99.9% CI?

There are 4 multivariant outliers according to the indicated criterion: observations 66-C 82-C 166-F and 296-J. Observation 166 without any doubt a multivariate outlier, the one with the largest Mahalanobis distance.

```
library(chemometrics)
res.mout <- Moutlier( df[ , c(4:9)], quantile = 0.999, plot=F )

par(mfrow=c(1,1))
plot( res.mout$md, res.mout$rd )
abline( h=res.mout$cutoff, lwd=2, col="red")
abline( v=res.mout$cutoff, lwd=2, col="red")</pre>
```



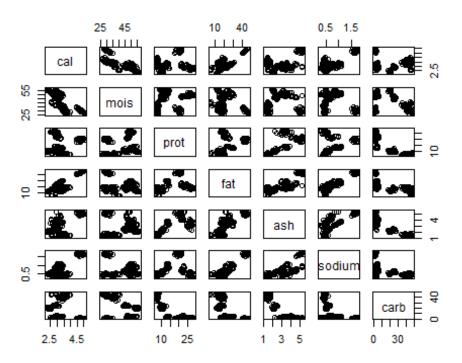
```
11mout <- which( ( res.mout$md > res.mout$cutoff ) & (res.mout$rd > res.m
out$cutoff) );llmout
## [1] 66 82 166 296
df[llmout,]
##
               id mois
                        prot
                                fat ash sodium carb cal ingredients sevout
## 66
          C 14029 49.73 25.65 19.98 2.51
                                          0.52
                                                2.13 2.91
                                                               100.00
                                          0.41 3.31 2.83
## 82
          C 24124 49.57 26.91 18.00 2.21
                                                               100.00
                                                                          0
## 166
          F 24055 27.93 7.88 17.49 1.44
                                          0.47 45.26 3.96
                                                               100.00
                                                                          0
## 296
          J 34044 44.91 11.07 17.00 2.49
                                          0.66 25.36 2.91
                                                               100.83
res.mout$md[llmout]
## [1]
       4.843280 5.651025 15.825626 4.826506
df$mout <- 0
df$mout[ llmout ] <- 1</pre>
df$mout <- factor( df$mout, labels = c("MvOut.No", "MvOut.Yes"))</pre>
```

5. Indicate by using exploratory data analysis tools which are apparently the most associated variables with the numeric response variable (only the contributing variables to the ingredients are to be taken as active variables). Use also FactoMineR profiling tools at 99% significance level.

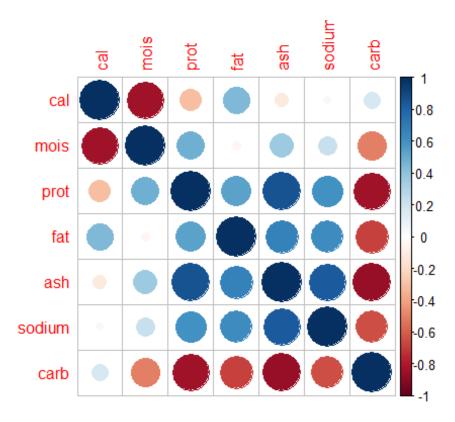
The globally most associated numeric variables are fat (direct relation) and mois (inverse relation), following sodium and ash (direct relation). Brand is globally

