Common Probability Distributions, Means, Variances, and Moment-Generating Functions

Table 1 Discrete Distributions

| Distribution | Probability Function | Mean | Variance | Moment- Generating Function |
|-------------------|---|----------------|---|--|
| Binomial | $p(y) = \binom{n}{y} p^{y} (1-p)^{n-y};$ | np | np(1-p) | $[pe^t + (1-p)]^n$ |
| | $y=0,1,\ldots,n$ | | | |
| Geometric | $p(y) = p(1-p)^{y-1};$ | $\frac{1}{p}$ | $\frac{1-p}{p^2}$ | $\frac{pe^t}{1-(1-p)e^t}$ |
| | $y=1,2,\ldots$ | Ρ | p- | $1-(1-p)e^{s}$ |
| Hypergeometric | $p(y) = \frac{\binom{r}{y} \binom{N-r}{n-y}}{\binom{N}{n}};$ | $\frac{nr}{N}$ | $n\left(\frac{r}{N}\right)\left(\frac{N-r}{N}\right)\left(\frac{N-n}{N-1}\right)$ | does not exist in closed form |
| | $y = 0, 1,, n \text{ if } n \le r,$ y = 0, 1,, r if n > r | | | |
| Poisson | $p(y) = \frac{\lambda^y e^{-\lambda}}{y!};$ | λ | λ | $\exp[\lambda(e^t-1)]$ |
| | $y=0,1,2,\ldots$ | | | |
| Negative binomial | $p(y) = {\binom{y-1}{r-1}} p^r (1-p)^{y-r};$ $y = r, r+1, \dots$ | $\frac{r}{p}$ | $\frac{r(1-p)}{p^2}$ | $\left[\frac{pe^t}{1-(1-p)e^t}\right]^r$ |

APPENDIX 3

Tables

Table 1 Binomial Probabilities

Tabulated values are $P(Y \le a) = \sum_{y=0}^{a} p(y)$. (Computations are rounded at third decimal place.)

| 0.05 | 0.10 | 0.20 | 0.000 | | | | | | | | | |
|------------|----------------|---------------|--------------|--------------|------|--------------|------|---|------|------|---------|---------------|
| | | 0.20 | 0.30 | 0.40 | 0.50 | 0.60 | 0.70 | 0.80 | 0.00 | | | |
| .774 | .590 | 220 | 160 | | | 0.00 | 0.70 | 0.80 | 0.90 | 0.95 | 0.99 | |
| .977 | | .328 | .168 | .078 | .031 | .010 | .002 | .000 | .000 | .000 | .000 | _ |
| 20000-0000 | .919 | .737 | .528 | .337 | .188 | .087 | .031 | .007 | | | | |
| .999 | .991 | .942 | .837 | .683 | .500 | | | 200000000000000000000000000000000000000 | .000 | .000 | .000 | |
| 1.000 | 1.000 | 003 | | | | .317 | .163 | .058 | .009 | .001 | .000 | |
| | | | 1000000 | | .812 | .663 | .472 | .263 | .081 | 023 | 001 | |
| 1.000 | 1.000 | 1.000 | .998 | .990 | .969 | 922 | 832 | | | | | |
| 1.000 | 1.000 1.000 | .993 1.000 | .969 .998 | .913 .990 | .812 | .663 .922 | | .058 .263 .672 | .0 | | 81 .023 | 081 .023 .001 |

(b)
$$n = 10$$

| | | | | | | | p | | | | | | | |
|---|-------|---|-------|-------|----------------------|-------|---|------|------|------|------|------|------|---|
| а | 0.01 | 0.05 | 0.10 | 0.20 | 0.30 | 0.40 | 0.50 | 0.60 | 0.70 | 0.80 | 0.90 | 0.95 | 0.00 | |
| 0 | .904 | .599 | .349 | .107 | .028 | .006 | 001 | | | | 0.30 | 0.93 | 0.99 | 0 |
| 1 | .996 | .914 | .736 | .376 | 2041 March 120 (200) | | .001 | .000 | .000 | .000 | .000 | .000 | .000 | (|
| 2 | 1.000 | .988 | .930 | | .149 | .046 | .011 | .002 | .000 | .000 | .000 | .000 | .000 | 1 |
| 3 | 1.000 | .999 | .987 | .678 | .383 | .167 | .055 | .012 | .002 | .000 | .000 | .000 | .000 | 2 |
| 4 | 1.000 | 1.000 | | .879 | .650 | .382 | .172 | .055 | .011 | .001 | .000 | .000 | .000 | - |
| 5 | 1.000 | 0.0000000000000000000000000000000000000 | .998 | .967 | .850 | .633 | .377 | .166 | .047 | .006 | .000 | .000 | | 3 |
| 6 | | 1.000 | 1.000 | .994 | .953 | .834 | .623 | .367 | .150 | .033 | | | .000 | 4 |
| | 1.000 | 1.000 | 1.000 | .999 | .989 | .945 | .828 | .618 | .350 | | .002 | .000 | .000 | 5 |
| 7 | 1.000 | 1.000 | 1.000 | 1.000 | .998 | .988 | .945 | .833 | | .121 | .013 | .001 | .000 | 6 |
| 8 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .998 | .989 | | .617 | .322 | .070 | .012 | .000 | 7 |
| 9 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 0.5000000000000000000000000000000000000 | .954 | .851 | .624 | .264 | .086 | .004 | 8 |
| | | | | | 1.000 | 1.000 | .999 | .994 | .972 | .893 | .651 | .401 | .096 | 9 |

