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XGBoost

$$\begin{aligned} XGBoost &= eXtreme + GBDT \\ &= eXtreme + (Gradient + BDT) \\ &= eXtreme + Gradient + (Boosting + DecisionTree) \\ Boosting &\rightarrow BDT \rightarrow GBDT \rightarrow XGBoost \end{aligned}$$

XGBoost原理

提升方法 (Boosting)

提升方法使用加法模型和前向分步算法。

加法模型

$$f(x) = \sum_{m=1}^M \beta_m b(x; \gamma_m) \quad (1.1)$$

其中, $b(x; \gamma_m)$ 为基函数, γ_m 为基函数的参数, β_m 为基函数的系数。

在给定训练数据 $\{(x_i, y_i)\}_{i=1}^N$ 及损失函数 $L(y, f(x))$ 的条件下, 学习加法模型 $f(x)$ 成为经验风险极小化问题:

$$\min_{\beta_m \gamma_m} \sum_{i=1}^N L \left(y_i, \sum_{m=1}^M \beta_m b(x_i; \gamma_m) \right) \quad (1.2)$$

前向分步算法求解这一优化问题的思路：因为学习的是加法模型，可以从前向后，每一步只学习一个基函数及其系数，逐步逼近优化目标函数式 (1.2)，则可以简化优化复杂度。具体地，每步只需优化如下损失函数：

$$\min_{\beta, \gamma} \sum_{i=1}^N L(y_i, \beta b(x_i; \gamma)) \quad (1.3)$$

算法1.1 前向分步算法

输入：训练数据集 $T = \{(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)\}$ 损失函数 $L(y, f(x))$ ；基函数集合 $\{b(x; \gamma)\}$ ；

输出：加法模型 $f(x)$

(1) 初始化 $f_0(x) = 0$

(2) 对 $m = 1, 2, \dots, M$

(a) 极小化损失函数

$$(\beta_m, \gamma_m) = \arg \min_{\beta, \gamma} \sum_{i=1}^N L(y_i, f_{m-1}(x_i) + \beta b(x_i; \gamma)) \quad (1.4)$$

得到参数 β_m, γ_m

(b) 更新

$$f_m(x) = f_{m-1}(x) + \beta_m b(x; \gamma_m) \quad (1.5)$$

(3) 得到加法模型

$$f(x) = f_M(x) = \sum_{m=1}^M \beta_m b(x; \gamma_m) \quad (1.6)$$

前向分步算法将同时求解从 $m = 1$ 到 M 所有参数 β_m, γ_m 的优化问题简化为逐次求解各个 β_m, γ_m 的优化问题。

提升决策树 (BDT, Boosting Decision Tree)

以决策树为基函数的提升方法为提升决策树。

提升决策树模型可以表示为决策树的加法模型：

$$f_M = \sum_{m=1}^M T(x; \Theta_m) \quad (2.1)$$

其中， $T(x; \Theta_m)$ 表示决策树； Θ_m 为决策树的参数； M 为树的个数。

提升决策树采用前向分步算法。首先确定初始提升决策树 $f_0(x) = 0$ ，第 m 步的模型是

$$f_m(x) = f_{m-1}(x) + T(x; \Theta_m) \quad (2.2)$$

其中， $f_{m-1}(x)$ 为当前模型，通过经验风险极小化确定下一棵决策树的参数 Θ_m ，

$$\hat{\Theta}_m = \arg \min_{\Theta_m} \sum_{i=1}^N L(y_i, f_{m-1}(x_i) + T(x_i; \Theta_m)) \quad (2.3)$$

已知训练数据集 $T = \{(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)\}$, $x_i \in \mathcal{X} \subseteq \mathbb{R}^n$, \mathcal{X} 为输入空间, $y_i \in \mathcal{Y} \subseteq \mathbb{R}$, \mathcal{Y} 为输出空间。如果将输入空间 \mathcal{X} 划分为 J 个互不相交的区域 R_1, R_2, \dots, R_J , 并且在每个区域上确定输出的常量 c_j , 那么决策树可表示为

$$T(x; \Theta) = \sum_{j=1}^J c_j I(x \in R_j) \quad (2.4)$$

其中, 参数 $\Theta = \{(R_1, c_1), (R_2, c_2), \dots, (R_J, c_J)\}$ 表示决策树的区域划分和各区域上的常量值。 J 是决策树的复杂度即叶子结点个数。

提升决策树使用以下前向分步算法:

$$\begin{aligned} f_0(x) &= 0 \\ f_m(x) &= f_{m-1}(x) + T(x; \Theta_m), \quad m = 1, 2, \dots, M \\ f_M(x) &= \sum_{m=1}^M T(x; \Theta_m) \end{aligned}$$

在前向分步算法的第 m 步, 给定当前模型 $f_{m-1}(x)$, 需要求解

$$\hat{\Theta}_m = \arg \min_{\Theta_m} \sum_{i=1}^N L(y_i, f_{m-1}(x_i) + T(x_i; \Theta_m))$$

得到 $\hat{\Theta}_m$, 即第 m 棵树的参数。

当采用平方误差损失函数时,

$$L(y, f(x)) = (y - f(x))^2$$

其损失变为

$$\begin{aligned} L(y, f_{m-1}(x) + T(x; \Theta_m)) &= [y - f_{m-1}(x) - T(x; \Theta_m)]^2 \\ &= [r - T(x; \Theta_m)]^2 \end{aligned}$$

其中,

$$r = y - f_{m-1}(x) \quad (2.5)$$

是当前模型拟合数据的残差 (residual)。对回归问题的提升决策树, 只需要简单地拟合当前模型的残差。

算法2.1 回归问题的提升决策树算法

输入: 训练数据集 $T = \{(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)\}$

输出: 提升决策树 $f_M(x)$

(1) 初始化 $f_0(x) = 0$

(2) 对 $m = 1, 2, \dots, M$

(a) 按照式 (2.5) 计算残差

$$r_{mi} = y_i - f_{m-1}(x_i), \quad i = 1, 2, \dots, N$$

(b) 拟合残差 r_{mi} 学习一个回归树, 得到 $T(x; \Theta_m)$

(c) 更新 $f_m(x) = f_{m-1}(x) + T(x; \Theta_m)$

(3) 得到回归提升决策树

$$f_M(x) = \sum_{m=1}^M T(x; \Theta_m)$$

梯度提升决策树 (GBDT, Gradient Boosting Decision Tree)

梯度提升算法使用损失函数的负梯度在当前模型的值

$$-\left[\frac{\partial L(y, f(x_i))}{\partial f(x_i)}\right]_{f(x)=f_{m-1}(x)} \quad (3.1)$$

