

```

from numpy import *
from vpython import *
from random import *
from time import *

# constants
m = 1.0
kp = 40.0
kc = 250.0
f_0 = 50.0
v_0 = 0.01

# changeable constants
# number of blocks
n = 500
# long timestep
dt1 = 0.03
# short timestep
dt2 = 0.003
# final time
t_f = 1000.0
# number of runs
n_events = 10
# window size
window_w = 400
window_h = 400
# plus or minus factor to initial positions
rand = 0.001
# use uniformly distributed start or not
equil = False

# returns force of friction
def calculate_friction(f_opposed, v_i_t):
    # if block not moving
    if (v_i_t == 0.0):
        # if force on block less than equal to f_0
        if (f_opposed <= f_0):
            return -f_opposed
        # if force on block greater than f_0
        else:
            return sign(-f_opposed) * f_0
    else:
        # calculate kinetic friction
        return (-(f_0 * sign(v_i_t)) / (1.0 + abs(v_i_t)))

# return array of zeros
def initialize_positions_uniform(positions):
    return positions

# return array of positions adding or subtracting rand from each one
def initialize_positions_random(positions, rand):
    for i in range(n):
        switch_value = randint(0, 1)
        if (switch_value == 0):
            positions[i] = rand
        else:
            positions[i] = -rand
    return positions

# return array of random masses in hardcoded range
def initialize_masses_random(masses):
    for i in range(n):
        masses[i] = uniform(0.5, 2.0)
    return masses

# return array of random kcs in hardcoded range

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def initialize_kcs_random(kcs):
    for i in range(n):
        kcs[i] = uniform(200.0, 300.0)
    return kcs

# return array of random kps in hardcoded range
def initialize_kps_random(kps):
    for i in range(n):
        kps[i] = uniform(30.0, 50.0)
    return kps

# return value for force on block i
def calculate_force(i):
    # if first block then no block to the left
    if (i == 0):
        f_opposed = kcs[i] * (positions[i + 1] - positions[i])
    # if last block then no block to the right
    elif (i == n - 1):
        f_opposed = kcs[i] * (positions[i - 1] - positions[i])
    else:
        f_opposed = kcs[i] * (positions[i + 1] + positions[i - 1] - 2.0 * positions[i])
    # add force from leaf spring
    f_opposed += kps[i] * (v_0 * t_i - positions[i])
    # calculate and add friction
    ff = calculate_friction(f_opposed, velocities[i])
    return f_opposed + ff

# returns value for velocity of block i
def calculate_velocity(i, f_i):
    # calculate velocity of next step
    v_i = (f_i * dt) / masses[i] + velocities[i]
    # if velocity is not zero and it changes direction
    if ((velocities[i] != 0.0) and (sign(velocities[i]) != sign(v_i))):
        return 0.0
    return v_i

# returns value for position of block i
def calculate_position(i, v_i_t1):
    return (v_i_t1 * dt) + positions[i]

# plots the distribution
def plots(magnitudes):
    # set up buckets
    diff = 0.5
    max_m = int(max(magnitudes)) + 1
    min_m = int(min(magnitudes)) - 1
    magnitude_counts = [0] * (int((max_m - min_m) / diff) + 1)
    # iterate through magnitudes and put in buckets
    for i in magnitudes:
        index = int((i - min_m) / diff)
        magnitude_counts[index] = magnitude_counts[index] + 1
    # print info
    print(magnitude_counts)
    print(sum(magnitude_counts))
    # plot on logarithmic y scale
    distribution = graph(align = 'left', xmin = min_m, xmax = max_m, width = window_w, height = window_h, \
        title = 'Distribution of magnitudes', xtitle = 'Magnitude', ytitle = 'Number of events')
    g_distribution = gdots(color=color.cyan)
    for i in range(len(magnitude_counts)):
        if (magnitude_counts[i] == 0):
            g_distribution.plot(pos = [min_m + i * diff, magnitude_counts[i]])
        else:
            g_distribution.plot(pos = [min_m + i * diff, math.log(magnitude_counts[i])])

# get start time
start = time()

```

```
magnitudes = []
```

```
# iterate through runs
```

```
for k in range(n_events):
```

```
# initialized constants
```

```
# array of positions for each block
```

```
positions = resize(array([0.0]), n)
```

```
# array of velocities for each block
```

```
velocities = resize(array([0.0]), n)
```

```
# array of forces for each block
```

```
forces = resize(array([0.0]), n)
```

```
# array of masses for each block
```

```
masses = resize(array([0.0]), n)
```

```
masses = initialize_masses_random(masses)
```

```
# array of kc factors for each block
```

```
kcs = resize(array([0.0]), n)
```

```
kcs = initialize_kcs_random(kcs)
```

```
# array of kp factors for each block
```

```
kps = resize(array([0.0]), n)
```

```
kps = initialize_kps_random(kps)
```

```
t_i = 0.0
```

```
moment = 0.0
```

```
dt = dt1
```

```
# initialize positions
```

```
if (equil):
```

```
    positions = initialize_positions_uniform(positions)
```

```
else:
```

```
    positions = initialize_positions_random(positions, rand)
```

```
# keeps track of switching dt
```

```
first = False
```

```
# keeps track of dt having been switched until quake start
```

```
second = False
```

```
# for this amount of time
```

```
while (t_i < t_f):
```

```
# copy arrays so as not to overwrite them
```

```
temp_positions = positions.copy()
```

```
temp_velocities = velocities.copy()
```

```
temp_forces = forces.copy()
```

```
# keeps track of all velocities being zero
```

```
zeros = True
```

```
# iterate through blocks
```

```
for i in range(n):
```

```
    f_i = calculate_force(i)
```

```
    v_i_t1 = calculate_velocity(i, f_i)
```

```
# if block is moving
```

```
if (v_i_t1 != 0.0):
```

```
# if using long timestep
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```
if (dt == dt1):
```

```
# go back
```

```
t_i = t_i - dt
```

```
# switch to short timestep
```

```
dt = dt2
```

```
first = True
```

```
zeros = False
```

```
break
```

```
# marks quake start
```

```
if (second):
```

```
    second = False
```

```
zeros = False

x_i_t1 = calculate_position(i, v_i_t1)

# put calculated values in arrays
temp_forces[i] = f_i
temp_velocities[i] = v_i_t1
temp_positions[i] = x_i_t1

# if not switch (when go back in time)
# update arrays
if (not first):
    forces = temp_forces
    velocities = temp_velocities
    # update moment
    moment += sum(velocities) * dt
    positions = temp_positions

# after switched
else:
    first = False
    second = True

# marks that quake is over
if (zeros and not second):
    if (moment != 0.0):
        magnitudes.append(math.log(moment))
        moment = 0.0
    # switch to long timestep
    dt = dt1

t_i += dt

# keep track of time
if (k % 1 == 0):
    print(k, ': ', time() - start)

plots(magnitudes)
print('Finish: ', time() - start)
```