Table 1 (Continued) (c) n = 15

0.01

.860

0.05

.463

0.10

.206

0.20

.035

0.30

| | 2 1. 3 1. 4 1. 5 1. 6 1. 7 1. 8 1. 9 1. 9 1. 9 1. 9 1. 9 1. 9 1. 9 1. 9 | 000 000 000 1 000 1 000 1 000 1 000 1 000 1 000 1 000 1 000 1 000 1 000 1 | 964 995 999 000 .000 1.0 000 1.0 000 1.0 000 1.0 | 987 998 000 000 . 000 . | 982 996 | 950 | .000 .005 .027 .091 .217 .403 | .000 .000 .004 .018 .059 | .00 .00 .00 .00 .009 | 00 .0 00 .0 2 .0 9 .0 | 000 . 000 . 000 . | .000 .000 .000 | .000 | .000 .000 .000 | .000 .000 .000 .000 | |
|---|---|---|--|-------------------------------------|-------------------------------------|--|--|--------------------------------------|----------------------------------|--------------------------------|-------------------------|----------------------|--------------|----------------------|------------------------------|------|
| 3 6 7 8 9 10 11 12 13 | 3 1.0 4 1.0 5 1.0 6 1.0 7 1.0 1.0 1.0 1.0 1.0 1.0 | 000 000 1.0 000 1.0 000 1.0 000 1.0 000 1.0 000 1.0 | 995 999 000 000 1.0 000 1.0 000 1.0 000 1.0 | 944 987 998 000 000 . | .398 .648 .836 .939 982 | .127 .297 .515 .722 .869 .950 | .027 .091 .217 .403 .610 | .004 .018 .059 .151 | .00. :00. | 0 .0 2 .0 9 .0 | 000 . 000 . 001 . | .000 . | .000 | .000 .000 .000 | .000 .000 .000 | |
| 5 6 7 8 9 10 11 12 13 | 4 1.05 5 1.05 7 1.03 3 1.00 1.00 1.00 | 000 000 1.0 000 1.0 000 1.0 000 1.0 00 1.0 00 1.0 | 999 . 900 . 900 1. 900 1. 900 1. 900 1. 900 1. 900 1. | 987 998 000 000 .000 . | .648 .836 .939 982 996 | .297 .515 .722 .869 .950 | .091 .217 .403 .610 | .018 .059 .151 | .00. | 2 .0 9 .0 | 000 . 001 . | 000 . | .000 | .000 | .000 | |
| 5 6 7 8 9 10 11 12 13 | 5 1.0 5 1.0 7 1.0 3 1.0 1.0 1.0 1.0 1.0 | 000 1.0 000 1.0 000 1.0 000 1.0 000 1.0 00 1.0 00 1.0 | 999 900 900 1 900 1 900 1 900 1 900 1 | 987 998 000 000 .000 . | .836 .939 982 996 | .515 .722 .869 .950 | .217 .403 .610 | .059 .151 | .009 | 9 .0 | . 001 | | .000 | .000 | .000 | |
| 10 11 12 13 | 5 1.0 7 1.0 3 1.0 1.0 1.00 1.00 | 000 1.0 000 1.0 000 1.0 00 1.0 00 1.0 | 000 000 1.0 000 1.0 000 1.0 000 1.0 | 998 000 000 . 000 . | .939 982 996 | .722 .869 .950 | .403 .610 | .151 | | | | 000 | | | | |
| 7 8 9 10 11 12 13 | 7 1.0 3 1.0 1.0 1.0 1.0 1.0 1.0 | 000 1.0 000 1.0 000 1.0 000 1.0 000 1.0 | 000 1.0 000 1.0 000 1.0 000 1.0 00 1.0 | 000 . 000 . 000 . | 982 996 | .869 .950 | .610 | | 02/ | 4 - | | | | | 000 | |
| 8 9 10 11 12 13 | 3 · 1.0 1.0 1.0 1.0 1.0 | 00 1.0 00 1.0 00 1.0 00 1.0 | 000 1.0 000 1.0 000 1.0 00 1.0 | 000 . 000 . 000 1.0 | 996 | 950 | | | | | | . 000 | | | 000 | |
| 9 10 11 12 13 | 1.0 1.0 1.0 1.0 | 00 1.0 00 1.0 00 1.0 | 000 1.0 00 1.0 00 1.0 | 000 . 000 1. | | | | .304 | .095 | | | 001 .(| | | 000 | |
| 10 11 12 13 | 1.00 1.00 1.00 | 00 1.0 00 1.0 00 1.0 | 00 1.0 00 1.0 | 000 1.0 | ,,,, | 985 | 787 | .500 | .213 | | 50 .0 | | | | 000 | |