作为回归问题提升决策树算法中残差的近似值，拟合一个回归树。

算法3.1 梯度提升算法

输入：训练数据集 $T = \{(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)\}$ 损失函数 $L(y, f(x))$

输出：梯度提升决策树 $\hat{f}(x)$

(1) 初始化

$$f_0(x) = \arg \min_c \sum_{i=1}^N L(y_i, c)$$

(2) 对 $m = 1, 2, \dots, M$

(a) 对 $i = 1, 2, \dots, N$, 计算

$$r_{mi} = -\left[\frac{\partial L(y, f(x_i))}{\partial f(x_i)}\right]_{f(x)=f_{m-1}(x)}$$

(b) 对 r_{mi} 拟合一个回归树，得到第 m 棵树的叶结点区域 $R_{mj}, j = 1, 2, \dots, J$

(c) 对 $j = 1, 2, \dots, J$, 计算

$$c_{mj} = \arg \min_c \sum_{x_i \in R_{mj}} L(y_i, f_{m-1}(x_i) + c)$$

(d) 更新 $f_m(x) = f_{m-1}(x) + \sum_{j=1}^J c_{mj} I(x \in R_{mj})$

(3) 得到回归梯度提升决策树

$$\hat{f}(x) = f_M(x) = \sum_{m=1}^M \sum_{j=1}^J c_{mj} I(x \in R_{mj})$$

极限梯度提升 (XGBoost, eXtreme Gradient Boosting)

训练数据集 $\mathcal{D} = \{(\mathbf{x}_i, y_i)\}$, 其中 $\mathbf{x}_i \in \mathbb{R}^m, y_i \in \mathbb{R}, |\mathcal{D}| = n$.

决策树模型

$$f(\mathbf{x}) = w_{q(\mathbf{x})} \quad (4.1)$$

其中, $q: \mathbb{R}^m \rightarrow \{1, \dots, T\}$ 是有输入 \mathbf{x} 向叶子结点编号的映射, $w \in \mathbb{R}^T$ 是叶子结点向量, T 为决策树叶子节点数。

提升决策树模型预测输出

$$\hat{y}_i = \phi(\mathbf{x}_i) = \sum_{k=1}^K f_k(\mathbf{x}_i) \quad (4.2)$$

其中, $f_k(\mathbf{x})$ 为第 k 棵决策树。

正则化目标函数

$$\mathcal{L}(\phi) = \sum_i l(\hat{y}_i, y_i) + \sum_k \Omega(f_k) \quad (4.3)$$

其中, $\Omega(f) = \gamma T + \frac{1}{2} \lambda \|w\|^2 = \gamma T + \frac{1}{2} \lambda \sum_{j=1}^T w_j^2$.

第 t 轮目标函数

$$\mathcal{L}^{(t)} = \sum_{i=1}^n l\left(y_i, \hat{y}_i^{(t-1)} + f_t(\mathbf{x}_i)\right) + \Omega(f_t) \quad (4.4)$$

第 t 轮目标函数 $\mathcal{L}^{(t)}$ 在 $\hat{y}^{(t-1)}$ 处的二阶泰勒展开

$$\begin{aligned} \mathcal{L}^{(t)} &\simeq \sum_{i=1}^n \left[l\left(y_i, \hat{y}^{(t-1)}\right) + \partial_{\hat{y}^{(t-1)}} l\left(y_i, \hat{y}^{(t-1)}\right) f_t(\mathbf{x}_i) + \frac{1}{2} \partial_{\hat{y}^{(t-1)}}^2 l\left(y_i, \hat{y}^{(t-1)}\right) f_t^2(\mathbf{x}_i) \right] + \Omega \\ &= \sum_{i=1}^n \left[l\left(y_i, \hat{y}^{(t-1)}\right) + g_i f_t(\mathbf{x}_i) + \frac{1}{2} h_i f_t^2(\mathbf{x}_i) \right] + \Omega(f_t) \end{aligned}$$

其中, $g_i = \partial_{\hat{y}^{(t-1)}} l\left(y_i, \hat{y}^{(t-1)}\right)$, $h_i = \partial_{\hat{y}^{(t-1)}}^2 l\left(y_i, \hat{y}^{(t-1)}\right)$.

第 t 轮目标函数 $\mathcal{L}^{(t)}$ 的二阶泰勒展开移除关于 $f_t(\mathbf{x}_i)$ 常数项

$$\begin{aligned} \tilde{\mathcal{L}}^{(t)} &= \sum_{i=1}^n \left[g_i f_t(\mathbf{x}_i) + \frac{1}{2} h_i f_t^2(\mathbf{x}_i) \right] + \Omega(f_t) \\ &= \sum_{i=1}^n \left[g_i f_t(\mathbf{x}_i) + \frac{1}{2} h_i f_t^2(\mathbf{x}_i) \right] + \gamma T + \frac{1}{2} \lambda \sum_{j=1}^T w_j^2 \end{aligned} \quad (4.6)$$

定义叶结点 j 上的样本的下标集合 $I_j = \{i | q(\mathbf{x}_i) = j\}$, 则目标函数可表示为按叶结点累加的形式

$$\tilde{\mathcal{L}}^{(t)} = \sum_{j=1}^T \left[\left(\sum_{i \in I_j} g_i \right) w_j + \frac{1}{2} \left(\sum_{i \in I_j} h_i + \lambda \right) w_j^2 \right] + \gamma T \quad (4.7)$$

由于

$$w_j^* = \arg \min_{w_j} \tilde{\mathcal{L}}^{(t)}$$

可令

$$\frac{\partial \tilde{\mathcal{L}}^{(t)}}{\partial w_j} = 0$$

得到每个叶结点 j 的最优分数为

$$w_j^* = - \frac{\sum_{i \in I_j} g_i}{\sum_{i \in I_j} h_i + \lambda} \quad (4.8)$$

代入每个叶结点 j 的最优分数, 得到最优化目标函数值

$$\tilde{\mathcal{L}}^{(t)}(q) = - \frac{1}{2} \sum_{j=1}^T \frac{\left(\sum_{i \in I_j} g_i \right)^2}{\sum_{i \in I_j} h_i + \lambda} + \gamma T \quad (4.9)$$

假设 I_L 和 I_R 分别为分裂后左右结点的实例集, 令 $I = I_L \cup I_R$, 则分裂后损失减少量由下式得出

$$\mathcal{L}_{split} = \frac{1}{2} \left[\frac{\left(\sum_{i \in I_L} g_i \right)^2}{\sum_{i \in I_L} h_i + \lambda} + \frac{\left(\sum_{i \in I_R} g_i \right)^2}{\sum_{i \in I_R} h_i + \lambda} - \frac{\left(\sum_{i \in I} g_i \right)^2}{\sum_{i \in I} h_i + \lambda} \right] - \gamma \quad (4.10)$$

