HW 3

2023-04-18

Question 12.22 From Hansen Econometrics

Part a)

```
# Estimate 12.86 loggdp = b0 + b1risk
reg1 = ajr_df %>% lm(loggdp ~ risk,.) |> summary()

# Estimate 12.87 risk = b0 + b1 logmortality
reg2 = ajr_df %>% lm(risk ~ logmort0,.)
# Get the fitted values
risk_fitted = reg2$fitted.values
reg2 = summary(reg2)

# Estimate 12.88 logGdp = b0 + risk with risk now endogenous
reg3 = lm(ajr_df$loggdp ~ risk_fitted) |> summary()
```

Part b)

risk ## 0.051

```
# Restimate the above with both homoskedastic and heteroskedastic standard errors. The fixest package a
reg1_het = ajr_df %>% feols(loggdp ~ risk,., vcov = "HC1")
reg2_het = ajr_df %>% feols(risk ~ logmort0,., vcov = "HC1")
reg3_het = ajr_df %>% feols(loggdp ~ 1 | risk ~ logmort0,., vcov = "HC1")

# Compare SE's for 12.86
reg1$coefficients[2,2]; reg1_het$se[2] # Homoskedastic se's are reported

## [1] 0.063
```

```
# 12.87
reg2$coefficients[2,2]; reg2_het$se[2] # Homoskedastic se's are reported
## [1] 0.13
## logmort0
##
      0.15
# 12.88
reg3$coefficients[2,2]; reg3_het$se[2] # Homoskedastic se's are reported
## [1] 0.13
## fit_risk
      0.17
Part c)
# Estimate 2SLS with indirect least squares
# First estimate effect of instrument on outcome
reg4 = ajr_df %>% lm(loggdp ~ logmort0,.) |> summary()
# Then divide that effect by effect of instrument on endogenous variable found in reg2
reg4$coefficients[2,1] / reg2$coefficients[2,1] # The same as part b
## [1] 0.93
Part d)
# Estimate 2SLS with two stage approach
reg_2sls = ivreg(loggdp ~ risk | logmort0, data = ajr_df)
coef(reg_2sls)[2] # Same as before
## risk
## 0.93
Part e)
# Get error terms from 2SLS regression and add them to data set
uhat2 = residuals(reg_2sls)
ajr_df = mutate(ajr_df, uhat2 = uhat2)
# Run control variable approach
reg_control = ajr_df %>% lm(loggdp ~ risk + logmort0 + uhat2,.)
coef(reg_control)[2] #Same as before
## risk
## 0.93
```

Part f)

```
# Add latitude and africa as regressors
(reg_africa = ajr_df %>% lm(loggdp ~ risk + latitude + africa,.))
##
## Call:
## lm(formula = loggdp ~ risk + latitude + africa, data = .)
## Coefficients:
## (Intercept)
                      risk
                                latitude
                                               africa
         5.652
                      0.377
                                   1.382
                                               -0.723
##
# Africa is significant at any alpha level, lattitude is only significant at the 10% level
Part g)
(reg_africa_2sls = ivreg(loggdp ~ risk + africa + latitude | logmort0 + africa + latitude, data = ajr_d
##
## Call:
## ivreg(formula = loggdp ~ risk + africa + latitude | logmort0 + africa + latitude, data = ajr_df)
## Coefficients:
                      risk
## (Intercept)
                                  africa
                                             latitude
       2.9951
                     0.8000
                                 -0.3479
                                              -0.0553
##
# Africa and latitude are not longer significant
Part h)
# Add exponential of mortality to data
ajr_df = mutate(ajr_df, mortality0 = exp(logmort0))
# Run baseline regresssion with mortality
(reg_mortality = ivreg(loggdp ~ risk | mortality0, data = ajr_df))
##
## Call:
## ivreg(formula = loggdp ~ risk | mortality0, data = ajr_df)
## Coefficients:
## (Intercept)
                      risk
##
         0.489
                      1.161
```

The authors prefered log mortality because it has an easier interpretation than this level of mortality.

Part i)

```
# Add square root to data set
ajr_df = mutate(ajr_df, mortsquare = logmort0^2)
(reg_square = ivreg(loggdp ~ risk | mortality0 + mortsquare, data = ajr_df))
##
## Call:
## ivreg(formula = loggdp ~ risk | mortality0 + mortsquare, data = ajr_df)
## Coefficients:
## (Intercept)
                       risk
                      0.939
##
         1.934
# The result is back to the same result as earlier for risk
Part j)
stock_yogo_test(X =~ 1, D =~ risk, Z =~ mortality0 + mortsquare, B = 0.1, size_bias = "size", data = ajr
## Results of Stock and Yogo test for weak instruments:
##
        Null Hypothesis:
##
                                      Instruments are weak
        Alternative Hypothesis:
##
                                      Instruments are not weak
##
        Data:
##
                                      ajr_df
##
        Controls:
                                      ~1
        Treatments:
##
                                      ~risk
        Instruments:
##
                                      ~mortality0 + mortsquare
##
##
        Alpha:
                                            0.05
                                     10% Wald test distortion.
##
        Acceptable level of bias:
##
        Critical Value:
##
##
        Cragg-Donald Statistic:
                                              11
        Df:
##
                                              61
The instruments are weak
Part k)
summary(reg_square, vcov = sandwich, diagnostics = TRUE)
##
## Call:
## ivreg(formula = loggdp ~ risk | mortality0 + mortsquare, data = ajr_df)
```

```
##
## Residuals:
      Min
               1Q Median
## -2.4275 -0.5506 0.0837 0.7034 1.7147
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                 1.934
                            1.128
                                     1.71
                                             0.092 .
## (Intercept)
## risk
                  0.939
                            0.169
                                     5.55 6.3e-07 ***
##
## Diagnostic tests:
                   df1 df2 statistic p-value
                     2 61
                                8.58 0.00052 ***
## Weak instruments
                                       6e-05 ***
## Wu-Hausman
                     1 61
                               18.61
## Sargan
                     1 NA
                                0.63 0.42624
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
\mbox{\tt \#\#} Residual standard error: 0.96 on 62 degrees of freedom
## Multiple R-Squared: 0.173, Adjusted R-squared: 0.159
## Wald test: 30.8 on 1 and 62 DF, p-value: 6.34e-07
```

The Wu-Hausaman test is significant so we conclude the instruments are exogenous.

Part j)

```
# Create IVmodel object
ivmod = ivmodel(Y = as.numeric(ajr_df$loggdp), D = as.numeric(ajr_df$risk), Z = ajr_df[, c("mortality0"
liml = LIML(ivmod)
liml$point.est
```

Estimate ## [1,] 0.96