| 11 12 13 | 1.00 1.00 | 00 1.0 00 1.0 | 00 1.0 | | | | 905 | .696 | .390 | | 31 .0 | | 20000000 | | 000 | |
| 12 13 | 1.00 | 00 1.0 | | | | | 966 | .849 | .597 | .27 | | | | | 000 | |
| 13 | 1.00 | | 00 1.0 | | | | 991 | .941 | .783 | .48 | | | | | | |
| 13 | | | | | | | 998 | .982 | .909 | | 100 | | | | 000 | 10 |
| 14 | | | | | | | 000 | .996 | .973 | .87 | | B1000 | | | 00 | 11 |
| 17 | 1.00 | 1000 | | | | | | .000 | .995 | .96 | | | | | 00 | 12 |
| | -100 | 1.00 | 00 1.00 | 00 1.0 | 00 1.0 | 00 1.0 | 000 1 | .000 | 1.000 | .99 | | | | | 10 | 13 |
| (d) n | = 20 | | | | | | - | | | .,,, | | | .5. | 37 .14 | 40 | 14 |
| (-) | - 20 | | | | | | | 8) | | | | | | | | |
| | | | | | | | p | | | | | | | | | _ |
| a | 0.01 | 0.05 | 0.10 | 0.20 | 0.3 | 0 0.4 | | .50 | 0.60 | | | | | | | |
| 2 | | | | | | - 0.1 | 0. | .50 | 0.60 | 0.70 | 0.80 | 0.90 | 0.9 | 5 0.9 | 9 | a |
| 0 1 | .818 .983 | | | | | 1 .00 | 0. 0 | 000 | .000 | .000 | | | | | | 7 |
| 2 | .999 | | | | | 8 .00 | | | .000 | .000 | .000 | | 200.00 | | | 0 |
| 3 | 1.000 | | | | | 5 .00 | | 2000 | .000 | | .000 | | | |) | 1 |
| | | .984 | | | | | | · . | 000 | .000 | .000 | | | |) | 2 . |
| | 1.000 | .997 | .957 | .630 | .23 | | | | | .000 | .000 | | | .000 | | 3 |
| | 1.000 | 1.000 | .989 | .804 | | | | | | .000 | .000 | / | | .000 | | 4 |
| | 1.000 | 1.000 | .998 | .913 | .608 | | | | | .000 | .000 | .000 | .000 | | | 5 |
| 0.00 | 1.000 | 1.000 | 1.000 | .968 | .772 | | | | | .000 | .000 | .000 | .000 | | | 5 |
| | 1.000 | 1.000 | 1.000 | .990 | .887 | | | | | .001 | .000 | .000 | .000 | | 7 | |
| | 1.000 | 1.000 | 1.000 | .997 | .952 | | - | | | .005 | .000 | .000 | .000 | .000 | 8 | |
| | 1.000 | 1.000 | 1.000 | .999 | .983 | | | | | .017 | .001 | .000 | .000 | .000 | 9 | |
| | .000 | 1.000 | 1.000 | 1.000 | .995 | .872 | | | | 048 | .003 | .000 | .000 | .000 | 10 | |
| | .000 | 1.000 | 1.000 | 1.000 | .993 | .943 | .74 | | | 113 | .010 | .000 | .000 | .000 | | |
| | .000 | 1.000 | 1.000 | 1.000 | | .979 | .868 | | | 228 | .032 | .000 | .000 | .000 | 11 | 1 |
| | .000 | 1.000 | 1.000 | 1.000 | 1.000 | .994 | .942 | (i) (iii) | | 392 | .087 | .002 | .000 | | 12 | |
| | .000 | 1.000 | 1.000 | 1.000 | 1.000 | .998 | .979 | | | 584 | .196 | .011 | .000 | .000 | 13 | |
| | .000 | 1.000 | 1.000 | | 1.000 | 1.000 | .994 | | | 762 | .370 | .043 | | .000 | 14 | (42) |
| | 000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .999 | .98 | | | .589 | .133 | .003 | .000 | 15 | |
| | 000 | 1.000 | | 1.000 | 1.000 | 1.000 | 1.000 | | | | .794 | | .016 | .000 | 16 | |
| | 000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | | | | .931 | .323 | .075 | .001 | 17 | 10 |
| | | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | | | | .931 .988 | .608 .878 | .264 .642 | .017 .182 | 18 19 | |

