

Monte-Carlo Task Perfect art

1. The stable distribution $S(\alpha = 1.7, 0, 1, 1)$ was generated according to the report Adam Misiorek, Rafał Weron “Heavy-tailed distributions in VaR calculations” http://prac.im.pwr.edu.pl/~hugo/RePEc/wuu/wpaper/HSC_10_05.pdf (page #10). I generated a variable U uniformly distributed on $(-\pi/2, \pi/2)$ and an independent exponential random variable W with mean 1. Then I generated $X = \sin(1.7U)/\cos(U)^{1/\alpha} * (\cos(U - \alpha U)/W)^{(1-\alpha)/\alpha}$. The required random variable of 1-day return is $Y = X + 1$.
2. Random choice of the **Price** on the first day.
3. Using the **Price** and vector X , the vector of prices was calculated.
4. The 10 days returns values were calculated.
5. 0.01 percentile was calculated, just by sorting 10 days returns and taking the $\text{int}(751/100.+1)$ element.
6. This algorithm allows us to generate the required spectrum of the quantiles.
7. The remaining question is about the dependence of the method on the initial random value of the **Price**. I assume that the spectrum of the quantiles shouldn't be dependent on the **Price**. How much Monte-Carlo events we need in order to check this hypothesis.
8. I chose two different values of the **Price** (0.001 and 1000) and checked that the two massives correspond to the same generalized sample. In principle, I can use Kolmogorov-Smirnov's theorems to compare two data sets. But it looks too routine, so I have created a simplified method.
9. If the elements of none of the arrays are localized the number of MC events is sufficient. In the method I compare two vectors corresponding to different **Prices** and check how often array values are experienced. Other words, it's required that the sorted values in the vectors are similar to each other.