

Fys2140

oblig 2

Eirik Lud / eathund

3.3 a) $E = E_1 - E_2 \rightarrow \gamma$ en del av energien overføres til atomet som E_k (rehyll).

Antar ikke-relativistisk: $E_k = \frac{p^2}{2m} = \left(\frac{h\nu}{c}\right)^2 \frac{1}{2m}$

$$p_\gamma = \frac{h\nu}{c}$$

$$E = \frac{h\nu}{c} + \frac{h^2\nu^2}{c^2} \frac{1}{2m} = E_1 - E_2$$

$$\Delta E = \frac{(m_i^2 - m_f^2) c^4}{2E} = \frac{(h\nu)^2}{2Mc^2}$$

b) $0 p_c + p_\gamma \rightarrow p'_c$

$$0 + \frac{h\nu}{c} \rightarrow mv \quad \text{gir } v = \frac{h\nu}{mc} \quad (*)$$

$$k_E = \frac{1}{2}mv^2 \quad \text{innsatt } (*) : \Delta E = \frac{(h\nu)^2}{2Mc^2}$$

c) Regn ut $\frac{\Delta E}{h\nu}$ for overgang $E_2 - E_1 = 4.86 \text{ eV}$
i et kvikkeskall atom $m_{\text{Hg}} = 200 \text{ mp}$

$$4.86 \text{ eV} = h\nu \quad \nu = 1.175 \cdot 10^{15}$$

$$\left(\frac{4.86 \text{ eV}}{2Mc^2}\right) = \frac{(h\nu)^2}{2Mc^2} = 1.295 \cdot 10^{-11}$$

3.5 oppgitt potensial :

$$V(r) = V_0 \left(\frac{r}{a} \right)^k, \text{ kvantiserings bet. } L = n\hbar$$

$$L = mvr = n\hbar \quad r = \frac{n\hbar}{mv}$$

$$F = -\frac{dV(r)}{dr} = -\frac{V_0 k r^{k-1}}{a^k}$$

Bohr sentripetal akselerasjon, sirkulær bevegelse $\frac{mv^2}{r}$

$$\frac{mv^2}{r} = V_0 k \frac{r^{k-1}}{a^k} \quad v^2 = \frac{V_0 k r^k}{m a^k}, \quad v^2 = \frac{V_0 k}{m} \left(\frac{r}{a} \right)^k$$

$$E = \frac{1}{2}mv^2 + V(r) = \frac{1}{2} \frac{V_0 k}{m} \left(\frac{r}{a} \right)^k + V_0 \left(\frac{r}{a} \right)^k$$

$$E = \frac{V_0}{2} \left(\frac{r}{a} \right)^k (k+2)$$

$$V_i \text{ har at } r = \frac{n\hbar}{mv}, \quad v^2 = \frac{V_0 k}{m} \left(\frac{r}{a} \right)^k$$

$$r^k = \frac{V_0^{\frac{1}{k}} a^k m}{V_0 k} \quad r^k = \left(\frac{n^2 \hbar^2 a^k m}{m^2 V_0 k} \right)^{\frac{1}{k+2}}$$

$$r(k, n) = \left(\frac{\hbar^2 a^k}{m V_0 k} n^2 \right)^{\frac{1}{k+2}}$$

$$E(n, k) = \frac{V_0 (k+2)}{2 a^k} \left(\frac{\hbar^2 a^k}{m V_0 k} n^2 \right)^{\frac{k}{k+2}}$$

• kontroller n-avhengighet ved $k = -1$

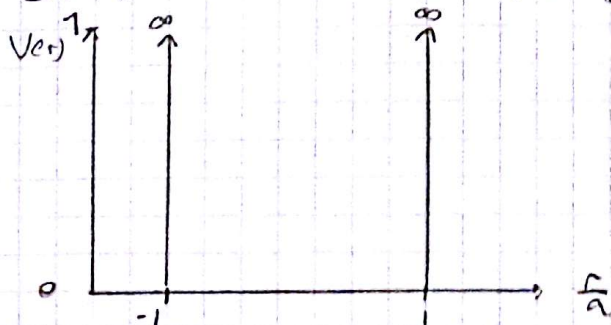
$$E(n, -1) = \frac{V_0 (-1+2)}{2 a^{-1}} \left(\frac{\hbar^2 a^{-1}}{m V_0 -1} n^2 \right)^{-\frac{1}{1+2}} = -\frac{V_0 a}{2} \left(\frac{n^2 \hbar^2 a^{-1}}{m V_0 -1} \right)^{-1}$$

$$E(n, -1) = -(V_0 a)^2 \frac{m}{2n^2 \hbar^2}$$

$$\text{hvis } (V_0 a)^2 = k e^2 c^4$$

Så får vi at $E(n, k=-1) = -13.6 \text{ eV} \frac{1}{n^2}$ Bohr

dette kalles et Coulombpotensial.