associated to cal, thus the number of calories per 100g of pizza depends on the brand. In particular, A and F brands are those having average caloric contribution greater than the mean (being A brand very remarkable) and J and I brands lie under the mean caloric contribution (mainly I brand).

```
res.con <- condes( df[,c(1,3:9)], num.var=8, proba = 0.01 )
res.con$quanti
                           p.value
##
          correlation
## fat
            0.7645671 8.656128e-59
## sodium
            0.6719575 9.322465e-41
            0.3264685 7.021205e-09
## ash
           -0.7644405 9.279582e-59
## mois
res.con$quali
##
                R2
                         p.value
## brand 0.9293717 3.264747e-161
res.con$category
##
             Estimate
                           p.value
## brand=A 1.4988622 1.983234e-66
## brand=F 0.3210691 2.348708e-03
## brand=G 0.3202415 2.911370e-03
## brand=D -0.2714934 9.575679e-03
## brand=C -0.4260420 1.821239e-04
## brand=J -0.3964934 1.300208e-04
## brand=I -0.8907930 8.680093e-18
plot(df[,c(9,3:8)])
```



```
cor(df[,c(9,3:8)], method="spearman")
##
                                    prot
                                                fat
                                                          ash
                                                                 sodium
               cal
                         mois
## cal
          1.0000000 -0.84373723 -0.3038314
                                         0.44513377 -0.1158363
                                                              0.0416364
## mois
         -0.8437372 1.00000000 0.4804072 -0.04594197 0.3613436
                                                               0.2216707
         -0.3038314 0.48040722
                              1.0000000
                                        0.53426888 0.8659212
                                                              0.6002271
## prot
## fat
          0.4451338 -0.04594197 0.5342689
                                        1.00000000 0.6713663
                                                              0.6281431
## ash
         0.8321020
## sodium 0.0416364 0.22167073 0.6002271 0.62814312 0.8321020
                                                              1.0000000
## carb
          0.1770379 -0.50109708 -0.8448299 -0.68186774 -0.8653723 -0.6440725
##
               carb
## cal
          0.1770379
## mois
         -0.5010971
## prot
         -0.8448299
## fat
         -0.6818677
## ash
         -0.8653723
## sodium -0.6440725
## carb
          1.0000000
corrplot(cor(df[,c(9,3:8)], method="spearman"), is.corr=T)
```



6. Use brand target factor and determine the most relevant global associations at 99% CI. Profile A and I brands.

Global association to brand factor is depending on mean carbohidrates, protein and water composition. Nevertheless, all available ingredients are shown to have average values depending on brand.

- Brand A has remarkable sodium, fat, cal, protein and ash over the global mean for those ingredients, while water and carbohidrates lie under their mean for A brand.
- Brand B has a mean content of water, sodium, fat and ashes over the mean. Carbohidrate contents is under the mean.
- Brand C shows a mean content of proteins, water and ashes over the mean and mean sodium, calories and carbohidrates under the mean.