用以评估待分裂结点。

算法4.1 分裂查找的精确贪婪算法

输入：当前结点实例集 I ;特征维度 d

输出：根据最大分值分裂

- (1) $gain \leftarrow 0$
- (2) $G \leftarrow \sum_{i \in I} g_i, H \leftarrow \sum_{i \in I} h_i$
- (3) for $k = 1$ to d do
 - (3.1) $G_L \leftarrow 0, H_L \leftarrow 0$
 - (3.2) for j in sorted(I , by \mathbf{x}_{jk}) do
 - (3.2.1) $G_L \leftarrow G_L + g_j, H_L \leftarrow H_L + h_j$
 - (3.2.2) $G_R \leftarrow G - G_L, H_R = H - H_L$
 - (3.2.3) $score \leftarrow \max \left(score, \frac{G_L^2}{H_L + \lambda} + \frac{G_R^2}{H_R + \lambda} - \frac{G^2}{H + \lambda} \right)$
 - (3.3) end
- (4) end

XGBoost应用

XGBoost参数

XGBoost主要参数类型：

1. 通用参数：控制整体功能；
2. 提升器参数：在每一步控制单个提升器（tree、regression）；
3. 学习任务参数：控制最优化执行。

通用参数

booster [default=gbtree]

选择每次迭代的模型，有两个选择：

- gbtree：基于树的模型；
- gbmliner：线性模型。

silent [default=0]

- 设置为1，静默模式被开启，不会显示运行信息；
- 通常设置为0，运行信息会更好的帮助理解模型。

nthread [default=最大可能的线程数]

- 该参数用以并行处理，应设置为系统内核数；
- 如果你希望使用所有内核，则不应设置该参数，算法会自动检测。

提升器参数

eta [default=0.3]

- 学习率;
- 典型值: 0.01-0.2。

min_child_weight [default=1]

- 定义最小叶子节点样本权重和;
- 用于控制过拟合。较大的值可以避免模型学习到局部的特殊样本;
- 太大的值会导致欠拟合。

max_depth [default=6]

- 树的最大深度;
- 用于控制过拟合。较大的值模型会学到更具体更局部的样本;
- 典型值为3-10。

max_leaf_nodes

- 树中终端节点或叶子的最大数目;
- 可以代替max_depth参数。由于创建的是二叉树, 一个深度为 n 的树最多生成 2^n 个叶子;
- 如果该参数被定义, max_depth参数将被忽略。

gamma [default=0]

- 只有在节点分裂后损失函数值下降, 才会分裂该节点。gamma参数指定了节点分裂所需的最小损失函数下降值;
- 该参数的值越大, 算法越保守。该参数的值和损失函数相关, 所以是需要调整的。

max_delta_step [default=0]

- 该参数限制每棵树权重改变的最大步长。如果该参数为0, 则表示没有约束。如果将其设置为正值, 则使更新步骤更加保守;
- 通常该参数不需要设置。但是当各类别的样本十分不平衡时, 它对逻辑回归是很有帮助的。

subsample [default=1]

- 该参数控制对于每棵树随机采样的比例;
- 减小该参数的值, 算法会更加保守, 避免过拟合。但是, 如果该设置得过小, 它可能会导致欠拟合;
- 典型值: 0.5-1。

colsample_bytree [default=1]

- 该参数用来控制每棵树随机采样的列数的占比(每一列是一个特征);
- 典型值: 0.5-1。

colsample_bylevel [default=1]

- 该参数用来控制树的每一级的每一次分裂, 对列数的采样的占比;
- 该参数和subsample参数可以起到相同的作用。

lambda [default=1]

- 权重的L2正则化项。(类似于岭回归)。

alpha [default=0]

- 权重的L1正则化项。(类似于套索回归);
- 可以应用在很高维度的情况下, 使得算法的速度更快。

scale_pos_weight [default=1]

- 在各类别样本十分不平衡时, 把这个参数设定为一个正值, 可以使算法更快收敛。

学习任务参数

objective [default=reg:linear]

该参数定义需要被最小化的损失函数。常用值有:

- binary:logistic 二分类的逻辑回归, 返回预测的概率(不是类别);
- multi:softmax 使用softmax的多分类器, 返回预测的类别(不是概率)。在这种情况下, 你还需要多设一个参数: num_class(类别数目);
- multi:softprob 和multi:softmax参数一样, 但是返回的是每个数据属于各个类别的概率。

eval_metric [default according to objective]

- 对于有效数据的度量方法;
- 对于回归问题, 默认值是rmse, 对于分类问题, 默认值是error;
- 典型值:
 - rmse 均方根误差
 - mae 平均绝对误差
 - logloss 负对数似然函数值
 - error 二分类错误率(阈值为0.5)
 - merror 多分类错误率
 - mlogloss 多分类logloss损失函数
 - auc 曲线下面积

seed [default=0]

- 随机数的种子
- 设置它可以复现随机数据的结果, 也可以用于调整参数

XGBoost的基本使用应用

导入XGBoost等相关包:

In [3]:

```
from numpy import loadtxt
from xgboost import XGBClassifier
from sklearn.model_selection import train_test_split
from sklearn.metrics import accuracy_score

import os
os.environ['KMP_DUPLICATE_LIB_OK']='True'
```

加载数据, 提取特征集和标签:

In [4]:

```
dataset = loadtxt('./data/pima-indians-diabetes.csv', delimiter=',')  
  
X = dataset[:, 0:8]  
y = dataset[:, 8]
```

将数据划分为训练集和测试集:

In [5]:

```
seed = 7  
test_size = 0.33  
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=test_size, random_state=seed  
)
```

In [6]:

```
X_train.shape, X_test.shape, y_train.shape, y_test.shape
```

Out[6]:

```
((514, 8), (254, 8), (514,), (254,))
```

创建及训练模型:

In [7]:

```
model = XGBClassifier(n_jobs=-1)  
model.fit(X_train, y_train)
```

Out[7]:

```
XGBClassifier(base_score=0.5, booster='gbtree', colsample_bylevel=1,  
              colsample_bytree=1, gamma=0, learning_rate=0.1, max_delta_step=0,  
              max_depth=3, min_child_weight=1, missing=None, n_estimators=100,  
              n_jobs=-1, nthread=None, objective='binary:logistic',  
              random_state=0, reg_alpha=0, reg_lambda=1, scale_pos_weight=1,  
              seed=None, silent=True, subsample=1)
```

使用训练后的模型对测试集进行预测, 并计算预测值与实际之间的acc值:

In [8]:

```
y_pred = model.predict(X_test)  
accuracy = accuracy_score(y_test, y_pred)  
print("Accuracy: %.2f%%" % (accuracy * 100.0))
```

