Cake Puzzle

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Function to implement Monte Carlo simulation

```
runSim <- function(nSim = 1000) {</pre>
    # set up an array to store parameter estimates
    estArray \leftarrow array(0, dim = c(nSim, 1))
    for (i in 1:nSim) {
        A <- runif(1)
        B <- runif(1)
        C <- runif(1)</pre>
        if ((B > A && B < C) | (A > B && A < C)) {
        } else {
             res = 0
        }
        estArray[i] <- res
    list(estArray = estArray)
}
x \leftarrow runSim(nSim = 99999)
mean(x$estArray, na.rm = TRUE)
```

[1] 0.3372334

Analytical solution

Simulation is a little overkill for this problem, but a good programming excercise. We can use permutations.

Denote the location of the candles as A and C and the location of the cut B. Remember that repetition is allowed in permutations unlike in combinations.

 ${}^{n}p_{r}:% =0$ which means the number of permutations of n items taken r items at a time.

For example; given 3 letters ABC find ³p₃

```
ABC, BAC, BCA, CBA, CAB, ACB
```

which mean that there are 6 ways, in other words ${}^{3}p_{3}=6$.

Lets look at the permutation function using factorials:

$$n!/(n-r)! = 3!/(3-3)! = 3x2x1/0! = 6/1 = 6.$$

We can see that B is in the middle of 'ABC, BAC, BCA, CBA, CAB, ACB' 2 out of 6 times. So the chance that both pieces of the cake have a candle on them is 1/3.

Computing Environment

sessionInfo()

```
R version 3.6.1 (2019-07-05)
Platform: x86_64-w64-mingw32/x64 (64-bit)
Running under: Windows 10 x64 (build 17134)
Matrix products: default
locale:
[1] LC_COLLATE=English_United Kingdom.1252
[2] LC_CTYPE=English_United Kingdom.1252
[3] LC_MONETARY=English_United Kingdom.1252
[4] LC_NUMERIC=C
[5] LC_TIME=English_United Kingdom.1252
attached base packages:
[1] stats
              graphics grDevices utils
                                             datasets
[6] methods
              base
other attached packages:
[1] knitr_1.23
loaded via a namespace (and not attached):
 [1] compiler_3.6.1 magrittr_1.5 formatR_1.7
[4] tools_3.6.1 htmltools_0.3.6 yaml_2.2.0 [7] Rcpp_1.0.1 stringi_1.4.3 rmarkdown_1.14
[10] stringr_1.4.0 xfun_0.8
                                digest_0.6.20
```

This took 0.6 seconds to execute.

[13] evaluate_0.14