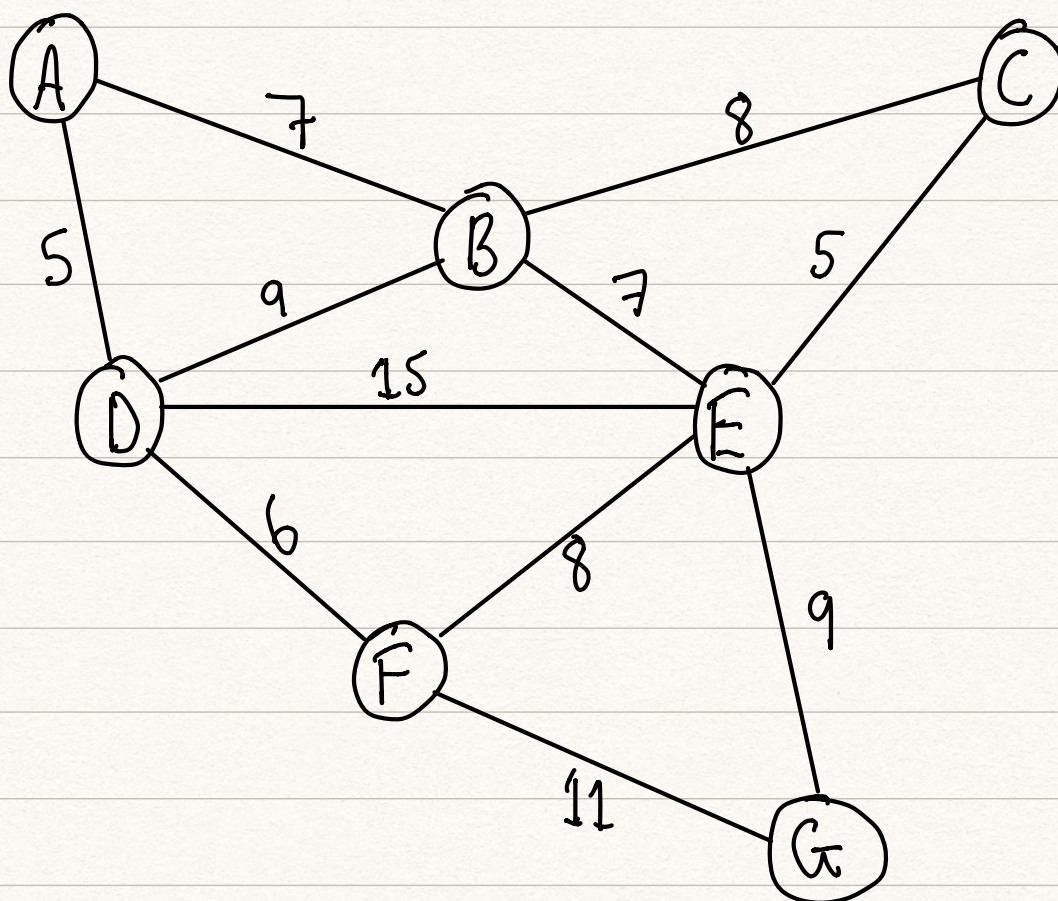


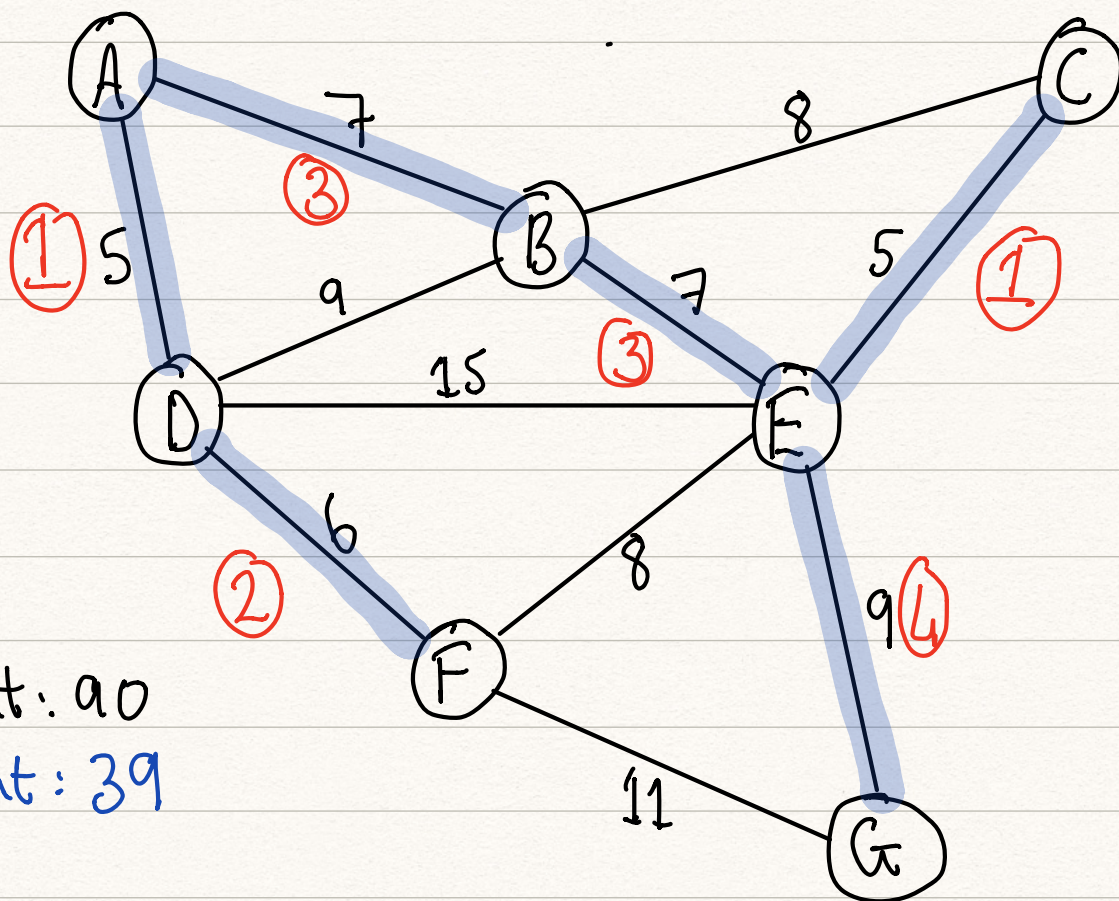
Given this following tree structure



Kruskal's Algorithm

Finds a safe edge to add to a growing forest by finding all the edges that connect any two trees in the forest an edge (u,v) of least weight. It uses a disjoint-set data structure where each vertex is initially in its own set. This is known as UnionFind in my implementation.

Minimum Weight + Union Find



Path Compression

1. $[A D], [B], [C E], [F] [G]$

2. $[A D F], [B], [C E], [G]$

3. $[A D F C E B], [G]$

4. $[A D F C E B G]$

Kruskal PseudoCode

MST-KRUSKAL (G, w)

MST = \emptyset

for each vertex v in $G.VL$

MAKE-SET(v)

sort edges of $G.EL$ ascendingly by weight

for each edge (u, v) in $G.EL$ order by weight

if ($\neg \text{connected}(u, v)$)

UNION(u, v)

MST.insert(Edge)

return MST

Expected Output

A \rightarrow D 5

C \rightarrow E 5

D \rightarrow F 6

A \rightarrow B 7

B \rightarrow E 7

E \rightarrow G 9

39 total weight

39 < 90 therefore is minimum tree.