Accuracy: 77.95%

使用训练后的模型对测试集进行预测, 得到每个类别的预测概率:

In [9]:

```
y_pred = model.predict(X_test)
y_pred
```

Out[9]:

```
array([0., 1., 1., 0., 1., 1., 0., 0., 1., 0., 1., 0., 1., 1., 0., 0., 0.,
       1., 0., 0., 0., 0., 1., 1., 0., 0., 0., 0., 0., 1., 1., 0., 0., 0.,
       0., 1., 1., 0., 1., 0., 1., 1., 1., 0., 0., 0., 1., 0., 0., 1., 0.,
       0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 1., 1., 1., 0., 1.,
       1., 1., 1., 1., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0.,
       0., 1., 0., 1., 0., 1., 0., 1., 0., 0., 1., 1., 0., 1., 0., 1., 0.,
       0., 0., 0., 1., 0., 0., 0., 1., 0., 1., 0., 0., 1., 1., 0., 0., 0.,
       1., 0., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0., 1., 0., 0., 0., 0.,
       0., 0., 0., 1., 0., 1., 0., 0., 0., 0., 0., 1., 0., 0., 1., 0.,
       0., 0., 0., 1., 0., 1., 0., 0., 0., 0., 0., 1., 0., 1., 0., 0., 1.,
       0., 1., 0., 0., 1., 0., 1., 0., 1., 0., 1., 0., 0., 0., 0., 0., 0.,
       0., 0., 1., 1., 0., 1., 1., 0., 0., 1., 0., 0., 1., 0., 1., 1., 1.,
       0., 0., 1., 0., 0., 0., 1., 1., 0., 1., 0., 0., 0., 1., 0., 0.,
       0., 1., 0., 1., 1., 1., 1., 1., 0., 0., 1., 0., 0., 0., 0., 0., 1.,
       0., 0., 1., 1., 0., 0., 1., 0., 1., 0., 0., 1., 1., 1.]])
```

In [10]:

```
y_pred_proba = model.predict_proba(X_test)
y_pred_proba
```

Out[10]:

```
array([[0.9545844 , 0.04541559],
       [0.05245447, 0.9475455 ],
       [0.41897488, 0.5810251 ],
       [0.9831998 , 0.0168002 ],
       [0.4119159 , 0.5880841 ],
       [0.31113452, 0.6888655 ],
       [0.9705527 , 0.02944732],
       [0.93274003, 0.06725994],
       [0.11494881, 0.8850512 ],
       [0.6501156 , 0.34988442],
       [0.03848034, 0.96151966],
       [0.99019825, 0.00980172],
       [0.07478714, 0.92521286],
       [0.0899508 , 0.9100492 ],
       [0.8759558 , 0.12404419],
       [0.8833156 , 0.11668438],
       [0.7805242 , 0.21947582],
       [0.35131902, 0.648681  ],
       [0.98205894, 0.01794105],
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       [0.79318744, 0.20681255],
       [0.3731498 , 0.6268502 ],
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       [0.613425 , 0.386575  ],
       [0.7924037 , 0.2075963 ],
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       [0.7400504 , 0.25994962],
```

[0.749115 , 0.25088504],
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[0.5444821 , 0.4555179],
[0.27095395, 0.72904605],

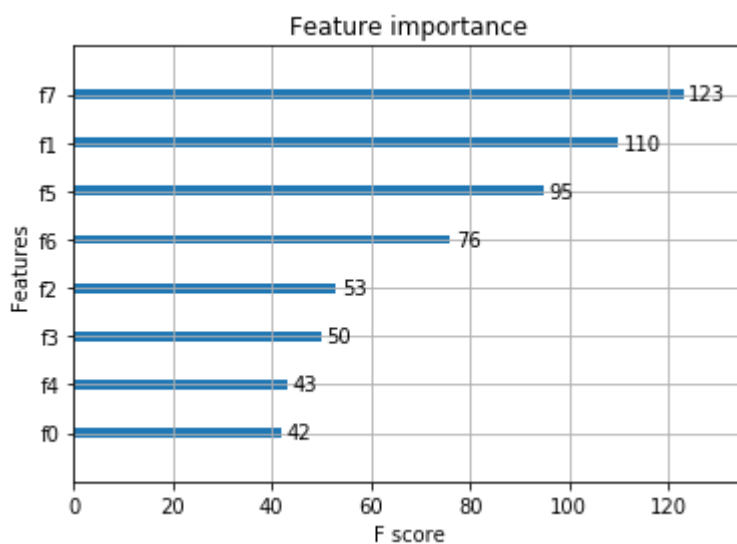
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[0.6039266 , 0.3960734],
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```
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[0.42821795, 0.57178205],  
[0.2364142 , 0.7635858 ],  
[0.05780089, 0.9421991 ]], dtype=float32)
```

输出各特征重要程度：

In [11]:

```
from xgboost import plot_importance  
from matplotlib import pyplot  
%matplotlib inline  
  
plot_importance(model)  
pyplot.show()
```

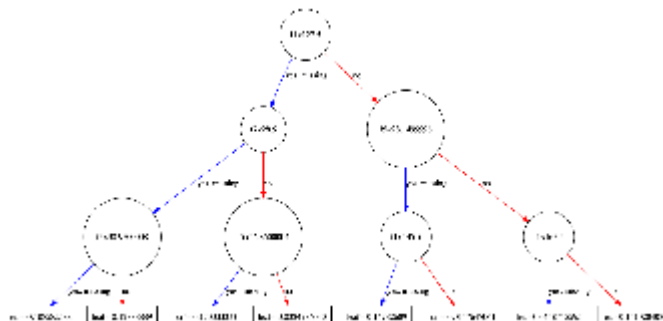


In [12]:

```
from xgboost import plot_tree  
plot_tree(model)
```

Out[12]:

<matplotlib.axes._subplots.AxesSubplot at 0x1a23d5db70>



导入调参相关包:

In [13]:

```
from sklearn.model_selection import GridSearchCV  
from sklearn.model_selection import StratifiedKFold
```

创建模型及参数搜索空间:

In [14]:

```
model_GS = XGBClassifier()  
learning_rate = [0.0001, 0.001, 0.01, 0.1, 0.2, 0.3]  
max_depth = [1, 2, 3, 4, 5]  
param_grid = dict(learning_rate=learning_rate, max_depth=max_depth)
```

设置分层抽样验证及创建搜索对象:

In [15]:

```
kfold = StratifiedKFold(n_splits=10, shuffle=True, random_state=seed)  
grid_search = GridSearchCV(model_GS, param_grid=param_grid, scoring='neg_log_loss', n_jobs=-1, cv=kfold)  
grid_result = grid_search.fit(X, y)
```

In [16]:

```
y_pred = grid_result.predict(X_test)  
accuracy = accuracy_score(y_test, y_pred)  
print("Accuracy: %.2f%%" % (accuracy * 100.0))
```

Accuracy: 81.10%

In [17]:

```
grid_result.best_score_, grid_result.best_params_
```

Out[17]:

```
(-0.47171179660714796, {'learning_rate': 0.2, 'max_depth': 1})
```

XGBoost与LightGBM的对比分析

In [18]:

```
import time

import numpy as np
import pandas as pd
import matplotlib as mpl
import matplotlib.pyplot as plt
from matplotlib.pylab import rcParams
import seaborn as sns

from sklearn.metrics import accuracy_score
from sklearn.model_selection import GridSearchCV

import xgboost as xgb
from xgboost import XGBClassifier

import lightgbm as lgb
from lightgbm import LGBMClassifier
```

In [19]:

```
fetch_from = './data/fashionmnist/fashion-mnist_train.csv'
train = pd.read_csv(fetch_from)

fetch_from = './data/fashionmnist/fashion-mnist_test.csv'
test = pd.read_csv(fetch_from)
```

In [20]:

```
X_train, y_train, X_test, y_test = train.iloc[:, 1:], train['label'], test.iloc[:, 1:], test['label']
X_train.head()
```

Out[20]:

	pixel1	pixel2	pixel3	pixel4	pixel5	pixel6	pixel7	pixel8	pixel9	pixel10	...	pixel7
0	0	0	0	0	0	0	0	0	0	0	...	0
1	0	0	0	0	0	0	0	0	0	0	...	0
2	0	0	0	0	0	0	0	5	0	0	...	0
3	0	0	0	1	2	0	0	0	0	0	...	3
4	0	0	0	0	0	0	0	0	0	0	...	0

5 rows × 784 columns



In [21]:

```
X_train.shape, y_train.shape, X_test.shape, y_test.shape
```

Out[21]:

```
((60000, 784), (60000,), (10000, 784), (10000,))
```

In [22]:

```
def plot_digits(instances, images_per_row=10, **options):
    size = 28
    images_per_row = min(len(instances), images_per_row)
    images = [instance.reshape(size, size) for instance in instances]
    n_rows = (len(instances) - 1) // images_per_row + 1
    row_images = []
    n_empty = images_per_row * n_rows - len(instances)
    images.append(np.zeros((size, size * n_empty)))
    for row in range(n_rows):
        rimages = images[row * images_per_row : (row + 1) * images_per_row]
        row_images.append(np.concatenate(rimages, axis=1))
    image = np.concatenate(row_images, axis=0)
    plt.imshow(image, cmap=matplotlib.cm.binary, **options)
    plt.axis("off")
```

In [23]:

```
plt.figure(figsize=(10,10))
example_images = X_train[:100]
plot_digits(example_images.values)
plt.show()
```



In [24]:

```
def show_time(diff):
    m, s = divmod(diff, 60)
    h, m = divmod(m, 60)
    s, m, h = int(round(s, 0)), int(round(m, 0)), int(round(h, 0))

    print("Execution Time: " + "{0:02d}:{1:02d}:{2:02d}".format(h, m, s))
```

In [25]:

```
training_times = []
testing_times = []
scores = []
```

In [26]:

```
def training_and_testing(clf, X, y, X_test, y_test):
    print("Training...")
    start = time.time()
    model = clf.fit(X, y)
    end = time.time()
    training_times.append(end - start)
    show_time(end - start)

    print("\nTesting...")
    start = time.time()
    scores.append(accuracy_score(y_test, model.predict(X_test)))
    end = time.time()
    testing_times.append(end - start)
    show_time(end - start)

    return model
```

In [34]:

```
xgb_model = training_and_testing(XGBClassifier(n_estimators=50, max_depth=5), X_train, y_train,
X_test, y_test)
```

Training...

Execution Time: 00:21:04

Testing...

Execution Time: 00:00:00

In [35]:

```
lgb_model = training_and_testing(LGBMClassifier(n_estimators=50, max_depth=5), X_train, y_train,
X_test, y_test)
```

Training...

Execution Time: 00:01:46

Testing...

Execution Time: 00:00:01

In [27]:

```
def training_and_testing_with_grid_search(clf, params, X, y, X_test, y_test):
    print("Training with Grid Search...")
    start = time.time()
    model = GridSearchCV(clf, params, scoring='accuracy', n_jobs=-1, cv=5).fit(X, y).best_estimator_
    end = time.time()
    training_times.append(end - start)
    show_time(end - start)

    print("Testing with Grid Search...")
    start = time.time()
    scores.append(accuracy_score(y_test, model.predict(X_test)))
    end = time.time()
    testing_times.append(end - start)
    show_time(end - start)

    return model
```

In [38]:

```
param_grid = [{'max_depth': [5, 10],
                'n_estimators': [100],
                'learning_rate': [0.05, 0.1],
                'colsample_bytree': [0.8, 0.95]}]

xgb_model_gs = training_and_testing_with_grid_search(XGBClassifier(random_state=42), param_grid,
                                                    X_train[:4000], y_train[:4000], X_test, y_test)
```

Training with Grid Search...

/anaconda3/envs/dev/lib/python3.6/site-packages/sklearn/externals/joblib/externals/loky/process_executor.py:706: UserWarning: A worker stopped while some jobs were given to the executor. This can be caused by a too short worker timeout or by a memory leak.

"timeout or by a memory leak.", UserWarning

Execution Time: 00:45:16

Testing with Grid Search...

Execution Time: 00:00:01

In [37]:

```
lgb_model_gs = training_and_testing_with_grid_search(LGBMClassifier(random_state=42), param_grid,
                                                    X_train[:4000], y_train[:4000], X_test, y_test)
```

Training with Grid Search...

Execution Time: 00:17:14

Testing with Grid Search...

Execution Time: 00:00:01

In [39]:

```
scores, training_times, testing_times
```

Out[39]:

```
([0.8716, 0.8717, 0.8509, 0.8476],  
 [1264.2565653324127,  
  106.44469475746155,  
  1033.7386996746063,  
  2716.4520568847656],  
 [0.42176175117492676,  
  0.5533642768859863,  
  1.329496145248413,  
  0.7895469665527344])
```

In [41]:

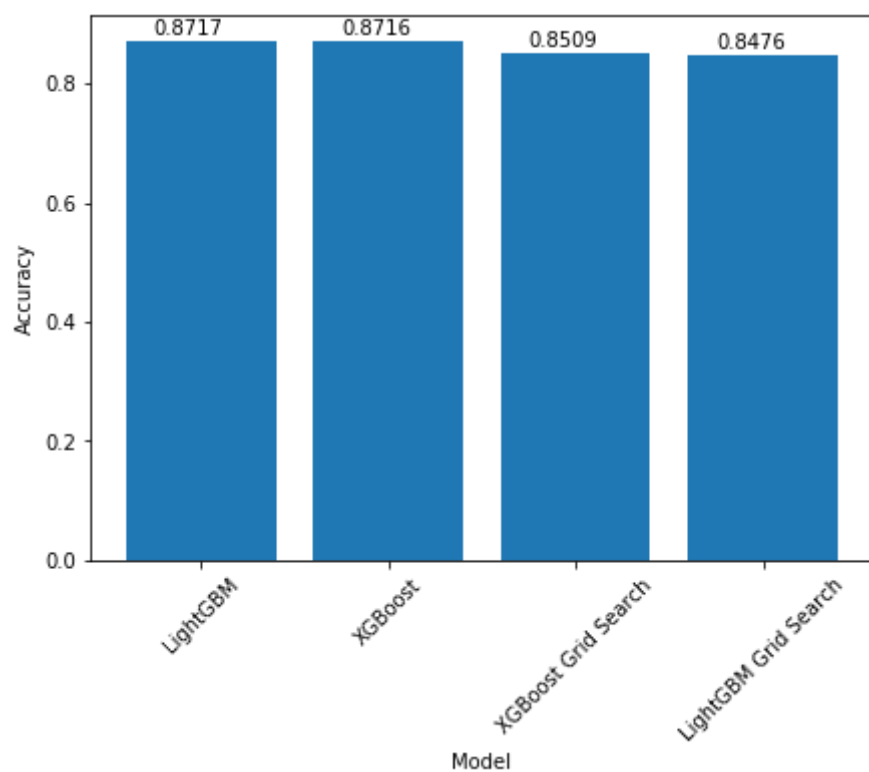
```
models = [('XGBoost', xgb_model),  
          ('LightGBM', lgb_model),  
          ('XGBoost Grid Search', xgb_model_gs),  
          ('LightGBM Grid Search', lgbm_model_gs)]
```

In [28]:

```
def plot_metric(model_scores, score='Accuracy'):  
    rcParams['figure.figsize'] = 7,5  
    plt.bar(model_scores['Model'], height=model_scores[score])  
    xlocs, xlabs = plt.xticks()  
    xlocs=[i for i in range(0,6)]  
    xlabs=[i for i in range(0,6)]  
    for i, v in enumerate(model_scores[score]):  
        plt.text(xlocs[i] - 0.25, v + 0.01, str(v))  
    plt.xlabel('Model')  
    plt.ylabel(score)  
    plt.xticks(rotation=45)  
    plt.show()
```

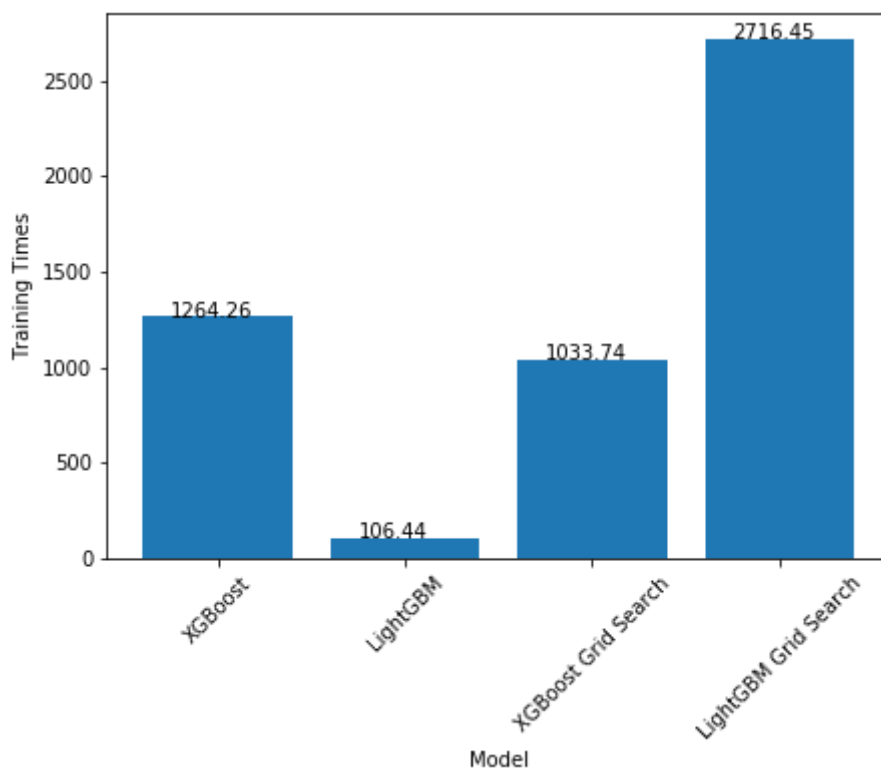
In [49]:

```
model_scores = pd.DataFrame({ 'Model': [name for name, _ in models], 'Accuracy': scores })
model_scores.sort_values(by='Accuracy', ascending=False, inplace=True)
plot_metric(model_scores)
```



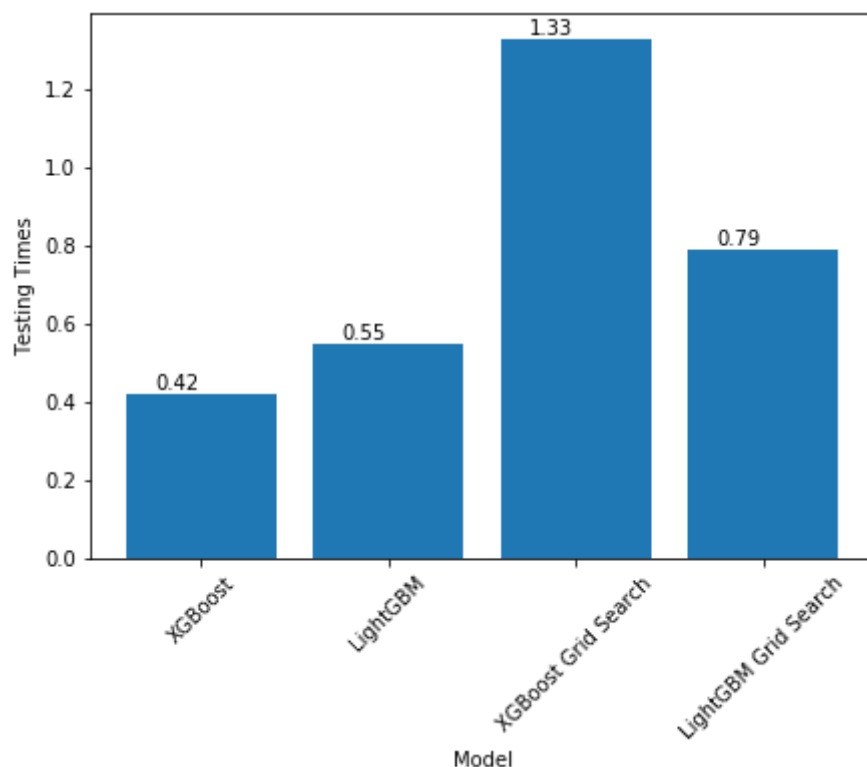
In [50]:

```
training_times = [round(time,2) for time in training_times]
model_train_times = pd.DataFrame({ 'Model': [name for name, _ in models], 'Training Times': training_times })
plot_metric(model_train_times, score='Training Times')
```



In [54]:

```
testing_times = [round(time,2) for time in testing_times]
model_train_times = pd.DataFrame({ 'Model': [name for name, _ in models], 'Testing Times': testing_times })
plot_metric(model_train_times, score='Testing Times')
```

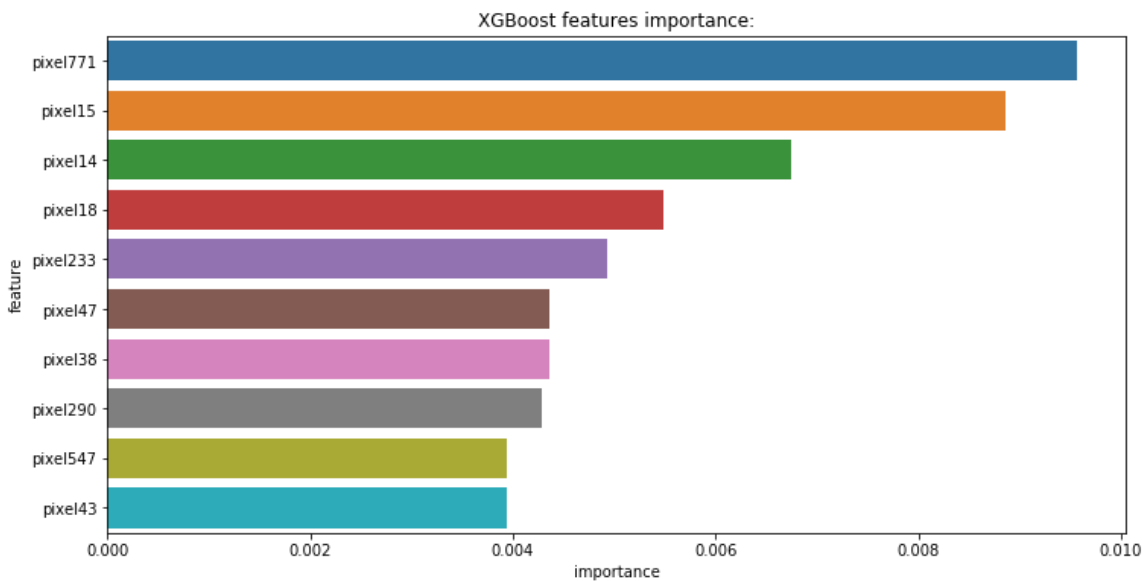


In [29]:

```
def feature_importances(df, model, model_name, max_num_features=10):
    feature_importances = pd.DataFrame(columns = ['feature', 'importance'])
    feature_importances['feature'] = df.columns
    feature_importances['importance'] = model.feature_importances_
    feature_importances.sort_values(by='importance', ascending=False, inplace=True)
    feature_importances = feature_importances[:max_num_features]
    # print(feature_importances)
    plt.figure(figsize=(12, 6));
    sns.barplot(x="importance", y="feature", data=feature_importances);
    plt.title(model_name+' features importance:');
```

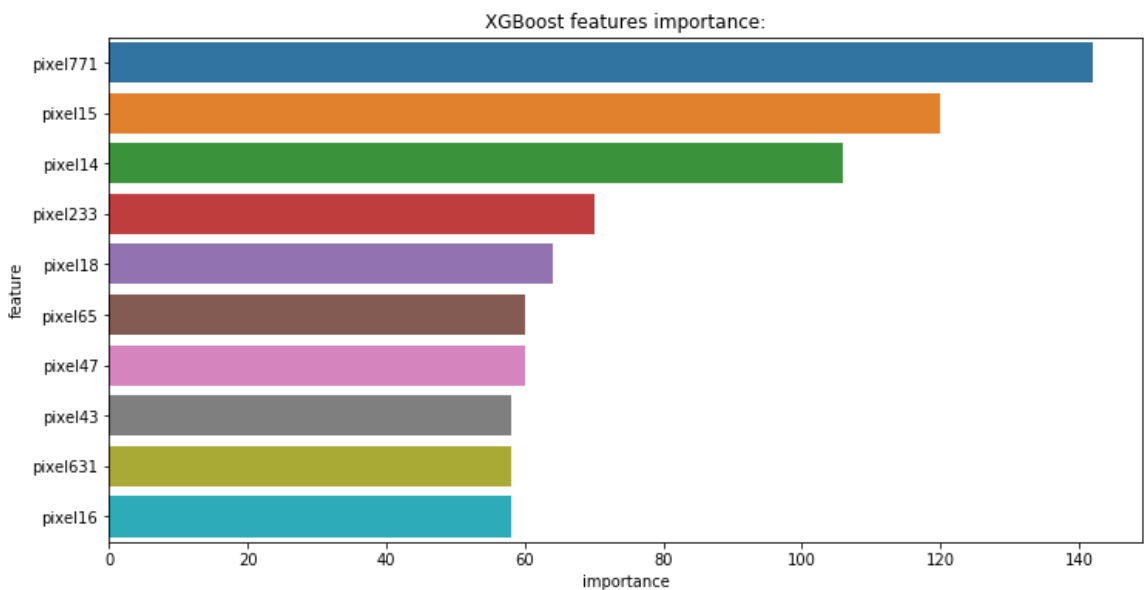
In [59]:

```
feature_importances(X_train, xgb_model, 'XGBoost')
```



In [60]:

```
feature_importances(X_train, lgb_model, 'XGBoost')
```



In [61]:

```
rcParams['figure.figsize'] = 80, 50
```

In [64]:

```
xgboost.plot_tree(xgb_model);
```

In [66]:

```
lightgbm.plot_tree(lgb_model)
```

Out[66]:

<matplotlib.axes._subplots.AxesSubplot at 0x1a1c927198>



LightGBM的应用

In [80]:

```
# 导入相关包
import numpy as np
import pandas as pd

import lightgbm as lgb

from sklearn.metrics import mean_squared_error
```

In [70]:

```
# 加载训练数据和测试数据，以及对应的权重数据
df_train = pd.read_csv("./data/binary.train", header=None, sep='\t')
df_test = pd.read_csv("./data/binary.test", header=None, sep='\t')

