Instructions: Five points total. Show all work for credit. GS: Scan TWO pages for your solutions.

2.5 pts. 1. Find the arc length to the helix  $\mathbf{r}(t) = \langle 5\cos(2t), 5\sin(2t), 2t \rangle$  as t varies from t = 0 to  $t = 2\pi$ . Simplify your answer for full credit.

Compute Solfi(t) | dt

$$\Gamma(t) = 2 - 10 \sin(2t), 10 \cos(2t), 2$$

$$|\vec{F}'(t)| = \int (-10 \text{ sin}(2t))^2 + (10 \cos(2t))^2 + 4$$

$$= \int 100 \left( \sin^2(2t) + \cos^2(2t) \right) + 4$$

$$= \int 104 \qquad 104 = 4.26$$

Therefore,

$$L = \int_{0}^{2\pi} 2\sqrt{26} \, dt = 4\pi \sqrt{26}$$

Answer: Arc length =

411 526

2.5 pts.

2. Consider the space curve with vector equation

$$\langle 3 + t^2, 7 + t^3, 0 \rangle$$
.

Give a formula for the curvature function  $\kappa(t)$ .

We will use:

$$k(t) = \frac{\left| \vec{r}'(t) \times \vec{r}''(t) \right|}{\left| \vec{r}'(t) \right|^3}$$

$$F'(t) = \langle 2t, 3t^2, 0 \rangle$$

$$\vec{r}'(t) \times \vec{r}''(t) = \begin{cases} \hat{\lambda} & \hat{\lambda} \\ 2t & 3t^2 \end{cases} = \begin{bmatrix} (2t)(6t) - 2(3t^2) \end{bmatrix} \hat{k}$$

$$2 \quad (6t) \quad 0$$

$$=(12t^2-6t^2)\hat{k}=(t^2\hat{k}=\langle 0,0,6t^2\rangle$$

The magnitude | F'(t) x F''(t) | = Gt2.

The magnitude 
$$|\vec{r}'(t)| = |\langle 2t, 3t^2, 0 \rangle| = \int (2t)^2 + (3t^2)^2 + 0^2$$

$$= \int 4t^2 + 9t^4$$

Thus, 
$$k(t) = 6t^2$$

$$\sqrt{4t^2 + 9t^4}$$

Answer: 
$$\kappa(t) = \frac{6t^2}{\sqrt{4t^2 + 9t^4}}$$