p

0.50

0.60

0.70

0.80

0.90

0.95

0.99

0.40

Table 1 (Continued) (e) n = 25

| | | | | | | | p | | | | | | | |
|-----|--------|-------|-------|-------|-------|-------|-------|-------|-------|------|------|------|------|----|
| а | 0.01 | 0.05 | 0.10 | 0.20 | 0.30 | 0.40 | 0.50 | 0.60 | 0.70 | 0.80 | 0.90 | 0.95 | 0.99 | а |
| 0 | .778 | .277 | .072 | .004 | .000 | .000 | .000 | .000 | .000 | .000 | .000 | .000 | .000 | 0 |
| 1 | .974 | .642 | .271 | .027 | .002 | .000 | .000 | .000 | .000 | .000 | .000 | .000 | .000 | 1 |
| 2 | .998 | .873 | .537 | .098 | .009 | .000 | .000 | .000 | .000 | .000 | .000 | .000 | .000 | 2 |
| 3 | 1.000 | .966 | .764 | .234 | .033 | .002 | .000 | .000 | .000 | .000 | .000 | .000 | .000 | 3 |
| 4 | 1.000 | .993 | .902 | .421 | .090 | .009 | .000 | .000 | .000 | .000 | .000 | .000 | .000 | 4 |
| 5 | 1.000 | .999 | .967 | .617 | .193 | .029 | .002 | .000 | .000 | .000 | .000 | .000 | .000 | 5 |
| 6 | 1.000 | 1.000 | .991 | .780 | .341 | .074 | .007 | .000 | .000 | .000 | .000 | .000 | .000 | 6 |
| 7 | 1.000 | 1.000 | .998 | .891 | .512 | .154 | .022 | .001 | .000 | .000 | .000 | .000 | .000 | 7 |
| 8 | 1.000 | 1.000 | 1.000 | .953 | .677 | .274 | .054 | .004 | .000 | .000 | .000 | .000 | .000 | 8 |
| . 9 | 1.000 | 1.000 | 1.000 | .983 | .811 | .425 | .115 | .013 | .000 | .000 | .000 | .000 | .000 | 9 |
| 10 | 1.000 | 1.000 | 1.000 | .994 | .902 | .586 | .212 | .034 | .002 | .000 | .000 | .000 | .000 | 10 |
| 11 | 1.000 | 1.000 | 1.000 | .998 | .956 | .732 | .345 | .078 | .006 | .000 | .000 | .000 | .000 | 11 |
| 12 | 1.000 | 1.000 | 1.000 | 1.000 | .983 | .846 | .500 | .154 | .017 | .000 | .000 | .000 | .000 | 12 |
| 13 | 1.000 | 1.000 | 1.000 | 1.000 | .994 | .922 | .655 | .268 | .044 | .002 | .000 | .000 | .000 | 13 |
| 14 | 1.000 | 1.000 | 1.000 | 1.000 | .998 | .966 | .788 | .414 | .098 | .006 | .000 | .000 | .000 | 14 |
| 15 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .987 | .885 | .575 | .189 | .017 | .000 | .000 | .000 | 15 |
| 16 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .996 | .946 | .726 | .323 | .047 | .000 | .000 | .000 | 16 |
| 17 | .1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .999 | .978 | .846 | .488 | .109 | .002 | .000 | .000 | 17 |
| 18 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .993 | .926 | .659 | .220 | .009 | .000 | .000 | 18 |
| 19 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .998 | .971 | .807 | .383 | .033 | .001 | .000 | 19 |
| 20 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .991 | .910 | .579 | .098 | .007 | .000 | 20 |
| 21 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .998 | .967 | .766 | .236 | .034 | .000 | 21 |
| 22 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .991 | .902 | .463 | .127 | .002 | 22 |
| 23 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .998 | .973 | .729 | .358 | .026 | 23 |
| 24 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | .996 | .928 | .723 | .222 | 24 |

Tables 843

Table 3 Poisson Probabilities

| | | | | | 1 | P(Y ≤ | $\leq a) = \sum_{i=1}^{n} a_i$ | $\sum_{i=1}^{a} e^{-\lambda} \frac{\lambda}{a}$ | <u>y</u> | | | | |
|----------|---------|------|-------|----------------|-------|---------------|--------------------------------|---|----------|-------|--|----------|---|
| 1 | a | | - | | | | . , | y=0 y | ! | | | | |
| <u>λ</u> | 7 | 0 | 1 | | 2 | 3 | 4 | 1 : | 5 | 6 | 7 | 8 | 0 |
| | | .980 | 1.00 | 00 | | | | | | | <u>, </u> | <u> </u> | 9 |
| | | .961 | 0.99 | 99 1.0 | 00 | | | | | | | | |
| | | .942 | 0.99 | 98 1.0 | 00 | | | | | | | | |
| | | .923 | 0.99 | 7 1.0 | 00 | | | | | | | | |
| 0. | 10 0. | 905 | 0.99 | 5 1.00 | 00 | | | | | | | | |
| 0.1 | 15 0. | 861 | 0.99 | 0 0.99 | 00 | 1 000 | | | | | | | |
| 0.2 | | 819 | 0.98 | | | 1.000 | | | 1.60 | | | | |
| 0.2 | | 779 | 0.974 | | | 1.000 | | | | | | | |
| 0.3 | | 741 | 0.963 | | | 1.000 1.000 | | • | | | | | |
| 0.3 | | | | | | | ž | | | | | | |
| 0.3 | | 705 | 0.951 | | | 1.000 | | | | | 0.5 | | |
| 0.4 | _ | | 0.938 | | |).999 | 1.000 |) | | | | | |
| | | | 0.925 | | | .999 | 1.000 |) | | | | | |
| 0.50 | 0.6 | 07 | 0.910 | 0.986 | 6 0 | .998 | 1.000 | | | | | | |
| 0.55 | 5 . 0.5 | 77 | 0.894 | 0.982 | . 0 | .988 | 1.000 | | | | | | |
| 0.60 | | | 0.878 | 0.977 | 0 000 | .997 | 1.000 | | | | | | |
| 0.65 | | 22 (| 0.861 | 0.972 | | 996 | 0.999 | | e: | | | • | |
| 0.70 | - | | 0.844 | 0.966 | 5555 | 994 | 0.999 | 1.000 | | | | | |
| 0.75 | 0.47 | 2 (| 0.827 | 0.959 | | 993 | 0.999 | 1.000 | | | | | |
| 0.80 | 0.44 | 0 0 | .809 | | | | | | | | | | |
| 0.85 | 0.42 | | .791 | 0.953 | | 991 | 0.999 | 1.000 | | | | | |
| 0.90 | 0.40 | _ | .772 | 0.945 0.937 | | 989 | 0.998 | 1.000 | | | | | |
| 0.95 | 0.38 | | .754 | 0.937 | | 987 | 0.998 | 1.000 | | | | | - |
| 1.00 | 0.368 | | .736 | 0.929 | | 81 | 0.997 | 1.000 | | | | | |
| | | | | 0.920 | 0.9 | 81 | 0.996 | 0.999 | 1.000 | | | | |
| 1.1 | 0.333 | | 699 | 0.900 | 0.9 | 74 | 0.995 | 0.999 | 1.000 | | | | |
| 1.2 | 0.301 | | 663 | 0.879 | 0.9 | 66 . | 0.992 | 0.998 | 1.000 | | | | |
| 1.3 | 0.273 | | 627 | 0.857 | 0.9 | | 0.989 | 0.998 | 1.000 | | | | |
| 1.4 | 0.247 | | 592 | 0.833 | 0.9 | | 0.986 | 0.997 | 0.999 | 1.000 | | | |
| .5 | 0.223 | 0.5 | 558 | 0.809 | 0.93 | | 0.981 | 0.996 | 0.999 | 1.000 | | | |
| .6 | 0.202 | 0.5 | 525 | 0.783 | 0.92 | | | | | 1.000 | | | |
| .7 | 0.183 | 0.4 | | 0.757 | 0.92 | | 0.976 | 0.994 | 0.999 | 1.000 | | | |
| .8 | 0.165 | 0.4 | | 0.737 | 0.89 | | 0.970 | 0.992 | 0.998 | 1.000 | | | |
| .9 | 0.150 | 0.4 | | 0.704 | 0.87 | 83 |).964 | 0.990 | 0.997 | 0.999 | 1.000 | | |
| .0 | 0.135 | 0.4 | | 0.677 | 0.85 | |).956).947 | 0.987 | 0.997 | 0.999 | 1.000 | | |
| | | | | | 0.03 | , 0 | .94/ | 0.983 | 0.995 | 0.999 | 1.000 | | |

