

# Determination of Magnitude and Intrinsic Flux of HD 227858 and HD 338931 from Landholt Standard SA 113475

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## Introduction

While the casual astrophotographer might only care about seeing as many stars as possible in an image, in academic astronomy, we often want to have quantifiable data about stars, for example the magnitude (measure of brightness) of the star to compare it to others, either in terms of total light or broken into sections of the electromagnetic spectrum by filters. Or, we might want to have the flux (photon energy or number per area each second). However, besides having proper equipment, much calibration must take place to account for all present factors - atmospheric extinction of photons travelling at different angles through Earth's atmosphere, ever-present and never-present pixels in our sensor, absorption in mirrors and lenses, etc. Here, I work through calculating the magnitude and intrinsic flux (flux just outside the atmosphere) of stars HD 227858 and HD 338931 based on the Landhold Standard star SA 113475 [?].

Filter	$\lambda_0$ [ $\mu\text{m}$ ]	$\Delta\nu$ [Hz]	Absolute Spectral Radiance [ $\text{erg cm}^{-2}\text{s}^{-1}\text{\AA}^{-1}$ ]
B	0.44	3.06E15	6.60E-9
V	0.55	3.37E15	3.64E-9
R	0.70	1.36E15	1.36E-9
I	0.90	6.81E14	8.30E-10

Table 1: Johnson Filter Band parameters, with  $\lambda_0$  as the central wavelenth,  $\Delta\nu$  as the FWHM of frequency of the filter and absolute spectral radiance as the flux per wavelength to be observed through the filter for a 0-magnitude star in the band.

Star	Filter	t [s]	$X = \sec z$	$S_{*,sky}$ SUM	$S_*$ FLUX = SUM – MSKY * AREA
HD 227858	B	30	1.294	117809	39381
HD 227858	V	30	1.301	388133	131079
HD 227858	R	30	1.307	567655	254168
HD 227858	I	30	1.323	417430	260971
HD 338931	B	30	1.394	255793	152570
HD 338931	V	30	1.405	767017	494401
HD 338931	R	30	1.413	1390626	977589
HD 338931	I	30	1.424	1285304	1075136
SA 113475	B	30	1.206	169993	38822
SA 113475	B	30	1.482	179149	33471
SA 113475	V	30	1.207	477466	154874
SA 113475	V	30	1.498	665531	147737
SA 113475	R	30	1.209	802783	344417
SA 113475	R	30	1.498	1064716	332641
SA 113475	I	30	1.213	477466	154874
SA 113475	I	30	1.521	665531	147737

Table 2: Signal for each target star as extracted from IRAF’s `apphot phot` function, presented with signal including background signal ( $S_{*,sky}$ ), and signal with sky removed ( $S_*$ ).  $t$  is the exposure time in seconds, and  $X$  is the airmass given as the secant of the zenith angle of the observation.

## Methods

Using the 16” telescope in Robert Lee Moore Hall at the University of Texas at Austin, I and my classmates used a 1024x1024 CCD imaging system, coupled with a selection of Johnson-type filters for the B, V, R, and I parts of the spectrum. Parameters of the filters can be found in Table 1. After taking dark frame and flat frame images (to account for the CCD’s inherent background response to temperature and non-uniform sensitivity, respectively), we were able to use the IRAF suite of programs to isolate the count (in Arbitrary Data Units [ADU]) in the image due to photons from the stars of interest and the count associated with background light from other sources. These data are found in Table 2.

To determine the relative magnitudes of the target stars, it is sufficient to account for two factors: atmospheric extinction and airmass. Airmass is simply a measure of how much of the atmosphere relative to the most direct path ( $z = 0$ ) the photon had to travel and atmospheric extinction is a loss of photons due to absorption in the atmosphere before reaching the telescope. For a single star  $a$  measured once with airmass  $X$ , and exposure time  $t$ , giving rise to signal  $S$ , then measured again with  $X'$ ,  $t'$  giving  $S'$ , we have the relation given in

Filter	k
B	0.583
V	0.176
R	0.131
I	0.166

Table 3: Extinction coefficients determined from the two observations of SA 113475 as seen in Table 2 using Equation 1.

Filter	Intrinsic Magnitude
B	11.362
V	10.304
R	9.736
I	9.208

Table 4: Intrinsic magnitude of SA 113475 from **FIXME** **FIXME** **FIXME**

Equation 1,

$$m_a - m'_a = k(X_a - X'_a) = -2.5 \log_{10} \frac{S_a t'_a}{S'_a t_a} \quad (1)$$

where  $m_a$  and  $m'_a$  are the associated apparent magnitudes of the star in the different positions in the sky and  $k$  is the extinction coefficient (in the filter band used). From the  $S - X$  data in Table 2 for our standard star, we can calculate the extinction coefficients for each filter band (see Table 3).