The same interpretation pattern has to be followed for the other brands.

```
res.cat <- catdes( df[,c(1,3:9)], num.var=1, proba = 0.01)
res.cat$quanti.var
##
               Eta2
                          P-value
          0.9911957 3.087183e-292
## carb
          0.9861491 1.036517e-263
## prot
## mois
          0.9774313 5.578472e-233
## sodium 0.9709591 4.116312e-217
## ash
          0.9683272 1.184316e-211
          0.9293717 3.264747e-161
## cal
          0.9273634 1.889056e-159
## fat
```

```
res.cat$quanti
## $A
##
              v.test Mean in category Overall mean sd in category Overall sd
## sodium 15.096829
                             1.656207
                                           0.669400
                                                         0.06354004
                                                                       0.369740
                            43,446897
## fat
          14.656206
                                          20.229533
                                                         1.83069820
                                                                       8.960686
## cal
          13.732781
                             4.773793
                                           3.271000
                                                         0.16078286
                                                                       0.619000
## ash
                             5.014483
                                           2.633233
                                                         0.20088745
                                                                       1.267606
          10.626022
## prot
           5.929520
                                                                       6.423659
                            20.107241
                                          13.373567
                                                         1.06066634
## mois
          -6.486769
                            29.966207
                                          40.903067
                                                         1.92140289
                                                                       9.537052
## carb
          -6.718160
                             1.486897
                                          22.864767
                                                         0.60894541 17.999648
##
                p.value
## sodium 1.699107e-51
## fat
          1.229536e-48
## cal
          6.460533e-43
## ash
          2.255290e-26
##
  prot
          3.038206e-09
          8.769645e-11
## mois
## carb
          1.840330e-11
##
## $B
##
              v.test Mean in category Overall mean sd in category Overall sd
## mois
           6.404050
                           51.3077419
                                          40.903067
                                                         1.70058569
                                                                       9.537052
## sodium
           5.007937
                            0.9848387
                                           0.669400
                                                         0.09641546
                                                                       0.369740
                                          20.229533
                           27.6203226
                                                                       8.960686
## fat
           4.841610
                                                         2.14682283
## ash
           3.845024
                            3.4635484
                                           2.633233
                                                         0.23394993
                                                                       1.267606
## carb
          -6.162050
                            3.9696774
                                          22.864767
                                                         0.60446449
                                                                     17.999648
##
                p.value
## mois
          1.513088e-10
## sodium 5.501641e-07
## fat
          1.287911e-06
## ash
          1.205406e-04
## carb
          7.180902e-10
##
## $C
##
             v.test Mean in category Overall mean sd in category Overall sd
## prot
          10.710567
                           26.0255556
                                          13.373567
                                                         1.18318883
                                                                       6.423659
## mois
           4.889031
                           49.4774074
                                          40.903067
                                                         1.48152722
                                                                       9.537052
## ash
           2.788895
                            3.2833333
                                           2.633233
                                                         0.40139571
                                                                       1.267606
## sodium -3.008943
                            0.4648148
                                           0.669400
                                                         0.08941664
                                                                       0.369740
## cal
                                                         0.17299825
          -3.708278
                            2.8488889
                                           3.271000
                                                                       0.619000
## carb
          -6.289570
                            2.0462963
                                          22.864767
                                                         0.80335015
                                                                     17.999648
##
                p.value
##
  prot
          9.080429e-27
## mois
          1.013338e-06
## ash
          5.288819e-03
## sodium 2.621584e-03
## cal
          2.086735e-04
## carb
          3.183464e-10
##
## $D
##
           v.test Mean in category Overall mean sd in category Overall sd
## prot
         8.239120
                          22.231250
                                        13.373567
                                                        1.3674012
                                                                    6.423659
##
  ash
         7.931710
                           4.315937
                                         2.633233
                                                        0.4426896
                                                                    1.267606
## mois
        4.240345
                          47.671250
                                        40.903067
                                                        1.1203480
                                                                    9.537052
```

```
## cal -2.582723
                           3.003437
                                         3.271000
                                                       0.1504287
                                                                    0.619000
## carb -6.217024
                           4.136250
                                        22.864767
                                                       1.7560729 17.999648
##
             p.value
## prot 1.734818e-16
## ash 2.161490e-15
## mois 2.231768e-05
## cal 9.802407e-03
  carb 5.066716e-10
##
##
## $E
##
             v.test Mean in category Overall mean sd in category Overall sd
## carb
                           39.5921429
                                          22.864767
                                                        3.12111971
                                                                     17.999648
           5.155775
## mois
                           36.0832143
                                          40.903067
                                                        1.72366315
                                                                      9.537052
          -2.803818
## fat
          -3.166170
                           15.1157143
                                          20.229533
                                                        4.03342059
                                                                      8.960686
## sodium -3.302798
                            0.4492857
                                           0.669400
                                                        0.03358662
                                                                      0.369740
                                                                      6.423659
## prot
          -4.871710
                            7.7328571
                                          13.373567
                                                        0.38725091
##
  ash
          -5.064542
                            1.4760714
                                           2.633233
                                                        0.09611523
                                                                      1.267606
##
               p.value
## carb
          2.525838e-07
## mois
          5.050147e-03
## fat
          1.544605e-03
## sodium 9.572536e-04
## prot
          1.106367e-06
## ash
          4.093841e-07
##
## $F
##
             v.test Mean in category Overall mean sd in category Overall sd
## carb
           7.020075
                            44.787333
                                          22.864767
                                                        1.72395849 17.999648
           3.026266
                             3.596000
                                           3.271000
## cal
                                                        0.15116437
                                                                      0.619000
## sodium -3.233156
                             0.462000
                                           0.669400
                                                        0.03177001
                                                                      0.369740
## prot
          -4.913160
                             7.898000
                                          13.373567
                                                        0.21575295
                                                                      6.423659
## ash
                                           2.633233
                                                        0.08557583
                                                                      1.267606
          -5.272613
                             1.473667
## mois
          -6.949446
                            29.404333
                                          40.903067
                                                        0.90676231
                                                                      9.537052
##
               p.value
## carb
          2.217497e-12
## cal
          2.475947e-03
## sodium 1.224306e-03
## prot
          8.962010e-07
## ash
          1.344947e-07
          3.667226e-12
## mois
##
## $G
##
             v.test Mean in category Overall mean sd in category Overall sd
## carb
           7.406098
                           46.4317241
                                          22.864767
                                                        1.64332520
                                                                     17.999648
## cal
           2.962343
                            3.5951724
                                           3,271000
                                                        0.13197755
                                                                      0.619000
## fat
                           15.6437931
                                          20.229533
          -2.894797
                                                        1.85630968
                                                                      8.960686
## sodium -3.451484
                            0.4437931
                                           0.669400
                                                        0.02265389
                                                                      0.369740
## prot
          -4.523538
                                          13.373567
                            8.2365517
                                                        0.18475101
                                                                      6.423659
## ash
          -5.293876
                            1.4468966
                                           2.633233
                                                        0.10399282
                                                                      1.267606
## mois
          -7.509988
                           28.2410345
                                          40.903067
                                                        1.47993789
                                                                      9.537052
##
               p.value
## carb
          1.300697e-13
## cal
          3.053074e-03
## fat
          3.794038e-03
## sodium 5.575118e-04
```

