



Early Warning Signals Toolbox: A novel approach for Detecting Critical Transitions

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1 References

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