From Equation 1 and reference data for SA 113475, we arrive at the extinction coefficients in Table 3.

If we generalize Equation 1 to account for comparing two different stars (which would not in general have the same absolute brightness), we arrive at Equation 2. Equation 2 allows for the simple calculation of  $m_*$ , the magnitude of the target star, given information already known with the sole addition of the magnitude of the reference star, which is found in Table 4.

$$m_* - m_r = k(X_r - X_*) - 2.5 \log_{10} \frac{S_* t_r}{S_r t_*} \quad (2)$$

Applying Equation 2 gives us the intrinsic magnitude of each of our target stars as seen in Table 5.

To calculate flux of the target stars, we need the flux from a reference star. While our reference star was able to provide enough information to relate magnitudes, these magnitudes, even coupled with signals are insufficient to provide

Star	Filter	$m_*$
HD 227858	B	+11.295
HD 227858	V	+10.469
HD 227858	R	+10.053
HD 227858	I	+8.623
HD 338931	B	+9.766
HD 338931	V	+9.009
HD 338931	R	+8.576
HD 338931	I	+7.018

Table 5: Based on Table 4 and Equation 2, the intrinsic magnitudes of the target stars.

Filter	Measured Flux [erg cm <sup>-2</sup> s <sup>-1</sup> ]
B	7.44E-10
V	1.46E-9
R	1.18E-9
I	1.5E-9

Table 6: Flux for SA 113475 by filter for  $X \approx 1.21$ , calculated with Equation 3 from Table 1 and Table 4, and extinction coefficients in Table 3.

more than a ratio. However, the “absolute spectral irradiance” aspect of the filter is defined to be the physical flux that would pass through the filter for a 0-magnitude source. Thus, rewriting Equation 2 to solve for flux, given  $f_0$  for the filter, we can calculate the flux of our reference star with Equation 3. The measured flux for SA 113475 is given in Table 6.

$$f_{ref} = f_0 10^{-(m_{ref} + k(X_{ref} - 1))/2.5} \quad (3)$$

We can now do some algebraic sleuthing to determine how our telescope reacts to light with each filter. For a given filter, we have that  $S_* = \frac{\Delta\nu \bar{\Phi} t f_* A}{g}$  where  $\Delta\nu$  is the FWHM of the filter in frequency,  $t$  is the exposure time,  $A$  is the aperture of the telescope,  $g$  is the system gain,  $f_*$  is the measured flux of the star,  $S_*$  is the measured signal from the star and  $\bar{\Phi}$  is the averaged impact of losses due to reflection, transmission, etc. By converting the flux from an energy flux to photon flux then that photon flux to number of photons per area per time (see Equation 4), we can calculate  $R$ , the system response, which is the average number of counts generated per photon in the filter band. With the signal data from Table 2 for SA 113475, coupled with Equation 4, we arrive at

Filter	Signal Response [count photon <sup>-1</sup> ]
B	0.0061
V	0.0100
R	0.0216
I	0.0076

Table 7: Signal response for each Johnson-type filter in ADU count per photon.

Star	Filter	Measured Flux [erg cm <sup>-2</sup> s <sup>-1</sup> ]
HD 227858	B	7.55E-10
HD 227858	V	1.24E-9
HD 227858	R	8.71E-10
HD 227858	I	2.53E-9
HD 338931	B	2.92E-9
HD 338931	V	4.66E-9
HD 338931	R	3.35E-9
HD 338931	I	1.04E-8

Table 8: FIXME

the signal responses in 7.

$$S_* = \frac{\Delta\nu\overline{\Phi}_{\lambda_0}^{hc}}{g}n_\gamma = R \cdot n_\gamma \quad (4)$$

A handy consequence of Equation 4 is that using the same filter and telescope setup for two stars at the same exposure time gives  $\frac{S_1}{S_2} = \frac{f_1}{f_2}$ . As such, we can easily calculate the measured flux of each target star for each filter (see Table 8).

## Results

Assuming  $g = 3.0e^-/ADU$ , and that each incoming photon that is not scattered, absorbed, or reflected energizes one electron, the flux at the top of the telescope should be 3.0 times that as measured. If we apply Equation 5, which expresses the non-atmospherically-extincted flux as a function of airmass and measured flux (in this case, just above the telescope), we arrive at the intrinsic flux for each star as stated in Table 9.

$$F = f10^{\frac{kX}{2.5}} \quad (5)$$

Star	Filter	Intrinsic Magnitude	Intrinsic Flux [erg cm <sup>-2</sup> s <sup>-1</sup> ]
HD 227858	B		
HD 227858	V		
HD 227858	R		
HD 227858	I		
HD 338931	B		
HD 338931	V		
HD 338931	R		
HD 338931	I		
SA 113475	B		
SA 113475	V		
SA 113475	R		
SA 113475	I		

Table 9: FIXME

**Analysis**

**Conclusion**

**References**