Table 3 (Continued)

| Àa | 0 | 1 | 2 | 3 | 4 | . 5 | 6 | 7 | 8 | 9 |
|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 2.2 | 0.111 | | | | | | | 0.998 | 1.000 | |
| 2.4 | 0.091 | 0.308 | 0.570 | | | | | 0.997 | 0.999 | 1.00 |
| 2.6 | | | 0.518 | | | | | 0.995 | 0.999 | 1.00 |
| 2.8 | 0.061 | 0.231 | 0.469 | 0.692 | 0.848 | 0.935 | | 0.992 | 0.998 | 0.99 |
| 3.0 | 0.050 | 0.199 | 0.423 | 0.647 | 0.815 | 0.916 | 0.966 | 0.988 | 0.996 | 0.99 |
| 3.2 | 0.041 | 0.171 | 0.380 | 0.603 | 0.781 | 0.895 | 0.955 | 0.983 | 0.994 | 0.99 |
| 3.4 | 0.033 | | | 0.558 | 0.744 | 0.871 | 0.942 | 0.977 | 0.992 | 0.99 |
| 3.6 | 0.027 | 0.126 | | 0.515 | 0.706 | 0.844 | 0.927 | 0.969 | 0.988 | 0.996 |
| 3.8 | 0.022 | 0.107 | 0.269 | 0.473 | 0.668 | 0.816 | 0.909 | 0.960 | 0.984 | 0.994 |
| 4.0 | 0.018 | 0.092 | 0.238 | 0.433 | 0.629 | 0.785 | 0.889 | 0.949 | 0.979 | 0.992 |
| 4.2 | 0.015 | 0.078 | 0.210 | 0.395 | 0.590 | 0.753 | 0.867 | 0.936 | 0.972 | 0.989 |
| 4.4 | 0.012 | 0.066 | 0.185 | 0.359 | 0.551 | 0.720 | 0.844 | 0.921 | 0.964 | 0.985 |
| 4.6 | 0.010 | 0.056 | 0.163 | 0.326 | 0.513 | 0.686 | 0.818 | 0.905 | 0.955 | 0.980 |
| 4.8 | 0.008 | 0.048 | 0.143 | 0.294 | 0.476 | 0.651 | 0.791 | 0.887 | 0.944 | 0.975 |
| 5.0 | 0.007 | 0.040 | 0.125 | 0.265 | 0.440 | 0.616 | 0.762 | 0.867 | 0.932 | 0.968 |
| 5.2 | 0.006 | 0.034 | 0.109 | 0.238 | 0.406 | 0.581 | 0.732 | 0.845 | 0.918 | 0.960 |
| 5.4 | 0.005 | 0.029 | 0.095 | 0.213 | 0.373 | 0.546 | 0.702 | 0.822 | 0.903 | 0.951 |
| 5.6 | 0.004 | 0.024 | 0.082 | 0.191 | 0.342 | 0.512 | 0.670 | 0.797 | 0.886 | 0.941 |
| 5.8 | 0.003 | 0.021 | 0.072 | 0.170 | 0.313 | 0.478 | 0.638 | 0.771 | 0.867 | 0.929 |
| 6.0 | 0.002 | 0.017 | 0.062 | 0.151 | 0.285 | 0.446 | 0.606 | 0.744 | 0.847 | 0.916 |
| | 10 | 11 | 12 | 13 | 14 | 15 | 16 | | | |
| 2.8 | 1.000 | | | | | | | | | |
| 3.0 | 1.000 | | | | | | | 9 8 | 99 | |
| 3.2 | 1.000 | | * | | | | | | | |
| 3.4 | 0.999 | 1.000 | | | | | | | | |
| 3.6 | 0.999 | 1.000 | | | | | | | | |
| 3.8 | 0.998 | 0.999 | 1.000 | | | | | | | 3 |
| 1.0 | 0.997 | 0.999 | 1.000 | | 22 | | | | | |
| 1.2 | 0.996 | 0.999 | 1.000 | | | | | | | |
| 1.4 | 0.994 | 0.998 | 0.999 | 1.000 | | | v | - 1 | | |
| .6 | 0.992 | 0.997 | 0.999 | 1.000 | | | | | | |
| .8 | 0.990 | 0.996 | 0.999 | 1.000 | | | | | | |
| 0. | 0.986 | 0.995 | 0.998 | 0.999 | 1.000 | | | | | |
| .2 | 0.982 | 0.993 | 0.997 | 0.999 | 1.000 | | | | | |
| .4 | 0.977 | 0.990 | 0.996 | 0.999 | 1.000 | | | | | |
| .6 | 0.972 | 0.988 | 0.995 | 0.998 | 0.999 | 1.000 | × | | | |
| .8 | 0.965 | 0.984 | 0.993 | 0.997 | 0.999 | 1.000 | | | | |
| .0 | 0.957 | 0.980 | 0.991 | 0.996 | 0.999 | 0.999 | 1.000 | | | |