How to compile my code

```
Eamonn Keogh@DESKTOP-0A91N31 MINGW64 ~/eclipse-workspace/Algorithms-DS/src (master)
$ javac kruskal/*.java
Note: kruskal\Graph.java uses unchecked or unsafe operations.
Note: Recompile with -Xlint:unchecked for details.
```

There is a warning because java doesn't like casting generic arrays

How to run my code (cmd line input)

```
Eamonn Keogh@DESKTOP-0A91N31 MINGW64 ~/eclipse-workspace/Algorithms-DS/src (master)
$ java kruskal.Main myGraph.txt
```

My code takes command line arguments
myGraph.txt is the argument

Program Output

```
Eamonn Keogh@DESKTOP-0A91N31 MINGW64 ~/eclipse-workspace/Algorithms-DS/src (master)
$ java kruskal.Main myGraph.txt
Vertices: 7 Edges: 11

Adjacency List: 90 weighting
A -> [B, 7] [D, 5]
B -> [C, 8] [D, 9] [E, 7]
C -> [E, 5]
D -> [E, 15] [F, 6]
E -> [F, 8] [G, 9]
F -> [G, 11]

Minimum Spanning Tree: 39 weighting
[D, 5]
[E, 5]
[F, 6]
[B, 7]
[E, 7]
[G, 9]

Eamonn Keogh@DESKTOP-0A91N31 MINGW64 ~/eclipse-workspace/Algorithms-DS/src (master)
$ █
```