W_train = pd.read_csv("./data/binary.train.weight", header=None)[0]
W_test = pd.read_csv("./data/binary.test.weight", header=None)[0]

y_train = df_train[0].values
X_train = df_train.drop(0, axis=1).values

y_test = df_test[0].values
X_test = df_test.drop(0, axis=1).values

num_train, num_feature = X_train.shape

lgb_train = lgb.Dataset(X_train, y_train, weight=W_train, free_raw_data=False)
lgb_eval = lgb.Dataset(X_test, y_test, weight=W_test, free_raw_data=False)
```

In [71]:

```
#设置模型参数
params = {
    'boosting_type': 'gbdt',
    'objective': 'binary',
    'metric': 'binary_logloss',
    'num_leaves': 31,
    'learning_rate': 0.05,
    'feature_fraction': 0.9,
    'bagging_fraction': 0.8,
    'bagging_freq': 5,
    'verbose': 0
}
```

In [73]:

```
#训练模型1-10轮迭代
```

```
lgb_model = lgb.train(params,  
                      lgb_train,  
                      num_boost_round=10,  
                      valid_sets=lgb_train,  
                      feature_name=feature_name)
```

```
[1] training's binary_logloss: 0.680151  
[2] training's binary_logloss: 0.671664  
[3] training's binary_logloss: 0.664144  
[4] training's binary_logloss: 0.655383  
[5] training's binary_logloss: 0.647397  
[6] training's binary_logloss: 0.640486  
[7] training's binary_logloss: 0.634669  
[8] training's binary_logloss: 0.628028  
[9] training's binary_logloss: 0.621547  
[10] training's binary_logloss: 0.615672
```

In [74]:

```
#保存模型
```

```
lgb_model.save_model('./data/lgb_model.txt')
```

Out[74]:

```
<lightgbm.basic.Booster at 0x1a2815bb00>
```

In [72]:

```
#重新加载模型进行预测
```

```
lgb_model_reload = lgb.Booster(model_file='./data/lgb_model.txt')  
y_pred = lgb_model_reload.predict(X_test)  
print(mean_squared_error(y_test, y_pred) ** 0.5)
```

```
0.472411476758235
```

In [76]:

```
#用已训练模型初始化模型训练11-20轮迭代
lgb_model_retrain = lgb.train(params,
                               lgb_train,
                               num_boost_round=10,
                               init_model='./data/lgb_model.txt',
                               valid_sets=lgb_eval
                               # categorical_feature=[21]
                               )
```

```
[11] valid_0's binary_logloss: 0.617554
[12] valid_0's binary_logloss: 0.614363
[13] valid_0's binary_logloss: 0.609672
[14] valid_0's binary_logloss: 0.606011
[15] valid_0's binary_logloss: 0.602056
[16] valid_0's binary_logloss: 0.599294
[17] valid_0's binary_logloss: 0.595538
[18] valid_0's binary_logloss: 0.591744
[19] valid_0's binary_logloss: 0.58883
[20] valid_0's binary_logloss: 0.585746
```

/anaconda3/envs/dev/lib/python3.6/site-packages/lightgbm/basic.py:814: UserWarning: The prediction of init_model will be overridden by init_score.
warnings.warn("The prediction of init_model will be overridden by init_score.")

In [79]:

```
#调整学习率训练模型21-30轮迭代
lgb_model_retrain = lgb.train(params,
                               lgb_train,
                               num_boost_round=10,
                               init_model=lgb_model_retrain,
                               learning_rates=lambda iter: 0.05 * (0.99 ** iter),
                               valid_sets=lgb_eval)
```

```
[41] valid_0's binary_logloss: 0.617554
[42] valid_0's binary_logloss: 0.614394
[43] valid_0's binary_logloss: 0.609792
[44] valid_0's binary_logloss: 0.606231
[45] valid_0's binary_logloss: 0.602417
[46] valid_0's binary_logloss: 0.599771
[47] valid_0's binary_logloss: 0.59621
[48] valid_0's binary_logloss: 0.592633
[49] valid_0's binary_logloss: 0.589609
[50] valid_0's binary_logloss: 0.586783
```

In [78]:

```
#调整其他参数训练模型31-40轮迭代
```

```
lgb_model_retrain = lgb.train(params,
                               lgb_train,
                               num_boost_round=10,
                               init_model=lgb_model_retrain,
                               valid_sets=lgb_eval,
                               callbacks=[lgb.reset_parameter(bagging_fraction=[0.7] * 5 + [0.6]
* 5)])
```

```
[31] valid_0's binary_logloss: 0.617579
[32] valid_0's binary_logloss: 0.614267
[33] valid_0's binary_logloss: 0.609643
[34] valid_0's binary_logloss: 0.605865
[35] valid_0's binary_logloss: 0.60161
[36] valid_0's binary_logloss: 0.598602
[37] valid_0's binary_logloss: 0.595474
[38] valid_0's binary_logloss: 0.593449
[39] valid_0's binary_logloss: 0.591171
[40] valid_0's binary_logloss: 0.588738
```

In [81]:

```
#自定义损失函数
```

```
def loglikelihood(preds, train_data):
    labels = train_data.get_label()
    preds = 1. / (1. + np.exp(-preds))
    grad = preds - labels
    hess = preds * (1. - preds)
    return grad, hess
```

```
#自定义评估函数
```

```
def binary_error(preds, train_data):
    labels = train_data.get_label()
    return 'error', np.mean(labels != (preds > 0.5)), False
```

```
#使用自定义损失及评估函数训练模型41-50轮迭代
```

```
lgb_model_retrain = lgb.train(params,
                               train_set=lgb_train,
                               num_boost_round=10,
                               init_model=lgb_model_retrain,
                               fobj=loglikelihood,
                               feval=binary_error,
                               valid_sets=lgb_eval)
```

```
[51] valid_0's binary_logloss: 5.16783      valid_0's error: 0.402
[52] valid_0's binary_logloss: 5.46634      valid_0's error: 0.392
[53] valid_0's binary_logloss: 5.07286      valid_0's error: 0.39
[54] valid_0's binary_logloss: 5.30891      valid_0's error: 0.382
[55] valid_0's binary_logloss: 5.54901      valid_0's error: 0.37
[56] valid_0's binary_logloss: 5.65039      valid_0's error: 0.368
[57] valid_0's binary_logloss: 5.56936      valid_0's error: 0.356
[58] valid_0's binary_logloss: 5.73844      valid_0's error: 0.354
[59] valid_0's binary_logloss: 5.66427      valid_0's error: 0.352
[60] valid_0's binary_logloss: 5.61407      valid_0's error: 0.35
```