Table 3 (Continued)

| 000000 | | ······································ | | | | | | | | |
|------------------|----------------|--|---------|--|----------------------|---------|-------|---------|----------------|-------|
| $\sqrt{\lambda}$ | a | 0 | 1 | | 3 4 | . 5 | 6 | 7 | | |
| (| 6.2 0.0 | 002 0. | 015 0.0 | | | | | | 8 | 9 |
| 6 | | | | | 134 0.2. 119 0.2. | | | | | |
| . 6 | 5.6 0.0 | | 010 0.0 | | 0.2 | | | | 7), | |
| 6 | 5.8 0.0 | | 0.0 0.0 | -0.000 | | | | | | |
| 7 | 0.0 | 0.0 | 0.0 | | | | | | | |
| 7 | .2 0.0 | 01 00 | | | | | | 0.59 | 9 0.729 | 0.830 |
| | .4 0.0 | | 0.05 | | | | | 0 0.569 | 0.703 | 0.810 |
| | .6 0.0 | | 0.02 | | | | | | | |
| 7. | | | | | _ | | | | | 0.765 |
| | | JU U.U | 04 0.01 | 16 0.04 | 48 0.11: | 2 0.210 | 0.33 | | | 0.741 |
| 8. | | | 0.01 | 4 0.04 | 2 0.100 | 0.191 | 0.313 | 0.450 | | |
| 8 | | | 0.00 | 9 0.03 | | | | | | 0.717 |
| 9.0 | | | | | | | | | | 0.653 |
| 9.5 | 8 | | | 4 0.01 | | | | | | 0.587 |
| 10.0 | 0.00 | 0.00 | 0.00 | | | | | | 0.392 | 0.522 |
| | 10 | 11 | 12 | 12 | | | 0.150 | 0.220 | 0.333 | 0.458 |
| 6.2 | | | | 13 | 14 | 15 | 16 | 17 | 18 | 19 |
| 6.4 | | | | | | 0.999 | 1.000 | | | |
| 6.6 | | | | | | 0.999 | 1.000 | | | |
| 6.8 | | | | 10-10-10-10-10-10-10-10-10-10-10-10-10-1 | | 0.999 | 0.999 | 1.000 | 755) | |
| 7.0 | | | | | | 0.998 | 0.999 | 1.000 | | |
| | 0.000.000 | | | 0.987 | 0.994 | 0.998 | 0.999 | 1.000 | | |
| 7.2 | 0.887 | | | 0.984 | 0.993 | 0.997 | 0.999 | 0.999 | 1 000 | |
| 7.4 | 0.871 | 0.926 | | 0.980 | 0.991 | 0.996 | 0.998 | 0.999 | 1.000 | |
| 7.6 | 0.854 | 0.915 | | 0.976 | 0.989 | 0.995 | 0.998 | 0.999 | 1.000 1.000 | |
| 7.8 | 0.835 | 0.902 | 0.945 | 0.971 | 0.986 | 0.993 | 0.997 | 0.999 | 1.000 | |
| 8.0 | 0.816 | 0.888 | 0.936 | 0.966 | 0.000 | | | | | |
| 8.5 | 0.763 | 0.849 | | 0.949 | 0.983 | 0.992 | 0.996 | 0.998 | 0.999 | 1.000 |
| 9.0 | 0.706 | 0.803 | 0.876 | 0.926 | 0.973 0.959 | 0.986 | 0.993 | 0.997 | | 0.999 |
| 9.5 | 0.645 | 0.752 | 0.836 | 0.898 | 0.939 | 0.978 | 0.989 | | 0.998 | 0.999 |
| 10.0 | 0.583 | 0.697 | 0.792 | 0.864 | 0.940 | 0.967 | 0.982 | | | 0.998 |
| | 20 | 21 | 22 | 0.004 | 0.917 | 0.951 | 0.973 | 0.986 | 0.993 (| 0.997 |
| 8.5 | | | | | | | | | | |
| 9.0 | 1.000 1.000 | | | | | | | | | |
| 9.5 | 0.999 | 1 000 | | | | | | | | 19 |
| 0.0 | 0.999 | 1.000 | 1 000 | | | | | | | |
| ···· | U.770 | 0.999 | 1.000 | | | | | | | |

