

Documentation of MSAP3-34 for PLATO

Validation

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Table 1: Author information

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1 Introduction

1.1 Scope of the document

This document aims to provide a description of the validation algorithm for the selection and validation module of the MSAP5. It provides technical details (inputs, outputs, data types) as well as the functional description (implementation). The justification for the choice of this specific algorithm and a description of its scientific performances is provided in [please provide the reference of the justification document]. Moreover, the exact position of this algorithm within the data processing pipeline is described in [RD1].

TODO – Andrea, can you help here?

1.2 Nomenclature

See 3 and 4.

Table 3: Nomenclature

| Term | Description |
|------|---|
| M | mass of the star in units of the solar mass M_{\odot} |
| R | radius of the star in units of the solar radius R_{\odot} |
| A | age of the star in units of Gyr |

Table 4: Standard data types

| Type | Size | Values |
|-------|-----------|--------|
| array | arbitrary | floats |

1.3 Referenced documents

MSAP3-31

MSAP3-32

1.4 Abbreviations

2 General overview

2.1 Name of the algorithm and status

The algorithm is MSAP5-34, *Validation*. The baseline algorithm has been implemented, but revisions are expected. In particular, this algorithm currently works with the publically available MIST stellar tracks [Dotter, 2016, Choi et al., 2016], but needs to be updated to use the official stellar models used in the PLATO mission.

2.2 Synopsis

The objective of MSAP5-34 is to validate the selected values of mass (M), radius (R), and age (A). In particular, we check whether these values are physically consistent with stellar models. We achieve this with a χ^2 statistical test in which we reject the null hypothesis at a significance level of 0.01. If the validation check succeeds (i.e., we fail to reject the null hypothesis), then we return the mean, standard deviation, and source of each measurement.

2.3 Model

We find the model in the grid with the smallest χ^2 , defined as:

$$\chi^2 = \frac{(M - \hat{M})^2}{\sigma_M^2} + \frac{(R - \hat{R})^2}{\sigma_R^2} + \frac{(A - \hat{A})^2}{\sigma_A^2}. \quad (1)$$

Here M, R, A are the mean values of the selected measurements provided by MSAP5-32; $\sigma_M, \sigma_R, \sigma_A$ are their standard deviations; and $\hat{M}, \hat{R}, \hat{A}$ are the theoretical values from the grid of models. We then use `scipy 1.10.1` to compute the χ^2 test statistic.

3 Lists of inputs and outputs

3.1 Complete list of inputs

See documentation for MSAP5-31.

3.2 Complete list of outputs

Table 5: Output parameters

| Name | Status | Data type | Dimension | Unit |
|-------------------------|-----------|-----------|-----------|-------------|
| DP5_125_MASS | mandatory | float | 0 | M_{\odot} |
| DP5_125_MASS.STD | mandatory | float | 0 | M_{\odot} |
| DP5_125_MASS.METADATA | mandatory | string | 1 | N/A |
| DP5_125_RADIUS | mandatory | float | 0 | R_{\odot} |
| DP5_125_RADIUS.STD | mandatory | float | 0 | R_{\odot} |
| DP5_125_RADIUS.METADATA | mandatory | string | 1 | N/A |
| DP5_125_AGE | mandatory | float | 0 | Gyr |
| DP5_125_AGE.STD | mandatory | float | 0 | Gyr |
| DP5_125_AGE.METADATA | mandatory | string | 1 | N/A |

4 Processing description

4.1 Type of delivery

Prototype

4.2 Algorithm maturity

Algorithm concept defined, but interfaces (inputs/outputs) unstable. Has been tested with randomly-generated pseudo inputs, but needs to be tested with actual inputs from all of the PLATO modules.

4.3 Algorithm source

The implemented algorithm and test cases are shipped directly to WP12 office alongside this document as a compressed archive.

4.4 Pseudo-code

N/A

4.5 Flow diagram

N/A

5 Test case(s)

5.1 Implementation test case(s)

The test cases are the same as MSAP5_31 and MSAP5_32. These tests are run in `MSAP5-34-validation.ipynb`.

Case 1

- All consistent measurements.
- Inputs: Defaults
- Outputs: [(0.9962651773334784, 0.03987402416784018, 'IDP_MASS_SEISMIC'), (1.0005801453727239, 0.010773401555852083, 'IDP_RADIUS_SEISMIC'), (4.523488989174997, 0.4577944489853377, 'IDP_AGE_SEISMIC')]

Case 2

- One inconsistent mass measurement. Additionally, in this case, the seismic radius measurement is missing.
- Inputs: Defaults, except 1 is added to all the samples from the first mass method
- Outputs: [None, (1.0001027661859054, 0.010833272851737678, 'IDP_RADIUS_GRANULATION_CGBM'), (4.523488989174997, 0.4577944489853377, 'IDP_AGE_SEISMIC')]

Case 3

- Two inconsistent radius measurements. Additionally, in this case, the seismic and granulation mass measurements are missing.
- Inputs: Defaults, except 0.5 is added to all the samples from the first radius method, and 1 is added to all the samples from the second radius method
- Outputs: [(1.0019919549716714, 0.04171507064562778, 'IDP_MASS_GRANULATION_CGBM'), None, (4.523488989174997, 0.4577944489853377, 'IDP_AGE_SEISMIC')]

Case 4

- Three inconsistent age measurements.
- Inputs: Defaults, except 2, 4, 6 are added to the first, second, third age methods
- Outputs: [(0.9962651773334784, 0.03987402416784018, 'IDP_MASS_SEISMIC'), (1.0005801453727239, 0.010773401555852083, 'IDP_RADIUS_SEISMIC'), None]

Case 5

- Consistent but invalid measurements.
- Inputs: Defaults, except the radii are 10 solar masses larger
- Outputs: [None, None, None]

5.2 Scientific test case(s)

Simulated data would be highly valuable in testing the algorithm.

Bibliography

Aaron Dotter. MESA Isochrones and Stellar Tracks (MIST) 0: Methods for the Construction of Stellar Isochrones. , 222(1):8, January 2016. doi: 10.3847/0067-0049/222/1/8.

Jieun Choi, Aaron Dotter, Charlie Conroy, Matteo Cantiello, Bill Paxton, and Benjamin D. Johnson. Mesa Isochrones and Stellar Tracks (MIST). I. Solar-scaled Models. , 823(2):102, June 2016. doi: 10.3847/0004-637X/823/2/102.