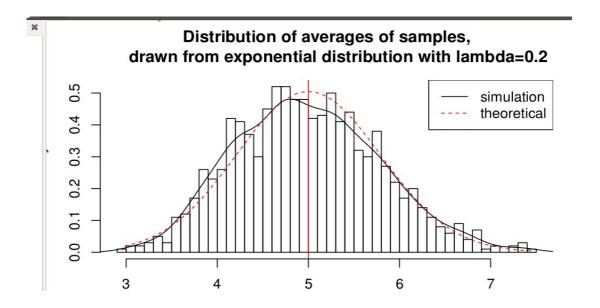
STATISTICAL INFERENCE COURSE PROJECT: PART 1

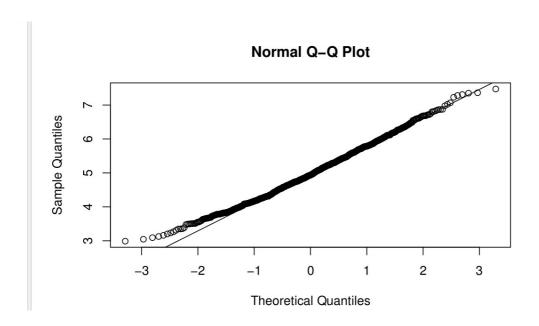
The exponential distribution can be simulated in R with rexp(n, lambda) where lambda λ is the rate parameter. The mean of exponential distribution is $1/\lambda$ and the standard deviation is also $1/\lambda$. For this simulation, we set $\lambda = 0.2$. In this simulation, we investigate the distribution of averages of 40 numbers sampled from exponential distribution with $\lambda = 0.2$.

Let's do a thousand simulated averages of 40 exponentials.

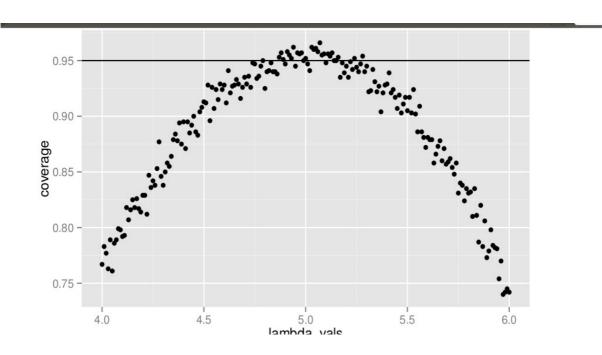


The distribution of sample means is centered at 4.9866 and the theoretical center of the distribution is $\lambda^{-1} = 5$. The variance of sample means is 0.6258 where the theoretical variance of the distribution is $\sigma^2/n = 1/(\lambda^2 n) = 1/(0.04 \times 40) = 0.625$.

Due to the central limit theorem, the averages of samples follow normal distribution. The figure above also shows the density computed using the histogram and the normal density plotted with theoretical mean and variance values. Also, the q-q plot below suggests the normality.



Finally, let's evaluate the coverage of the confidence interval for $1/\lambda = X \pm 1.96$



The 95% confidence intervals for the rate parameter (λ) to be estimated (λ') are λ'_{lower} - λ'_{lower