Table 3 (Continued)

| à | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|------|-------|---------|-------|-------|-------|-------|-------|-------|-------|-------|
| 10.5 | 0.000 | 0.000 | 0.002 | 0.007 | 0.021 | 0.050 | 0.102 | 0.179 | 0.279 | 0.397 |
| 11.0 | 0.000 | 0.000 | 0.001 | 0.005 | 0.015 | 0.038 | 0.079 | 0.143 | 0.232 | |
| 11.5 | | | | 0.003 | 0.011 | 0.028 | 0.060 | 0.114 | 0.191 | 0.289 |
| 12.0 | | | 0.001 | 0.002 | 0.008 | 0.020 | 0.046 | 0.090 | 0.155 | 0.242 |
| 12.5 | 0.000 | 0.000 | 0.000 | 0.002 | 0.005 | 0.015 | 0.035 | 0.070 | 0.125 | 0.201 |
| 13.0 | | 0.000 | 0.000 | 0.001 | 0.004 | 0.011 | 0.026 | 0.054 | 0.100 | 0.166 |
| 13.5 | | 0.000 | 0.000 | 0.001 | 0.003 | 0.008 | 0.019 | 0.041 | 0.079 | 0.135 |
| 14.0 | | 0.000 | 0.000 | 0.000 | 0.002 | 0.006 | 0.014 | 0.032 | 0.062 | 0.109 |
| 14.5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.010 | 0.024 | 0.048 | 0.088 |
| 15.0 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.003 | 0.008 | 0.018 | 0.037 | 0.070 |
| | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 |
| 10.5 | 0.521 | 0.639 | 0.742 | 0.825 | 0.888 | 0.932 | 0.960 | 0.978 | 0.988 | 0.994 |
| 11.0 | 0.460 | 0.579 | 0.689 | 0.781 | 0.854 | 0.907 | 0.944 | 0.968 | 0.982 | 0.991 |
| 11.5 | 0.402 | | 0.633 | 0.733 | 0.815 | 0.878 | 0.924 | 0.954 | 0.974 | 0.986 |
| 12.0 | 0.347 | 0.462 | 0.576 | 0.682 | 0.772 | 0.844 | 0.899 | 0.937 | 0.963 | 0.979 |
| 12.5 | 0.297 | 0.406 | 0.519 | 0.628 | 0.725 | 0.806 | 0.869 | 0.916 | 0.948 | 0.969 |
| 13.0 | 0.252 | 0.353 | 0.463 | 0.573 | 0.675 | 0.764 | 0.835 | 0.890 | 0.930 | 0.957 |
| 13.5 | 0.211 | 0.304 | 0.409 | 0.518 | 0.623 | 0.718 | 0.798 | 0.861 | 0.908 | 0.942 |
| 14.0 | 0.176 | 0.260 | 0.358 | 0.464 | 0.570 | 0.669 | 0.756 | 0.827 | 0.883 | 0.923 |
| 14.5 | 0.145 | 0.220 | 0.311 | 0.413 | 0.518 | 0.619 | 0.711 | 0.790 | 0.853 | 0.901 |
| 15.0 | 0.118 | 0.185 | 0.268 | 0.363 | 0.466 | 0.568 | 0.664 | 0.749 | 0.819 | 0.875 |
| | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 |
| 10.5 | 0.997 | 0.999 | 0.999 | 1.000 | | | | | | |
| 11.0 | 0.995 | 0.998 | 0.999 | 1.000 | | | | | | |
| 11.5 | 0.992 | 0.996 | 0.998 | 0.999 | 1.000 | | | | | |
| 12.0 | 0.988 | 0.994 | 0.997 | 0.999 | 0.999 | 1.000 | | | | |
| 12.5 | 0.983 | 0.991 | 0.995 | 0.998 | 0.999 | 0.999 | 1.000 | | | |
| 13.0 | 0.975 | 0.986 | 0.992 | 0.996 | 0.998 | 0.999 | 1.000 | | | |
| 13.5 | | € 0.980 | 0.989 | 0.994 | 0.997 | 0.998 | 0.999 | 1.000 | | |
| 14.0 | 0.952 | 0.971 | 0.983 | 0.991 | 0.995 | 0.997 | 0.999 | 0.999 | 1.000 | |
| 14.5 | 0.936 | 0.960 | 0.976 | 0.986 | 0.992 | 0.996 | 0.998 | 0.999 | 0.999 | 1.000 |
| 15.0 | 0.917 | 0.947 | 0.967 | 0.981 | 0.989 | 0.994 | 0.997 | 0.998 | 0.999 | 1.000 |