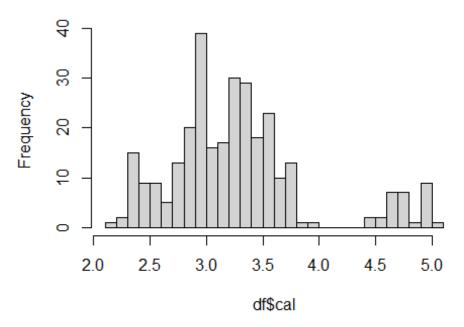
```
6.081431e-06
## prot
         1.197503e-07
## ash
## mois
          5.913294e-14
##
## $H
##
            v.test Mean in category Overall mean sd in category Overall sd
                                                     2.56523251 17.999648
## carb
          5.984341
                         40.5839394
                                       22.864767
## mois
         -3.236743
                         35.8251515
                                       40.903067
                                                     1.36110499
                                                                  9.537052
## fat
         -4.028443
                         14.2915152
                                       20.229533
                                                    3.53491770
                                                                  8.960686
## sodium -4.165271
                          0.4160606
                                       0.669400
                                                     0.02214818
                                                                  0.369740
                                       13.373567
## prot
         -5.185103
                          7.8945455
                                                     0.41615186
                                                                  6.423659
## ash
          -5.885163
                          1.4060606
                                       2.633233
                                                     0.12782420
                                                                  1.267606
##
              p.value
## carb
         2.172671e-09
## mois
         1.209022e-03
         5.614757e-05
## fat
## sodium 3.109829e-05
        2.158952e-07
## prot
## ash
         3.976621e-09
##
## $I
##
            v.test Mean in category Overall mean sd in category Overall sd
                         54.5927586
                                        40.90307
                                                     0.96211296
## mois
          8.119504
                                                                  9.537052
## prot
         -2.633334
                         10.3831034
                                        13.37357
                                                     0.53367369
                                                                  6.423659
## sodium -2.786784
                          0.4872414
                                         0.66940
                                                     0.02317796
                                                                  0.369740
         -4.525408
                         13.0606897
                                        20.22953
                                                     0.90310167
                                                                  8.960686
## fat
         -8.104298
## cal
                          2.3841379
                                         3.27100
                                                     0.07151162
                                                                  0.619000
##
              p.value
         4.680938e-16
## mois
## prot
         8.455122e-03
## sodium 5.323398e-03
## fat
       6.027898e-06
## cal
          5.305112e-16
##
## $J
##
          v.test Mean in category Overall mean sd in category Overall sd
                                                                9.537052
## mois 3.215215
                        46.035000
                                      40.90307
                                                   1.37306227
## fat -2.604206
                        16.324063
                                      20.22953
                                                   1.11237319
                                                                8.960686
## prot -2.611272
                        10.566250
                                      13.37357
                                                   0.63352067
                                                                6.423659
## cal -3.789321
                         2.878437
                                       3.27100
                                                   0.09718248
                                                                0.619000
##
             p.value
## mois 0.0013034674
## fat 0.0092087434
## prot 0.0090206160
## cal 0.0001510599
```

7. Say a few words about the hypothetical distribution that was assumed in the past. Use graphical and inferential arguments.