4.2

De Broglie, relasjoner:

$$\lambda = \frac{h}{p} \quad \text{vi har } E_c' = \sqrt{p^2 c^2 + m_0^2 c^4}$$

$$p^2 = E^2 m_0 \quad p = \sqrt{E^2 m_0} = \sqrt{\left(\frac{E}{c}\right)^2 - m_0^2 c^2}$$

$$a) E_{\text{tot}} = E_k + E_p \quad E_{\text{tot}} = E_k + m_0 c^2$$

$E_k = eV$ pga potensial til e-tillet

$$E_{\text{tot}} = eV + m_0 c^2 \quad \text{tilsett til } p = \sqrt{\left(\frac{eV + m_0 c^2}{c}\right)^2 - m_0^2 c^2}$$

$$p = \sqrt{\frac{eV^2 + 2eV m_0 c^2 + m_0^2 c^4}{c^2} - m_0^2 c^2}$$

$$\sqrt{2eV m_0 \left(1 + \frac{eV}{2m_0 c^2}\right)^{\frac{1}{2}}}$$

$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2eV m_0} \left(1 + \frac{eV}{2m_0 c^2}\right)^{\frac{1}{2}}}$$

$$b) \text{ ikke-relativistisk: } E_{\text{tot}} = E_k + E_p$$

$$eV = \frac{1}{2} m v^2$$

$$p = \sqrt{2 m eV}$$

$$\lambda = \frac{h}{\sqrt{m_0^2 v^2}} \left(1 + \frac{m_0 v^2}{4 m_0 c^2}\right)^{-\frac{1}{2}} \quad v \ll c \quad \text{så } \frac{v}{c} \approx 0$$

$$\lambda = \frac{h}{\sqrt{m_0^2 v^2}} (1 + 0) = \frac{h}{m_0 v}$$

4.2

c) $p = \gamma m_0 v$ der $\gamma = \frac{1}{\sqrt{1 - \frac{v}{c}}}$

$$\lambda = \frac{h}{\gamma m_0 v} = \frac{h}{m_0 v} \sqrt{1 - \frac{v}{c}} \quad \text{oppgitt } \beta = \frac{v}{c}$$

$$\lambda = \frac{h}{m_0 v} \sqrt{1 - \beta} \quad E_0 \text{ oppgitt } h m_0 c^2$$

Så vi ganger inn $\frac{c}{c}$

$$\Rightarrow \frac{hc^2}{m_0 c^2 v} \sqrt{1 - \beta} \Rightarrow \frac{hc^2}{E_0 v} \sqrt{1 - \beta}$$

$$\Rightarrow \frac{hc \sqrt{1 - \beta}}{E_0 \frac{v}{c}}$$

$$\lambda = \frac{1.24 \cdot 10^{-12+10}}{E_0 (\text{MeV}) \beta} \quad \text{som vi skulle vise.}$$

$$\lambda = \frac{1.24 \cdot 10^{-2}}{E_0 (\text{MeV}) \beta} \sqrt{1 - \beta}$$

4.3 Relasjoner: $p = \frac{h}{\lambda} = \frac{h\nu_{\min}}{c}$, $E = h\nu$

a) $\nu_{\min} = \frac{c}{\lambda} = 5 \cdot 10^{17} \text{ Hz}$

b) $E = h\nu_{\min} = 2.069 \text{ keV}$

c) $E_{\gamma} = \sqrt{(pc)^2 + m_0^2 c^4} = \sqrt{\frac{h^2 c^2}{\lambda^2} + m_0^2 c^4} = 510 \text{ keV}$

$$E_{\text{ikket}} = \frac{p^2}{2m} = \frac{h^2}{2m\lambda^2} = 4.15 \text{ eV}$$

Det mest vanlige er elektronmikroskop for å observere nanoskala