Table 3 (Continued)

| | o sides | Continue | a) | | | | | | - | | | | | |
|----|----------------|----------------|----------------|------------|---------------------|----------|------------|-------|----------|-------|--------|-------|-------|-------|
| , | λ ^a | 4 | 5 | 6 | - | 7 | 8 | | <u> </u> | | | | | |
| - | 16 0 | .000 | | 0.004 | | | | - 9 | | 10 | 11 | | 12 | 13 |
| | | | | 0.004 | 0.0 | | .022 | 0.0 | | 077 | 0.12 | 7 0.3 | 193 | 0.275 |
| | | | | 0.002 | 0.0 | | 013 | 0.0 | | 049 | 0.08 | | 135 | 0.201 |
| | | | | 0.001 | 0.00 | | 007 | 0.0 | | 030 | 0.055 | 5 0.0 | 92 | 0.143 |
| | | | | 0.000 | 0.00 | | 004 | 0.00 | | 018 | 0.035 | | 61 | 0.098 |
| | | | | 0.000 | 0.00 | | 002 001 | 0.00 | | 011 | 0.021 | | | 0.066 |
| | 22 0. | 000 0 | | 0.000 | 0.00 | | 001 | 0.00 | | | 0.013 | | 25 | 0.043 |
| 2 | 23 0.0 | 000 0 | | 0.000 | 0.00 | | 000 | 0.00 | | | 0.008 | | | 0.028 |
| | 24 0.0 | 000 0. | | .000 | 0.00 | | - | 0.00 | | | 0.004 | | | 0.017 |
| 2 | 25 0.0 | 000 0. | 000 0 | .000 | 0.00 | 000 | | 0.00 | | | 0.003 | 0.00 | | 0.011 |
| | 1 | 4 | | 16 | 17 | | | | | | 0.001 | 0.00 |)3 (| 0.006 |
| 1 | 6 0.3 | | | | | 18 | | 19 | 20 |) | 21 | 22 | | 23 |
| 1 | | | | 566 | 0.659 | | | 0.812 | | 68 0 | .911 | 0.94 | 2 0 | .963 |
| 18 | | | | 468 375 | 0.564 | | | 0.736 | | 05 0 | .861 | 0.90 | | .937 |
| 19 | | | | | 0.469 | | | 0.651 | 0.73 | 1 0 | .799 | 0.85 | | .899 |
| 20 | | | | | 0.297 | | | 0.561 | 0.64 | - | .725 | 0.793 | | .849 |
| 21 | 0.07 | | | | 0.297 | | | 0.470 | 0.55 | | 644 | 0.721 | | 787 |
| 22 | | 8 0.0 | | | 0.227 | 0.30 | | 0.384 | 0.47 | | 558 | 0.640 | | 716 |
| 23 | 0.03 | | | | 0.109 | 0.23 | | 0.306 | 0.38 | | 472 | 0.556 | | 637 |
| 24 | 0.02 | | | | 0.087 | 0.17 | | 0.238 | 0.31 | | 389 | 0.472 | 0 | 555 |
| 25 | 0.01 | | | | 0.060 | 0.12 | | 0.180 | 0.243 | | 314 | 0.392 | 0.4 | 473 |
| | 24 | 25 | | | | <u> </u> | |).134 | 0.185 | 0.2 | 247 | 0.318 | 0.3 | 394 |
| 16 | 0.978 | | | | 27 | 28 | | 29 | 30 | 3 | 1 ′ | 32 | 3 | 3 |
| 17 | 0.959 | | 7 0.99 | | .996 | 0.998 | _ | .999 | 0.999 | 1.0 | 00 | | | _ |
| 18 | 0.932 | | | | .991 | 0.995 | | .997 | 0.999 | | | 1.000 | | |
| 19 | 0.893 | | | | 983 | 0.990 | | 994 | 0.997 | 0.9 | | 0.999 | 1.0 | 00 |
| 20 | 0.843 | 0.888 | | | 969 | 0.980 | | 988 | 0.993 | 0.9 | | 0.998 | 0.9 | |
| 21 | 0.782 | 0.838 | | | 948 | 0.966 | | 978 | 0.987 | 0.99 | 92 (| 0.995 | 0.99 | |
| 22 | 0.712 | 0.777 | | | 917 8 7 7 | 0.944 | | 963 | 0.976 | 0.98 | 2000 E | 0.991 | 0.99 | |
| 23 | 0.635 | 0.708 | | 102.0 | | 0.913 | | 940 | 0.959 | 0.97 | 73 (| 0.983 | 0.98 | |
| 24 | 0.554 | 0.632 | | | 827 768 | 0.873 | | 809 | 0.936 | 0.95 | 6 0 |).971 | 0.98 | |
| 25 | 0.473 | 0.553 | | | | 0.823 | | 368 | 0.904 | 0.93 | | .953 | 0.96 | |
| | 34 | 35 | 36 | | | 0.763 | 0.8 | | 0.863 | 0.90 | 0 0 | .929 | 0.95 | |
| 19 | | | | 3 | / | 38 | 3 | 9 | 40 | 41 | | 42 | 43 | _ |
| 20 | 0.999 0.999 | 1.000 | | | | | | | | | | | | - |
| 21 | 0.999 | 0.999 | 1.000 | | | | | | | | | | | |
| 22 | 0.997 | 0.998 0.996 | 0.999 | 0.9 | 9/// | 000.1 | - 2 | | | x | | | | |
| 23 | 0.988 | 0.996 | 0.998 | 0.9 | |).999 | 1.00 | | | | | | | |
| 24 | 0.979 | 0.993 | 0.996 | 0.99 | | .999 | 0.99 | | .000 | | | | | |
| 25 | 0.966 | 0.987 | 0.992 0.985 | 0.99 | | .997 | 0.99 | _ | .999 | 0.999 | 1.0 | 000 | | |
| | | 0.576 | 0.983 | 0.99 | 1 0 | .991 | 0.99 | 7 0 | .998 | 0.999 | | | 1.000 | |