Either considering histogram chart, or by assessing normal distribution on the logarithm transformation. Using input data analysis and distribution fitting tools, the distribution is shown to lie close to lognormal in the beta area.

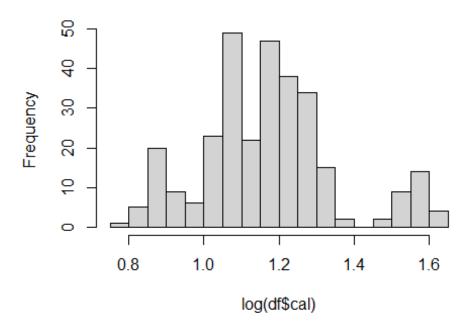
```
hist(df$cal,30)
```

Histogram of df\$cal



hist(log(df\$cal),30)

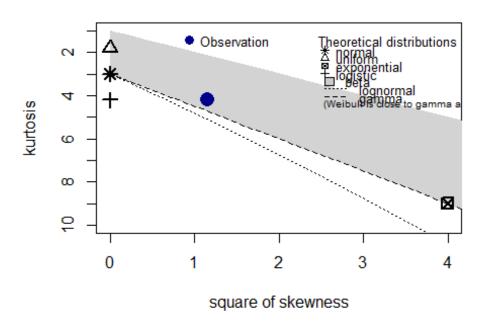
Histogram of log(df\$cal)



shapiro.test(log(df\$cal))

```
##
## Shapiro-Wilk normality test
##
## data: log(df$cal)
## W = 0.9536, p-value = 3.768e-08
library(fitdistrplus)
descdist( df$cal )
```

Cullen and Frey graph



```
## summary statistics
## -----
## min: 2.18 max: 5.08
## median: 3.215
## mean: 3.271
## estimated sd: 0.6200343
## estimated skewness: 1.074278
## estimated kurtosis: 4.188494
```

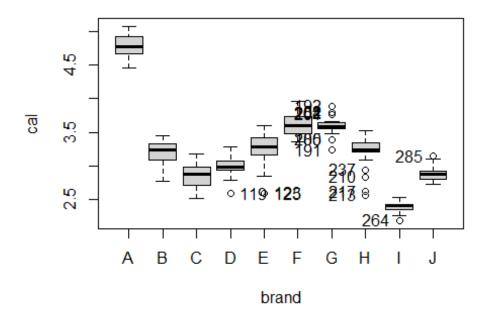
8. Let us focus on cal variate dispersion behavior according to the brand. Use numeric, graphics and inferential tools to address the topic.

Numeric summary across brand standard deviation for calories, allow to classify brands according to low standard deviation for I and J, medium for A, B, C, D, F and G and high for E and H. Inferential testing using Fligner-Killeen test a null hypothesis of homogeinity of variance allows to reject the null hypothesis because pvalue is 0.0003 lower than any common significative level.

```
tapply( df$cal, df$brand, sd ) # E and H overdispersed I and J underdispe
rsed

## A B C D E F G
## 0.16362880 0.17197587 0.17629375 0.15283576 0.25444696 0.15374856 0.13431362
## H I J
## 0.22080946 0.07277741 0.09873749

Boxplot( cal~brand, data = df )
```



```
## [1] "119" "123" "125" "180" "191" "205" "182" "192" "201" "202" "204"
"210"
## [13] "213" "217" "237" "264" "285"

fligner.test( cal~brand, data = df )

##
## Fligner-Killeen test of homogeneity of variances
##
## data: cal by brand
## Fligner-Killeen:med chi-squared = 30.956, df = 9, p-value = 0.0003012
```

9. Let us focus on cal variate mean behavior according to the brand. Use numeric, graphics and inferential tools to address whether the mean of the target depends on the brand or not.

