# CSE 380: Final Project Canned Project

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#### Overview

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# Third-Party Libraries

Catch unit testing, header-defined

Eigen working with vectors and matrices easily, header-defined

HDF5 output format to store data

**GSL** scientific library

INIReader way to define configuration options easily, header-defined

#### Problem 1

For this simple problem, I solved the simple ODE

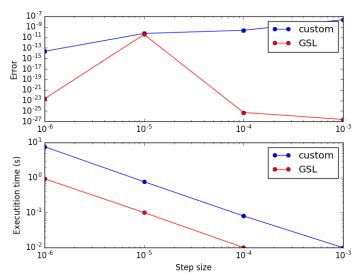
$$\dot{y}(t) = -0.1 \cdot y(t)$$

which of course has the solution

$$y(t) = y(t_0)e^{-0.1(t-t_0)}$$

for an initial condition specified at  $t_0$ .

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#### Results

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- My implementation is also less accurate than GSL's RK4 on the same step size
- This shouldn't be surprising, as forward Euler is in general less accurate than more general Runge-Kutta methods. Furthermore, I decided to use Eigen for handling vectors for problem 2 and the same overhead is present here.
- Not entirely sure why GSL does relatively poorly for  $h = 10^{-5}$ , but perhaps the larger step sizes were spuriously accurate

#### Problem 2

I used *Mathematica* to solve the system of ODEs for the following analytical solutions

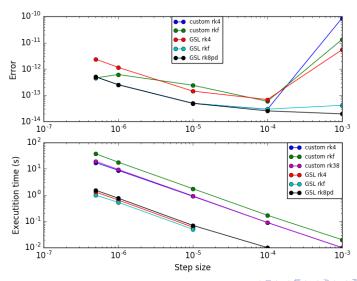
$$x(t) = \frac{20\tau e^{-\frac{t}{\tau}} \left(\tau \omega \sin(t\omega) + e^{t/\tau} - \cos(t\omega)\right)}{\tau^2 \omega^2 + 1}$$

$$y(t) = -\frac{20\tau e^{-\frac{t}{\tau}} \left(\tau \omega e^{t/\tau} - \tau \omega \cos(t\omega) - \sin(t\omega)\right)}{\tau^2 \omega^2 + 1}$$

$$z(t) = 2\tau e^{-\frac{t}{\tau}} \left(e^{t/\tau} - 1\right)$$

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### Results



#### Results I

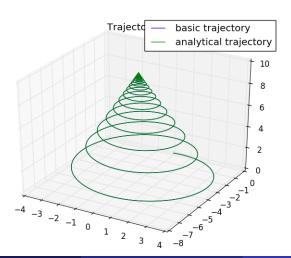
- Due to initially misreading the project assignment, I implemented my own RK solvers ("custom" in previous slide).
- Similar to problem 1, my solutions are slower in execution time (again, likely due to Eigen).
- Accuracy above  $h = 10^{-4}$  behaves as expected, with my solutions being less accurate, and all solutions worsening.
- I can't explain why the accuracy gets worse (simulation was fixed total time), but maybe the numerical error levels out at some point?
- Interestingly, the GSL implementation of Runge-Kutta-Fehlberg was the fastest GSL, followed by RK4 then Runge-Kutta Prince-Dormand (a higher order solver)
- For my solutions, RK4 and the "3/8" rule RK method showed similar timing, while Runge-Kutta-Fehlberg was slowest.

#### Results II

- In terms of accuracy, RK4 as implemented by GSL was the worst overall at small step size, and the worst out of the GSL options at all step sizes.
- The RK4 and "3/8" RK methods I implemented performed nearly identically in time and in accuracy.

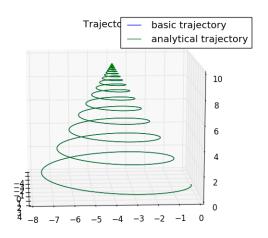
#### Simulation Results

This is a high-resolution result computed on Stampede for 1M iterations with a step size of 0.0001 (RK4).



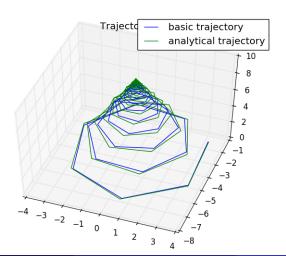
#### Simulation Results

This is a lower-resolution result computed on Stampede for 10K iterations with a step size of 0.01 (RK4).



#### Simulation Results

This is a minimal-resolution result computed on Stampede for 500 iterations with a step size of 0.2 (RK4).



## References

# Appendix A