Homework Asssignment 10

Instructions: Read appropriately relevant sections of Chapter 5 in your textbook. Then read sections 7.1 - 7.3. Homework is due by the beginning of class on **Wednesday**, **November 4**.

- 1. Explicitly construct the unique non-Abelian group G of order 21 as a subgroup of an appropriately chosen symmetric group S_n .
- 2. Let p be a prime.
 - (a) Consider the Abelian group $A = \mathbb{Z}_{p^2}$. Find the automorphism group $\operatorname{Aut}(A)$ and its order. Justify your answer.
 - (b) Consider the Abelian group $A = Z_p \times Z_p$. Find the automorphism group $\operatorname{Aut}(A)$ and its order. Justify your answer.
- 3. Let p = 3. Explicitly list all the subgroups of $Z_3 \times Z_3$ of order 3.

Wesley: 1, §7.1: 5, 6, 7, 8, 11 Olha: 2a, 3, §7.1: 13, 14, 24, 25 Oscar: 2b, §7.2: 6, 7, 8 §7.3: 1, 2