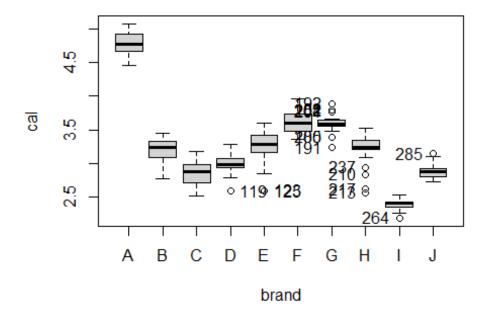
The mean calories for C, I and J brands seems to be less than those for other brands taking into account mean summary across brand levels. A brand has the highest value

for mean calories and it is remarkable higher than the rest. Using the non-parametric Kruskal-Wallis homogeneity test for means, the null hypothesis is absolutely rejected (pvalue 2.2e-16).

```
tapply( df$cal, df$brand, mean ) # A overmean I undermean

## A B C D E F G H
## 4.773793 3.190968 2.848889 3.003437 3.253929 3.596000 3.595172 3.224545
## I J
## 2.384138 2.878437

Boxplot( cal~brand, data = df )
```



```
## [1] "119" "123" "125" "180" "191" "205" "182" "192" "201" "202" "204"
"210"
## [13] "213" "217" "237" "264" "285"

kruskal.test( cal~brand, data = df )
##
## Kruskal-Wallis rank sum test
##
## data: cal by brand
## Kruskal-Wallis chi-squared = 255.14, df = 9, p-value < 2.2e-16</pre>
```

10. Continuing with the former question, on the positive case which brands show a remarkable difference in mean behavior among them. Use one-sided tests.

Pairwise non-parametric one-sided tests can be applied. A brand mean calories are significantively greater than other brand means. D brand mean is greater than C brand mean at 5% significance level. E brand mean calories is greater than C and D brand means. F and G brand mean calories are greater that B, C, D, and E brand means. J brand mean calories is greater than I brand mean.

```
pairwise.wilcox.test( df$cal, df$brand, alternative="less" )
## Pairwise comparisons using Wilcoxon rank sum test with continuity cor
rection
##
## data: df$cal and df$brand
##
                  C D
                                               G
##
    Α
## B 5.8e-10 -
## C 2.1e-09 1.2e-06 -
## D 4.5e-10 0.00051 1.00000 -
## E 1.5e-09 1.00000 1.00000 1.00000 -
## F 7.9e-10 1.00000 1.00000 1.00000 - -
## G 1.1e-09 1.00000 1.00000 1.00000 1.00000 -
## H 3.3e-10 1.00000 1.00000 1.00000 8.3e-09 5.7e-09 -
## I 1.1e-09 5.8e-10 2.5e-09 4.5e-10 1.5e-09 7.9e-10 1.1e-09 3.3e-10 -
## J 4.5e-10 7.7e-08 1.00000 0.00039 1.3e-06 3.2e-10 4.5e-10 1.6e-07 1.00000
##
## P value adjustment method: holm
pairwise.wilcox.test( df$cal, df$brand, alternative="greater" )
##
## Pairwise comparisons using Wilcoxon rank sum test with continuity cor
rection
##
## data: df$cal and df$brand
##
                                  Ε
##
                   C
                                                 G
## B 1.00000 -
## C 1.00000 1.00000 -
## D 1.00000 1.00000 0.03808 -
## E 1.00000 1.00000 4.3e-06 0.00014 -
## F 1.00000 1.2e-09 2.1e-09 3.2e-10 3.1e-06 -
## G 1.00000 3.3e-09 2.8e-09 6.5e-10 1.0e-06 1.00000 -
## H 1.00000 1.00000 1.1e-06 0.00013 1.00000 1.00000 -
## I 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 -
## J 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 4.7e-10
## P value adjustment method: holm
```

11. The standard deviation of the number of calories for brand A should not exceed 0.15cal. For the simple random sample in your dataset calculate the

deviation of calories for 100g assuming a normal distribution for 100 g calories. Stating any assumptions, you need (write them), test at the 1% level the null hypothesis that the population standard deviation is not larger than 0.15cal against the alternative that it is.

Hipothesis testing for population variances on normal data is addressed using chisquared distribution and sample variance. Null hypothesis is stated one-sided

$$H_0$$
: $\sigma^2 = 0.15^2$

And

$$H_1$$
: $\sigma^2 > 0.15^2$

Chi-squared statistic takes a 33.32 value with 29-1=28 degrees of freedom. P value is 0.224 > 0.01 significance level, thus H0 fails to be rejected taking into account the subsample defined for A brand. Using varTest() is possible and the same result is obtained once arguments are properly set.

```
tapply(df$cal,df$brand,sd)
                                C
## 0.16362880 0.17197587 0.17629375 0.15283576 0.25444696 0.15374856 0.13431362
                      Ι
## 0.22080946 0.07277741 0.09873749
table(df$brand)
##
## A B C D E F G H I J
## 29 31 27 32 28 30 29 33 29 32
ss <- 0.16362880
# HO: sigma^2= 0.15^2 H1: sigma > 0.15^2 Normal population (n-1)ss^2/si
qma^2 \sim X2(n-1)
# (n-1)ss^2/sigma^2
chi<-(29-1)*(ss^2)/(0.15^2);chi
## [1] 33.31923
1-pchisq(chi, 28) # pvalue > 0.01 H0 can not be rejected
## [1] 0.2241883
# b - 99% CI
library(EnvStats)
x <- df$cal[df$brand=="A"];x</pre>
## [1] 4.93 4.84 4.95 4.74 4.67 4.67 4.63 4.72 4.93 4.95 4.98 4.97 4.91 4.72 4.67
## [16] 4.77 4.47 4.46 4.53 4.66 5.08 4.97 4.68 4.70 4.56 4.80 4.91 4.79 4.78
varTest(x, sigma.squared=0.15^2, alternative="greater",conf.level=0.99)
```

12. Figure out the 99% upper threshold for the number of calories for brand A population variance. Normal distribution for calories is assumed to hold.

Using varTest() once arguments are properly set, an upper value of 0.05527 is obtained for the variance and thus 0.2351 for the standard deviation of A brand calories.

```
varTest(x, sigma.squared=0.15^2, alternative="less",conf.level=0.99)
##
   Chi-Squared Test on Variance
##
##
## data:
## Chi-Squared = 33.319, df = 28, p-value = 0.7758
## alternative hypothesis: true variance is less than 0.0225
## 99 percent confidence interval:
## 0.0000000 0.05526714
## sample estimates:
##
    variance
## 0.02677438
sqrt(0.05526714)
## [1] 0.2350896
```

13. Build a 99% confidence interval for the difference in the mean of 100 g calories between brands A and C. Assume that equal variances in the population calories per brand does not hold.

Equal variances for A and C brand calories can be tested using Fligner-Killeen test. Homogeneity of variances can not be rejected, thus a pooled variance can be calculated and a two-sided t.test assuming equal variances for the null hypothesis of mean calories being equal in both brands is clearly rejected. Mean cal difference (A - C) 99% CI is defined to be between 1.80 and 2.05.

```
tapply(df$cal,df$brand,mean)
## A B C D E F G H
## 4.773793 3.190968 2.848889 3.003437 3.253929 3.596000 3.595172 3.224545
```

```
## I J
## 2.384138 2.878437
tapply(df$cal,df$brand,sd)
                                C
##
                      В
                                           D
                                                      Ε
## 0.16362880 0.17197587 0.17629375 0.15283576 0.25444696 0.15374856 0.13431362
                        Ι
## 0.22080946 0.07277741 0.09873749
table(df$brand)
##
## A B C D E F G H I J
## 29 31 27 32 28 30 29 33 29 32
11 <- which( df$brand %in% c("A", "C"))</pre>
dff <- df[11,]</pre>
dff$brand <- factor(dff$brand)</pre>
muA <- 4.773793
muC <- 2.848889
ssA <-0.16362880
ssC <- 0.16362880
ssta <-((ssA^2)/29)
sstc <- ((ssC<sup>2</sup>)/27)
deffree <- ((ssta+sstc)^2); deffree</pre>
## [1] 3.666836e-06
denom<- ((ssta^2)/28)+((sstc^2)/26);denom
## [1] 6.826427e-08
deffree <- deffree / denom; deffree</pre>
## [1] 53.71531
loth \leftarrow (muA - muC) - qt(0.995, deffree)*sqrt(((ssA^2)/29)+((ssC^2)/27));
loth
## [1] 1.808044
upth <- (muA - muC) + qt(0.995, deffree)*sqrt(((ssA^2)/29)+((ssC^2)/27));
upth
## [1] 2.041764
loth;upth
## [1] 1.808044
## [1] 2.041764
```

```
t.test(dff$cal~dff$brand, conf.level=0.99)
##
## Welch Two Sample t-test
##
## data: dff$cal by dff$brand
## t = 42.264, df = 52.858, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 99 percent confidence interval:
## 1.803204 2.046605
## sample estimates:
## mean in group A mean in group C
                          2.848889
          4.773793
fligner.test(dff$cal,dff$brand, conf.level=0.99)
##
##
   Fligner-Killeen test of homogeneity of variances
##
## data: dff$cal and dff$brand
## Fligner-Killeen:med chi-squared = 0.078778, df = 1, p-value = 0.779
t.test(dff$cal~dff$brand, conf.level=0.99, var.equal = T)
##
## Two Sample t-test
##
## data: dff$cal by dff$brand
## t = 42.378, df = 54, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 99 percent confidence interval:
## 1.803629 2.046180
## sample estimates:
## mean in group A mean in group C
                          2.848889
          4.773793
```

14. Out of 100 people, 60 prefer A to C. Determine a 99% confidence interval for the population proportion that favors A in front of C. Test the null hypothesis that selecting A and C has equal probability.

An approximate proportion test can be addressed using prop.test() method and setting properly the arguments. Null hypothesis assuming equal A and C brand choice can not be rejected at the 1% significance level. 99% CI for A brand choice percentage lies between 47.14% and 71.61%.

```
prop.test(60, n=100, p=0.5, conf.level=0.99, correct=F) # H0 can not be r
ejected at 1%

##
## 1-sample proportions test without continuity correction
##
```

```
## data: 60 out of 100, null probability 0.5
## X-squared = 4, df = 1, p-value = 0.0455
## alternative hypothesis: true p is not equal to 0.5
## 99 percent confidence interval:
## 0.4714191 0.7161367
## sample estimates:
## p
## 0.6
```

15. A second survey considered 200 people, 110 prefer A to C. Determine a 99% confidence interval for the difference in the population proportion that favors A in front of C accounting the two surveys. Test the null hypothesis that selecting A brand has a lower probability in the second of the surveys.

Difference in proportions stands for 1st - 2on survey comparison. One-sided test is stated as $H0: \pi_1 <= \pi_2$ and the alternative hypothesis is $H1: \pi_1 > \pi_2$. H0 fails to be rejected and 99% CI for proportion difference has a lower threshold of -0.090 (0 is included).

```
prop.test(c(60,110), n=c(100,200), conf.level=0.99, correct=F, alternativ
e="greater") # H0 can not be rejected at 1%

##
## 2-sample test for equality of proportions without continuity
## correction
##
## data: c(60, 110) out of c(100, 200)
## X-squared = 0.67873, df = 1, p-value = 0.205
## alternative hypothesis: greater
## 99 percent confidence interval:
## -0.09030597 1.000000000
## sample estimates:
## prop 1 prop 2
## 0.60 0.55
```

Do not forget to Knit to .pdf before posting your answers in ATENEA.